# Cohesive energy, local magnetic properties, and Curie temperature of Fe<sub>3</sub>B studied using the self-consistent LMTO method

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The electronic structure of Fe<sub>3</sub>B in orthorhombic (o-Fe<sub>3</sub>B) and body-centered tetragonal (bct-Fe<sub>3</sub>B) structures are calculated using the spin-polarized linear muffin-tin orbitals method. Based upon the calculated electronic structure, we present theoretical results on the cohesive energy ( $E_{coh}$ ), local magnetic moment ( $\mu_{loc}$ ), and hyperfine magnetic field (H<sub>hf</sub>) for the two phases of Fe<sub>3</sub>B. Effects of the neighboring atoms on  $\mu_{loc}$  and  $E_{coh}$  at individual Fe sites have been discussed in detail. Within the framework of the spin fluctuation of local moments we have evaluated the ratio of the Curie temperature  $T_C$  for o- and bct-Fe<sub>3</sub>B, and also investigated the volume dependence of  $T_C$ . Some numerical results are given and the theoretical results agree qualitatively with the experimental results. [S0163-1829(97)08430-0]

#### I. INTRODUCTION

The binary iron metalloid compound Fe<sub>3</sub>B crystallizes into two phases: the body-centered tetragonal (bct-Fe<sub>3</sub>B) and the orthorhombic  $(o-\text{Fe}_3\text{B})$ . In recent years they have been subjected to intense experimental and theoretical studies.<sup>1-4</sup> The great attention to Fe<sub>3</sub>B is not only because of the interest given to  $Fe_{1-x}B_x$  rapidly quenched crystalline alloys in which metastable Fe<sub>3</sub>B have been extensively discussed,<sup>5,6</sup> but also because Fe<sub>3</sub>B has the potential for significant applications. Metastable bct-Fe<sub>3</sub>B is the main phase in melt-spun permanent magnets with the approximate composition Nd<sub>4</sub>Fe<sub>78</sub>B<sub>18</sub>.<sup>7-9</sup> Due to the low Nd content the material is potentially much cheaper than the Nd<sub>2</sub>Fe<sub>14</sub>B isotropic meltspun ribbons. In a previous theoretical calculation of the electronic structure for o-Fe<sub>3</sub>B by Ching et al.<sup>4</sup> using the first-principles orthogonalized linear combinations of atomic orbitals method (OLCAO), the band structure of o-Fe<sub>3</sub>B was discussed.

To study systematically the magnetic properties of  $Fe_3B$ compounds and to investigate the effect of local environments on the properties of the compounds, we have carried out self-consistent theoretical calculations for bct-Fe<sub>3</sub>B and o-Fe<sub>3</sub>B. Based upon the results of the spin-polarized calculations for Fe<sub>3</sub>B, we study the cohesive energy  $(E_{coh})$  and magnetic properties of Fe<sub>3</sub>B in the two structures, and discuss the effects of neighboring atoms on the local magnetic moments ( $\mu_{\rm Fe}$ ) and Fermi contact hyperfine fields ( $H_{\rm FC}$ ) at the Fe sites when combining the calculated lattice-spacing dependences of  $\mu_{\rm Fe}$  and  $H_{\rm FC}$  for the two phases. Using the Mohn-Wohlfarth approximation within the framework of the spin fluctuation of local moments, we also discuss the Curie temperature  $T_C$  of Fe<sub>3</sub>B. Our theoretical results should be of value in understanding the electronic and magnetic properties of the  $Fe_{1-x}B_x$  alloy, and these results may clarify the magnetic properties of rapidly quenched Nd-Fe-B magnets with low Nd content.

This paper is organized as follows. We will describe the crystal structure of  $Fe_3B$  compounds in Sec. II. The linear muffin-tin orbitals (LMTO) method and the calculated tech-

niques are briefly described in Sec. III, and the calculated results on the electronic structure of Fe<sub>3</sub>B are also given in this section. In Sec. IV the cohesive energy and the magnetic properties of Fe<sub>3</sub>B are further discussed. Volume dependences of  $\mu_{\text{Fe}}$  and  $H_{\text{FC}}$  at Fe sites in both phases are also presented. Some concluding remarks are included in Sec. V.

