# **NbSe3: Effect of uniaxial stress on the threshold field and fermiology**

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We have measured the effect of elastic strain  $\epsilon$  on the threshold field  $E_T$  for the motion of the highertemperature charge density wave (CDW) in NbSe<sub>3</sub>. We find that  $E_T$  exhibits a critical behavior,  $E_T \sim (1$  $-\epsilon/\epsilon_c$ )<sup> $\gamma$ </sup> where  $\epsilon_c$  is about 2.6%,  $\gamma \sim 1.2$ . This expression remains valid over more than two decades of  $E_T$ , up to the highest fields of about 1.5 kV/m measured using pulse techniques. Neither  $\gamma$  nor  $\epsilon_c$  is very sensitive to the impurity content of the sample. The transition temperature is linear with  $\epsilon$ , and  $dT_P/d\epsilon=10$  K/% shows no anomaly near  $\epsilon_c$ . The slope of the narrow band noise frequency versus the CDW current does not change appreciably with  $\epsilon$ . Shubnikov–de Haas measurements show that the extremal area of the Fermi surface decreases with increasing  $\epsilon$ . We conclude that there is a very intimate relationship between pinning and the fermiology in NbSe<sub>3</sub>.  $[$0163-1829(98)12619-X]$ 

## **I. INTRODUCTION**

The recent discovery of the Aharonov-Bohm effect exhibited by the sliding charge density wave  $(CDW)$  in NbSe 3 has revived interest for the field of  $CDW<sup>1</sup>$ . Nonlinear conductivity is the outstanding characteristic of charge-density-wave materials.<sup>2</sup> The presence of a threshold field  $E_T$ , above which the resistance decreases, is the signature that the CDW can be made to move under a small electric field.<sup>3,4</sup> The dependence of  $E_T$  on temperature  $(T)$ , number of impurities  $(n_i)$ ,<sup>5,6</sup> contact position, size,<sup>7</sup> pressure,<sup>8</sup> and uniaxial stress,<sup>9,10</sup> has been extensively reported. Here we report further studies on the effect of elastic, uniaxial stress  $\sigma$  on  $E_T$ for the upper CDW in  $NbSe_3$ . This paper will show that  $E_T \sim 1/|\sigma - \sigma_c|$ , where  $\sigma_c \approx 260$  GPa and that this is related to the change in fermiology as shown from low-temperature Shubnikov-de Haas (SdH) studies.

#### **II. EXPERIMENTAL TECHNIQUES AND RESULTS**

## **A. Samples**

The experiments were conducted on nominally pure as well as Fe doped NbSe  $_3$  samples. Fe doping was achieved by mixing either 4.7% or 7% of Fe in the starting materials; about one-tenth that much doping is expected in the resulting whiskers.<sup>11</sup> Samples of medium purity with a room temperature resistance ratio  $(RRR)$  of 70 were grown in house; the high purity samples, RRR  $>200$ , were provided by R. E. Thorne. The samples were mounted on a stressing device described elsewhere.<sup>12</sup> Uniaxial stress was applied along the needle axis, the **b** crystal axis. The strain  $\varepsilon$  was directly measured, and can be converted to stress using the Young's modulus,  $S_{22} \approx 100$  GPa.<sup>10</sup> Four electrical contacts were made using conducting silver paint. Epoxy overlaid these contacts and formed the mechanical grips. Typical sample dimensions were  $2000\times20\times1$   $\mu$ m<sup>3</sup>.

