Hall effect in LuNi₂B₂C and YNi₂B₂C borocarbides: A comparative study

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The Hall effect in LuNi₂B₂C and YNi₂B₂C borocarbides has been investigated in normal and superconducting mixed states. The Hall resistivity ρ_{xy} for both compounds is negative in the normal as well as in the mixed state and has no sign reversal below T_c typical for high- T_c superconductors. In the mixed state the behavior of both systems is quite similar. The scaling relation $\rho_{xy} \sim \rho_{xx}^{\beta}$ (ρ_{xx} is the longitudinal resistivity) was found with $\beta = 2.0$ and 2.1 for annealed Lu- and Y-based compounds, respectively. The scaling exponent β decreases with increasing degree of disorder and can be varied by annealing. This is attributed to a variation of the strength of flux pinning. In the normal state weakly temperature dependent Hall coefficients were observed for both compounds. A distinct nonlinearity in the ρ_{xy} dependence on field H was found for LuNi₂B₂C in the normal state below 40 K, accompanied by a large magnetoresistance (MR) reaching +90% for H = 160 kOe at T = 20 K. At the same time for YNi₂B₂C only linear $\rho_{xy}(H)$ dependences were observed in the normal state with an approximately three times lower MR value. This difference in the normal-state behavior of the very similar Lu- and Y-based borocarbides seems to be connected with the difference in the topology of the Fermi surface of these compounds. [S0163-1829(99)11221-9]

I. INTRODUCTION

Investigation of the Hall effect in the normal and superconducting mixed states gives important information about the electronic structure and the vortex dynamics of the investigated materials. The nature of both of them is not settled yet for the superconducting quaternary borocarbides RNi_2B_2C (R=Y, rare earth).^{1,2} Despite the fact that the borocarbides have a strongly anisotropic, layered tetragonal crystal structure, their electronic properties indicate three dimensionality showing only a little anisotropy.³⁻⁹ Borocarbides based on magnetic rare earths show a wide range of competing effects between superconductivity and magnetism; see, e.g., Ref. 10. One of the interesting features of some borocarbides (R = Er, Lu, Y) is the vortex lattice (VL) with unusual square symmetry^{11–14} observed in the mixed state for magnetic fields H directed along tetragonal c axis at $H \ge 1$ kOe. Square symmetry of VL can be connected^{11,8} with the anisotropy of the upper critical magnetic field $H_{c_2}(T)$ observed in the *ab* plane for LuNi₂B₂C.^{8,9} Practically no anisotropy of $H_{c_2}(T)$ was found for YNi₂B₂C,^{6,9}

although this compound is very similar to $LuNi_2B_2C$. The reason for the difference in the behavior of these two boro-carbides is still unclear.

To our knowledge, no data on the Hall effect for LuNi₂B₂C and only few for some other borocarbides are known so far.^{15–18} Namely, normal-state Hall coefficients R_H were found to be negative and only weakly temperature dependent for polycrystalline borocarbides based on R = Y,^{15–17} Ho,^{15,17} La,¹⁵ and Gd.¹⁷ A negative but strongly temperature-dependent Hall coefficient was found for the heavy-fermion-like compound YbNi₂B₂C.¹⁸ No sign reversal of the Hall resistivity ρ_{xy} in the mixed state typical for high- T_c superconductors was observed in YNi₂B₂C,¹⁶ prepared under high pressure. The mixed state Hall effect was not yet systematically studied for borocarbides. Since the mixed state Hall effect may depend on the peculiarities of the vortex lattice, it is of interest to investigate it for LuNi₂B₂C and YNi₂B₂C with an anomalous square VL. Also it is interesting to compare the results on the Hall effect in the normal and in the mixed states for Lu- and Y-based borocarbides,

14 762

having substantially different types of anisotropy of the upper critical field.

The Hall effect in the superconducting mixed state, which was studied up to now mainly for high- T_c superconductors, has recently attracted a considerable attention and should be described in more detail. The magnetic field penetrates into a type-II superconductor by quantum vortices. In a transport current the flux lines experience the Lorentz force density

$$\mathbf{F} = \frac{1}{c} \, \mathbf{j} \times \mathbf{B},\tag{1}$$

where **j** is the transport current density and **B** is the magnetic induction. The motion of vortex lines induces a macroscopic electric field **E** given by the relation¹⁹

$$\mathbf{E} = -\frac{1}{c} \mathbf{v}_L \times \mathbf{B},\tag{2}$$

where \mathbf{v}_L is the velocity of vortex motion. The vortex motion along the Lorentz force (perpendicular to **j**) gives the dissipative field ($\mathbf{E} || \mathbf{j}$) and leads to the flux-flow resistivity. At the same time the vortex motion along the direction of transport current results in the Hall electric field ($\mathbf{E} \perp \mathbf{j}, B$). Thus the Hall effect is a sensitive test of vortex dynamics in the investigated material. On the other hand, normal carriers in the vortex core, experiencing a Lorentz force, can also give a contribution to the mixed state Hall effect by the usual mechanism.

Two unexpected effects have been experimentally found for high- T_c superconductors: (i) a sign reversal of the Hall resistivity ρ_{xy} below T_c and (ii) a striking scaling relationship between ρ_{xy} and the longitudinal resistivity ρ_{xx} in the superconducting transition region, $\rho_{xy} \sim \rho_{xx}^{\beta}$.

Sign reversal of the Hall resistivity ρ_{xy} has been observed experimentally over a range of temperatures and magnetic fields below T_c for several types of high- T_c superconductors, e.g., YBa₂Cu₃O_{7-y},^{20,21} Bi₂Sr₂CaCu₂O₈,^{21,22} Tl₂Ba₂CaCu₂O₈,²³ L_{2-x} Ce_xCuO₄ (L=Nd,Sm),^{24,25} $YBa_2Cu_3O_{7-y}/PrBa_2Cu_3O_{7-y}$ superlattices²⁶⁻²⁸ (YBCO, BSCCO, TBCCO, LCCO, YBCO/PBCO, respectively), as well as for some conventional superconductors: In-Pb alloys, V, Nb (see Ref. 29), $Mo_3Si_{,30}^{30} 2H - NbSe_2$.³¹ This Hall effect anomaly cannot be understood within the framework of the classical Bardeen-Stephen³² and Nozières-Vinen³³ theories of vortex motion predicting the same sign of the Hall voltage for both the superconducting and the normal state. Recently several models based on different approaches have been proposed for the description of this effect (see, e.g., Refs. 34-39 and references therein), but the origin of this phenomenon remains a controversial problem. Meanwhile, the sign reversal of ρ_{xy} below T_c is expected to be not a universal property, but its existence seems to dependent crucially on the peculiarities of the electronic structure.^{35–38} Experimentally the pronounced influence of the doping level on the sign of the Hall voltage close to T_c was observed for various high- T_c cuprates.^{40,41} The sign reversal of the Hall effect disappears for heavily underdoped⁴⁰ and strongly overdoped⁴¹ regimes.

