# Probing $(Bi_{0.92}Pb_{0.17})_2Sr_{1.91}Ca_{2.03}Cu_{3.06}O_{10+\delta}$ superconductors from 30 to 300 K by positron-lifetime measurements

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The present measurement of positron annihilation lifetimes for the high- $T_c$  superconductor  $(Bi_{0.92}Pb_{0.17})_2Sr_{1.91}Ca_{2.03}Cu_{3.06}O_{10+\delta}$  or (Bi,Pb)-2223, as a function of temperature, has been inspired by our recent DBPARL (Doppler-broadened positron annihilation radiation line shape) finding of a step and minima in the region around  $T_c(R=0) = 104$  K, in the variation with temperature, of the fraction of low momentum electrons at the annihilation sites. The positron annihilation lifetime in the superconductor probes the number density of electrons at the annihilation sites. The present work observes a reduction of lifetime components in the  $T_c$  region. Significant changes in the lifetime components in other temperature regions have also been observed and discussed. [S0163-1829(98)05745-2]

#### I. INTRODUCTION

The positron annihilation technique has been applied<sup>1</sup> to find out whether superconducting pairing in momentum space affects the number density of electrons (as probed by the positron lifetime) and their momentum distribution (as probed by the Doppler-broadening parameter S) since the 1950s for various conventional superconductors.<sup>2</sup> The effort has been continued for the past 12 years for various hightemperature superconductors (HTSC's).<sup>1,3</sup> No measurable change in these positron annihilation parameters across the superconducting critical temperature,  $T_c$ , was detected for conventional superconductors like A-15 compounds. However, for high-  $T_c$  superconductors the ratio  $\Delta/\epsilon_F$ , where  $2\Delta$ is the superconducting energy gap, and  $\epsilon_F$  is the Fermi energy, is much higher to favor<sup>1-4</sup> a relatively larger fraction of charge carriers forming pairs on cooling below  $T_c$ . As a result, relatively larger and hence measurable change,  $\delta \tau$ , in positron lifetime,  $\tau$ , in HTSC's has been expected<sup>1</sup> due to the superconducting transition:

$$rac{\delta au}{ au} \sim \left(rac{\Delta}{oldsymbol{\epsilon}_F}
ight)^2 \ln\!\left(rac{oldsymbol{\epsilon}_F}{\Delta}
ight).$$

Similar change has been expected due to the superconducting transition in the Doppler-broadened positron annihilation radiation line shape or DBPARL parameter, S, in HTSC samples. Here S represents the fraction of suitably defined<sup>5–7</sup> low momentum electrons among the electrons annihilating with the probing positrons. Many groups,<sup>1,3</sup> including ours, reported a steplike increase or decrease of  $\tau$ component/s and S at  $T_c$ , with some contradictions, and more than one explanation have been suggested.

Our recent DBPARL experiments<sup>5–7</sup> on (Bi,Pb)-2223 and Bi-2212 samples, however, repeatedly showed a new additional feature in the *S* versus *T* graphs, a minimum or two minima in the  $T_c$  region. It may be added that such a narrow minimum can be missed in readings at large intervals of temperature. This may explain previous reports of steplike changes<sup>1,3</sup> without any minimum. We found<sup>5</sup> two minima (at 99 K and 104 K) in the *S* -parameter of (Bi,Pb)-2223 having  $T_c$  (R=0) = 104 K, in addition to the above-mentioned step at  $T_c$ . Such minima, in the  $T_c$  region, in the fraction of low momentum electrons<sup>5–7</sup> among the annihilating electrons, call for a careful measurement across  $T_c$  also of the lifetime,  $\tau$ , that probes the density of electrons at the annihilation sites.

