# **Perpendicular interface resistances of sputtered Ag/Cu, Ag/Au, and Au/Cu multilayers**

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We report measurements of the increase in perpendicular specific resistance (area times total resistance, *ARt*! of multilayers of two nonmagnetic metals with increasing number of interfaces, when the total amount of each metal is held constant. For multilayers of Ag and Cu, Ag and Au, and Au and Cu sputtered under narrowly defined conditions, we find, per interface,  $AR_{AgCu} = 0.044 \pm 0.003$  f $\Omega$  m<sup>2</sup>;  $AR_{Ag/Au} = 0.050 \pm 0.004$  $f\Omega$  m<sup>2</sup>;  $AR_{Au/Cu}$ =0.149±0.006 f $\Omega$  m<sup>2</sup>. From independent estimates of the contributions to these values due to interface alloying, we conclude that such alloying can account for at least half and perhaps all of these values. These interface resistances are thus mostly not intrinsic.  $[$ S0163-1829(96)00542-5 $]$ 

#### **I. INTRODUCTION**

Understanding the scattering of electrons at metallic interfaces is crucial to understanding giant  $(G)$  magnetoresistance  $(MR)$  in ferromagnetic metal–nonmagnetic metal  $(F/N)$ multilayers.<sup>1</sup> Historically, attention has focused on scattering for current flow parallel to surfaces or interfaces.<sup>1,2</sup> Recently, however, interest has begun to shift to the experimentally more challenging case of perpendicular incidence, $^{1,3}$  partly stimulated by new techniques $4.5$  and measurements of the specific interface resistance,  $AR_{F/N}$ , the area *A* times perpendicular interface resistance,  $R_{F/N}$ , for Co/Ag,<sup>4</sup> Co/Cu,<sup>6,7</sup> and  $Ni<sub>84</sub>Fe<sub>16</sub>/Cu.<sup>7</sup>$ 

Interface contributions to GMR have been attributed to spin-dependent scattering from:<sup>1</sup> (a) interface alloys; (b) interface roughness;  $(c)$  localized interface states; or  $(d)$  spindependent potential steps at the interface. The specific contribution from interface alloying should be easier to establish in N1/N2 multilayers, due to the absence of the spin dependence inherent in F/N multilayers. In this paper, we present the first measurements of  $AR_{\text{N1/N2}}$  for N1/N2 multilayers for Ag/Cu, Ag/Au, and Au/Cu, sputtered under various conditions. We examine how much of  $AR_{N1/N2}$  can be ascribed simply to scattering from an interface alloy.

We chose Cu, Ag, and Au, for several reasons.  $(1)$  They have simple Fermi surfaces that are similar in form, $\delta$  so that intercomparisons should not be complicated by very different electronic structures.  $(2)$  They sputter easily with little contamination.  $(3)$  They span a wide range of solubilities<sup>9</sup> and resistivity increases per atomic percent impurity,  $\Delta\rho_0\!/\Delta c$  .  $^{10}$ 

### **II. SAMPLE PREPARATION AND CHARACTERIZATION**

Figure  $1(a)$  shows a simplified schematic drawing of a sample and Fig.  $1(b)$  shows the layering schematically. The N1/N2 multilayer is sandwiched between two 6 nm thick Co layers, outside of which are two crossed superconducting Nb strips, each 1.1 mm wide. The Co layers eliminate any proximity effect between the Nb and the multilayer.<sup>11</sup> The Nb strips are equipotentials, since Nb superconducts at our measuring temperature of 4.2 K. The ''short-wide'' sample geometry (length/width  $\approx 10^{-3}$ ) then ensures that essentially all of the current injected into one strip passes through the overlap area  $A \approx 1.25$  mm<sup>2</sup> and out of the other strip, giving a uniform current through  $A$ .<sup>12</sup> Using a reference resistor and superconducting quantum interference device-based measuring system, the total sample resistance  $R_t$  is measured with an uncertainty of about 1%. The measuring uncertainty in  $AR_t$  is  $\approx$ 2–5 %, dominated by the uncertainty in the Nb strip widths.<sup>4</sup>

