Infrared study of crystal-field excitations in NdBa₂Cu₃O₆

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We have observed absorption bands corresponding to Nd^{3+} crystal-field (CF) excitations in $NdBa_2Cu_3O_6$ by infrared spectroscopy. The observed absorption peaks are assigned to different transitions between CF levels of the ${}^{4}I_{9/2}$ ground state to the excited multiplets ${}^{4}I_{11/2}$, ${}^{4}I_{13/2}$, and ${}^{4}I_{15/2}$ of Nd^{3+} ions on the regular rare-earth sites. From fits to these levels, we have calculated a more precise set of CF parameters compared to previous results obtained on the basis of the ground state multiplet only. Crystal-field transitions from Nd^{3+} ions on the Ba site have also been observed. [S0163-1829(99)07009-5]

I. INTRODUCTION

A precise measurement of the crystal-field (CF) excitations in rare-earth (R) based high- T_c superconductors (HTSC) is essential for providing detailed information on the electronic structure of the R ion. This information is important in order to understand, for example, the observed coexistence between superconductivity and long-range magnetic ordering of the R ion sublattice at low temperatures.^I Furthermore, the CF excitations of f electrons in R elements can be used to study structural properties of high- T_c superconductors since they are sensitive on a very local scale to crystalline electric fields as well as magnetic fields generated by neighboring magnetic ions. The R ions in HTSC are usually sandwiched between two CuO₂ planes, where the superconducting carriers are located, and thus the crystal-field interaction at the R ion site has been used to probe the charge distribution and structural changes induced by doping and superconductivity.²⁻⁵

CF excitations in HTSC and related compounds have so far been mainly studied by inelastic neutron scattering (INS).^{6–8} However, such measurements have only in a few cases been extended beyond the ground-state multiplet,^{9–11} and intermultiplet transitions have hardly been reported for (*R*)Ba₂Cu₃O_{7- δ}.^{9,11} Usually, the observation of CF levels in the ground-state manifold is not sufficient for a precise determination of CF parameters since it provides rather limited information (there are only a few transitions compared to the number of parameters).¹² These parameters appear in the CF Hamiltonian as prefactors of either Stevens operator equivalents or spherical tensor operators.^{13–15} Therefore, it is important to detect as many transitions as possible. Recently, electronic Raman spectroscopy and infrared absorption have been successfully used to study intermultiplet CF excitations in $(R)_{2-x}Ce_xCuO_4(R=Nd, Sm, Pr; x=0.00)$ and 0.15).^{16–21} Sharp *f*-*f* transitions in the visible (R=Nd)have been observed in reflectivity and transmission measurements.²² However, for $(R)Ba_2Cu_3O_{7-\delta}$, reports on the direct measurement of CF excitations by optical techniques are scarce,²³ although indirect observations have been made in NdBa₂Cu₃O_{7- $\delta}$} (Nd123) by Raman scattering from coupled phonon-crystal field excitations.²⁴ In Nd123 a double-peak structure appears in the Raman spectra at low temperature. It is due to the hybridization of the B_{1g} O(2)-O(3) out-of-phase phonon with a nearby CF excitation. Via this coupling, the Raman efficiency of the CF excitation is borrowed from that of the phonon.

In this paper we report a systematic study of CF transitions from the ground state to all higher energy J multiplets of the ⁴I term in NdBa₂Cu₃O₆ by infrared absorption. We show that infrared measurements can be used as a valuable tool for CF studies. This optical technique complements inelastic neutron scattering experiments in a remarkable way, since it can be applied with high resolution to investigate small single crystals and is not limited to low energies.

II. EXPERIMENT

Single crystals of NdBa₂Cu₃O_{7- δ} were grown by the self-flux method described elsewhere.²⁵ In order to reduce the oxygen content, they were annealed in an argon flow at 750 °C for four days. The composition of the single crystals

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was determined by energy-dispersive x-ray (EDX) measurements and by neutron diffraction. A deviation from stoichiometry was found for Nd which has an excess content of about 1%. The oxygen content was derived from the weight change of the samples. For the samples investigated here, we found $\delta > 0.9$. Note that this specimen was already used in the Raman study of Ref. 2. In the following we assume that it has a nominal composition of NdBa₂Cu₃O₆. The infrared (IR) measurements were carried out using a Fouriertransform interferometer (BOMEM), equipped with a quartz halogen lamp, an InSb detector, and a CaF₂ beam splitter. The resolution was 2 cm^{-1} in the 1800–8000 cm⁻¹ range. The single crystals, with approximate dimensions of 1.5 $\times 0.5 \times 0.07$ mm³ were mounted on the cold finger of a helium-cooled flow-through cryostat and studied in two configurations with the *ab* and *ac* planes perpendicular to the direction of the unpolarized incident beam $(\vec{k} \| \vec{c} \text{ and } \vec{k} \perp \vec{c})$, respectively. The spectra were measured over the temperature range from 4.2 to 300 K.