#### **B.** Effect of  $\varepsilon$  on the upper CDW

At low strain and low fields, the threshold field was determined using the conventional lock in or *dV*/*dI* technique. At high  $\varepsilon$ , where high electric fields are required to reach  $E_T$ , the pulse method was used. The duty cycle was less than 1%; with typical pulse width of 10  $\mu$ s, and period 1 ms. The pulsed current and voltage were measured using a two channel boxcar signal averager, EG&G model 162. In this case,  $E_T$  was estimated from the plot of the chordal resistance *R* vs *E* or from the numerical derivative  $\Delta V/\Delta I$ . Previous studies<sup>9,10</sup> have shown that uniaxial stress affects  $E_T$  indirectly by  $\varepsilon$ -induced changes in  $T_p$  and directly by enhancing the pinning strength. It was shown that the indirect effect can be disentangled by conducting the experiments at a constant reduced temperature  $t = T/T_p(\varepsilon)$  where  $T_p(\varepsilon)$  is defined at the peak in  $dR(\varepsilon)/dT$ . Constant  $t=0.70$  was achieved by adjusting *T* for each value of  $\varepsilon$ . This value of *t* corresponds to the minimum value  $E_{\text{min}}$  on the  $E_T$  versus *t* curve. It was previously shown that  $E_{\text{min}}$  is proportional to the impurity concentration<sup>6,7</sup> and assumed to correspond to bulk pinning rather than contact pinning. Although this paper is devoted to the study of the effect of  $\varepsilon$  on  $E_{\text{min}}$ , for the sake of simplicity we will refer to it as the threshold field, or simply  $E_T$ .

Figure 1 shows a typical plot of  $E_T$  versus  $\varepsilon$  for an arbitrarily selected sample.  $E_T$  increases weakly at low strain and diverges near  $\varepsilon_c = 2.6 \pm 0.3$ %. The semilogarithmic plot of the same data shown in the inset indicates that  $E_T$  increases



FIG. 1.  $E_T$  vs  $\varepsilon$  for a nominally pure sample. The inset shows a semilogarithmic plot of the same data.



FIG. 2. The CDW transition temperature  $T_{p1}$  vs strain.  $T_{p1}$  decreases linearly with  $\varepsilon$  up to  $\varepsilon = 3\%$ . Typical  $R(\varepsilon)$  vs *T* plots are shown in the inset.

faster than a single exponential. In the few cases where we were able to pull beyond 2.6% strain,  $E_T$  exhibited a peak, decreasing above  $2.6 \pm 0.3$ %. Figure 2 shows the strain dependence of  $T_p$ .  $T_p$  decreases linearly with increasing  $\varepsilon$  up to 3% at a rate  $dT_p/d\varepsilon = 10$  K/%. There is no apparent feature around  $\varepsilon = 2.6\%$ , where  $E_T$  diverges. The inset in Fig. 2 shows a plot of  $R$  versus  $T$  for different values of  $\varepsilon$ . Note that the resistance anomaly  $\Delta R(\varepsilon) = R_p(\varepsilon) - R_{\text{fit}}(\varepsilon)$  is independent of  $\varepsilon$ , where  $R_p(\varepsilon)$  corresponds to the peak resistance for a given  $R(\varepsilon)$  versus *T* plot, and  $R(\varepsilon)_{\text{fit}}$  is the linearly extrapolated resistance at *T* peak from above 150 K. This result suggests that the CDW conductance  $(G<sub>CDW</sub>)$  $\sim n_{CDW}e\mu$ , where *e* is the charge of the electron and  $\mu$  the CDW mobility) at very large electric fields is independent of  $\varepsilon$ , which in turn implies that the fraction of condensed electrons  $n_{CDW}$  does not change appreciably with  $\varepsilon$ . This is consistent with narrow-band noise measurements, which showed almost no change in the slope of the CDW current versus the narrow-band frequency  $(dI_{CDW}/dF)$  with  $\varepsilon$ .<sup>13</sup>

#### **C.** Effect of  $\varepsilon$  on the Fermi surface

In this section we look for a connection between the effect of  $\varepsilon$  on the fermiology and the results reported in the previous section. The effect of  $\varepsilon$  on the dominant frequency of the Shubnikov–de Haas oscillations is reported. The magnetic field  $B_a$  was parallel to the  $(b,c)$  plane and perpendicular to the smallest extremal area of the Fermi surface, with a typical frequency of 0.28 MG at  $\varepsilon = 0.13-15$  Two methods were used. The first method is the conventional method,  $B_a$  was increased slowly with the sample under constant strain. In the second method,  $B_a$  was constant while sweeping  $\varepsilon$ . The experiments were conducted at constant *T* between 3.0 and 4.2 K.