Scaling behavior, $\rho_{xy} \sim \rho_{xx}^{\beta}$, in the superconducting mixed state was observed by Luo *et al.*⁴² for an YBCO thin film

 $(\beta = 1.7)$. The same relationship was also found for several types of high- T_c superconductors: YBCO single crystals (β ≈ 1.7),⁴³ BSCCO ($\beta \approx 2$),²² TBCCO ($\beta \approx 2$),^{23,44} LCCO $(\beta \approx 0.8)$,²⁵ (YBCO/PBCO) superlattices $(\beta \approx 1.7)$.^{28,26} In a recent investigation of superconducting indium thin films scaling with β value 2-3 was observed.⁴⁵ Theoretically, Dorsey and Fisher⁴⁶ (DF) have interpreted the observed behavior in the framework of glassy scaling near a vortex-glass transition. In their model, assuming the existence of a vortexglass transition in a three-dimensional vortex system, the region where scaling behavior should be observed is restricted to a narrow region near the vortex-glass transition. However, it should be mentioned that scaling behavior was observed far beyond the possible vortex-glass transition.²¹ A phenomenological model, based on an entirely different approach, has been proposed by Vinokur et al.,47 who have calculated the effect of pinning on the Hall resistivity. In their model the Hall conductivity $\sigma_{xy} \cong \rho_{xy} / \rho_{xx}^2$ ($|\rho_{xy}| \ll \rho_{xx}$) is independent of disorder and the scaling law $\rho_{xy} \sim \rho_{xx}^2$ is believed to be a general feature of any vortex state with disorderdominated dynamics. Therefore the value of $\beta = 2$ should not depend on the degree of disorder. On the other hand, Wang, Dong, and Ting⁴⁸ (WDT) recently modified their earlier work,³⁴ based on the normal core model proposed by Bardeen and Stephen.³² They developed a theory for the Hall effect including both pinning and thermal fluctuations. In the WDT theory scaling and sign reversal of ρ_{xy} are explained by specially taking into account the backflow current of vor-tices due to pinning.⁴⁸ Thereby β changes from 2 to 1.5 as the pinning strength increases.^{34,48} Controversial experimental results have been reported on the influence of disorder on the mixed state Hall effect. For irradiated YBCO samples, β was found to be 1.5 ± 0.1 compared to 2 ± 0.2 for unirradiated ones,⁴⁹ in accordance with WDT (see also Refs. 26–28). However, no influence of disorder on the scaling exponent was observed for TBCCO irradiated by heavy ions. In that case, $\beta = 1.85$ holds even after irradiation²³ (see also Ref. 50). A strong influence of pinning on the Hall effect in the mixed state was observed of YBCO single crystals.⁵¹ At the same time it was pointed out in Ref. 40 that pinning effects cannot be the only reason for the Hall anomaly for YBCO single crystals. All these controversial results show that more work is necessary for better understanding of the mixed state Hall effect and the influence of disorder on it.

Very recently Wang and Maki⁵² have interpreted the anisotropy of $H_{c_2}(T)$ observed for borocarbides in terms of a three-dimensional version of $d_{x^2-y^2}$ superconductivity. Possible *d*-wave nature of superconductivity for borocarbides gives an additional motivation for further study of their electronic properties. In the present study we have investigated the Hall effect in the normal as well as in the mixed state for LuNi₂B₂C and YNi₂B₂C compounds prepared under the same conditions. The results for LuNi₂B₂C have been briefly reported in Ref. 53.

II. EXPERIMENTAL DETAILS

Polycrystalline $LuNi_2B_2C$ (in the following denoted as PC AN) and YNi_2B_2C samples were prepared by arc melting in Ar atmosphere and subsequent careful annealing at

1100 °C, as described in more detail in Ref. 54. The phase purity of the samples was checked by x-ray diffraction on a Philips PW 1820 system with CoK_{α} radiation. The reflections revealed practically a single phase. The lattice parameters were a = 3.464 Å, c = 10.635 Å for LuNi₂B₂C and a = 3.528 Å, c = 10.546 Å for YNi₂B₂C. Bar-shaped samples were cut from the ingots. Typical dimensions of the samples were $3 \times 1 \times 0.3$ mm³. Hall contacts with typical misalignment of less than 0.1 mm were used (this is essential because the maximum of the Hall voltage does not exceed several tens of nanovolts). At each point the Hall voltage was measured for two inverse directions of the magnetic field. Most measurements of the Hall effect and of the ac susceptibility were done in magnetic fields up to 50 kOe using a Lake Shore model 7225 susceptometer with Keithley 182 nanovoltmeter and PAR-5209 Lock-in amplifier. Some measurements in magnetic fields up to 160 kOe were performed using an Oxford Teslatron system. The values of electrical current were 10-20 mA for dc measurements and 1 mA for ac ones. The magnetoresistance (MR) was measured by the standard four-probe method. For comparison some measurements were performed on an unannealed LuNi₂B₂C sample (denoted as PC UNAN) wich has a considerably higher degree of disorder.

III. RESULTS AND DISCUSSION

A. Resistivity and upper critical magnetic field

The experiments in the present work have been performed on polycrystalline samples (to the best of our knowledge, no data on the Hall effect for single crystalline borocarbides have been reported so far). For characterization of our samples the results on resistivity, upper critical field and magnetoresistance for them will be compared with data known for single crystals.

The temperature dependencies of the longitudinal resistivity $\rho_{xx}(T)$ for the annealed LuNi₂B₂C and YNi₂B₂C samples are depicted in Fig. 1. The $\rho_{xx}(T)$ curves obtained at H =50 kOe and 160 kOe are also shown. The resistivity of both compounds exhibits a weak temperature dependence just above superconducting transition temperature T_c . Both samples have a rather sharp superconducting transition, a low resistivity at low temperatures and high values of T_c and residual resistance the ratio RRR [RRR $=\rho_{xx}(300 \text{ K})/\rho_{xx}(17 \text{ K})$]. These parameters are compared in Table I with those reported recently for $LuNi_2B_2C$ and YNi₂B₂C single crystals.^{55,9,7,8} It should be pointed out that the resistivity of borocarbides is practically isotropic. The small difference ($\approx 2\%$) between the in-plane resistivity ρ_a and the resistivity along the c axis ρ_c observed for YNi₂B₂C single crystals⁷ at T=15-300 K is well within the experimental uncertainty. Thus it is reasonable to compare the values of resistivity for polycrystalline and single crystalline borocarbides.