III. RESULTS

Figure 1 shows IR transmittance measurements across ab and ac platelets of NdBa₂Cu₃O₆ obtained at 4.2 K in the regions where ${}^{4}I_{9/2} \rightarrow {}^{4}I_{11/2}$ transitions occur. In Fig. 1(a), the ab-platelet spectrum shows five strong CF absorption bands (filled circles). The existence of the 2092 cm⁻¹ peak is inferred from the much larger width of the 2099 cm⁻¹ feature as compared to, e.g., that at 1995 cm⁻¹. In addition, two weaker CF absorption bands (asterisk) are also observed. The spectrum of the ac platelet in Fig. 1(a) is very similar to that of the ab platelet, except that the lines at 2046, 2063, and 2092 cm⁻¹ are better resolved. In Fig. 1(b), three prominent CF absorption bands (filled circles) show up much stronger in the ac-plane than in the ab-plane spectrum. Four weaker absorption bands (asterisks) are also observed.

In Fig. 2 we present IR spectra in the range of the ${}^{4}I_{9/2}$ $\rightarrow {}^{4}I_{13/2}$ transitions. The spectra of *ab* and *ac* platelets in NdBa₂Cu₃O₆ exhibit several common strong absorption bands (filled circles). Several weaker features are also observed (asterisks), some of them being more prominent in the *ac*-platelet than in the *ab*- platelet spectrum.

IR spectra in the range of transitions from the groundstate manifold to the highest excited multiplet, ${}^{4}I_{9/2}$ $\rightarrow {}^{4}I_{15/2}$, are shown in Fig. 3. In the *ac* spectrum we detect eight prominent CF absorption bands (filled circles). Three weaker bands (asterisks) are also observed. In this region we did not find any absorption bands in the *ab* spectrum due to the very weak transmittance.

IV. DISCUSSION

The ground state manifold of the $4f^3$ configuration in Nd³⁺ is ${}^4I_{9/2}$; it is thus tenfold degenerate. The energies of the next higher multiplets for the free ion are about 2000, 4000, and 6000 cm⁻¹ for ${}^4I_{11/2}$, ${}^4I_{13/2}$, and ${}^4I_{15/2}$, respectively.²⁶ When the Nd³⁺ ion is placed in a D_{4h} site symmetry, as in NdBa₂Cu₃O₆, the ground-state manifold splits into five Kramers degenerate doublets, while the higher multiplets split into 6, 7, and 8 Kramers doublets, respectively.



FIG. 1. IR transmittance spectra across *ab*- and *ac*-oriented platelets of NdBa₂Cu₃O₆. (a) and (b) show different energy intervals of the spectra. The peaks are CF transitions from the ground state manifold, ${}^{4}I_{9/2}$, to levels in the first excited multiplet, ${}^{4}I_{11/2}$. Filled circles and asterisks indicate strong and weak absorption bands, respectively. See text for details.





FIG. 2. IR spectra of CF transitions in NdBa₂Cu₃O₆ from the ground state manifold, ${}^{4}I_{9/2}$, to the second excited multiplet, ${}^{4}I_{13/2}$ (*ab* and *ac* platelets at 4.2 K). (a) and (b) correspond to different energy intervals of the spectra. Filled circles and asterisks indicate strong and weak absorption bands, respectively. See text for details.

In the following we analyze our IR spectra in terms of the CF interaction, the strongest pertubation of free-ion 4f electron states of trivalent *R* ions in cuprates. The CF Hamiltonian is written in terms of one-electron irreducible tensor

FIG. 3. IR spectra of CF transitions in NdBa₂Cu₃O₆ from the ground state manifold, ${}^{4}I_{9/2}$, to the highest excited multiplet, ${}^{4}I_{15/2}$ (*ab* and *ac* platelets at 4.2 K). (a) and (b) correspond to different energy intervals of the spectra. Filled circles and asterisks indicate strong and weak absorption bands, respectively. See text for details.

operators C_{kq} , where the number of nonzero CF parameters depends on the site symmetry. Intermediate coupling²⁷ and J mixing within the entire ⁴I term is taken into account.