## II. CRYSTAL STRUCTURE OF Fe<sub>3</sub>B

All Fe<sub>3</sub>B in two structures are metastable at low temperature and their crystal structures have been completely clarified. The orthorhombic Fe<sub>3</sub>B phase is believed to be less stable than the tetragonal phase. The structural information for both phases including lattice constants, type, and number of neighboring atoms are listed in Table I.

o-Fe<sub>3</sub>B is isostructural with Fe<sub>3</sub>C (cementite),<sup>10</sup> which has an orthorhombic structure with a space group of  $V_h^{16}(D_{2h}^{16};Pbnm)$ .<sup>11,12</sup> The unit cell contains 4 f.u. and there are two stoichiometrically different Fe sites, Fe<sub>1</sub>(4*c*) and Fe<sub>II</sub>(8*d*), and one B site (4*c*) for a total of 16 atoms in the cell. Fe atoms have two B neighbors while a B atom is coordinated by two Fe<sub>1</sub> and four Fe<sub>II</sub>. Fe<sub>1</sub> and Fe<sub>II</sub> have respectively 12 and 11 Fe atoms as neighbors, and the Fe<sub>II</sub>-Fe distances are slightly smaller than the Fe<sub>1</sub>-Fe distances.

bct-Fe<sub>3</sub>B has a body-centered-tetragonal lattice with a space group of  $S_4^2(\overline{I4})^{1,13}$  and 8 f.u. per cell. The structure can be considered as rather close packed, resulting in high coordination numbers. Iron atoms in three sets of eightfold positions are assigned to three different Fe sites: Fe<sub>1</sub>, Fe<sub>II</sub>, and Fe<sub>III</sub>. Fe<sub>I</sub> has 12 iron neighbors but Fe<sub>II</sub> and Fe<sub>III</sub> have 10 iron neighbors, respectively. They are coordinated by 2, 4, and 3 B atoms in turn. The B atoms in one eightfold position have 9 iron neighbors which form a capped triangular prism.

## III. COMPUTATIONAL PARAMETERS AND CALCULATED RESULTS

Using the LMTO method that was described and reviewed in Refs. 14 and 15, we here perform a semirelativistic

56

3153

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<u>56</u>

	o-Fe <sub>3</sub> B			bct-Fe <sub>3</sub> B				
Structure	Orthorhombic			Body-centered tetragonal				
Lattice cons.	a = 0.4454			a=0.8630				
(nm)		b = 0.5433						
	c = 0.6656			c = 0.4290				
Z (mol/cell)	4			8				
Space group	$Pbnm(V_h^{16})$			$I\overline{4} S_4^2$				
Sites	Fe <sub>I</sub>	Fe <sub>II</sub>	В	Fe <sub>I</sub>	Fe <sub>II</sub>	Fe <sub>III</sub>	В	
Neighbor atoms	2Fe <sub>1</sub> ,10Fe <sub>II</sub> 2B	5Fe <sub>I</sub> ,6Fe <sub>II</sub> 2B	2Fe <sub>I</sub> ,4Fe <sub>II</sub>	5Fe <sub>1</sub> ,2Fe <sub>11</sub> 5Fe <sub>111</sub> ,2B	2Fe <sub>1</sub> ,5Fe <sub>11</sub> 3Fe <sub>111</sub> ,4B	5Fe <sub>1</sub> ,3Fe <sub>11</sub> 2Fe <sub>111</sub> ,3B	2Fe <sub>1</sub> ,4Fe <sub>11</sub> 3Fe <sub>111</sub>	

TABLE I. Crystal structure information of Fe<sub>3</sub>B compounds.

spin-polarized band calculation on the two phases of iron metalloid compound Fe<sub>3</sub>B: *o*- and bct-Fe<sub>3</sub>B. For the merits and disadvantages of the method, as well as the technique details, refer to Refs. 14 and 15. In our calculation, the exchange-correlation term is taken as the form deduced by von Barth and Hedin.<sup>16</sup> The Brillouin-zone integration is carried out for  $64\vec{k}$  and  $75\vec{k}$  points in the irreducible zone of bct-and *o*-Fe<sub>3</sub>B, respectively. We use partial waves up to l=2 for the valence electrons of Fe, which are 3d, 4s electrons, and apply *s*, *p* orbitals for the 2s, 2p electrons of B. The convergence is assumed when the root-mean-square error of the self-consistent potential is smaller than 1 mRy.

