

## Lattice effects on an impurity center: $\text{CuX}_4(\text{NH}_3)_2^{2-}$ centers ( $X = \text{Cl}, \text{Br}$ ) in $\text{NH}_4\text{X}$

J. A. Aramburu and M. Moreno

*Departamento de Ciencias de la Tierra y Física de la Materia Condensada, Facultad de Ciencias,  
Universidad de Cantabria, 39005 Santander, Spain*

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The optical properties of  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers embedded in  $\text{NH}_4\text{X}$  lattices ( $X = \text{Cl}, \text{Br}$ ) where  $\text{Cu}^{2+}$  occupies an *interstitial* position have been explored through MS  $X\alpha$  calculations performed at different values of the  $\text{Cu}^{2+}\text{-X}^-$  ( $R_{\text{eq}}$ ) and  $\text{Cu}^{2+}\text{-N}$  ( $R_{\text{ax}}$ ) distances. The calculations include the effect of the electrostatic potential due to the *rest of the lattice*,  $V_R$ , upon the *localized* electrons of the center. It has been shown that  $V_R$  decreases significantly the separation between  $n_L p(X)$  and  $2p(N)$  orbitals ( $n_L = 3$  for Cl;  $n_L = 4$  for Br) and thus plays a key role for understanding the existence of four charge transfer (CT) bands in the optical domain. The high splitting found between orbitals mainly built from  $|2p_z(N)\rangle$  and  $|2p_j(N)\rangle$  ( $j = x, y$ ) is shown to arise from an *internal* splitting in the  $\text{NH}_3$  molecule *transferred* to the complex. From the  $R_{\text{eq}}$  and  $R_{\text{ax}}$  dependence of CT transitions, it is shown that the  $600\text{-cm}^{-1}$  redshift undergone by the first CT transition of  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  in  $\text{NH}_4\text{Cl}$  just below  $T_c = 243$  K involves an  $R_{\text{eq}}$  increase of  $\sim 2$  pm in agreement with Raman data. The present results stress the importance of  $V_R$  for a right understanding of properties due to impurities placed at *off-center* positions. [S0163-1829(97)07225-1]

### I. INTRODUCTION

Optical and electron paramagnetic resonance (EPR) data due to impurities in insulators have usually been explained considering *only* the complex formed by the impurity and the anions of different species adjacent to the impurity. This idea was reinforced by the theoretical work carried out by Sugano and Shulman.<sup>1</sup> These authors pointed out that in cubic lattices like  $\text{KMgF}_3$  the electrostatic potential due to the *rest of the lattice* (called  $V_R$ ) upon the electrons of a  $\text{MF}_6$  complex ( $M = \text{Ni}^{2+}, \text{Mn}^{2+}$ , etc.) formed by a *substitutional* divalent impurity is certainly very flat. Therefore, if the electrons responsible for the properties of the impurity are localized in the complex, the potential  $V_R$  influences neither the optical transitions nor the wave functions and can be ignored.

Subsequent work on substitutional impurities in cubic materials has revealed the validity of such an idea. For instance, it has been shown experimentally that a given complex embedded in different host lattices, but of the *same type*, does not exhibit the same EPR and optical parameters through the series.<sup>2-8</sup> This fact has reasonably been explained simply through the changes on the metal-ligand distance of the complex,  $R$ , induced by changing from one host lattice another one.<sup>3-5,6,8</sup> Owing to this fact, a parameter like  $10Dq$  has been used to measure the actual  $R$  value of impurities like  $\text{Mn}^{2+}$  or  $\text{Ni}^{2+}$  in fluoroperovskites.<sup>6,8,4</sup>

It can reasonably be expected that the degree of flatness contained in  $V_R$  depends, however, not only on the *type* of lattice where the impurity is placed, but also on the *position* (substitutional, interstitial, off center) occupied by the impurity in the host lattice. The importance of this idea was partially realized in the analysis<sup>9</sup> of the experimental  $10Dq$  values of  $\text{CrF}_3$  and  $\text{K}_2\text{NaCrF}_6$ . Both materials<sup>9</sup> involve the same  $\text{CrF}_6^{3-}$  unit, but possess a *different* space group. Experimentally, it has been found that in the first compound  $R = 1.90 \text{ \AA}$  and  $10Dq = 14\,650 \text{ cm}^{-1}$ , while, in  $\text{K}_2\text{NaCrF}_6$ ,

$R = 1.93 \text{ \AA}$  and  $10Dq = 16\,100 \text{ cm}^{-1}$ . These results can hardly be understood in terms of isolated  $\text{CrF}_6^{3-}$  complexes subjected to a constant electrostatic potential. In fact, experimental studies on impurities like  $\text{Mn}^{2+}$  or  $\text{Cr}^{3+}$  in high-symmetry sites have shown<sup>6,8,10-12</sup> that the  $R$  dependence of  $10Dq$  can be written as

$$10Dq = KR^{-n}, \quad (1)$$

where the exponent  $n$  is close to 5. Theoretical calculations<sup>13,14</sup> on isolated complexes are in agreement with that experimental result, while the microscopic origin of Eq. (1) within a molecular orbital scheme has been analyzed recently.<sup>15</sup> The amazing increase of  $10Dq$  on passing from  $\text{CrF}_3$  ( $R = 1.90 \text{ \AA}$ ) to  $\text{K}_2\text{NaCrF}_6$  ( $R = 1.93 \text{ \AA}$ ) has reasonably been explained through the different form of  $V_R$  in both lattices.<sup>9</sup> In  $\text{CrF}_3$ ,  $V_R$  induces an *additional* separation between  $3d$  and ligand orbitals favoring a diminution of  $10Dq$ . A similar situation to this one has recently been encountered when comparing<sup>16</sup> the EPR data due to  $\text{Ag}^{2+}$  placed in a perovskite lattice ( $\text{CsCdF}_3$ ) and  $\text{NaF}$ . In the latter case, it has been shown that  $V_R$  induces a supplementary decrement of  $g_{\parallel} - g_0$ .