The large number of peaks observed in our experimental

TABLE I. CF parameters (in cm⁻¹) obtained from a fit to our IR measurements for CF transitions of Nd³⁺ ions on the regular (D_{4h}) site and calculations with the superposition model for Nd³⁺ on Ba sites (C_{4v}) (see Table II). A set of CF parameters determined previously from INS experiments (Ref. 8) is also shown. The uncertainty of each value is indicated in the brackets.

| Parameter | D_{4h} site (this work, fit) | D _{4h} (Ref. 8) | C_{4v} site (this work, calc.) | |
|------------------------|--------------------------------|-----------------------------|----------------------------------|--|
| B ₂₀ | 380(28) | 565 | 0 | |
| B_{40} | -2956(34) | -2981 | 14 | |
| B_{44} | 1664(25) | 1678 | -364 | |
| B_{60} | 526(15) | 556 | -468 | |
| <i>B</i> ₆₄ | 2021(10) | 1965 | 700 | |

IR spectra indicates that there exists more than one type of Nd site. Therefore we analyze the data in comparison with theoretical predictions for the ${}^{4}I$ spectra of Nd³⁺ ions at regular D_{4h} symmetry sites as well as C_{4n} symmetry Ba sites. For this purpose we use a semiphenomenological superposition model, based on the assumption that contributions from oxygen ligands dominate.¹² This model was found earlier to provide satisfactory predictions for the 4th and 6th order CF parameters of R ions on regular sites in cuprates.^{12,28,29} However, estimates for the 2nd order CF parameters by this model are unreliable due to their strong sensitivity to far-reaching CF interactions.³⁰ Note that ab initio calculations based on the full potential LAPW band structure in the framework of the local density approximation have recently provided good predictions for the 2nd order parameters,³¹ and efforts for their use in the present context are in progress.

In a first step, we calculate the ${}^{4}I$ CF spectrum for Nd³⁺ at D_{4h} sites with the CF parameters obtained by a best-fit treatment of inelastic neutron scattering data from the lowest energy J=9/2 multiplet only.⁸ The resulting ${}^{4}I$ CF spectrum is compared to the prominent peaks of the IR data (filled circles in Figs. 1–3). A rough assignment of intermultiplet transitions is done for the well-isolated experimental absorption bands within 20 cm⁻¹ of predicted CF levels. Together with the J=9/2 levels from INS (0, 90, 155, 286, 933 cm⁻¹)⁸ this yelds a set of J=9/2,11/2,13/2, and 15/2 CF levels which are used for a fit of CF parameters in a next step of refinement.

In a second fit we include in the input data also less wellisolated experimental lines, if they are close to calculated levels of the first fit within a few cm⁻¹. The best-fit CF parameters obtained by this procedure are given in Table I. The free-ion energies of the ${}^{4}I_{J}$ multiplets, varied along with the CF parameters in fitting the data, are 0, 1856, 3821 and 5844 cm⁻¹. Some lines, ascribed in the following to excitations at regular D_{4h} sites, were not included in the fit due to their close proximity to other lines (see Table II). To estimate the CF spectrum for Nd³⁺ ions at Ba sites from these $(D_{4h} \text{ site})$ CF parameters we used the superposition model¹² and ligand positions determined for NdBa₂Cu₃O_{6.12}.³² Due to the inapplicability of this model to 2nd order parameters B_{20} was set to zero. Note that the application of the above mentioned *ab initio* method for these sites would require considerable efforts going beyond the scope of this paper.

The experimental and the calculated CF levels are presented in Table II together with their respective symmetries. The observed absorption bands can be divided into three groups. The first group contains transitions that are assigned to CF levels of Nd^{3+} ions on regular D_{4h} sites. The fit is excellent for all the absorption bands in this group. The second group contains transitions which we ascribe to Nd^{3+} ions on the Ba site (C_{4v}) . Their experimental energies, given in Table II, are very close to the results of the superposition model calculation. The remaining absorption bands fall into a third group which we tentatively associate with Nd³⁺ ions on Ba sites surrounded by one or two chain oxygen ligands (named *defect* in Table II). Such defects may be present due to an incomplete reduction of the samples (see Sec. II). A superposition model calculation indicates that such extra oxygen ions increase the CF level splitting of Nd on Ba sites considerably. However, a quantitative description was not possible, and this assumption remains to be confirmed by further investigations, e.g., for Nd123 with varying oxygen or excess Nd content.

In Table I we compare our fitted $(D_{4h} \text{ site})$ CF parameters with the set obtained from INS measurements.8 The agreement between these data is rather good. However, it is interesting to note that the observation of infrared-active CF bands corresponding to d-d transitions within Nd³⁺ ions placed at the inversion center (the regular R site) is *electric* dipole forbidden. We conjecture that these bands become observable due to slight lattice imperfections related to a small amout of Nd³⁺ ions on the Ba sites, as detected in our experiment. The uncertainty associated with the mechanism which makes the observation of these IR transitions possible prevents us from using transition intensities in the data analysis beyond the ad hoc assignment of most of the strong peaks to transitions from the prevailing Nd^{3+} ions on D_{4h} sites. Note that due to the presence of a large amount of free carriers no transmission measurements can be performed in fully oxygenated samples (i.e., $\delta \approx 0$) of sufficient thickness to reveal dipole forbidden transitions. The quality of the crystal-field excitation wave functions associated with the fitted CF Hamiltonian could be checked, e.g., by calculating neutron scattering intensities or by comparing theory and data of the Zeeman effect in a similar way as has been done in one of our previous Raman studies.³³ Experiments on samples with varing oxygen or Ba content, analogous to the Raman study of Ref. 2, are in progress.