In the atomic-sphere approximation (ASA) the atomic radius assigned to the atomic sites should be chosen so as to satisfy  $V = (4 \pi/3) \sum_i Q_i S_i^3$ , where V is the volume of unit cell, and  $S_i$  is the atomic radius of the equivalent  $Q_i$  atoms in the cell. Here we take the same radius for iron atoms located at different sites in the cell. For both structures of Fe<sub>3</sub>B we take the same ratio of radius  $p = S_B/S_{Fe} = 0.75$  which is approximately equal to the ratio of the covalent radius between boron and iron atoms, so the values of  $S_{Fe}$  and  $S_B$  are automatically defined by the above equation in accordance with the cell volume.

The calculations are also performed for the two phases of  $Fe_3B$  with various unit cell volumes, so that one can investigate the volume dependences of magnetic properties for  $Fe_3B$ . Moreover, here we would like to point out that, since the calculated results are sensitive to the chosen atomic radius and affected by the choice of the exchange-correlation potentials, it is inevitable that there are some quantitative errors when we compare the calculated results with the experimental results. Nevertheless, the qualitative agreement with experimental results is meaningful.

The spin-projected density of states (DOS) curve for each site in both Fe<sub>3</sub>B are shown in Fig. 1. As can be seen, *d* states dominate the DOS of Fe atoms and peak shapes for different iron sites in the same Fe<sub>3</sub>B are very similar. In both Fe<sub>3</sub>B the Fermi level lies nearly above the spin-up *d* DOS but falls actually in *d* DOS. Thus the occupation number  $n_d^{\uparrow}$  of electrons in the spin-up *d* subband is more than that in the spin-down *d* subband, and the *d* states for both spin directions contribute to the DOS at Fermi level,  $N(E_F)$ . The hybridized *s* states between Fe and B form a discretized structure in the lowest-energy region. Certainly there are different features between the DOS of the two Fe<sub>3</sub>B. The *d* 

DOS at Fe sites in the two structures have indicated great difference. Most d DOS of Fe in bct-Fe<sub>3</sub>B construct two peaks but those in o-Fe<sub>3</sub>B form a continuous region. In Table II we have listed some electronic structure parameters calculated on the two structures of Fe<sub>3</sub>B. It can be seen that in both Fe<sub>3</sub>B the average occupation  $\overline{n_d}$  of d electrons is the same, although the occupation number  $n_d$  at different Fe sites is quite different.

# **IV. DISCUSSIONS**

## A. Cohesive energy

It is well known that the cohesive properties of transitionmetal compounds are closely related to their electronic structure. The cohesive properties of 3d transition metal carbides



FIG. 1. The calculated spin-polarized local DOS at individual sites for both structures of Fe<sub>3</sub>B.

TABLE II. Calculated electronic structure parameters for Fe<sub>3</sub>B compounds. Here *n* and  $n_l$  denote total and *l* occupation number at a site, respectively.  $N(E_F)$  is DOS at the Fermi level (in units of states/spin Ry) and  $E_{\text{total}}$  represents the total energy of the system (in units of Ry).

	o-Fe <sub>3</sub> B			bct-Fe <sub>3</sub> B				
	Fe <sub>I</sub>	Fe <sub>II</sub>	В	Fe <sub>I</sub>	Fe <sub>II</sub>	Fe <sub>III</sub>	В	
$n_s^{\uparrow}$	0.311	0.312	0.404	0.309	0.313	0.317	0.428	
$n_n^{\uparrow}$	0.421	0.439	0.748	0.413	0.456	0.448	0.690	
$n_d^{\uparrow}$	4.369	4.300		4.396	4.318	4.324		
$n^{\uparrow}$	5.101	5.051	1.152	5.119	5.087	5.089	1.118	
$n_s^{\downarrow}$	0.316	0.318	0.423	0.317	0.315	0.324	0.451	
$n_{n}^{\downarrow}$	0.453	0.474	0.861	0.454	0.482	0.490	0.816	
$n_d^{\downarrow}$	2.276	2.367		2.206	2.401	2.330		
$n^{\downarrow}$	3.045	3.158	1.284	2.977	3.198	3.144	1.267	
$n^{\uparrow} + n^{\downarrow}$	8.146	8.209	2.436	8.096	8.285	8.233	2.385	
$n^{\uparrow}-n^{\downarrow}$	2.056	1.893	-0.132	2.142	1.889	1.945	-0.149	
$N(E_F)^{\uparrow}$	5.209	6.666	0.541	7.796	6.849	8.378	0.816	
$N(E_F)^{\downarrow}$	10.274	8.313	0.357	8.145	9.937	8.082	0.326	
$N(E_F)$	15.483	14.979	0.898	15.941	16.786	16.460	1.142	
E <sub>total</sub>		- 30690.689			- 30690.228			