Figure 3(a) shows a typical plot of *R* vs *H* obtained using the conventional method, the inset shows  $dR/d(1/H)$  versus 1/*H*. The extremal area *A* was estimated from a plot of *n* versus  $1/H$  for each value of  $\varepsilon$ . Figure 3(b) shows that *A* decreases nearly linearly with increasing  $\varepsilon$ . A detailed study of the effect of uniaxial stress on the Fermi surface will be reported elsewhere. In this paper we note that uniaxial stress



FIG. 3. (a) shows a typical plot of  $R$  vs  $H$ , which exhibits Shubnikov–de Haas oscillations. The derivative  $dR/d(1/H)$  vs  $1/H$  is shown in the inset. In (b) the extremal area, in units of kG, decreases smoothly with increasing  $\varepsilon$ .

suppresses *A* linearly at the rate of 0.09 MG/%, suggesting that the whole pocket would be wiped out for  $\varepsilon \leq 3\%$ . A study of the strain dependence of the conductance at low temperature shows that 90% of the conductance is wiped out for  $\varepsilon \approx 2.6\%$ . This suggests that this pocket plays a predominant role in the normal state conductance of NbSe  $_3$  at low  $T$ .

The second method is equivalent to fixing the Landau tubes and shrinking the Fermi surface through them under the influence of  $\varepsilon$ . This leads to oscillations in the  $R$  vs  $\varepsilon$ plots as shown in Fig. 4(a). A systematic study of *R* versus  $\varepsilon$ for different values of  $B_a$  allows us to follow the strain and the field at which a given Landau tube is crossed. The results are summarized in Fig. 4(b), which shows a plot of  $\varepsilon$  vs  $B_a$ for each Landau tube identified by the integer next to its curve. The trajectory of a given Landau tube is nearly linear. This is consistent with the linear relationship between *A* and  $\varepsilon$  observed using the conventional technique. The solid lines in the figure are a guide to the eye. Note that at  $B_a=0$  T, all the lines converge to nearly the same  $\varepsilon_c^H \approx 2.6\%$ . This suggests that this piece of the Fermi surface would be wiped out at about 2.6%. Below we will also show that  $\varepsilon_c^H$  is equal to the critical strain  $\varepsilon_c^{E_T}$  derived from the critical plot of  $E_t$  of the upper CDW.

## **III. DISCUSSION**

Possible pinning mechanisms of the CDW are bulk impurity pinning as discussed by Fukuyama-Lee-Rice<sup>16</sup> (either



FIG. 4. (a) shows the oscillatory *R* vs  $\varepsilon$  plots for  $B = 5.4$  T. The oscillations are attributed to the intersection of the Landau tubes with the shrinking Fermi surface. (b) is a representation of this intersection in the  $(\varepsilon, B)$ space. The integers in the box correspond to the indices of the Landau levels.

strong or weak), commensurability pinning by the underlying lattice, or pinning by other defects such as surfaces, dislocations or contacts. The results in Fig. 3 could be due to one or a complex combination of the following effects:  $(1)$ strain-induced enhancement of the weak impurity pinning potential; (2) strain-induced crossover from weak pinning to strong pinning;  $(3)$  strain-induced incommensurate to commensurate transition; or (4) strain-induced enhancement of contact pinning. We now discuss each one of these effects separately, in inverse order of their likelihood.

Stress-induced enhancement of contact pinning is very unlikely. If this were the case, one would also expect a similar stress-induced enhancement of  $E_T$  for the lower CDW. However, previous studies have shown that stress does not enhance  $E_T$  for the lower CDW.<sup>9,10</sup> In addition, Tseng, Tessema, and Skove have shown<sup>9</sup> in the case of the upper CDW,  $E_T$  can be separated into two components, one attributed to contact pinning, and the other to bulk impurity pinning. They have argued that uniaxial stress does not enhance contact pinning. It also seems unlikely that uniaxial stress can affect surface pinning to that extent; if it did, our thinner samples would have shown a stronger effect.