It can be expected that effects arising from the nonflatness of  $V_R$  will be *more pronounced* for optical transitions involving *jumps* from a mainly *ligand level* to a mainly *d level*. This work is devoted to show the relevance of  $V_R$  for understanding the experimental charge transfer (CT) spectra of  $\text{Cu}(\text{NH}_3)_2\text{X}_4^{2-}$  centers formed in  $\text{NH}_4\text{X}$  ( $X = \text{Cl}, \text{Br}$ ) lattices.<sup>17-21</sup> Such centers are good candidates for observing effects coming from the electrostatic potential of the rest of the lattice because Cu is placed in an *interstitial* position and *not* in a substitutional one (Fig. 1). Owing to this fact, the  $\text{X}^-$  and  $\text{NH}_3$  ligands are placed in *nonequivalent* crystallographic directions of the  $\text{NH}_4\text{X}$  lattice. Moreover, the  $\text{N-Cu}^{2+}$  ( $R_{\text{ax}}$ ) and  $\text{Cl-Cu}^{2+}$  ( $R_{\text{eq}}$ ) distances are very different, favoring different  $V_R$  values at  $\text{Cl}^-$  or  $\text{NH}_3$  positions.

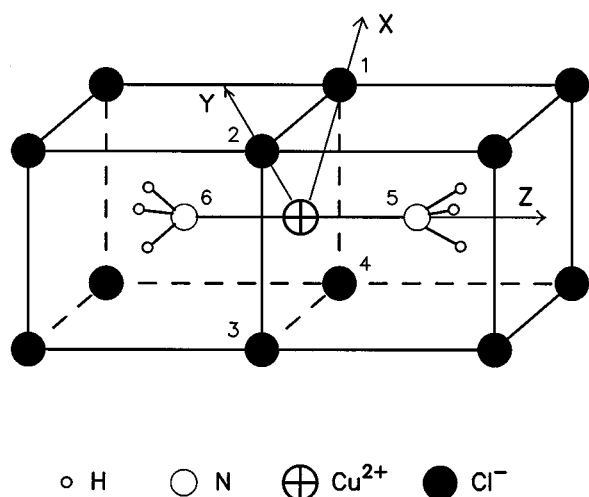


FIG. 1. Picture of the  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  center formed in  $\text{NH}_4\text{X}$  ( $X = \text{Cl}, \text{Br}$ ) host lattices.  $\text{Cu}^{2+}$  is placed interstitially in the middle of a (100) face made of  $\text{X}^-$  ions, while two  $\text{NH}_3$  molecules occupy  $\text{NH}_4^+$  vacancies.

Although  $R_{\text{ax}}$  and  $R_{\text{eq}}$  are not known for the present cases in compounds like  $\text{Cu}(\text{NH}_3)_2\text{X}_2$  ( $X = \text{Cl}, \text{Br}$ ), the  $\text{Cu}(\text{NH}_3)_2\text{X}_4^{2-}$  complexes are formed and so  $R_{\text{ax}}$  and  $R_{\text{eq}}$  have been measured<sup>22,23</sup> through x-ray diffraction. For instance, for the bromine complex,<sup>22</sup>  $R_{\text{ax}} = 2.03 \text{ \AA}$  and  $R_{\text{eq}} = 2.87 \text{ \AA}$  have been measured. These distances coincide with those expected for the  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  complex placed in the undistorted  $\text{NH}_4\text{Br}$  lattice as shown in Fig. 1. A similar situation occurs for the  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  complex for which the metal-ligand distances will be close to  $R_{\text{ax}} = 1.96 \text{ \AA}$  and  $R_{\text{eq}} = 2.76 \text{ \AA}$ .

The study of  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers is also attractive because of their peculiar electronic structure. In fact, in tetragonal centers of  $d^9$  ions ( $\text{Cu}^{2+}$ ,  $\text{Ag}^{2+}$ ,  $\text{Ni}^+$ ) the unpaired electron usually lies in a  $\sim x^2 - y^2$  orbital, while in the present cases it is located in a  $\sim 3z^2 - r^2$  orbital, giving rise to  $\sigma$  bonding with both equatorial and axial ligands. On the

other hand, a  $|3z^2 - r^2\rangle$  orbital can be hybridized with the  $|4s\rangle$  orbital of the central ion in a  $D_{4h}$  symmetry. It has been pointed out that such an hybridization is very sensitive to changes of  $R_{\text{eq}}$  and  $R_{\text{ax}}$ , inducing remarkable changes of the isotropic hyperfine constant  $A_{\text{iso}}$ , well observed experimentally.<sup>24,25</sup>

The CT spectra of systems containing  $\text{CuX}_6^{4-}$  ( $X = \text{Cl}, \text{Br}$ ) units is composed<sup>26-28</sup> of two prominent bands related to jumps from the two mainly ligand  $e_u$  orbitals. By contrast, in the CT spectra<sup>29</sup> of  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  in  $\text{NH}_4\text{Br}$  at  $T = 14 \text{ K}$  (in the cubic phase of  $\text{NH}_4\text{Br}$ ) it can clearly be seen the existence of four bands (Fig. 2) peaked at 25 500, 28 500, 31 600, and 37 500  $\text{cm}^{-1}$ . In the case of  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$ , apart from two dominant bands peaked at 33 700 and 39 500  $\text{cm}^{-1}$ , another band peaked at 43 200  $\text{cm}^{-1}$  is also visible.<sup>30</sup> If we accept that the two lowest bands in Fig. 2 involve  $\text{Br}^- \rightarrow \text{Cu}^{2+}$  jumps, it is not certainly easy to assign the bands peaked at 31 600 and 37 300  $\text{cm}^{-1}$  as being due to  $\text{NH}_3 \rightarrow \text{Cu}^{2+}$  jumps. In fact, following the optical electronegativity of  $\text{Br}$  ( $\chi = 2.8$ ) and  $\text{NH}_3$  ( $\chi = 3.3$ ), one could expect that the  $\text{NH}_3 \rightarrow \text{Cu}^{2+}$  CT bands of  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  start at about 45 000  $\text{cm}^{-1}$ .