More precisely, the value of $\rho_{xx}(17 \text{ K})$ for the annealed polycrystalline LuNi₂B₂C sample is 2.7 $\mu\Omega$ cm, which is close to that for LuNi₂B₂C single crystals (1.6–2.5 $\mu\Omega$ cm, Refs. 55,9,7,8), see Table I. The value of RRR is 41 for our LuNi₂B₂C sample, which is *significantly higher* than those observed for single crystals (23–27, see Refs. 55,9,7). Also

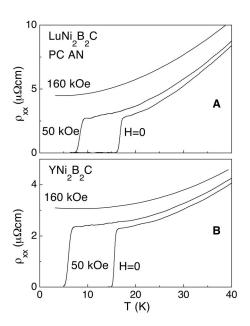


FIG. 1. Longitudinal resistivity ρ_{xx} as a function of temperature *T* at H=0, 50, and 160 kOe for the annealed LuNi₂B₂C and YNi₂B₂C samples.

the value of $T_c = 16.7$ K is slightly higher than that reported for single crystals (15.8–16.5 K, see Refs. 55,9,7,8). The width of the superconductig transition ΔT_c (determined from zero field ac-susceptibility curve, see Fig. 3) is 0.27 K which is close to the values 0.2–0.25 K typical for single crystals.^{55,9,7} The PC UNAN LuNi₂B₂C sample has a lower T_c (14.7 K), a wider superconducting transition, and a more than one order of magnitude higher value of $\rho_{xx}(17 \text{ K})$.

For the polycrystalline YNi₂B₂C sample the values of $\rho_{xx}(17 \text{ K})$, RRR, T_c , and ΔT_c are also comparable with the results reported for YNi₂B₂C single crystals,^{55,9,7} see Table I. At the same time our YNi₂B₂C sample has an approximately two times lower RRR value than LuNi₂B₂C prepared under the same conditions.

The results for the resistivity $\rho_{xx}(300 \text{ K})$ collected in Table I show surprisingly large discrepancies even for the single crystals. Thus an intersection of the $\rho_{xx}(T)$ dependences can be recognized for the two YNi2B2C single crystals.^{55,9} These facts could be naturally understood taking into account the large uncertainty in geometrical factor used to determine the value of ρ_{xx} from the experimentally measured resistance especially for small single crystals. To clarify this, linear $\rho_{xx}(T)$ dependences for two imaginary samples of the same imaginary compound with different RRR values (10 and 4 for samples A and B, respectively) have been plotted in Fig. 2. Mattissen's rule is expected to be valid for them, i.e., the difference in resistivities does not dependent on temperature. Let us suppose, that the measurements of $\rho_{xx}(T)$ give the "true" values for the sample A and underestimate it by 1/3 of its true value for the sample B (e.g., due to the uncertainty in the dimensions of the sample, final width of the contacts, etc.). In that case for the sample B the obtained ("measured") $\rho_{xx}(T)$ curve (denoted as B' on Fig. 2 and having the same value of RRR as the curve B) will cross the curve for the sample A. This example illustrates that an uncertainty of geometrical factor of $\approx 20-30\%$ could explain the difference in room-temperature resistivities

TABLE I. Resistivity ρ_{xx} at 300 and 17 K, residual resistance ratio RRR, critical temperature T_c , transition width ΔT_c , $|\partial H_{c_2}/\partial T|$ and magnetoresistance MR for LuNi₂B₂C and YNi₂B₂C polycrystals (our results) and single crystals (data from Refs. 55, 9, 7, and 8).

	Polycrystals				Single crystals					
	Lu	Y	Lu ^a	Lu	Lu	Lu	Lu	Y	Y	Y
	annealed		UN	[55]	[9]	[7]	[8]	[55]	[9]	[7]
$\rho_{xx}(300 \text{ K}) \ (\mu\Omega \text{ cm})$	110	50	134	68	47	36		108	67	36
$\rho_{xx}(17 \text{ K}) \ (\mu \Omega \text{ cm})$	2.7	2.3	43	2.5	1.9	1.6	1.7	2.5	3.8	2.1
RRR	41	22	3.1	27	25	23		43	18	17
T_c (K)	16.7	15.5	14.7	16.5	16.1	16.0	15.8	15.7	15.6	15.7
ΔT_c (K)	0.27	0.44	0.6	0.2	0.25			0.2	0.25	
$\left \partial H_{c_2} / \partial T \right $ (kOe/K) ^b	6.8	6.0	5.8	6.4	6.2		6.7	7.1	6.1	
MR(20 K, 50 kOe) (%)	25	10	0.7		7.3 ^c				7.5 ^d	
MR(20 K, 160 kOe) (%)	90	33	2.3							

^aUnannealed (PC UNAN) LuNi₂B₂C sample.

^bFor details of the $\left| \partial H_{c_2} / \partial T \right|$ determination for different samples, see text.

^cThe value obtained at $\tilde{T} = 20$ K and H = 45 kOe (H||c).

^dThe value obtained at T = 15 K and H = 45 kOe (H||c).

and surprising intersection of the $\rho_{xx}(T)$ dependences for the two YNi₂B₂C single crystals.^{55,9} A strong support for this explanation is that, for single crystals of different quality known, one would expect close resistivity values rather at room temperature than at low temperatures. We conclude that the quality of the borocarbide samples compared in Table I can be mainly judged from the RRR data, whereas resistivity values are strongly influenced by the uncertainty in the geometrical factor used for determination of ρ_{xx} . Noteworthy is that both room- and low-temperature resistivities for our LuNi₂B₂C sample are close to those reported for the YNi₂B₂C single crystal which has a similar value of RRR (Ref. 55) as our policrystalline LuNi₂B₂C sample (see Table I).

Superconducting transitions determined from acsusceptibility measurements are shown in Fig. 3 for different magnetic fields. Temperature dependences of upper critical magnetic fields $H_{c_2}(T)$ are depicted on Fig. 4 for the annealed and unannealed LuNi₂B₂C samples. [The value of H_{c_2} was determined, similar as in Ref. 8, by the extrapolation of the ac-susceptibility curve to zero susceptibility value, see Fig. 3(a).] For comparison the data from Ref. 8 for

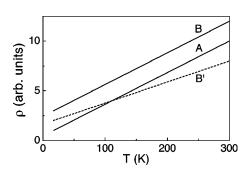


FIG. 2. Temperature dependence of the resistivity for two imaginary samples (A and B) with different RRR values (10 and 4, respectively). Line B' corresponds to the underestimated by 1/3 of ρ for sample B and has the same value of RRR as line B. See text for details.

a LuNi₂B₂C single crystal (SCR) with $H || \langle 110 \rangle$ are also shown. The upward curvature (UC) in the $H_{c_2}(T)$ dependence is clearly visible near T_c . Note that, in accordance with Ref. 55, the UC region is more pronounced and $|\partial H_{c_2}/\partial T|$ is higher for the annealed PC AN sample. This suggests⁵⁵ that this sample is close to the clean limit in terms of traditional theory of type-II superconductors. It is of interest to compare $|\partial H_{c_2}/\partial T|$ values for different samples determined from the approximately linear parts of the $H_{c_2}(T)$ dependences (H=20–50 kOe). The value of $|\partial H_{c_2}/\partial T|$

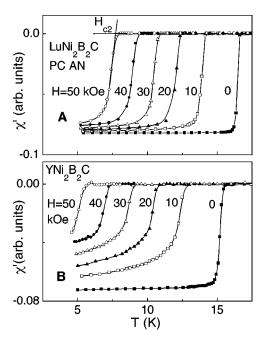


FIG. 3. Temperature dependence of the real part of the acmagnetic susceptibility for the LuNi₂B₂C (A) and YNi₂B₂C (B) samples in several magnetic fields. The upper critical field H_{c2} was determined by linear extrapolation of the ac-susceptibility curve to zero susceptibility value, as shown in the upper part of the figure. Lines are guides for the eye.