The FLR model considers two possible kinds of impurity pinning: strong pinning and weak pinning. Several experiments indicate that pinning in  $NbSe<sub>3</sub>$  is due to weak pinning.<sup>6,7</sup> Stress-induced crossover from weak pinning to strong pinning could be considered, in which case one would expect to see a change in the exponent  $\gamma$  with  $\varepsilon$ .  $\gamma$  is defined



FIG. 5. A critical plot of  $E_T$  for five different samples. The full triangles and the crossed squares correspond to Fe-doped samples, 0.7% and 0.47%, respectively. The normalized threshold  $e_T = E_T(\varepsilon)/E_T(0)$  is shown in the inset. Note that all five set of data fall on the same line.

in the next paragraph. The results show that  $\gamma$  is independent of  $\varepsilon$  and rule out this possibility as well. This is also supported by the fact that the same  $\gamma$  is obtained for the samples doped with Fe, which may be considered as a strong pinning impurity.

Experimental search for an incommensuratecommensurate transition (ICT) in CDW systems has not provided any clear evidence for these effects.<sup>17</sup> A stress-induced ICT would lead to changes in  $dT_p/d\sigma$  as well as solitonlike behavior near commensurability. Figure 2 shows that  $T_p$ does not show an anomaly near  $\varepsilon_c$ . Further, according to Fisher and Fisher<sup>18</sup> the approach to commensurability should behave critically with an exponent of  $\frac{1}{2}$  (for 2D) or be logarithmic. Figure 5 shows such a critical plot of  $E_T$  versus (1)  $-\varepsilon/\varepsilon_c$ ) in a log-log scale. A plot for the normalized threshold field

$$
e_T = E_T / E_{T_0} = (1 - \varepsilon / \varepsilon_c)^\gamma,\tag{1}
$$

where  $E_{T_0}$  is the threshold field at zero strain and  $\varepsilon_c$  and  $\gamma$ are adjustable parameters, is shown in the inset. In the following we will replace  $\varepsilon_c$  with  $\varepsilon_c^{E_T}$  in order to differentiate it with the critical strain defined from the fermiology study. Note that the results for five different samples with different impurity content, and Fe impurity fall along the same line, with nearly the same parameters. A list of the values of  $\varepsilon_c^{E_T}$ for different samples is shown in Table I. Although the figure is in qualitative agreement with Fisher and Fisher's prediction that  $E_T$  should behave critically in an ICT, the exponents are not in quantitative agreement with the model. Our larger samples are most likely 3D, and the exponent is not 1/2; therefore the critical behavior cannot be explained by a simple approach to commensurability. On the other hand, an argument in favor of ICT can be made based on the divergence of  $E_T$ . Since commensurability pinning is much stronger than impurity pinning,  $E_T$  is much more sensitive to stress-induced ICT than  $T_p$  is. This issue could be resolved using structural studies as a function of strain.

TABLE I. The fitting parameters  $\varepsilon_c^{E_T}$  and  $\gamma$  are shown together with other relevant parameters such as the nominal purity, the RRR, and the threshold field  $E_T$ . Only the nominal Fe doping levels are given.