In view of the above-mentioned expectation, the degree to which such minima/maxima and/or step have been observed in earlier positron lifetime measurements on Bi-based 2223 HTSC is reviewed briefly. Such a step in lifetime data can be presumed to be less prominent in Bi-HTSC than in Y-HTSC on the basis of presently available S-parameter results. Such minima observed<sup>8</sup> (with a resolution of 270 ps) in mixed (Bi-2212 and Bi-2223) phase samples by Zhang et al. in the  $T_c$  regions of the 2223 as well as 2212 phase appear to have been ignored due to the possible unreliability of data on mixed phases. Zhang *et al.* noted that the earliest work<sup>9</sup> had concluded no observable effect on  $\tau$  and S in mixed 2212-2223 samples, without presenting any data. An observable effect of the superconducting transition on S versus T has already been reported<sup>5-7</sup> for Bi-2212 and (Bi,Pb)-2223. Tang et al.<sup>10</sup> report (with a resolution of 245 ps) three narrow valleys near 120 K, 140 K, and 160 K and two wide valleys near 240 K and 270 K in their  $\tau_2$  versus temperature graph, where  $\tau_2$  is longer of the two short components  $\tau_1$  and  $\tau_2$ . This result has neither been clearly explained nor verified. They found  $\tau_1$  and the bulk lifetime,  $\tau_B$ , to be less sensitive to temperature. However, indications of minima in lifetime data in some cases<sup>11</sup> appear to have been ignored. Tang et al.<sup>10</sup> concentrated on the higher temperature region, and none of the above is a detailed measurement on single phase samples. Therefore, there is a clear need for high-resolution lifetime measurement, with readings at a closer interval of temperature, on single phase (Bi,Pb)-2223. This has been carried out in the present work.

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Here we report our positron annihilation lifetime measurements with a resolution of 190 ps down to 30 K on the same pair of (Bi,Pb)-2223 samples as were used<sup>5</sup> in our S versus T measurements. Our lifetime spectrum, N(t) versus t, is seen to consist of more than one lifetime component,  $\tau_i$ .

It is known that lifetime components will correspond to individual characteristic lifetimes of the components, if the sample is a mixture of noninteracting components. However, if the sample is a single-component substance, element, or compound, with a characteristic Bloch lifetime, a detection of two or more lifetime components indicates the presence of one or more trapping site/s (Ref. 12) or other physical processes such as positronium states. In this investigation, the longest component,  $\tau_3$ , can be identified<sup>13</sup> to be due to positronium (Ps) formation and ortho-Ps to para-Ps conversion. The simple two-state trapping model assumes annihilation from positron traps and the Bloch state (also called annihilation in the bulk). The lifetime for annihilation from the positron trap turns out to be  $\tau_2$ . The lifetime for annihilation from the Bloch state, called  $\tau_B$ , and that is supposed to probe the intrinsic properties of the material, can be easily shown to be given by the equation

$$\tau_B = \frac{(I_1 + I_2)}{\left(\frac{I_1}{\tau_1} + \frac{I_2}{\tau_2}\right)}$$

So, in this trapping model,  $\tau_B$  and  $\tau_2$  are the physically significant quantities, with  $\tau_2$  resulting from annihilation in regions of lower electron density. Such regions have been presumed to be vacancies or vacancy complexes in general, and unoccupied lattice sites<sup>4,14</sup> or oxygen vacancies<sup>15,16</sup> for various HTSC. Other positrons have been assumed, from simple rate calculations,<sup>16</sup> to annihilate mostly from oxygen valence electrons. However, the concept of a unique Bloch state, the concept of the traps being populated by positrons via the Bloch state only and not directly,<sup>17</sup> and hence the applicability of the above-mentioned model may be questioned, as some of the different parts of the complex HTSC structure are somewhat noninteracting. So results are given also in terms of mean lifetime,  $\overline{\tau}$ , without resorting to any particular model.