have been studied both experimentally and theoretically<sup>17</sup> and *ab initio* results in carbides and nitrides with NaCl-type structure are also reported.<sup>18</sup> However, no such results are available for the borides. It is therefore of considerable interest to calculate the cohesive energies of the more complex transition-metal borides. Basing upon the calculated total energy  $E_{\text{total}}$  for Fe<sub>3</sub>B, we can estimate the cohesive energy  $E_{\text{coh}}$  of Fe<sub>3</sub>B compounds.

The average cohesive energy per atom for the two phases of Fe<sub>3</sub>B can be defined by

$$E_{\rm coh} = -\left(\frac{1}{16}\right) \left(E_{\rm total} - \sum E_A\right),$$

where the total atomic energies  $E_A$  are to be summed over all 16 atoms of the cell. From the LMTO calculations we have found a total energy of  $E_{\text{total}} = -30690.689$  Ry and -30690.228 Ry for *o*- and bct-Fe<sub>3</sub>B, respectively. Using the atomic energies calculated by Häglund *et al.*,<sup>18</sup>  $E_{\text{Fe}} = -2540.787$  Ry and  $E_{\text{B}} = -48.537$  Ry, we obtain  $E_{\text{coh}} = 444$  mRy/atom $= 5.82 \times 10^5$  J/mol for *o*-Fe<sub>3</sub>B and

 $E_{\rm coh}$ =415 mRy/atom=5.44×10<sup>5</sup> J/mol for bct-Fe<sub>3</sub>B. It can be seen that the estimated value of  $E_{\rm coh}$  for *o*-Fe<sub>3</sub>B is slightly larger than that for bct-Fe<sub>3</sub>B, which is perhaps connected with the lower occupation energy of electrons in *o*-Fe<sub>3</sub>B. Unfortunately, no experimental results in  $E_{\rm coh}$  for Fe<sub>3</sub>B are available to compare our evaluated  $E_{\rm coh}$ , but the *ab initio* results on carbides and nitrides<sup>18</sup> have shown that the shift between theoretical and experimental energies is nearly remarkably constant and the theoretical values can be successfully used to study both general trends and details in the variation of  $E_{\rm coh}$ . Thus it will be interesting to compare our result for the  $E_{\rm coh}$  of Fe<sub>3</sub>B with results from future investigations of 3*d* transition-metal borides.

#### B. Local magnetic moment and hyperfine field

We have listed the calculated results on  $\mu_{\text{Fe}}$  at Fe atoms for Fe<sub>3</sub>B in both structures in Table III. Since Fe<sub>3</sub>B are metastable, no available experimental results in  $\mu_{\text{Fe}}$  for Fe <sub>3</sub>B can be used to compare our calculated  $\mu_{\text{Fe}}$ , but it can be seen that, for *o*-Fe<sub>3</sub>B, the calculated average magnetic mo-

TABLE III. Calculated  $\mu_{\text{Fe}}$  (in  $\mu_B$ ),  $H_{\text{FC}}$  (in T) and its valence contribution  $H_{\text{FC},\text{val}}$  and the coupling constants A and B (in  $T/\mu_B$ ) for Fe<sub>3</sub>B. And experimental results on  $\overline{\mu}_{\text{Fe}}$  (Ref. 10) and  $H_{\text{hf}}$  (Refs. 1 and 20).