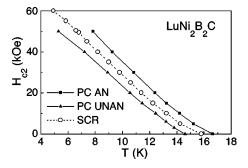


FIG. 4. Temperature dependence of the upper critical field H_{c_2} for three LuNi₂B₂C samples. Open symbols are the results of Ref. 8 for single crystal. Solid symbols are the results for PC AN and PC UNAN polycrystalline samples (see text). Lines are guides for the eye.

=6.8 kOe/K, obtained for the annealed LuNi₂B₂C sample, is in good agreement with those determined for single crystals: 6.7 kOe/K (calculated by arithmetic averaging of $|\partial H_{c_2}/\partial T|$ data reported in Ref. 8 for three directions of H, $\|\langle 100 \rangle$, $\langle 110 \rangle$, and $\langle 001 \rangle$), 6.4 kOe/K (reported for $H\|\langle 001 \rangle$ for another single crystal in Ref. 55) and 6.2 kOe/K (calculated by arithmetic averaging of the data reported in Ref. 9 for $H\|\langle 100 \rangle$ and $\langle 001 \rangle$). The $H_{c_2}(T)$ dependence for our YNi₂B₂C sample is similar to that observed for the LuNi₂B₂C PC AN one and also is in good agreement with the results reported for YNi₂B₂C single crystals.^{55,9} The value of $|\partial H_{c_2}/\partial T|$ for our YNi₂B₂C sample is 6.0 kOe/K, see Table I.

The low resistivity just above T_c , high RRR and T_c values, narrow superconducting transitions, pronounced UC region in the $H_{c_2}(T)$ dependences, and x-ray diffraction results give evidence for a good quality of our annealed LuNi₂B₂C and YNi₂B₂C samples.

B. Normal-state Hall effect

The temperature dependences of the Hall resistivity, $\rho_{xy}(H)$, for LuNi₂B₂C PC AN and PC UNAN samples as well as for YNi₂B₂C sample in the normal and in the mixed states are shown in Fig. 5. First of all, it should be emphasized that the Hall resistivity of all the samples is negative at $3.3 \le T \le 300$ K, and has no sign reversal below T_c .

In the normal state, a pronounced nonlinearity in the $\rho_{xy}(H)$ dependences is evident at $T \leq 40$ K for both LuNi₂B₂C samples. Linear $\rho_{xy}(H)$ dependences extrapolated from the low fields region are also shown in Fig. 5 by dashed lines. The deviation from linear $\rho_{xy}(H)$ dependence increases with lowering temperature. The anomaly is more pronounced for the annealed sample, although it is also distinctly seen for the unannealed one. More clearly the nonlinearity in the $\rho_{xy}(H)$ dependences can be seen in the insets of Figs. 5(a) and 5(b) where some results obtained in high magnetic fields (up to 160 kOe) are presented. It should be underlined that no nonlinearity in the $\rho_{xy}(H)$ dependence was observed for our YNi₂B₂C sample [see the inset of Fig. 5(c)]. Earlier, linear $\rho_{xy}(H)$ dependences have been reported for YNi₂B₂C (Ref. 16) and YbNi₂B₂C (Ref. 18) samples prepared under high pressure. No indications of nonlinear

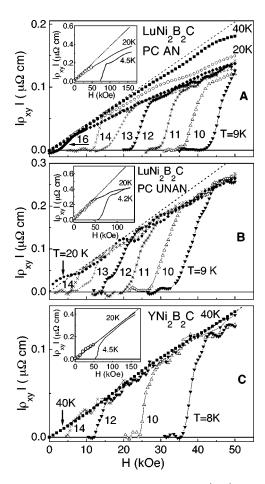


FIG. 5. Absolute value of the Hall resistivity $|\rho_{xy}|$ as a function of magnetic field *H* for the annealed (A) and unannealed (B) LuNi₂B₂C as well as for YNi₂B₂C (C) samples. The dashed lines are low-field asymptotes to the normal state curves. The inserts show the results for *H* up to 160 kOe. Open circles in the insets denote the data obtained for $H \leq 50$ kOe. Only some representative curves and data points are shown.

 $\rho_{xy}(H)$ dependences have been observed for Y-, Ho-, Gd-, and La-based borocarbides.^{15,17} Thus the nonlinearity in the $\rho_{xy}(H)$ dependence, found for LuNi₂B₂C samples with essentially different quality, can be considered as an intrinsic and specific property of the Lu-based borocarbide.

A nonlinear and even nonmonotonous $\rho_{xy}(H)$ dependence has been found earlier for the heavy fermion superconductor UBe₁₃ (Ref. 56) and has been interpreted in the framework of a two-band model.⁵⁶ In this model, at low fields, the light carriers with high mobilities give the prevalent contribution to the Hall effect, whereas at high fields the contribution of the heavier carriers having lower mobilities is more significant. Very recently a similar two-band model⁵⁷ has been used to interpret the results on the transport properties of Nd_{2-x}Ce_xCuO₄ epitaxial thin films. In an entirely different type of multiband models,⁵⁵ the existence of at least two bands with significantly different Fermi velocities was found to be very essential for the quantitative description of $H_{c_2}(T)$ curves with sizable UC for the Lu- and Y-based borocarbides. Several groups of carriers with different effective masses have been directly observed for YNi2B2C in dHvA experiments.⁵⁸ Thus some kind of a two-band model

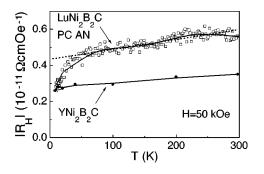


FIG. 6. Absolute value of the Hall coefficient $|R_H|$ (obtained at H = 50 kOe) as a function of temperature *T* for LuNi₂B₂C and YNi₂B₂C samples. Dotted line is linear extrapolation of high temperature data for LuNi₂B₂C. Solid lines are guides for the eye.

may be applicable for understanding of the nonlinear $\rho_{xy}(H)$ dependence found by us for LuNi₂B₂C borocarbide.