A reasonable explanation of these experimental features is attempted through this work by means of MS  $X\alpha$  calculations. Particular attention is paid to the form of  $V_R$  inside the  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers as well as to its influence upon the observed CT spectrum of such  $\text{Cu}^{2+}$  centers.

## II. THEORETICAL

Properly speaking, the symmetry group displayed by a  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  unit is not  $D_{4h}$ , but  $C_{2h}$ . We have verified, however, that in the orbitals of interest in the present work, the splitting induced by hydrogen atoms is essentially negligible. Therefore we shall label the electron orbitals according to the  $D_{4h}$  group. A picture of relevant one-electron levels is offered in Fig. 3. We have assumed for the  $\text{NH}_3$  molecule the

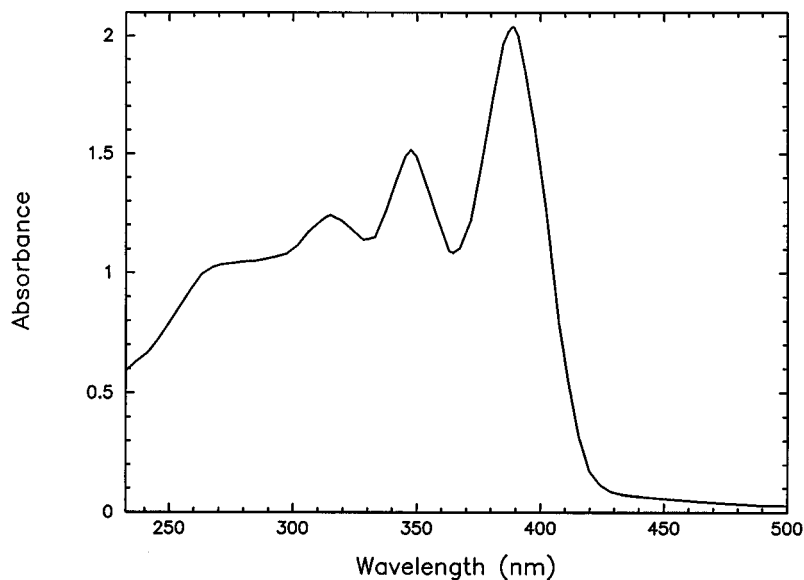


FIG. 2. Charge transfer spectrum of the  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  center in  $\text{NH}_4\text{Br}$  taken at 14 K (Ref. 29).

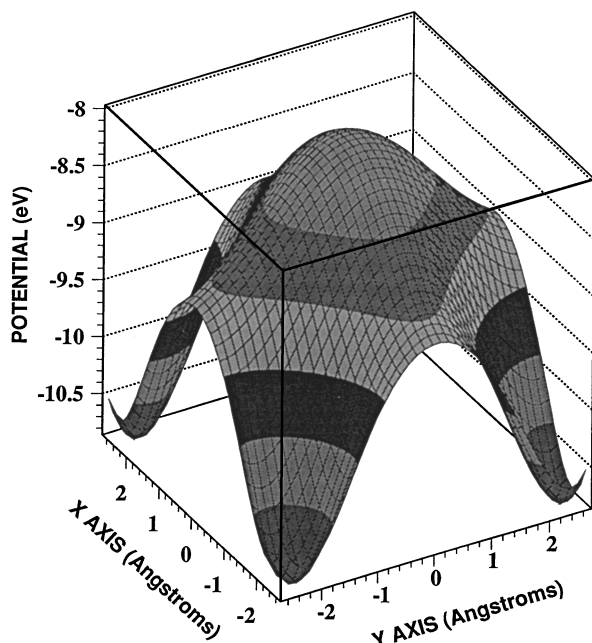


FIG. 3. Picture of the potential energy  $U_R(\mathbf{r})$  (in eV) due to the rest of the  $\text{NH}_4\text{Cl}$  lattice on an electron of the  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  center taken in the  $xy$  plane of Fig. 1. The point  $x=0, y=0$  corresponds to  $\text{Cu}^{2+}$  while the four  $\text{Cl}^-$  ions are found at  $(x=\pm 2.7, y=0)$ ;  $(x=0, y=\pm 2.7)$ . All distances are given in Å. In this region the lowest value of  $U_R$  is reached at the  $\text{Cu}^{2+}$  position, while, at  $\text{Cl}^-$ ,  $U_R$  is 1 eV higher.

same experimental geometry as the free molecule, while  $R_{\text{ax}}$  and  $R_{\text{eq}}$  distances have been varied, keeping a compressed  $D_{4h}$  geometry. This follows the interest in exploring the sensitivity of crystal-field (CF) and CT transition energies to changes of  $R_{\text{ax}}$  and  $R_{\text{eq}}$  as well as to the lack of precise  $R_{\text{ax}}$  and  $R_{\text{eq}}$  values for the equilibrium positions of the present systems.