#### **II. EXPERIMENTAL OUTLINE**

An appropriate mixture of the oxides/carbonate has been repeatedly ground, pelletized, and fired until x-ray diffraction showed<sup>13</sup> only the lines characteristic of the (Bi,Pb)-2223 phase. The superconducting critical temperature,  $T_c$ , of this sample has been determined as  $104 \pm 0.2$  K by electrical resistivity measurement<sup>5,7</sup> (standard four-probe method) and confirmed by ac magnetic susceptibility measurement.<sup>5,6</sup> A  $10\mu$ Ci <sup>22</sup>Na source, enclosed between two 2 mg/cm<sup>2</sup> nickel foils, has been sandwiched between two identical and planefaced 6 mm $\times$ 4 mm $\times$ 0.8 mm pellets of the above-mentioned (Bi,Pb)-2223. The positron annihilation lifetimes have been measured with a fast-slow coincidence assembly. The detectors are 25-mm-diam×25-mm-long cylindrical BaF<sub>2</sub> scintillators coupled to Philips XP2020Q photomultiplier tubes. The resolving time [full width at half maximum (FWHM)], measured with a <sup>60</sup>Co source and with the windows of the slow channels of the fast-slow coincidence assembly set to select pulses corresponding to 300 keV to 550 keV in one channel and 700 keV to 1320 keV in the other, is 190 ps. The source-sample sandwich has been mounted inside a vibration-free He cryogenerator (APD Cryogenics Inc., model no. DMX-20). Good thermal contact between the cold head of the cryogenerator and the sample has been ensured by using indium foil. The temperature of the system has been controlled by a temperature controller (Scientific Instruments Inc. 9620-1). For each temperature a total of ~ 10<sup>6</sup> coincidence counts have been recorded with 8000:1 peak to random ratio. The recorded N(t) versus *t* data have been analyzed by the PATFIT-88 computer program<sup>18</sup> with necessary source correction.

### **III. OBSERVATIONS AND DISCUSSION**

One- to four-component PATFIT-88 fittings have been carried out for each of the N(t) versus *t* lifetime spectra over 30 K to 300 K to decide the best fit for each spectrum. In the region 300 K to 215 K the best fit has been obtained with a three-component fit indicating the presence at a low intensity of a very long third component (1.3 ns~1.5 ns). The two-component fit worked better for lower temperatures.

The longest lifetime component can be attributed to positronium formation<sup>13</sup> and subsequent ortho-Ps to para-Ps conversion, quite likely in voids or intergranular spaces of the sintered samples. The presently observed low intensity of 0.5% to 1.0% of  $\tau_3$  compares well with earlier findings.<sup>8,13</sup> While Sedov et al.<sup>1</sup> have considered the contribution of the superconducting transition to the positron annihilation parameters to be positronium-related, most of the earlier workers have not done any detailed study of  $\tau_3$  due to its low intensity and an apparently temperature-independent nature. Here we confirm that ignoring this third component, in cases where it is present even with a small intensity of the order of 1%, leads<sup>13</sup> to a significantly wrong estimate of the smaller components in the forced two-component fit. This is simply due to its large value. The fact that our lifetime spectra below 215 K show the best fit with two components implies that either ortho-Ps to para-Ps conversion or positronium formation is not favored in the present samples at lower temperatures. More experiments on other samples, such as our recent finding<sup>19</sup> that 300 K lifetime spectra for HTSC single crystals show only two components, are needed to explain this temperature dependence. Our incompletely understood but observed temperature dependence of  $\tau_3$  can be supported from earlier experiments on Y-123 pellets by Wang et al.<sup>20</sup> Although their positron lifetime data in Y-123 (with  $T_c$  of 87.5 K) are discussed on the basis of a two-component fit, they found the positronium-related contribution to  $\tau_2$  to become more prominent as the temperature increased towards 300 K. In fact, their three-component fit showed  $\tau_3$  of about 1750 ps to be significant (1.2%) down to 200 K.

Figure 1 shows the temperature dependence of (a) the S parameter<sup>5</sup> and (b)  $\overline{\tau}$ . The S parameter as well as  $\overline{\tau}$  show the average effect of various positron annihilation processes in the solid, without resorting to any model or details of these processes. A decrease in the average positron lifetime,  $\overline{\tau}$ , is caused by an increase of electron density (at the annihilation sites) that should, in general, bring about a concomitant in-

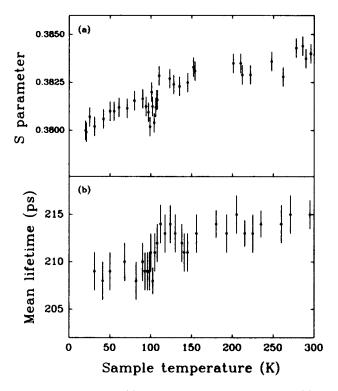


FIG. 1. Variation of (a) the DBPARL parameter, *S*, and (b) the mean positron lifetime,  $\overline{\tau}$ , with sample temperature for the sample (Bi,Pb)-2223.