In Fig. 6 the temperature dependences of the Hall coefficients $R_H(T) = \rho_{xy}(T,H)/H$ at H = 50 kOe are shown for the annealed LuNi₂B₂C and YNi₂B₂C samples. Below ~ 60 K the $R_H(T)$ dependence for LuNi₂B₂C shows a considerable deviation from the dotted line describing $R_H(T)$ at H = 50 kOe for higher temperatures. This deviation is obviously connected with the nonlinearity in $\rho_{xy}(H)$ curves shown in Fig. 5(a). At low temperatures the values of the Hall coefficient on the dotted line in Fig. 6 [obtained by the extrapolation of the high-temperature $R_H(T)$ curve] coincide with the values of the low-field Hall coefficient, calculated at low temperatures using the low-field asymptotes for the $\rho_{xy}(H)$ curves [shown in Fig. 5(a) by dashed line]. Only weak temperature dependences were observed for the lowfield Hall coefficients of LuNi2B2C and YNi2B2C borocarbides. This is in agreement with the observation of a weak $R_H(T)$ dependence for YNi₂B₂C in Refs. 15–17. Weak $R_H(T)$ dependences were reported also for La-, Ho-, and Gd-based borocarbides.^{15,17} Below ~60 K, the $R_H(T)$ curve obtained for LuNi₂B₂C at H = 50 kOe exhibits a pronounced temperature dependence connected with the nonlinearity found for $\rho_{xy}(H)$ at low temperatures. Noteworthy is that a strong decrease of the Hall coefficient was found with increasing temperature for YbNi₂B₂C (Ref. 18) borocarbide having moderate heavy-fermion-like behavior. The values of R_H obtained in this work for LuNi₂B₂C and YNi₂B₂C are comparable with those earlier reported for YNi_2B_2C ,^{15,17} but they are about five times (LuNi2B2C) or ten times (YNi₂B₂C) smaller than the value resulting from bandstructure calculations⁴ for LuNi₂B₂C $(3 \times 10^{-9} \text{ m}^3/\text{C})$ $= 3 \times 10^{-11} \ \Omega \text{ cm/Oe}$). These deviations may be caused by correlation effects in borocarbides. The estimation of the carrier density from the R_H value at T=300 K, by using a single band model which is a rough approximation, gives 1.5 and 2.4 carriers per unit cell for Lu- and Y-based borocarbides, respectively. (The estimation of the carrier density for YNi₂B₂C prepared under high pressure gives 0.6 carriers per unit cell,¹⁶ i.e., about four times smaller than present result and values reported in Refs. 15 and 17. Probably this difference is connected with high sensitivity of the Hall coefficient for method of sample preparation.)

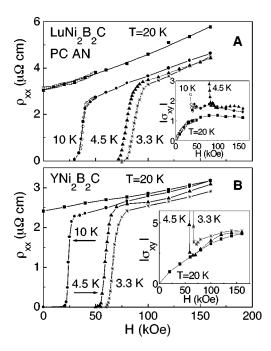


FIG. 7. Magnetic-field dependence of the longitudinal resistivity ρ_{xx} for LuNi₂B₂C and YNi₂B₂C. In the insets absolute value of the Hall conductivity $|\sigma_{xy}|$ (in $10^{-2} \mu \Omega^{-1} \text{ cm}^{-1}$) vs field is shown. Open circles in part A denote the results obtained for $H \leq 50$ kOe. Lines are guides for the eye.

C. Normal-state magnetoresistance

In Fig. 7 the field dependence of the longitudinal resistivity $\rho_{xx}(H)$ is shown for the annealed LuNi₂B₂C and LuNi₂B₂C samples. The values of magnetoresistance,

$$MR = \frac{\rho_{xx}(H) - \rho_{xx}(0)}{\rho_{xx}(0)},$$
(3)

for the annealed LuNi₂B₂C sample at T = 20 K are as high as 25 and 90% for H = 50 and 160 kOe, respectively (see also Fig. 1). At the same time considerably smaller values of MR were observed at these fields (10 and 33%, respectively) for the YNi₂B₂C sample, prepared under the same conditions as the Lu-based one, see Table I. It should be emphasized, that a magnetoresistance of only $\approx 7.3\%$ was observed, at H =45 kOe and T=20 K, for a LuNi₂B₂C single crystal with RRR=25 (*H* parallel to the tetragonal c axis),⁹ i.e., the value of MR for our LuNi₂B₂C polycrystalline sample is about 3.5 times higher, than that of this single crystal. The value of MR (7.5%) reported in Ref. 9 for YNi_2B_2C single crystal with RRR=18 ($H \| c$) is comparable with that found for investigated YNi₂B₂C sample. High values of MR can be considered as an additional indication of the high quality of our annealed samples, because the value of MR for the unannealed sample is approximately 40 times smaller (see Table I). It should be also noted that the impurities of magnetic rare earths, the concentration of which could be greater in Lubased sample than in Y-based one, cannot lead to the increase of MR, because the introduction of magnetic ions to nonmagnetic substance (e.g., borocarbide lattice) gives the negative contribution to MR due to decrease of spin-disorder scattering in a magnetic field, see, e.g., Refs. 7 and 16.

A possible reason for the very large positive MR in LuNi₂B₂C and for the significantly larger MR of the polycrystalline sample compared to the single crystal in Ref. 9 is the formation of open orbits on the Fermi surface of that compound for $H \perp c$. (In principle the possibility of the formation of open orbits for borocarbides was pointed out in band-structure calculations.^{5,3} In Ref. 5, e.g., it was claimed that one part of the Fermi surface is a cylinder along the caxis.) It is well known⁵⁹ that open orbits can lead to large values of MR $\propto H^2$, whereas closed orbits should give rise to saturation of magnetoresistance for large H. In that case, for polycrystals, the averaging of MR should lead to a practically linear $\rho_{xx}(H)$ dependence⁵⁹ (so-called Kapitza's law). In accordance with this, the observed $\rho_{xx}(H)$ dependences for our LuNi₂B₂C PC AN sample follow approximately a linear law; see Fig. 7. The MR(H) dependence for polycrystals, in the case of open orbits for some directions of H, should be stronger than that observed for single crystals for $H \| c$ where only closed orbits could be expected. Therefore the significantly larger MR found for the LuNi₂B₂C polycrystals, in comparison with that observed for the single crystal for $H \| c$, can be considered as an indication for the open-orbits formation in LuNi₂B₂C for $H \perp c$. Investigation of the MR in high fields for LuNi₂B₂C single crystals with the two configurations (i) $\mathbf{j} \| c$ and $H \perp c$ and (ii) $\mathbf{j} \perp c$ and $H \| c$ are necessary to check this conclusion.

The nonlinear $\rho_{xy}(H)$ dependence and the large MR, found in this study, as well as the anisotropy of H_{c_2} in the *ab* plane,^{8,9} earlier reported for LuNi₂B₂C, may be caused by the same reason, namely, by peculiarities of its electronic structure. It should be underlined, that all these anomalies are absent for YNi₂B₂C. [For YNi₂B₂C a linear $\rho_{xy}(H)$ dependence and a substantially smaller MR can be seen in Fig. 7 and only a very small anisotropy of $H_{c_2}(T)$ were reported in Refs. 6 and 9.] The differences in the properties of these very similar compounds should be connected with difference between their electronic structure. As has been noted in Ref. 3 the Fermi-surface topology of the borocarbides is very sensitive to the position of the Fermi level, which may be slightly different for the two cases, Lu and Y, due to, e.g., different lattice constants. From the obtained results the formation of open orbits seems to be easier in the case of LuNi₂B₂C in comparison with YNi₂B₂C. Nevertheless, only the comparative study of LuNi₂B₂C and YNi₂B₂C single crystals (e.g., investigation of the angular dependence of MR in high fields) can give definitive verification of the proposed model.