	o-Fe <sub>3</sub> B			bct-Fe <sub>3</sub> B				
-	Fe <sub>I</sub>	Fe <sub>II</sub>	Average	Fe <sub>I</sub>	Fe <sub>II</sub>	Fe <sub>III</sub>	Average	
$\mu_{ m Fe}$	2.06	1.89	1.95	2.14	1.89	1.95	1.99	
$\mu$ (Expt.)			2.0					
H <sub>FC</sub>	-26.8	-25.4	-25.9	-29.2	-23.0	-27.0	-26.4	
$H_{\rm FC,val}$	-1.72	-2.14	-2.01	-3.27	0.20	-3.11	-2.06	
$H_{\rm hf}$ (Expt.)	26.4	23.5	24.5	28.7	22.5	26.7	26.0	
	$\pm 0.5$	$\pm 0.5$	$\pm 0.5$	$\pm 0.2$	$\pm 0.2$	$\pm 0.3$	$\pm 0.3$	
Α	-12.18	-12.33		-12.11	-12.28	-12.26		
В	-0.90	-1.09		-1.62	0.10	-1.53		

ment  $\mu_{\text{Fe}}$  agrees well with the extrapolated value (listed in Table III) from Fe<sub>3</sub>C<sub>1-x</sub>B<sub>x</sub> at 4.2 K,<sup>10</sup> and the calculated  $\mu_{\text{Fe}}$  at individual Fe sites are also consistent with the results obtained by Ching *et al.*<sup>4</sup>

One of the characteristic quantities of spin-polarized electronic structure is that the local magnetic moment  $\mu_{loc}$  of an atom in the material depends closely upon the neighboring environment of the atom, i.e., the type and the number of neighbors, and the interatomic distances with neighbors. Ching *et al.*<sup>4</sup> have concluded that the  $\mu_{\rm Fe}$  is reduced by increasing the boron concentration. The calculated results for bct-Fe<sub>3</sub>B have shown that there is a great difference among the  $\mu_{\rm Fe}$  at three sites. The  $\mu_{\rm Fe}$  at Fe<sub>I</sub> (2.14 $\mu_B$ ) is much larger than that at Fe<sub>II</sub> (1.89 $\mu_B$ ), and the  $\mu_{\rm Fe}$  at Fe<sub>III</sub> is intermediate. Since the Fe neighbors of the Fe atom at three sites are very similar, the difference of  $\mu_{\rm Fe}$  is mainly determined by the effect of the neighboring boron. Fe<sub>1</sub> has only two boron neighbors while  $Fe_{II}$  has four boron atoms as neighbors; it is suggested that the bonding interactions between Fe and B promote the itinerancy of Fe 3d electrons and decrease the exchange splitting: the more boron neighbors of the Fe atom, the smaller the  $\mu_{\rm Fe}$  of the Fe atom. On the contrary, in o-Fe<sub>3</sub>B the Fe atoms at both sites all have two boron atoms as neighbors and the Fe-B distances are close, thus the effects of boron atoms on the  $\mu_{\rm Fe}$  seem to be alike and do not lead to such a large difference of  $\mu_{\text{Fe}}$  as that in bct-Fe<sub>3</sub>B. So the smaller  $\mu_{\rm Fe}$  at Fe<sub>II</sub> than that at Fe<sub>I</sub> can only be assigned to the influence of the neighboring Fe atoms. Analyzing the Fe-Fe distance, we can find that there are smaller interatomic distances between Fe<sub>II</sub> and its Fe neighbors when compared to those between Fe<sub>1</sub> and its Fe neighbors. It seems that the stronger hybridized interactions between Fe<sub>II</sub> and its Fe neighbors due to smaller Fe<sub>II</sub>-Fe distances decrease the exchange splitting of  $Fe_{II}3d$  electrons and result in a smaller  $\mu_{\rm Fe}$  at Fe<sub>II</sub>.