Sample	<b>RRR</b>	$E_{T0\!\!\! / \!\!/_{\!0}}$ $\varepsilon_c$	$\gamma$	$E_T$ (V/m)
Pure	250	2.6	1.58	8.0
Pure	200	3	1.23	11
Pure		2.6	1.23	6.3
Pure		2.6	1.66	10
4.7% Fe		3.2	1.14	28
4.7% Fe		2.6	1.08	31
7% Fe		2.7	1.23	63

According to the FLR theory,<sup>16</sup> the threshold field for weak pinning is given by

$$
eE_T \lambda \propto \frac{\Delta^2}{E_F} (\xi_x, \xi_y, \xi_z n_i^2) V_0^{[4/(4-D)]}, \tag{2}
$$

where  $\lambda$  is the wavelength of the CDW,  $\xi_x$ ,  $\xi_y$ , and  $\xi_z$  are coherence lengths for the CDW amplitude,  $E_T$  the threshold field, *e* the electric charge,  $E_F$  the Fermi energy,  $V_0$  the impurity potential, and  $D$  the dimensionality.<sup>16</sup> Stress could affect any or all of the parameters in Eq.  $(2)$ . However, for the sake of simplicity we will discuss separately the terms that are susceptible to change with  $T_p$ . In the conventional BCS model the CDW gap is proportional to  $T_p$ ,  $\Delta/T_p=4.8$ for NbSe<sub>3</sub>.<sup>1</sup> As in previous pressure work,<sup>8</sup> uniaxial stressinduced enhancement of the electron-phonon coupling constant could be considered. However, it would take more than an order of magnitude of change in order to account for our results. On the other hand if, in a first approximation, one assumes that this ratio is not affected by  $\varepsilon$ ,  $\Delta$  would decrease with  $T_p$ , which would lead to a decrease in  $E_T$ , contrary to our results. Another possibility is a strain-induced decrease in  $E_F$ . But the normal state conductivity around  $T_P$  is a weak function of  $\varepsilon$ , even up to 3%, suggesting that  $E_F$  is not strongly affected by  $\varepsilon$ . One likely possibility is that  $V_0$  is strongly affected by stress. Suppose there is a stress-induced tuning of the matching between the phase and wavelength of the CDW and the Friedel oscillations.<sup>19</sup> Then, although the changes in  $E_F$  due to the vanishing of this small pocket could be negligible, it could be sufficient to lead to a rapid increase

<sup>1</sup>Y. I. Latyshev *et al.*, Phys. Rev. Lett. **78**, 919 (1997).

of  $V_0$ . This mechanism would be independent of the type of impurity and concentration, in agreement with our experiments. One other possibility is that the pocket screens the impurity, and  $V_0$  increases when the pocket disappears. Below we will discuss the difference between the upper and lower CDW.

In a study of the combined effect of magnetic field and strain, Parilla, Carey, and Zettl<sup>20</sup> have shown that uniaxial stress and  $\mu_0H$  act on the same piece of the Fermi surface. This was confirmed by Tseng, Tessema, and Skove<sup>21</sup> who observed pronounced effect of strain on the resistance and thermopower of NbSe<sub>3</sub> below 59 K. Shi, Chepin, and Ross<sup>22</sup> have conducted NMR experiments to study the density of states on the different chains in  $NbSe<sub>3</sub>$ . Although magnetic fields effects on the Ohmic regime, below  $E_T$ , are much more pronounced below the second transition than below  $T_{p1}$ , their results show that most of the changes in FS are due to changes in density of states on the chain associated with the upper CDW rather than the lower CDW. This supports the notion that the strain-induced changes in  $E_T$  of the upper CDW are associated with changes in the Fermi surface most closely associated with the chain corresponding to the upper CDW. The relatively small effects on the density of states associated with the lower CDW could account for the rather weak effect on the  $E_T$  of the lower CDW.

# **IV. CONCLUSION**

It was previously reported that uniaxial stress enhances  $E_T$  for the upper CDW in NbSe<sub>3</sub>. In this paper we report a systematic study of the effect of  $\varepsilon$  on  $E_T$ ,  $T_P$ , and the Fermi surface of this compound. We show that the divergence of  $E_T$  near 2.6% strain is intimately related to stress-induced changes in fermiology. We propose that the two most likely possibilities for this phenomena are  $(1)$  a stress induced incommensurate to commensurate transition  $(2)$  or more likely an  $\varepsilon$  driven matching of the Friedel oscillations and the CDW oscillations of the upper CDW. Structural studies under stress should give a further insight into the subject.

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