Theoretically, it is more convenient to describe the behavior of the Hall effect in terms of the conductivity tensor rather than by the resistivity one; see, e.g., Ref. 59. As shown in the inset of Fig. 7(a), the nonlinearity in the dependence on magnetic field of the Hall conductivity, $\sigma_{xy}(H)$, in the normal state for LuNi₂B₂C is even more pronounced than the nonlinearity in the Hall resistivity curve $\rho_{xy}(H)$ (σ_{xy} $\cong \rho_{xy}/\rho_{xx}^2$, $\rho_{xx} \gg |\rho_{xy}|$). It is interesting to note that σ_{xy} for LuNi₂B₂C becomes practically independent of the magnetic field for H=80-160 kOe, at T=4.5-20 K [see Fig. 7(a)]. The nonlinear $\rho_{xy}(H)$ dependence and the large MR of LuNi₂B₂C are probably closely connected and result in a practically constant $\sigma_{xy}(H)$ at high magnetic fields. The reason why σ_{xy} is independent of *H* for high fields, resulting in $\rho_{xy} \sim \rho_{xx}^2$ in the *normal state*, is not yet understood. (It is noteworthy that $\rho_{xy} \sim \rho_{xx}^2$ scaling in the *normal state* was earlier observed for the superconducting heavy fermion compound UBe₁₃.⁵⁶) At the same time the Hall conductivity of YNi₂B₂C has only a slight nonlinearity at T=20 K [see the inset of Fig. 7(b)]. Only at T=4.5 and 3.3 K some tendency for saturation in $\sigma_{xy}(H)$ dependences was observed in high fields.

D. Mixed state Hall effect

In the mixed state, the variation of the Hall resistivity with magnetic field for both compounds can be described as follows: below T_c in low fields there is $\rho_{xy}=0$ as can be seen from the $\rho_{xy}(H)$ curves at, e.g., T = 10 K [Figs. 5(a)-5(c)]. At higher fields (in the region close to the resistive superconducting transition) the Hall resistivity increases in the absolute value and gradually reaches the $\rho_{xy}(H)$ curve obtained in the normal state at temperatures slightly higher than T_c . For YNi₂B₂C the normal-state $\rho_{xy}(H)$ dependence is very close to linear [see the curve obtained at T=40 K in Fig. 5(c)]. At the same time, for both LuNi₂B₂C samples the normal state $\rho_{xy}(H)$ dependences have a nonlinearity with negative curvature. This nonlinearity, as it was pointed out above, is more pronounced for the annealed sample; see Figs. 5(a) and 5(b). The Hall resistivity curve $\rho_{xy}(H)$ in the mixed state shifts with increasing temperature to lower magnetic fields similar to the behavior usually observed for the longitudinal resistivity curve $\rho_{xx}(H)$. Simultaneously the $\rho_{xy}(H)$ and $\rho_{xx}(H)$ transitions are shown in the insets of Fig. 8 for all samples. Their comparison is discussed below.

For LuNi2B2C as well as YNi2B2C no sign reversal of $\rho_{xy}(H)$, typical for high- T_c superconductors, was observed below T_c . The sign of the Hall resistivity is negative in the mixed as well as in the normal state. It should be noted, that for high- T_c superconductors not only the holelike materials, but also the electronlike ones usually experience sign reversal of the Hall effect (see, e.g., Ref. 25). The behavior of the two LuNi₂B₂C samples with significantly different quality (the RRR value for the PC UNAN is only \approx 3) in the mixed state is quite similar. Also the behavior of YNi₂B₂C in the mixed state is similar to that of LuNi₂B₂C. Therefore the absence of the sign reversal of the Hall effect seems to be an intrinsic property of the investigated borocarbides. This result has been obtained on polycrystalline samples, but, as has been discussed above, the anisotropy of the electronic properties of borocarbides is small, and the quality of our annealed samples is high. Therefore this conclusion should remain true also for the borocarbide single crystals. (For high- T_c superconductors, having considerably higher anisotropy in electronic properties, sign reversal in the Hall effect was observed usually for both poly- and single crystalline samples of the same system.)

In order to understand the absence of sign reversal in the ρ_{xy} for the investigated borocarbides, the following physical picture of the Hall effect in the mixed state^{35,36} can be used. There are two contributions to the Hall conductivity σ_{xy} in the superconducting state:

$$\sigma_{xy} = \sigma_n + \sigma_{sc} \,, \tag{4}$$

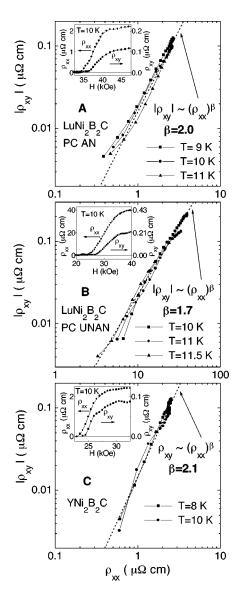


FIG. 8. $|\rho_{xy}|$ vs ρ_{xx} for the annealed (A) and unannealed (B) LuNi₂B₂C as well as for the YNi₂B₂C (C) samples. In the insets $|\rho_{xy}|$ and ρ_{xx} vs magnetic field are simultaneously shown for T = 10 K.

where σ_n is connected with normal quasiparticles that experience a Lorentz force in the vortex core (it is expected to be proportional to H) and σ_{sc} is an anomalous contribution connected with the motion of vortices parallel to the electrical current density j. In Refs. 35 and 36 it was claimed that $\sigma_{sc} \sim 1/H$ and could have a sign *opposite* to that of σ_n . Therefore at low magnetic fields, the $\sigma_{sc}(H)$ term is more essential but at higher fields $\sigma_n(H)$ will be dominant. If σ_{sc} has a different sign than σ_n it is possible to observe a sign reversal in the Hall effect at $T < T_c$.^{35,36} Equation (4) was verified and the term $\sigma_{sc} \sim 1/H$ was observed, e.g., for YBCO.⁶⁰ For LuNi₂B₂C and YNi₂B₂C the Hall conductivity decreases with increasing H, as can be clearly seen in the insets of Fig. 7 for the σ_{xy} vs H curves at $T < T_c$. At the same time it should be pointed out that observed σ_{xy} vs H dependences seem to change more rapidly than 1/H. A similar behavior was observed for cuprates; see, e.g., Refs. 61 and 41. Therefore the mechanism of the mixed state Hall effect connected with vortex motion seems to work for borocarbides as well. In theory³⁶ the sign of the Hall effect in the mixed state is determined by the energy derivative $\partial N(0)/\partial \mu$ of the density of states N(0) averaged over the Fermi surface. For a complicated Fermi surface which has electronlike and holelike parts the signs of σ_{xy} in the normal and in the mixed states may be different. In the phenomenological theory, based on Ginsburg-Landau equation and its gauge invariance,³⁷ the sign of the Hall conductivity is determined by $\partial \ln T_c / \partial \mu$, where μ is the chemical potential. In any case, the sign of the Hall effect in the mixed state depends on the details of the band structure (see also Ref. 38). From our results it follows, that, contrary to the case of high- T_c superconductors, the signs of σ_n and σ_{sc} for borocarbides are the same (see the insets of Fig. 7). This seems to be the reason for the absence of sign reversal in the Hall effect in these borocarbides.