We have illustrated the dependences of the  $\mu_{\rm Fe}$  at Fe sites and the  $\overline{\mu}_{Fe}$  in bct- and o-Fe<sub>3</sub>B on the volume of the unit cell in Fig. 2(a). It has been shown that the  $\mu_{\text{Fe}}$  at each Fe site in both Fe<sub>3</sub>B decrease greatly with the reduction of the unit cell volume. Using the formula  $\mu_{loc} = A + B \ln V$ , we can fit the changes of the  $\overline{\mu}_{Fe}$  for both Fe<sub>3</sub>B approximately and obtain the volume dependence of the  $\overline{\mu}_{\rm Fe}$  from the slope of the fitting curve,  $d\overline{\mu}_{\rm Fe}/d\ln V = 5.11 \mu_B$  and  $3.71 \mu_B$  for bct- and *o*-Fe<sub>3</sub>B, respectively. The decrease of  $\mu_{\text{Fe}}$  in bct-Fe<sub>3</sub>B with the unit cell compression is much larger than that in o-Fe<sub>3</sub>B. Moreover, it is interesting to notice that in bct-Fe<sub>3</sub>B the decrease of  $\mu_{\rm Fe}$  at Fe<sub>II</sub> with the reduction of the unit cell volume is much smaller than those at other sites. Since  $Fe_{II}$  has the most B neighbors, it is indicated that the strong shielding effect of B neighbors has partly cancelled the effect of volume compression on  $\mu_{\mathrm{Fe}}$  and makes the  $\mu_{\rm Fe}$  at Fe<sub>II</sub> relatively stable against the compression of the lattice.

The main contribution to the hyperfine magnetic field  $H_{\rm hf}$  of the atom is in the 3*d* transition metal compound  $H_{\rm FC}$  of an atom and can be decomposed into  $H_{\rm FC,core}$  and  $H_{\rm FC,val}$ . The former is the core contribution, which comes from the polarization of the core atoms, and the latter is the contribution of conducted electron polarization, which is



FIG. 2. The unit cell volume dependence of  $\mu_{\text{Fe}}$ ,  $H_{\text{FC}}$ , and its valence contribution  $H_{\text{FC,val}}$  in Fe<sub>3</sub>B. The solid and hollow symbols represent those in *o*- and bct-Fe<sub>3</sub>B, respectively.

mainly produced by the sd hybridization between the s orbitals of the atom and the d orbitals of its neighbors. In Table III we have also listed the calculated  $H_{\rm FC}$  of Fe and its valence contribution  $H_{\rm FC,val}$  for both Fe<sub>3</sub>B. Here  $H_{\rm FC}$  are calculated according to the prescription given by Akai et al.<sup>19</sup> It is found that the calculated  $H_{FC}$  at Fe in both Fe<sub>3</sub>B are slightly larger than the experimental results<sup>1,20</sup> at room temperature listed in the table. Since  $H_{\rm hf}$  decreases with increasing temperature, our results in  $H_{\rm FC}$  are in excellent agreement with the experimental results. Like most transition metal compounds the  $H_{\text{FC,val}}$  at Fe sites in both Fe<sub>3</sub>B are only a minor contribution to  $H_{\rm FC}$ . In o-Fe<sub>3</sub>B the  $H_{\rm FC,val}$  at the  $\mathrm{Fe}_{\mathrm{II}}$  site takes a larger portion in the  $H_{\mathrm{FC}}$  than that at an  $Fe_{I}$  site. It is the reason that the  $Fe_{II}$ -Fe interaction is stronger than that between  $Fe_I$  and Fe due to the shorter  $Fe_{II}$ -Fe distances, while in bct-Fe<sub>3</sub>B the strong shielding effect of four B neighbors surrounding an  $Fe_{II}$  site results in a small positive  $H_{\rm FC,val}$  at the Fe<sub>II</sub> site, which differs greatly from

those at the Fe<sub>I</sub> and Fe<sub>III</sub> sites. Generally  $H_{\text{FC,core}}$  is proportional to  $\mu_{\text{loc}}$  of an atom and  $H_{\text{FC,val}}$  is related to the average magnetic moments  $\mu_N$  of its neighbors. So the  $H_{\text{FC}}$  at an Fe site can be phenomenologically expressed as follows:<sup>19,21</sup>

$$H_{\rm FC} = H_{\rm FC,core} + H_{\rm FC,val} = A \mu_{\rm Fe} + B \overline{\mu}_N$$

where *A* and *B* are defined as hyperfine coupling constants. Using the calculated  $\mu_{\text{Fe}}$ , we have evaluated the coupling constants *A* and *B* and listed them in Table III, also. It has been found that in both Fe<sub>3</sub>B there are similar coupling coefficients *A* but greatly different coefficients *B*. In *o*-Fe<sub>3</sub>B a larger coefficient *B* at Fe<sub>II</sub> has indicated a stronger Fe<sub>II</sub>-Fe interaction while in bct-Fe<sub>3</sub>B a positive *B* at Fe<sub>II</sub> has revealed the shielding effect of boron atoms which has changed the Fe<sub>II</sub>-Fe interactions and reversed the polarization direction of the *sd* hybridization between Fe<sub>II</sub> and Fe.