crease in electron momentum,<sup>3</sup> implying a decrease in S. This expected correlation between S and  $\overline{\tau}$  with respect to their temperature dependence can be seen to be roughly satisfied by our results in Figs. 1(a) and 1(b) from two entirely different experiments. A sharp decrease of S and  $\overline{\tau}$  on cooling across  $T_c$  is most notable among the similarities, which are, however, not quantitative. Hints of minima or maxima at temperatures between 125 K and 300 K in Fig. 1(b) can be better discussed in the next graphs. These minima or maxima need to be ignored and the average graph drawn to observe the effect, on  $\overline{\tau}$ , of lattice expansion only. Such a graph shows a steplike break at  $T_c$ . The slow increase of  $\overline{\tau}$  with temperature for the 30 K to  $T_c$  segment as well as for the segment between  $T_c$  and 300 K is in agreement with the slight decrease in electron density due to lattice expansion.<sup>5,21</sup> The steplike decrease of  $\overline{\tau}$  below  $T_c$  is less than that in Y-123, in agreement with positron density distribution calculation $^{3,8,22}$  arguments. There appears to be a minimum between 140 K and 150 K. Next, on cooling from 140 K towards  $T_c$ ,  $\overline{\tau}$  increases. But it shows a steep fall for  $T < T_c$ . So  $\overline{\tau}$  shows a steplike decrease across  $T_c = 104$  K. This feature in the  $T_c$  region will be clearer in the  $\tau_2$  versus T figure.

Using the two-state trapping model,  $\tau_B$  has been calculated, as already discussed, over the 30 K to 300 K range (Fig. 2). For example,  $\tau_B$  at 295 K has been calculated to be 206 ps from the fitting results:  $\tau_1 = (193 \pm 2)$  ps and  $\tau_2 = (359 \pm 7)$  ps. Here  $\tau_2/\tau_B$  is 1.74 at 295 K and about 1.71 if averaged over 30 K to 295 K. These compare well with the room temperature values 1.55 and 2.34 calculated from Ref. 9 and Ref. 11, respectively. To estimate the effect on  $\tau_B$  (Fig.

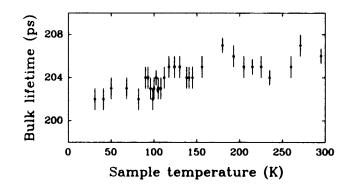


FIG. 2. Variation of the bulk lifetime,  $\tau_B$ , with sample temperature for positron annihilation in (Bi,Pb)-2223.

2) of lattice contraction due to cooling, one must draw an average graph ignoring structures such as the broad minimum between 200 and 270 K, as was done for Fig. 1. The graph is seen to have two branches—30 K to  $T_c$  and  $T_c$  to 300 K. The steplike change of  $\tau_B$  at  $T_c$  can be seen to be smaller than in  $\overline{\tau}$ . In fact, the lowest temperature value of  $\tau_{R}$ is seen to be only about 4 ps lower than the roomtemperature value, as we observed in an earlier work.<sup>3</sup> One cannot consider the variations (within the error bars) in the  $T_c$  region, to be hints of minima or maxima in  $\tau_B$ . These variations are certainly less convincing than the double minima in the S parameter for (Bi,Pb)-2223 pellets, Fig. 1(a), and Y-123 single crystals<sup>23</sup> and than the single minimum in Bi-2212 pellets.<sup>7</sup> Figure 3 (a) shows that between 30 K and 175 K the intensity of the intermediate component,  $I_2$ , decreases with lowering of temperature. This implies that the probability of positrons annihilating in the vacancylike traps decreases at lower temperatures. In Fig. 3(b),  $\tau_2$  has been plotted against temperature. The most prominent feature of this plot is a broad minimum at around 175 K. While the possible link of this 175 K minimum to the opening up of the recently discovered spin gap<sup>24,25</sup> will be investigated in a