In the mixed state two regions concerning the behavior of ρ_{xy} and ρ_{xx} can be distinguished. At low magnetic fields both ρ_{xy} and ρ_{xx} vanishes. For higher fields it is clearly seen that the scaling behavior $|\rho_{xy}| = A \rho_{xx}^{\beta}$ holds for all three samples (see Fig. 8). The values of β are 2.0±0.1 and 2.1 ± 0.1 for Lu- and Y-based annealed samples, respectively. It decreases to 1.7±0.1 for unannealed LuNi₂B₂C sample having a one order of magnitude higher resistivity at T = 17 K. This may be connected with an increase of pinning strength for the PC UNAN due to the considerably larger concentration of defects leading to the larger resistivity of this sample. The decrease of the scaling exponent with increasing pinning strength was obtained in the WDT theory⁴⁸ taking into account the backflow current of vortices due to the effects of pinning. Another manifestation of the pinning effects, predicted by the WDT model, can be seen in the insets of Fig. 8 where the $\rho_{xy}(H)$ and $\rho_{xx}(H)$ curves in the superconducting transition region are simultaneously shown. For decreasing fields, ρ_{xx} vanishes at definitely lower values of H than $|\rho_{xy}|$ for all three samples. The same behavior was described by WDT taking into account the effect of pinning. In accordance with Ref. 34, the Hall resistivity can be observed only in the flux flow regime of superconducting transition. Prior to the flux flow, the longitudinal resistivity may become finite due to flux creep at finite temperature, while the Hall resistivity is still zero. [Vortices in the flux creep regime are pinned, and they are only able to creep along the $\mathbf{j} \times \mathbf{B}$ direction assisted by thermal activation. Creep of flux lines in this direction, in accordance with Eq. (2), does not lead to a Hall voltage.] From the obtained results it is obvious that pinning effects are considerably important for the mixed state Hall effect in the investigated borocarbides. However, as for high- T_c cuprates (see, e.g., Refs. 40 and 41) not only pinning effects will govern the mixed state Hall effect in borocarbides.

IV. CONCLUSIONS

We have investigated the Hall effect for LuNi₂B₂C and YNi₂B₂C borocarbides in the normal and in the superconducting mixed state. A negative and only slightly temperature-dependent low-field Hall coefficient was found for both compounds above T_c . The value of the Hall coefficient R_H is about one order of magnitude smaller, than that resulting from band-structure calculations.⁴ A pronounced

nonlinearity in the field dependence of the Hall resistivity $\rho_{xy}(H)$ was found for LuNi₂B₂C in the normal state below 40 K accompanied by a very large positive magnetoresistance MR. An only linear $\rho_{xy}(H)$ dependence was observed for YNi₂B₂C. The possibility of open-orbits formation on the Fermi surface for $H \perp c$ is pointed out for LuNi₂B₂C contrary to YNi₂B₂C. Measurements of the angular dependence of MR in high magnetic fields for Lu- and Y-based single crystals are necessary to check the proposed model. In the mixed state the behavior of Lu- and Y-based borocarbides is quite similar. Scaling behavior $\rho_{xy} \sim \rho_{xx}^{\beta}$ was observed but no sign

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- ¹R. Nagarjan, C. Mazumdar, Z. Hossain, S. K. Dhar, K. V. Gopalakrishnan, L. C. Gupta, C. Godart, B. D. Padalia, and R. Vijayaraghavan, Phys. Rev. Lett. **72**, 274 (1994).
- ²R. J. Cava, H. Takagi, B. Batlog, H. W. Zandbergen, J. J. Kraewski, W. F. Peck, Jr., R. B. van Dover, R. J. Felder, T. Siegrist, K. Mizuhashi, J. O. Lee, H. Eisaki, S. A. Carter, and S. Uchida, Nature (London) **367**, 252 (1994).
- ³J. I. Lee, T. S. Zao, I. G. Kim, B. I. Min, and S. J. Youn, Phys. Rev. B **50**, 4030 (1994).
- ⁴W. E. Pickett and D. J. Singh, Phys. Rev. Lett. **72**, 3702 (1994).
- ⁵H. Kim, C.-D. Hwang, and J. Ihm, Phys. Rev. B **52**, 4592 (1995).
- ⁶E. Johnston-Halperin, J. Fiedler, D. E. Farrell, M. Xu, B. K. Cho, P. C. Canfield, D. K. Finnemore, and D. C. Johnston, Phys. Rev. B **51**, 12 852 (1995).
- ⁷I. R. Fisher, J. R. Cooper, and P. C. Canfield, Phys. Rev. B **56**, 10 820 (1997).
- ⁸V. Metlushko, U. Welp, A. Koshelev, I. Aranson, G. W. Crabtree, and P. C. Canfield, Phys. Rev. Lett. **79**, 1738 (1997).
- ⁹K. D. D. Rathnayaka, A. K. Bhatnagar, A. Parasiris, D. G. Naugle, P. C. Canfield, and B. K. Cho, Phys. Rev. B 55, 8506 (1997).
- ¹⁰ H. Eisaki, H. Takagi, R. J. Cava, B. Batlogg, J. J. Krajewski, W. F. Peck, Jr., K. Mizuhashi, J. O. Lee, and S. Uchida, Phys. Rev. B 50, 647 (1994).
- ¹¹Y. de Wilde, M. Iavarone, U. Welp, V. Metlushko, A. E. Koshelev, I. Aranson, G. W. Crabtree, and P. C. Canfield, Phys. Rev. Lett. **78**, 4273 (1997).
- ¹² M. R. Eskildsen, P. L. Gammel, B. P. Barber, U. Yaron, A. P. Ramirez, D. A. Huse, D. J. Bishop, C. Bolle, C. M. Lieber, S. Oxx, S. Sridhar, N. H. Andersen, K. Mortensen, and P. C. Canfield, Phys. Rev. Lett. **78**, 1968 (1997).
- ¹³ M. Yethiraj, D. McK. Paul, C. V. Tomy, and E. M. Forgan, Phys. Rev. Lett. **78**, 4849 (1997).
- ¹⁴M. R. Eskildsen, P. L. Gammel, B. P. Barber, A. P. Ramirez, D. J. Bishop, N. H. Andersen, K. Mortensen, C. A. Bolle, C. M. Lieber, and P. C. Canfield, Phys. Rev. Lett. **79**, 487 (1997).
- ¹⁵I. R. Fisher, J. R. Cooper, and R. J. Cava, Phys. Rev. B 52, 15 086 (1995).
- ¹⁶V. N. Narozhnyi, V. N. Kochetkov, A. V. Tsvyashchenko, and L. N. Fomicheva, J. Low Temp. Phys. **105**, 1647 (1996).
- ¹⁷P. Mandal and K. Winzer, Solid State Commun. **103**, 679 (1997).
- ¹⁸V. N. Narozhnyi, V. N. Kochetkov, A. V. Tsvyashchenko, and L. N. Fomicheva, J. Allovs Compd. **275-277**, 484 (1998).
- ¹⁹B. D. Josephson, Phys. Lett. 16, 242 (1965).