For a  $\text{Cu}^{2+}$  impurity placed in a local  $D_{4h}$  symmetry, electric dipole CT jumps of the type  $|L\rangle \rightarrow |a_{1g}^*\rangle$  require that  $|L\rangle$  belong to  $E_u$  or  $A_{2u}$ . For a  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  center, it is easy to see that *three*  $E_u$  levels and *two*  $A_{2u}$  levels should appear, considering the four  $n_{LP}$  atomic orbitals of halogens ( $n_L=3$  for Cl,  $n_L=4$  for Br) and the two  $2p(\text{N})$  orbitals. The electronic structure of  $E_u$  and  $A_{2u}$  levels involved in the allowed CT transitions is rather complex. So in a  $A_{2u}$  level there is in principle a *hybridization* between equatorial ligand orbitals and axial ligand orbitals as well as an admixture of the  $|4p_i(\text{Cu})\rangle$  wave function. Besides for a  $E_u$  orbital, there are also *two* different types of linear combination of atomic orbitals (LCAO) involving *only* the equatorial ligands. The inclusion of the six involved H atoms lowers the symmetry to  $C_{2h}$ , giving rise to a splitting of all  $e_u$  orbitals. In our calculations such a splitting is found to be *always less* than  $30 \text{ cm}^{-1}$ . It is worth noting, however, that the  $1s$  orbitals of six H atoms play an important role in the description of some relevant charge transfer levels. This point is discussed in detail in Sec. III. Calculations on  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers embedded in  $\text{NH}_4\text{X}$  lattices have been performed by means of the self-consistent field multiple-scattering  $X\alpha$  (MS  $X\alpha$ ) method.<sup>31,32</sup> Atomic sphere radii were chosen using the Norman criterion,<sup>33</sup> with a small modification in or-

der to take into account the specificity of the H atoms.<sup>34</sup> So sphere radii that contain the atomic number of electrons were calculated from the initial molecular potential derived from neutral atoms. Then these radii were reduced by a factor of 0.98, given an average overlap ratio of about 20%. Always using this procedure, not only the experimental CF and CT transitions of several centers involving  $d^9$  and  $d^3$  ions have been reasonably explained, but also their sensitivity to variations of metal-ligand distances.<sup>16,35,36</sup> In  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  complexes, the calculated H radii are, however, greater than N-H distances, and so we have always considered radii equal to 1 bohr.<sup>34</sup> The  $\alpha$  values used in the atomic regions were those determined by Schwarz.<sup>37</sup> Transition energies were considered using the Slater transition-state procedure.<sup>31</sup> More details can be found in Ref. 35.

In order to clarify the role played by the rest of the lattice potential,  $V_R$ , upon the electronic properties of  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers, two types of calculations have been carried out for each couple of  $R_{\text{eq}}$  and  $R_{\text{ax}}$  distances. In the first one,  $V_R$  has simply been approximated by a constant potential using a Watson sphere of  $+2e$  charge coincident with the outer sphere. In the second type,  $V_R$  on an atomic sphere has been taken as the Madelung potential due to all  $X^-$  and  $\text{NH}_4^+$  ions of the lattice *not* involved in the  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  center. In this case, a weighted average potential has been used for the intersphere region, while a  $Q/r$  ( $Q=+2e$ ) potential has been taken for the outer sphere. Ewald's method<sup>38</sup> has been used for computing  $V_R$ .

### III. REMAINDER OF THE LATTICE POTENTIAL

Let us take the origin of coordinates in Fig. 1 at the  $\text{Cu}^{2+}$  position. The electrostatic potential at a point  $\mathbf{r}$  of the  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  center due to the rest of the lattice can easily be calculated as

$$V_R(\mathbf{r}) = V_T(\mathbf{r}) - V_C(\mathbf{r}). \quad (2)$$

Here  $V_T(\mathbf{r})$  means the electrostatic potential due to the full  $\text{NH}_4\text{X}$  lattice at  $\mathbf{r}$ , while  $V_C(\mathbf{r})$  is the potential generated by the four  $X^-$  anions at  $(\pm a\sqrt{2}/2, 0, 0)$  and  $(0, \pm a\sqrt{2}/2, 0)$  and the two  $\text{NH}_4^+$  ions at  $(0, 0, \pm \frac{1}{2}a)$  in the perfect lattice.

For the present purposes, when  $\mathbf{r}$  corresponds to a lattice point  $R_L$ , the self-potentials  $\bar{V}_T(\mathbf{r})$  and  $\bar{V}_C(\mathbf{r})$  should be employed instead of  $V_T(\mathbf{r})$  and  $V_C(\mathbf{r})$ . It just means that the contribution arising from the ion at  $\mathbf{R}_L$  should be omitted.<sup>38</sup> The potential energy for an electron "feeling"  $V_R$  is just  $U_R = (-e)V_R$  and is shown in Figs. 3 and 4. Both figures clearly reveal that  $U_R$  is far from being flat in the  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  center placed in  $\text{NH}_4\text{Cl}$ . For instance,  $U_R$  at the  $\text{Cl}^-$  position is about 1 eV smaller than at the  $\text{Cu}^{2+}$  position. At the same time,  $U_R$  increases the energy of electrons at the  $\text{NH}_3$  position with respect to those at the  $\text{Cu}^{2+}$  position by 2.8 eV.

The main aspects about  $U_R$  depicted in Figs. 3 and 4 can easily be derived using the results for the potential  $\psi(\mathbf{r})$  of the so-called neutralized cubic lattice explained in Ref. 38. For instance, at the  $\text{Cu}^{2+}$  position  $V_T$  is simply given by

$$V_T(\text{Cu}^{2+}) = e\{\psi(1/2, 0, 0) - \psi(1/2, 1/2, 0)\}, \quad (3)$$

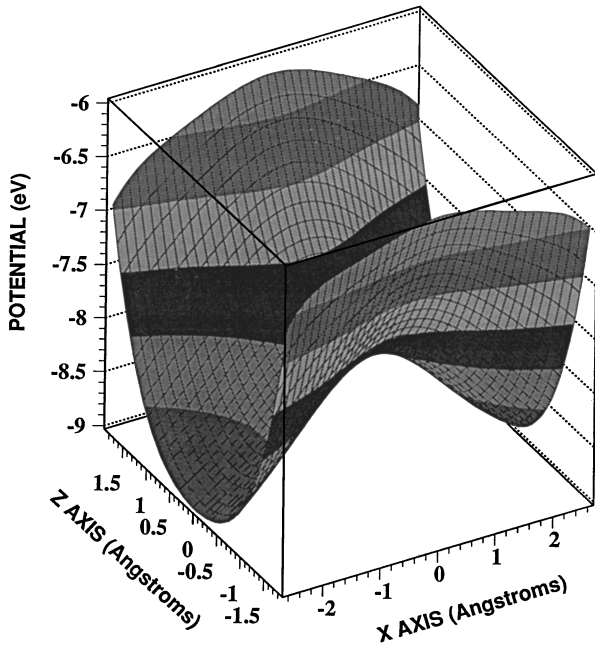


FIG. 4. Picture of  $U_R(\mathbf{r})$  for the electrons of the  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  center embedded in  $\text{NH}_4\text{Cl}$  when  $\mathbf{r}$  varies along the  $xz$  plane of Fig. 1. The difference between the potential energy at  $\text{N}(x=0, z=1.9)$  and at  $\text{Cl}(x=2.7, z=0)$  is equal to 4.8 eV. The distances are given in Å.