The average  $H_{\rm FC}$  and the average  $H_{\rm FC,val}$  at Fe sites in both Fe<sub>3</sub>B are given in Figs. 2(b) and 2(c), in which the solid symbols represent the  $\overline{H}_{FC}$  and the  $\overline{H}_{FC,val}$  in *o*-Fe<sub>3</sub>B while the hollow symbols describe those in bct-Fe<sub>3</sub>B. Assuming a linear relation between the  $\overline{H}_{FC}$  and the logarithmic volume of the unit cell, we find that the value of  $\overline{H}_{\rm FC}$  at Fe sites decreases with the compression of the unit cell by  $d|\overline{H}_{\rm FC}|/d\ln V = 37.93$  and 56.94 T for o- and bct-Fe<sub>3</sub>B, respectively. The  $H_{\rm FC}$  at Fe sites in o-Fe<sub>3</sub>B is more stable than that in bct-Fe<sub>3</sub>B against the compression of the unit cell volume. In both Fe<sub>3</sub>B the changes of the  $\overline{H}_{FC,val}$  at Fe sites with the logarithmic volume are not monotonous and indicate the complexity of the volume dependence of the Fe-Fe interactions in Fe<sub>3</sub>B. Especially, we show the  $H_{FC,val}$  at an Fe<sub>II</sub> site in bct-Fe<sub>3</sub>B under various unit cell volumes in Fig. 2(c), also. It is interesting to observe that the  $H_{FC,val}$  of the Fe<sub>II</sub> atom in bct-Fe<sub>3</sub>B changes not only its amplitude but also its sign, which implies that the compression of the unit cell volume changes not only the strength of Fe<sub>II</sub>-Fe interactions but also the polarized direction of the sd hybridization between them.

#### C. Curie temperature

Curie temperature  $T_C$  is the important characteristic temperature of the metallic ferromagnetic materials and its pressure (volume) dependence is a property of unusual physical interest. Experimentally, Fruchart *et al.*<sup>10</sup> have extracted the  $T_C$  (897 K) of the *o*-Fe<sub>3</sub>B by extrapolating the  $T_C$  of Fe<sub>3</sub>C<sub>1-x</sub>B<sub>x</sub>, and the  $T_C$  (786 ± 3 K) of bct-Fe<sub>3</sub>B (Ref. 7) has also been determined, although both Fe<sub>3</sub>B are metastable. According to the calculated results of electronic structure, we can use the Mohn-Wohlfarth approximation<sup>22</sup> to discuss the  $T_C$  of Fe<sub>3</sub>B and their volume dependence within the framework of the spin fluctuations of local magnetic moment. In Mohn-Wohlfarth theory  $T_C$  is determined by the solution of the equation

$$T_C^2/T_S^2 + T_C/T_{\rm sf} - 1 = 0$$

where  $T_s$  is the Stoner-model Curie temperature, and  $T_{sf}$  is a characteristic temperature describing the influence of spin fluctuations and given by



FIG. 3. The volume dependence of the  $T_C$  for Fe<sub>3</sub>B.

$$T_{\rm sf} = (M_0^2/40k_B) [1/N_{\uparrow}(E_F) + 1/N_{\downarrow}(E_F) - 2I],$$

where  $M_0$  is the zero-temperature magnetic moment,  $k_B$  is the Boltzmann's constant,  $N_{\uparrow}(E_F)$  and  $N_{\downarrow}(E_F)$  are the upand down-spin DOS at  $E_F$ , and I is the Stoner parameter. The quantities  $M_0, N_{\uparrow}(E_F)$ , and  $N_{\downarrow}(E_F)$  are directly determined by theoretical electronic structure. The Stoner parameter I for transition metals and their compounds may be written as<sup>23</sup>

$$I = \sum_{t} I_{t} [N_{t}(E_{F})/N(E_{F})]^{2},$$

where  $I_t$  and  $N_t(E_F)$  are the Stoner parameter and the DOS for the atom at site t. For  $I_t$  we have used the values from the work of Janak.<sup>24</sup>