The samples are made in a computer-controlled, cryopumped, UHV compatible, sputtering system, $12$  with a base pressure  $\leq 2 \times 10^{-8}$  Torr. All data shown are for samples sputtered at an argon pressure  $\approx$  2.5 mTorr, but a few Ag/Cu multilayers sputtered at 13 mTorr gave results similar to those shown. A 300 nm thick, bottom Nb strip is first sput-



FIG. 1. (a) Sample schematic drawing. (b) Layering schematic drawing.

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Metals	Ag(1)/Cu(2)	Ag(1)/Au(2)	Au(1)/Cu(2)
$1^a \rho_{N1}$ ; $\rho_{N2}$ (n $\Omega$ m;n $\Omega$ m)	$7\pm 2$ ; $6\pm 2$	$7\pm 2$ ; $13\pm 3$	$13\pm3$ ; $6\pm2$
2 <sup>b</sup> Solubilities	Small	100%	Large
$3^c \Delta \rho_0 / \Delta c$ (n $\Omega$ m/at. %)	$0.7$ ?: 1.4?	3.6:3.5	4.3; 5.3
$4^d \rho(50\%)$ (Indep. Msmt.) (n $\Omega$ m)	19?	90	140
$5^e$ $\rho(50\%)$ (Nordh.) (n $\Omega$ m)	26?	89	120
$6f \rho(50%)$ (Sputt. films) (n $\Omega$ m)	$42 \pm 13$	$100 \pm 20$	$170 \pm 30$
$7^g \rho(50\%) = \Delta (AR_t)/t_T \ (n\Omega \ m)$	$51 \pm 9$	$86^{+13}_{-5}$	$125 \pm 12$
$8^h$ $ρ_{BE}$ (50%) (nΩ m)	$42 \pm 10$	$90 \pm 10$	$140 \pm 20$
$9^i t_{Ix}$ (nm)	0.5	0.5	0.4
$10^{j} t_{Ie}$ (nm)	$0.9 \pm 0.2$	$0.6 \pm 0.1$	$1.2 \pm 0.2$

TABLE I. Various properties of the metal pairs.

<sup>a</sup>From measurements on 300 nm thick films.

<sup>b</sup>Reference 9.

<sup>c</sup>From Ref. 10. Listed first is N2 and N1, then N1 in N2. ?= large uncertainty.

<sup>d</sup>From Ref. 17: Ag/Au, uniform alloy; Au/Cu, rapidly quenched alloy (slow cooling gives an ordered alloy with much lower  $\rho$ ); Ag/Cu, two-phase mixture.

<sup>e</sup>Estimated from the Nordheim equation [Eq. (4) in text] using the average of the  $\Delta \rho_0 / \Delta c s$  for the two metals (see row 3).

 ${}^f$ From sputtered multilayer films with 0.5–1.0 ML thick layers (see text).

 ${}^{g}$ From the data in Fig. 2 (see text).

hBest estimate from the information in rows  $4-7$  (see text).

<sup>i</sup>From x rays (see text).

 $j$ From Fig. 2 (see text).

tered through a strip mask. In 1–2 min, this mask is replaced, *in situ*, by a "sample" mask. A 6 nm thick Co layer is sputtered, then the multilayer, composed of *N* bilayers of metals N1 and N2, and finally a 6 nm thick Co capping layer. The sample mask is then exchanged for a strip mask perpendicular to the first one, and a 300 nm thick, top Nb strip is sputtered. Except for the very thinnest N1 and N2 layers, most of each layer is deposited while the substrate is at rest above a sputtering gun. However, some deposition occurs during the fraction of a second that the substrate moves into and out of the sputtering plume. The computer program takes this additional deposition into account in setting the time a substrate stays over each target. Most samples had total thickness  $t_T$ =360 nm, but several of each set were made with  $t_T$ =540 nm to check that a different total thickness gave compatible results.