where  $\psi(1/2, 0, 0) = -0.096/a$ ,  $\psi(1/2, 1/2, 0) = -0.583/a$ , and  $a$  is the lattice parameter of the CsCl-like lattice. From here and Eq. (2), it is derived that

$$U_R(\text{Cu}^{2+}) = -2.14 \frac{e^2}{a} \quad (4)$$

and, similarly,

$$U_R(\text{X}^-) = -2.43 \frac{e^2}{a}, \quad U_R(\text{NH}_3) = -1.58 \frac{e^2}{a}. \quad (5)$$

As the difference found between  $U_R(\text{NH}_3)$  and  $U_R(\text{X}^-)$  is certainly high (about 4 eV), one can thus envisage that

$U_R$  plays a relevant role for achieving a right microscopic understanding of optical transitions due to  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers in  $\text{NH}_4\text{X}$  lattices.

#### IV. RESULTS

The transition energies for the allowed CT and the parity-forbidden CF transitions of the  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  center in  $\text{NH}_4\text{Br}$  calculated at different  $R_{\text{ax}}$  and  $R_{\text{eq}}$  values are displayed in Table I. The results obtained either including the properly  $V_R$  or taking it just as a constant are both reported in Table I. Insight into the composition of the one-electron orbitals associated with the  ${}^2A_{1g}$  ground state is given in Table II. In this case the figures correspond to a calculation performed at  $R_{\text{ax}} = 2.0$  Å,  $R_{\text{eq}} = 2.85$  Å, and including the effect of the rest of the lattice electrostatic potential  $V_R$ .

The ordering of relevant one-electron orbitals found in the present calculations is outlined in Table I. For the three couples of axial and equatorial distances, the unpaired electron is found to be placed in the antibonding  $5a_{1g}$  level. Though this level is mainly built from the  $3z^2 - r^2$  wave function of Cu (Table II), it exhibits, however, a significant admixture of  $4p(\text{Br})$ ,  $2p(\text{N})$ , and also  $4s(\text{Cu})$  wave functions. That admixture reflects, but indirectly, the presence of bonding levels mainly built from  $4p(\text{Br})$  and  $2p(\text{N})$  not far from the antibonding CF levels. This is confirmed by Table I where the separation between the highest CF excitation and the lowest allowed CT transition is always less than  $13\,000\text{ cm}^{-1}$ .

The lowest CT transitions involve the  $4e_u$ ,  $3e_u$ , and  $3a_{2u}$  levels. It is worth noting that  $4e_u$  and  $3e_u$  levels exhibit an almost pure  $4p(\text{Br})$  character, while in  $3a_u$ , though mainly built from  $4p(\text{Br})$ , the amount of  $2p(\text{N})$  character increases by a factor close to 7 with respect to what is found in  $3e_u$ . The highest allowed CT transition involves a  $2e_u$  orbital where only a 1% of  $4p(\text{Br})$  is present. Nevertheless, this  $2e_u$  orbital is far from displaying a pure  $2p(\text{N})$  character because it involves about 30% of  $1s$  orbitals of six hydrogens.

As shown in Table I, the inclusion of  $V_R$  in the calculations gives rise to *substantial* changes in the CT spectrum.

TABLE I. Values of crystal-field and allowed charge transfer transitions of the  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  unit embedded in  $\text{NH}_4\text{Br}$  calculated for different values of the axial ( $R_{\text{ax}}$ ) and equatorial ( $R_{\text{eq}}$ ) metal-ligand distances given in pm. In the calculation called ‘‘Madelung,’’ the effect of the rest of the lattice potential  $V_R$  has been considered, while in the so-called Watson  $V_R$  has been approximated by a constant potential. The energy of transitions (given in  $\text{cm}^{-1}$ ) have been computed using the Slater’s transition-state method. Experimental values are included for comparison (Ref. 29).

Transition	Experimental	$R_{\text{eq}} = 285$		$R_{\text{ax}} = 190$		$R_{\text{eq}} = 285$		$R_{\text{ax}} = 200$		$R_{\text{eq}} = 280$		$R_{\text{ax}} = 200$	
		Madelung	Watson	Madelung	Watson	Madelung	Watson	Madelung	Watson	Madelung	Watson	Madelung	Watson
$3b_{1g} \rightarrow 5a_{1g}$	—	9600	7980	8050	6210	8080	6290						
$3e_g \rightarrow 5a_{1g}$	$\sim 13300$	15650	14500	14430	12850	15030	13940						
$2b_{2g} \rightarrow 5a_{1g}$	$\sim 13300$	16290	14950	14870	13360	15450	13930						
$4e_u \rightarrow 5a_{1g}$	25550	28950	23890	26950	22220	27920	23100						
$3a_{2u} \rightarrow 5a_{1g}$	28530	31110	26720	28300	24690	29080	25660						
$3e_u \rightarrow 5a_{1g}$	31600	33300	28300	31460	26800	32830	28070						
$2a_{2u} \rightarrow 5a_{1g}$	36790	43730	51630	37170	45390	38130	45320						
$2e_u \rightarrow 5a_{1g}$		73790	85090	69430	80420	70180	80610						

TABLE II. Charge distribution (in %) corresponding to relevant one-electron levels of  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers embedded in  $\text{NH}_4\text{X}$  lattices. The values given here come from calculations properly including the effect of the rest of the lattice potential. First-row results correspond to  $X=\text{Br}$  computed at  $R_{\text{eq}}=285$  pm,  $R_{\text{ax}}=200$  pm, while those given in the second row are for  $X=\text{Cl}$  calculated at  $R_{\text{eq}}=270$  pm,  $R_{\text{ax}}=190$  pm.