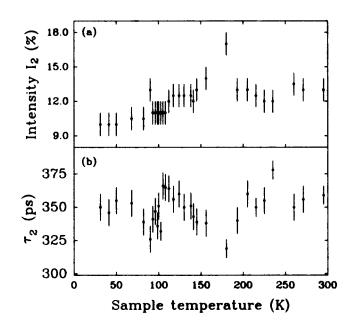


FIG. 3. Variation of the positron lifetime component  $\tau_2$ , and its intensity,  $I_2$ , with sample temperature for (Bi,Pb)-2223 pellets in (b) and (a).

separate work, other possibilities such as positron trapping at defects due to certain lattice instabilities<sup>10</sup> cannot be ruled out. However, the large  $I_2$  and small  $\tau_2$  at 175 K necessarily imply a larger number of smaller-sized traps (vacancylike defects). S parameter versus T graphs<sup>5-7</sup> for Bi-2212 and (Bi,Pb)-2223 also show significant variations in the temperature region between  $T_c$  and 300 K. Let it be pointed out that a few of the critically important data points of our graphs (at 230 K, 180 K, and 102.5 K, for example) have been taken twice, confirming the values presented in this work. Hints of a peak in  $\tau_2$  at around 235 K compare well with the anomaly reported near 240 K by at least four different groups, as reviewed by Manuel.<sup>14</sup> There is a rise of  $\tau_2$  on cooling towards  $T_c$ . But at  $T \simeq T_c$  there is a steep fall in the lifetime component  $\tau_2$ , as has been observed<sup>5-7</sup> in S versus T graphs in DBPARL experiments. Follow-up of this fall by one or two minimum/minima at lower temperatures is evident<sup>5-7</sup> in S versus T data but it is not so in  $\tau_2$  versus T data.

A number of neutron PDF (pair distribution function) experiments have indicated<sup>25</sup> a local structural response to a change in the electronic state, like the appearance of superconductivity and the opening of the pseudogap. Particular mention may be made of the complex maximum (Fig. 20 of Ref. 25) observed at the  $T_c$  region in TI-2212 HTSC of the PDF peak-height at 3.4 Å. It concerns the pair correlation between in-plane, O(1), oxygen and apical, O(2), oxygen. The striking similarity of this variation to our complex minimum<sup>5</sup> in S is noteworthy. The lower value at or near  $T_c$ of  $\tau_2$  physically implies a higher exposure to electrons of positrons trapped mostly at O vacancies.<sup>15,16</sup> In Y-123, the tunneling frequency of apical oxygen between two possible sites shows a maximum (Fig. 23 of Ref. 25) at  $T_c$ . Such a phenomenon in (Bi,Pb)-2223 is probable in view of superconductivity-related lattice effects,<sup>25</sup> receiving increased attention in recent years. The decrease of  $\tau_2$  on cooling below  $T_c$  can be related either to such enhanced jumping of oxygen ions between the two sites or to electron transfer<sup>15</sup> from CuO<sub>2</sub> layers to BiO regions.<sup>3,15</sup> These explanations need to be worked out more precisely to understand the changes observed in the positron annihilation parameters across  $T_c$ .

The lifetime component  $\tau_2$  can be a sensitive probe for lattice instabilities, giving rise to sites with low electron density. In this context we recall the well known lattice instability<sup>26</sup> in A-15 compounds on cooling towards  $T_c$  and its arrest by the appearance of superconductivity. Such an instability causing the rise of  $\tau_2$  on cooling towards  $T_c$  and its arrest at  $T_c$  leading to the sharp fall of  $\tau_2$  somewhere between 105 K and 102.5 K may be possible in such high- $T_c$  compounds.

# **IV. CONCLUSION**

Certain minima and maxima in positron lifetime components for  $T_c < T < 300$  K likely to be related to magnetic effects<sup>5,25</sup> or other lattice instabilities,<sup>10</sup> similar to those reported earlier for lifetime and S-parameter experiments, are confirmed. Their origin cannot be pinpointed without further clarifying experiments. More important is the steep fall in lifetime component  $\tau_2$  and mean lifetime  $\overline{\tau}$  on cooling below  $T_c$ . This removes the confusion in the literature on whether the positron lifetime in (Bi,Pb)-2223 HTSC is affected by the superconducting transition. A drastic redistribution of electrons on cooling across the superconducting transition temperature has been clearly observed in the present work.

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