The samples were sputtered onto *c*-axis oriented, singlecrystal sapphire substrates, the temperatures of which were held above  $-50$  °C and below 30 °C. The sputtering targets were  $\sim$  5.5 cm in diameter and  $\sim$  0.6 cm thick, made from 99.99% pure metals. The standard deposition rates were 1.0– 1.25 nm/s for Ag, 1.2–1.35 nm/s for Cu, and 1.0–1.1 nm/s for Au. To reduce the importance for thinner layers of computer corrections for entrance and exit times, we also used ''half'' deposition rates, achieved by reducing the sputtering voltage.

Layer thicknesses were checked by both low- and highangle  $\vartheta$ –2 $\vartheta$  x-ray scattering. We usually saw a single lowangle superlattice peak and both low-side and high-side high angle satellites about central peaks indicating  $(111)$  texture. The peak and satellite separations usually gave lengths agreeing with the intended bilayer thicknesses to within a few percent.

Attempts to derive interface alloying thicknesses  $t<sub>I</sub>$  from

computer fits of the high-angle satellite relative amplitudes were unsuccessful; the fits were insensitive to such alloying. We are thus limited to estimating bounds on  $t<sub>I</sub>$  from the layer thicknesses at which we do and do not see low-angle superlattice peaks. We define  $t_{Ix}$  as the smallest layer thickness at which x rays still show such a peak. This definition yielded the values  $t_{1x}$ =0.5 nm for Ag/Cu and Ag/Au, and 0.4 nm for Au/Cu, which we list in row 9 of Table I. These values of  $t_{Ix}$  $correspond to only about 2 monolayers (ML) of each$ metal—the  $(111)$  interplanar spacings are 0.20 nm for Cu and 0.22 nm for Ag and Au—as small as they could possibly be, given that we cannot stop and start sputtering at the ends of individual layers. They are also smaller than the interface thicknesses suggested by other measurements of different multilayers sputtered in our system.<sup>13</sup> Analysis of a linear interface alloying profile (see below) shows that x-ray satellites should still be seen even for a layer thickness smaller than the  $t_I$  appropriate for calculating the interface resistance [see Eq. (3) below]. We, thus, view  $t_{Ix}$  as a lower bound on  $t_I$ .

## **III. THEORY**

To isolate  $AR_{\text{N1/N2}}$ , we fix  $t_T$ , set the metal layer thicknesses  $t_{N1} = t_{N2} = t_T/2N$ , and vary only the bilayer number *N*. So long as quantum interference can be neglected, and the layer properties do not vary with their thicknesses,  $AR<sub>t</sub>$  for the sample in Fig.  $1(b)$  should be self-averaging, i.e., given simply by the series sum of the resistivities times layer thicknesses,  $\rho t$ , for each layer, and of the  $AR$ 's for each interface, independent of the sizes of the electron mean free paths in the layers: $4,14$ 

$$
AR_t = 2AR_{Nb/Co} + 2\rho_{Co}(6 \text{ nm}) + AR_{Co/N1} + AR_{Co/N2} + \rho_{N1}(t_T/2) + \rho_{N2}(t_T/2) + (2N - 1)AR_{N1/N2}. \quad (1)
$$