It is worthwhile noting that Woods et al.<sup>25</sup> are already successful in predicting the relative change of  $T_C$  in ironbased rare-earth compounds with applying the Mohn-Wohlfarth theory, although the absolute  $T_C$  of strong ferromagnets cannot be correctly determined by this model.<sup>26</sup> In our discussion, we do not directly evaluate the absolute  $T_C$ of Fe<sub>3</sub>B with this model but work out the ratio  $T_C(V)/T_C(V_0)$  with the compression of the unit cell volume. Using this model, we have first evaluated the ratio  $T_C^{bct}/T_C^o$ between the  $T_C$  for both Fe<sub>3</sub>B to be 0.83, which agrees well with the experimental result 0.88. It is also suggested that the prediction of the volume dependence of the  $T_C$  for Fe<sub>3</sub>B with this model will be qualitatively correct. We have plotted the evaluated  $T_C(V)/T_C(V_0)$  for both Fe<sub>3</sub>B with the volume compression in Fig. 3 and fitted them well with the second order polynomial of the logarithmic unit cell volume. From the fitted curve a critical volume  $V_c$  corresponding to the disappearing point of ferromagnetism can be evaluated to be  $0.85V_0$  for *o*-Fe<sub>3</sub>B but cannot be found for bct-Fe<sub>3</sub>B. Moreover, from the obvious linear relation between  $dT_C/d\ln V$ 

# **V. CONCLUSIONS**

We have performed self-consistent spin-polarized electronic structure calculations on the ferromagnetic Fe<sub>3</sub>B crystallizing in orthorhombic and body-centered-tetragonal structures using the LMTO methods. The theoretical results on  $\mu_{\rm Fe}$  and  $H_{\rm FC}$  agree well with experimental measurements. According to the calculated results, the effects of neighboring atoms on  $\mu_{\rm Fe}$  and  $H_{\rm FC}$  at individual Fe sites have been discussed in detail. Using the Mohn-Wohlfarth theory we have discussed the volume dependence of the Curie temperature  $T_C$  for *o*- and bct-Fe<sub>3</sub>B. In summary some concluding remarks are presented as follows.

(1) The cohesive energy per atom in cell  $E_{\rm coh}$  has been evaluated from the calculated electrons total energy. The evaluated  $E_{\rm coh}$  for *o*-Fe<sub>3</sub>B is slightly larger than that for bct-Fe<sub>3</sub>B.

(2) The local magnetic moment and hyperfine field of an Fe atom are related closely to the neighboring environments of the Fe atom. The B neighbors surrounding an Fe atom decrease the exchange splitting at the Fe site and then reduce the magnetic moment of the Fe atom. The more B neighbors

surrounding an Fe atom, the smaller the magnetic moment of the Fe atom. The larger Fe-Fe distances produce a larger Fe magnetic moment but a smaller valence contribution to  $H_{\rm FC}$ .

(3) The shielding effect from B atoms makes  $\mu_{\text{Fe}}$  at an Fe<sub>II</sub> in bct-Fe<sub>3</sub>B much more stable against the volume compression. It also changes the Fe<sub>II</sub>-Fe interactions and leads to a small positive  $H_{\text{FC,val}}$  at the Fe<sub>II</sub> site.

(4) According to our calculated results, the ferromagnetism of o-Fe<sub>3</sub>B will disappear when the compression of the unit cell volume is larger than 15%. For two structures of Fe<sub>3</sub>B the derived volume dependences of the  $T_C$  all follow  $(1 + CT_C)^{1/2}$ , where C is a constant.

Since the Fe<sub>3</sub>B in both structures are not stable phases, there are not enough experimental results to be compared with our calculated results. We expect to compare completely our calculated results with experimental measurements from future investigations of Fe<sub>3</sub>B.

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