Orbital	Cu			X		N		H
	3d	4s	4p	$n_{Ls}$	$n_{LP}$	2s	2p	1s
$5a_{1g}$	57.34	6.15		1.62	20.58	1.51	12.15	0.65
	60.56	8.98		2.49	15.98	1.14	10.27	0.55
$4e_u$			1.11	0.21	98.33		0.22	0.13
			0.87	0.14	98.50		0.33	0.16
$3e_u$			2.49	0.20	95.49		1.22	0.60
			2.02	0.11	95.51		1.57	0.79
$3a_{2u}$			1.30		90.43	1.16	6.69	0.42
			3.17		82.33	1.44	12.22	0.83
$2a_{2u}$			18.95		8.86	2.11	64.89	5.18
			18.92		15.50	1.61	59.05	4.91
$2e_u$			0.90	0.42	1.36		67.15	30.17
			1.15	0.45	1.90		66.43	30.07

Let us call  $\Delta_{1,5}$  the separation between the lowest ( $4e_u \rightarrow 5a_{1g}$ ) and the highest ( $2e_u \rightarrow 5a_{1g}$ ) allowed CT excitations. When  $V_R$  is taken as constant  $\Delta_{1,5} = 57\,000\text{ cm}^{-1}$ , while when it is properly included  $\Delta_{1,5}$  becomes equal only to  $42\,000\text{ cm}^{-1}$ . The origin of this significant reduction can basically be understood from the results given in Sec. III. It was shown there that  $V_R$  tends to raise the one-electron energies of  $2p(\text{N})$  orbitals while decreasing the corresponding to  $4p(\text{Br})$  orbitals.

As shown in Table I, the agreement between the experimental<sup>29</sup> CT transitions and the calculated ones is certainly improved when the effect of  $V_R$  is properly taken into account. For instance, at  $R_{\text{ax}}=2.00\text{ \AA}$  and  $R_{\text{eq}}=2.85\text{ \AA}$  the present calculations not only predict the existence of four (and not five) CT transitions of the  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  center in  $\text{NH}_4\text{Br}$  lying in the optical domain, but also the reported values are in reasonable agreement with experimental<sup>29</sup> data. By contrast, when the effect of the actual  $V_R$  is discarded the separation  $\Delta_{1,4}$  between the lowest and highest CT transitions lying in the optical domain is about  $20\,000\text{ cm}^{-1}$ , while experimentally  $\Delta_{1,4}$  is close to  $11\,000\text{ cm}^{-1}$ .

The calculated  $3b_{1g} \rightarrow 5a_{1g}$  and  $3e_g \rightarrow 5a_{1g}$  CF transitions are also close to the experimental figures. As expected, these transitions coming from the  $d \rightarrow d$  transitions of copper are less sensitive to the inclusion of  $V_R$ .

Let us mention that the analysis of experimental data<sup>29</sup> indicated that the second CT transition observed at 14 K corresponds to  $3e_u \rightarrow 5a_{1g}$  and not to  $3a_{2u} \rightarrow 5a_{1g}$  as obtained in the present calculations. The separation between such transitions amounts, however, only to  $\sim 3000\text{ cm}^{-1}$  and is only resolved at low temperatures in the cubic phase of  $\text{NH}_4\text{Br}$ .

The results<sup>30</sup> for the  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  center in  $\text{NH}_4\text{Cl}$  collected in Table III display similar trends to those corresponding for the  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  center in  $\text{NH}_4\text{Br}$ . Nevertheless, though the ordering of levels is the same, the first  $4e_u \rightarrow 5a_{1g}$  CT transition is calculated to appear at about  $36\,000\text{ cm}^{-1}$  for  $R_{\text{eq}}=2.70\text{ \AA}$  and  $R_{\text{ax}}=1.90\text{ \AA}$ , implying a blueshift of  $\sim 9000\text{ cm}^{-1}$  with respect to what was found for  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$ . This blueshift is thus consistent with the higher optical electronegativity<sup>31</sup> of chlorine ( $\chi=3.0$ ) when compared to that of bromine ( $\chi=2.8$ ).

TABLE III. Transition energies (in  $\text{cm}^{-1}$ ) of the  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  center embedded in  $\text{NH}_4\text{Cl}$  computed at different values of the metal-ligand distances  $R_{\text{ax}}$  and  $R_{\text{eq}}$  (given in pm). In the calculations denoted as ‘‘Madelung,’’ the effect of  $V_R$  has been included. Experimental values (measured at 14 K) are included for comparison purposes (Ref. 30).

Transition	Experimental	$R_{\text{eq}}=260$	$R_{\text{ax}}=190$	$R_{\text{eq}}=270$	$R_{\text{ax}}=190$	$R_{\text{eq}}=270$	$R_{\text{ax}}=200$
		Madelung	Watson	Madelung	Watson	Madelung	Watson
$3b_{1g} \rightarrow 5a_{1g}$	9300	10730	8960	10590	8820	9180	6920
$3e_g \rightarrow 5a_{1g}$	12400	17030	16260	16020	14950	15250	13600
$2b_{2g} \rightarrow 5a_{1g}$	13950	17570	16530	16610	15010	15440	13670
$4e_u \rightarrow 5a_{1g}$	33720	38280	30620	36150	29440	33990	26350
$3a_{2u} \rightarrow 5a_{1g}$		37170	32830	37500	31650	33940	28250
$3e_u \rightarrow 5a_{1g}$	39480	42850	35450	40070	33520	37980	30650
$2a_{2u} \rightarrow 5a_{1g}$	43200	45250	52190	44250	52050	37630	45850
$2e_u \rightarrow 5a_{1g}$		75700	85960	75500	85670	71310	

The increase of CT excitation energies on going from  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  to  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  also favors a parallel decrement of covalency well observed in Table III. For instance, for the  $5a_{1g}$  orbital of  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  the fraction of  $3p(\text{Cl})$  character is 16%, while in the case of  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  the fraction of  $4p(\text{Br})$  amounts to 21% (Table III).