V. CONCLUSIONS

We have observed electric dipole forbidden CF excitations of Nd³⁺ in the infrared transmission spectra of NdBa₂Cu₃O₆. The CF level energies correspond to transitions from the ground state manifold, ${}^{4}I_{9/2}$, to the three higher multiplets ${}^{4}I_{11/2}$, ${}^{4}I_{13/2}$, and ${}^{4}I_{15/2}$. Most of the CF excitations can be assigned to Nd³⁺ ions on the regular *R* site of the compound. Some of the observed CF transitions are assigned to Nd³⁺ ions on Ba sites. From a fit to the infrared measurements we obtain CF parameters which are more precise than those determined by inelastic neutron scattering.

TABLE II. Nd^{3+} CF levels in $NdBa_2Cu_3O_6$ as observed experimentally in the infrared transmission spectra of *ab*- and *ac* -oriented platelets and the corresponding energies obtained from the fit of a CF Hamiltonian to the data (see Table I). The CF levels given for D_{4h} and C_{4v} sites are for the Nd^{3+} ion on the regular site and on the Ba site, respectively. The C_{4v} levels were calculated from the CF parameters for the D_{4h} site levels using the superposition model. Levels in the column labeled *defect* might be associated with Nd^{3+} ions on Ba sites surrounded by one or two chain oxygen ligands. The experimental uncertainty is ± 2 cm⁻¹. Experimental data for the J=9/2 manifold from INS are also included (Ref. 8).

| Multiplet | Experiment | | | Theory | | |
|---------------------------------------|-------------------------|---------------|-------------|---------------|---------------|---------------|
| | D_{4h} site | C_{4v} site | defect | D_{4h} site | Symmetry | C_{4v} site |
| | (cm^{-1}) | (cm^{-1}) | (cm^{-1}) | (cm^{-1}) | $i(\Gamma_i)$ | (cm^{-1}) |
| | | | | | | |
| | 6836 | | | 6833 | 6 | 6193 |
| | 6736 | | | 6736 | 7 | 6192 |
| | 6658 | | 6093 | 6655 | 7 | 6044 |
| | 6624 | | | 6623 | 6 | 5998 |
| ⁴ <i>I</i> _{15/2} | 5927 | | | 5935 | 6 | 5989 |
| | 5842 ^a | | 5826 | 5846 | 6 | 5896 |
| | 5834 ^a | | 5806 | 5831 | 7 | 5864 |
| | 5724 | | | 5723 | 7 | 5776 |
| | 1535 | 4060 | 1573 | 4530 | 7 | 4063 |
| | 4526 | 4000 | 4373 | 4530 | 6 | 4003 |
| | 4505 | 4023 | 4400 | 4523 | 0 | 3081 |
| | 3000 | 3075 | 4400 | 3001 | 7 | 3962 |
| | 3986 | 3964 | 4330 | 3084 | 6 | 3928 |
| 41 | 3036 | 3904 | 4233 | 3036 | 0 | 3928 |
| 113/2 | 3028 | 3912 | 4210 | 3030 | 0 | 3910 |
| | 3928 | 3870 | 4200 | 3930 | / | 3877 |
| | | | 3800 | | | |
| | | | 3886 | | | |
| | | | 3816 | | | |
| | | | | | | |
| | 2568 | 2052 | 2480 | 2568 | 6 | 2050 |
| | 2542 | | 2476 | 2545 | 6 | 2024 |
| | 2092/2099 ^b | | 2456 | 2099 | 7 | 2005 |
| ${}^{4}I_{11/2}$ | 2063 ^b | | 2417 | 2061 | 7 | 1975 |
| | 2046 ^b | | 2405 | 2046 | 6 | 1954 |
| | 1994/1995 | | 2070 | 1992 | 6 | 1939 |
| | 033 ^a | | | 038 | 6 | 273 |
| | 733 206 a | | | 930 202 | 7 | 213 |
| 41 | 200 155 ^a | | | 203 156 | I E | 214 64 |
| 19/2 | 133 00 a | | | 130 | 0 7 | 04 54 |
| | 90 0.ª | | | 0 | 1 | 0 |
| | 0 | | | 0 | 0 | 0 |

^aFrom INS. (Ref. 8).

^bEnergy levels not included in the fitting procedure due to their proximity to other lines.

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