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ACKNOWLEDGMENTS

This work was supported by RFBR Grant No. 96-02-00046G and DFG Grant No. MU1015/4-1.

- ²⁰M. Galffy and E. Zirngiebl, Solid State Commun. **68**, 929 (1988).
- ²¹H.-C. Ri, R. Gross, F. Gollnik, A. Beck, R. P. Huebener, P. Wagner, and H. Adrian, Phys. Rev. B **50**, 3312 (1994).
- ²²A. V. Samoilov, Phys. Rev. Lett. **71**, 617 (1993).
- ²³ R. C. Budhani, S. H. Liou, and Z. X. Cai, Phys. Rev. Lett. **71**, 621 (1993).
- ²⁴S. J. Hagen, A. W. Smith, M. Rajeswari, J. L. Peng, Z. Y. Li, R. L. Greene, S. N. Mao, X. X. Xi, S. Bhattacharya, Q. Li, and C. J. Lobb, Phys. Rev. B **47**, 1064 (1993).
- ²⁵M. Cagigal, J. Fontcuberta, M. A. Crusellas, J. L. Vicent, and S. Pinol, Physica C 248, 155 (1995).
- ²⁶K. Li, Y. Zhang, and H. Adrian, Phys. Rev. B 53, 8608 (1996).
- ²⁷ H. C. Yang, L. M. Wang, and H. E. Horng, Phys. Rev. B 56, 99 (1997).
- ²⁸L. M. Wang, H. C. Yang, and H. E. Horng, Phys. Rev. Lett. 78, 527 (1997).
- ²⁹Y. B. Kim and M. J. Stephen, in *Superconductivity*, edited by R. D. Parks (Marcel Dekker, New York, 1969).
- ³⁰A. W. Smith, T. W. Clinton, C. C. Tsuei, and C. J. Lobb, Phys. Rev. B **49**, 12 927 (1994).
- ³¹S. Bhattacharya, M. J. Higgins, and T. V. Ramakrishnan, Phys. Rev. Lett. **73**, 1699 (1994).
- ³²J. Bardeen and M. J. Stephen, Phys. Rev. **140**, A1197 (1965).
- ³³P. Nozières and W. F. Vinen, Philos. Mag. 14, 667 (1966).
- ³⁴Z. D. Wang and C. S. Ting, Phys. Rev. Lett. **67**, 3618 (1991).
- ³⁵A. T. Dorsey, Phys. Rev. B 46, 8376 (1992).
- ³⁶N. B. Kopnin, B. I. Ivlev, and V. A. Kalatsky, J. Low Temp. Phys. **90**, 1 (1993).
- ³⁷A. G. Aronov, S. Hikami, and A. I. Larkin, Phys. Rev. B **51**, 3880 (1995).
- ³⁸A. van Otterlo, M. Feigel'man, V. Geshkenbein, and G. Blatter, Phys. Rev. Lett. **75**, 3736 (1995).
- ³⁹D. I. Khomskii and A. Freimuth, Phys. Rev. Lett. **75**, 1384 (1995).
- ⁴⁰R. Jin and H. R. Ott, Phys. Rev. B 57, 13 872 (1998).
- ⁴¹T. Nagaoka, Y. Matsuda, H. Obara, A. Sawa, T. Terashima, I. Chong, M. Takano, and M. Suzuki, Phys. Rev. Lett. **80**, 3594 (1998).
- ⁴²J. Luo, T. P. Orlando, J. M. Graybeal, X. D. Wu, and R. Muenchausen, Phys. Rev. Lett. **68**, 690 (1992).
- ⁴³J. P. Rice, N. Rigakis, D. M. Ginsberg, and J. M. Mochel, Phys. Rev. B 46, 11 050 (1992).
- ⁴⁴A. V. Samoilov, Z. G. Ivanov, and L. G. Johansson, Phys. Rev. B 49, 3667 (1994).
- ⁴⁵S. Okuma and N. Kokubo, Phys. Rev. B 56, 410 (1997).
- ⁴⁶A. T. Dorsey and M. P. A. Fisher, Phys. Rev. Lett. **68**, 694 (1992).
- ⁴⁷V. M. Vinokur, V. B. Geshkenbein, M. V. Feigelman, and G.

Blatter, Phys. Rev. Lett. 71, 1242 (1993).

- ⁴⁸Z. D. Wang, J. Dong, and C. S. Ting, Phys. Rev. Lett. **72**, 3875 (1994).
- ⁴⁹W. N. Kang, D. H. Kim, S. Y. Shim, J. H. Park, T. S. Hahn, S. S. Choi, W. C. Lee, J. D. Hettinger, K. E. Gray, and B. Glagola, Phys. Rev. Lett. **76**, 2993 (1996).
- ⁵⁰A. V. Samoilov, A. Legris, F. Fullier-Albenque, P. Lejay, S. Bouffard, Z. G. Ivanov, and L.-G. Johansson, Phys. Rev. Lett. **74**, 2351 (1995).
- ⁵¹V. N. Morgoon, V. A. Shklovskij, V. Bindilatti, A. V. Bondarenko, R. F. Jardim, C. C. Becerra, C. Y. Shigue, and A. V. Sivakov, J. Low Temp. Phys. **105**, 963 (1996).
- ⁵²G. Wang and K. Maki, Phys. Rev. B 58, 6493 (1998).
- ⁵³ V. N. Narozhnyi, J. Freudenberger, V. N. Kochetkov, K. A. Nenkov, G. Fuchs, and K.-H. Müller, Solid State Commun. **109**, 549 (1999).

- ⁵⁴K. Eversmann, A. Handstein, G. Fuchs, L. Gao, and K.-H. Müller, Physica C 266, 27 (1996).
- ⁵⁵S. V. Shulga, S.-L. Drechsler, G. Fuchs, K.-H. Müller, K. Winzer, M. Heinecke, and K. Krug, Phys. Rev. Lett. **80**, 1730 (1998).
- ⁵⁶N. E. Alekseevskii, V. I. Nizhankovskii, V. N. Narozhnyi, E. P. Khlybov, and A. V. Mitin, J. Low Temp. Phys. **64**, 87 (1986).
- ⁵⁷F. Gollnik and M. Naito, Phys. Rev. B 58, 11 734 (1998).
- ⁵⁸L. H. Nguyen, G. Goll, E. Steep, A. G. M. Jansen, P. Wyder, O. Jepsen, M. Heinecke, and K. Winzer, J. Low Temp. Phys. **105**, 1653 (1996).
- ⁵⁹I. M. Lifshitz, M. Ya. Azbel', and M. I. Kaganov, in *Electron Theory of Metals* (Consultants Bureau, New York, 1973).
- ⁶⁰D. M. Ginsberg and J. T. Manson, Phys. Rev. B 51, 515 (1995).
- ⁶¹Y. Matsuda, T. Nagaoka, G. Suzuki, K. Kumagai, M. Suzuki, M. Machida, M. Sera, M. Hiroi, and N. Kobayashi, Phys. Rev. B 52, 15 749 (1995).