As regards the theoretical values of CT excitation energies in  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$ , only those obtained considering the true  $V_R$  potential lead again to a reasonable agreement with experimental findings. In particular, the present calculations support the fact that the shoulder observed experimentally<sup>30</sup> at  $43\,200\text{ cm}^{-1}$  can be reasonably assigned to a  $2a_{2u} \rightarrow 5a_{1g}$  transition. Also, the first assignment of the experimental transitions at  $33\,720$  and  $39\,480\text{ cm}^{-1}$  as being due to electron jumps from the mainly  $3p(\text{Cl})$   $e_u$  orbitals is supported by the present theoretical study. With respect to the  $3a_{2u} \rightarrow 5a_{1g}$  transition, the present results indicate that it would lie between the  $4e_u \rightarrow 5a_{1g}$  and  $3e_u \rightarrow 5a_{1g}$  transitions. Experimentally, such a transition has, however, not yet been resolved maybe because the associated band is masked by those coming from  $4e_u \rightarrow 5a_{1g}$  and  $3e_u \rightarrow 5a_{1g}$  transitions whose bandwidth is close to  $2000\text{ cm}^{-1}$ . The calculated fifth allowed CT transition appears out of the optical domain as also happened for the  $\text{CuBr}_4(\text{NH}_3)_2^{2-}$  center in  $\text{NH}_4\text{Br}$ .

Although the present calculations indicate that only four of the allowed CT transitions lie in the optical range, it is also necessary to *understand why* the difference between the  $a_{2u}$  and  $2e_u$  orbitals is so high. In fact, taking as a guide the case of  $\text{CuCl}_4(\text{NH}_3)_2^{2-}$  both orbitals exhibit a *dominant*  $2p(\text{N})$  character, but the  $a_{2u}$  orbital is separated by *only*  $4000\text{ cm}^{-1}$  from the  $3e_u$  orbital, which exhibits a strong  $3p(\text{Cl})$  character. This makes possible a significant presence of  $3p(\text{Cl})$  character in  $a_{2u}$  and also of  $2p(\text{N})$  character in  $3a_{2u}$ . By contrast, the  $2e_u$  orbital, being mainly built from  $2p(\text{N})$ , is certainly far from the mainly  $3p(\text{Cl})$  levels. This feature is thus consistent with the almost negligible  $2p(\text{N})$  character displayed by  $3e_u$  and  $4e_u$  orbitals.

Let us now analyze the origin of the separation (called  $\Delta_{4,5}$ ) between the  $2a_{2u} \rightarrow 5a_{1g}$  and  $2e_u \rightarrow 5a_{1g}$  transitions. As shown Tables I and III  $\Delta_{4,5}$  is about  $32\,000\text{ cm}^{-1}$  for the present  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers formed in  $\text{NH}_4\text{X}$  lattices. For comparison purposes we have first looked at the results of MS  $X\alpha$  calculations<sup>39</sup> reached on the *compressed*  $D_{4h}$   $\text{CuCl}_6^{4-}$  species where *all* the ligands are single  $\text{Cl}^-$  ions. For instance, for  $R_{\text{ax}} = 2.20\text{ \AA}$  and  $R_{\text{eq}} = 2.80\text{ \AA}$  it is found<sup>39</sup> that  $\Delta_{4,5} = 3000\text{ cm}^{-1}$ , while  $\Delta_{4,5} = 5500\text{ cm}^{-1}$ , for  $R_{\text{ax}} = 2.10\text{ \AA}$  and  $R_{\text{eq}} = 2.80\text{ \AA}$ . These data clearly indicate that  $\Delta_{4,5}$  for the  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  center is roughly *one order of magnitude* larger than for the compressed  $\text{CuCl}_6^{4-}$  species. The value  $\Delta_{4,5}$  found for this case is also comparable to the splitting between  $e_u$  and  $a_{2u}$  orbitals in the simple case of the square-planar  $\text{CuCl}_4^{2-}$  unit where only equatorial ligands are present.

From this digression it appears that the  $\Delta_{4,5}$  splitting in  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers should arise mainly from an *intramolecular* splitting of the ammonia molecule. This idea is certainly reinforced when we look at the electronic structure<sup>40</sup> of  $\text{NH}_3$ . As this  $C_{3v}$  molecule is nearly planar, the highest occupied orbital is a  $A$  singlet, being also denoted as

$3\sigma$ . In this orbital, mainly composed of  $|p_z(\text{N})\rangle$ , the lone pair of  $\text{NH}_3$  is placed. The  $z$  direction involved in  $|p_z(\text{N})\rangle$  is depicted in Fig. 1. Below the  $A$  singlet orbital, a doublet  $E$  orbital (also denoted as  $1\pi$ ) appears where bonding effects with the hydrogen atoms are much stronger. This is again a direct consequence of the  $78^\circ$  angle between a  $\text{NH}$  direction and the principal axis of the  $\text{NH}_3$  molecule. Associated with this important difference between the bonding in the  $A$  singlet and the  $E$  doublet, a separation of  $\sim 40\,000\text{ cm}^{-1}$  appears between them.<sup>40</sup> This separation can of course be related to the  $\Delta_{4,5}$  values found for  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers (Tables I and III). Also, it is now easy to understand why the amount of  $1s(\text{H})$  in  $2e_u$  (Table II) is about 6 times higher than the corresponding to the  $2a_{2u}$  orbital, which as pointed out is related to the orbital of free  $\text{NH}_3$  where the lone pair is located.

Let us now briefly focus on the sensitivity to  $R_{\text{ax}}$  and  $R_{\text{eq}}$  changes displayed by the energy  $E$  of CT and CF transitions. As shown in Tables I and III the CT transition energies are in general more sensitive than CF transitions like  $3e_g \rightarrow 5a_{1g}$  or  $2b_g \rightarrow 5a_{1g}$  to variations of metal-ligand distances. This feature has also been found for other  $d^9$  systems as well as for  $\text{Cr}^{3+}$  in fluorides.<sup>35,36,39</sup> Analyzing the  $R_i$  dependence for CT transition energy in transition-metal complexes with moderate covalency, it has been shown<sup>36</sup> that  $\partial E/\partial R_i$  mainly reflects  $\partial(U_M - U_L)/\partial R_i$ . Here  $U_M$  means the electrostatic energy experienced by an electron placed in the metallic cation due to charged ligands, while  $U_L$  denotes the same contribution when the electron is located on a ligand. As normally  $U_M > U_L$  and  $\partial U_M/\partial R_i > \partial U_L/\partial R_i$ , the negative sign of  $\partial E/\partial R_i$  simply reflects an increase of the repulsive  $U_M$  energy upon decreasing  $R_i$ . For the  $4e_u \rightarrow 5a_{1g}$  and  $3e_u \rightarrow 5a_{1g}$  transitions of  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers,  $\partial E/\partial R_{\text{eq}}$  would be about  $-300\text{ cm}^{-1}/\text{pm}$ . This figure is smaller than  $\partial E/\partial R_{\text{eq}} \cong -600\text{ cm}^{-1}/\text{pm}$  measured<sup>41</sup> and calculated<sup>42</sup> for CT transitions of the square-planar  $\text{CuCl}_4^{2-}$  unit. This significant difference partially reflects the smaller value of  $R_{\text{eq}}$  corresponding to  $\text{CuCl}_4^{2-}$  ( $R_{\text{eq}} = 226\text{ pm}$ ) when compared to the equilibrium  $R_{\text{eq}}$  value of  $\text{CuX}_4(\text{NH}_3)_2^{2-}$ . On passing from  $\text{CuCl}_4^{2-}$  to  $\text{CrF}_6^{3-}$ , the increase of ligand number as well as the diminution of  $R$  ( $R = 190\text{ pm}$  for  $\text{CrF}_6^{3-}$  typically) leads<sup>36</sup> to values  $\partial E/\partial R_{\text{eq}} \cong -1500\text{ cm}^{-1}/\text{pm}$ .

Upon cooling from room temperature, the  $\text{NH}_4\text{Cl}$  lattice experiences a structural phase transition at  $T_c = 243\text{ K}$  which *decreases* by  $0.4\text{ pm}$  the lattice parameter.<sup>43</sup> The optical spectrum due to the  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  center embedded in  $\text{NH}_4\text{Cl}$  shows,<sup>30</sup> however, that the first  $4e_u \rightarrow 5a_{1g}$  transition undergoes a *redshift* of  $600\text{ cm}^{-1}$  (instead of a blueshift) just below  $T_c$ . This redshift was reasonably explained in terms of an *outwards* relaxation of  $\text{Cl}^-$  ions just below  $T_c$ , an idea which was corroborated by subsequent Raman experiments.<sup>44</sup> Accepting  $\partial E/\partial R_{\text{eq}} \cong -300\text{ cm}^{-1}/\text{pm}$ , the  $600\text{ cm}^{-1}$  redshift would imply an increase of  $R_{\text{eq}}$ ,  $\Delta R_{\text{eq}}$ , equal to  $\Delta R_{\text{eq}} = 2\text{ pm}$ , which is now in good agreement with the figure derived from Raman data.<sup>44</sup>

## V. FINAL REMARKS

It has been shown in the present work that the optical spectrum of  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers embedded in  $\text{NH}_4\text{X}$  can

be understood *only* when the effect of  $V_R$  is properly taken into account.  $V_R$  raises the  $2p(N)$  levels with respect to the  $n_L p(X)$  levels of the halide, favoring the existence of four CT's in the optical range. The fifth allowed CT transition is predicted to appear around  $70\,000\text{ cm}^{-1}$  mainly as a result of a high *intramolecular splitting* between  $A$  and  $E$  levels of  $\text{NH}_3$  molecules transferred to the center. It is worth noting that the first exciton band of pure  $\text{NH}_4\text{Br}$  appears<sup>45</sup> at  $51\,000\text{ cm}^{-1}$ , thus preventing the observation of any impurity absorption beyond that frequency.

As regards the intensities displayed by CT transitions, let us recall that in simple complexes like  $\text{CuCl}_4^{2-}$  CT transitions involving  $e_u$  orbitals are much more intense than the allowed  $2b_{2u} \rightarrow 3b_{1g}$  ( $\sim x^2 - y^2$ ) transitions, which have not been observed experimentally. Denoting a CT jump simply as  $\gamma_L \rightarrow \gamma_M$ , it has been shown<sup>41,46</sup> that CT transitions where *both* orbitals involve  $\sigma$  bonding exhibit a much higher oscil-

lator strength than the rest of the transitions. It is worth noting that for  $\text{CuX}_4(\text{NH}_3)_2^{2-}$  centers the *four* observed CT transitions involve jumps where the ligand orbital  $\gamma_L$  and the antibonding  $5a_{1g}$  *both* involve  $\sigma$  bonding. In fact, at variance with a  $\sim x^2 - y^2$  orbital, a  $\sim 3z^2 - r^2$  orbital can establish  $\sigma$  bonding with *both* axial as well as equatorial ligands.

As a general conclusion, the importance that  $V_R$  can play for a right understanding of properties due to impurity centers in partially ionic materials has been stressed through the present work. Such a relevance is increased for centers containing neighbor atoms in nonequivalent crystallographic positions. Further work along this line is now under way.

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