Equation  $(1)$  should be valid if  $AR_{N1/N2}$  represents either an interface of negligible thickness, or one of finite thickness  $t_I'$  due to interface alloying. In the latter case,  $AR_{N1/N2}$  is the increase in  $AR_t$  due to alloying, above and beyond  $\rho_{avg}t_I^{\prime}$ , where  $\rho_{\text{avg}}$  is the average of the resistivities of N1 and N2. If Eq. (1) applies, a plot of  $AR_t$  vs  $N$  should give a straight line with ordinate intercept just the sum of the first six terms minus  $AR_{N1/N2}$ , and slope  $2AR_{N1/N2}$ . To check its applicability, independent measurements of each of the first six terms were made on similarly sputtered sandwiches and thin films, giving;  $2AR_{Nb/Co} = 6.1^{+1}_{-0.3}$  fΩ m<sup>2</sup>;<sup>15</sup>  $\rho_{Co} = 50 \pm 10$  nΩ m;  $\rho_{Ag}$ =7±2 n $\Omega$  m;  $\rho_{Cu}$ =6±2 n $\Omega$  m;  $\rho_{Au}$ =13±3 n $\Omega$  m;<sup>16</sup> and  $AR_{\text{Co/N1}}$  and  $AR_{\text{Co/N2}}$ —the interface resistances between Co and N1 and N2— $\approx 0.25 \pm 0.05$  fΩ m<sup>2</sup> each.<sup>4,6</sup> For  $t_T$ =360 nm, including our derived values of  $AR_{\text{N1/N2}}$   $\leq$  0.15 f $\Omega$  m<sup>-2</sup> (see below), the ordinate intercepts of Eq.  $(1)$  are predicted to be  $9.5^{+1.9}_{-1.2}$  f $\Omega$  m<sup>2</sup> for Ag/Cu,  $10.8^{+2.1}_{-1.4}$  f $\Omega$  m<sup>2</sup> for Ag/Au, and  $10.5^{+2.1}_{-1.4}$  f $\Omega$  m<sup>2</sup> for Au/Cu. For  $t_T$ =540 nm, they should be just over 1 f $\Omega$  m<sup>2</sup> larger for Ag/Cu and slightly less than 2 f $\Omega$  m<sup>2</sup> larger for Au/Ag and Au/Cu.

When the interfaces begin to overlap, the rate of increase of *ARt* with *N* should slow, and *ARt* should saturate when the sample reaches a uniform 50–50 % alloy. In this state, the last term in Eq.  $(1)$  should be replaced by the constant term

$$
\Delta(AR_t) = \rho(50\%)t_T, \tag{2}
$$

where  $\rho$ (50%) is the resistivity of a 50–50 % alloy. We will use Eq. (2) to help establish  $\rho$ (50%), one of the two parameters we need to estimate  $AR_{\text{N1/N2}}$ , as we now describe.

If interface alloying fully determines  $AR_{\text{N1}/\text{N2}}$ , and if the alloy profile is a constant 50% of both metals over a thickness  $t_I$  (square profile), then the interface specific resistance is just

$$
AR_{\rm N1/N2} = \rho(50\%)t_I.
$$
 (3)

In this case, to estimate  $AR<sub>N1/N2</sub>$  due to alloying, we need values for  $\rho$ (50%) and  $t_I$ .

When the profile is not square, we can still write  $AR_{N1/N2}$ in the form of Eq.  $(3)$ , but  $t_I$  must then represent an effective thickness smaller than the real one,  $t_I^{\prime}$ , over which the nonuniform alloy actually extends. We evaluate also a continuous linear interface profile, both because it is easy to calculate and because the unknown profile probably lies between linear and square—closer to square in the middle and to linear at its edges. Estimating the resistance of a linear interface using Nordheim's rule, $^{17}$ 

$$
\Delta \rho(c) = (\Delta \rho_0 / \Delta c)_{\text{avg}} (c/100\%) (100\% - c), \tag{4}
$$

the  $t_I$  needed for Eq. (3) to give the same  $AR_{N1/N2}$  as for a linear profile is  $t_I = 2/3t_I^{\prime}$ .

For a square interface profile, saturation will be abrupt, and the common  $t_{\text{N1}}=t_{\text{N2}}$  at which saturation occurs will be  $t_I$ . For a nonsquare profile,  $AR_t$  will saturate more gradually. For the linear profile, the value of  $t<sub>I</sub>$  to be used in Eq. (3) is given by the  $t_{\text{N1}}=t_{\text{N2}}$  at which the extrapolation of the linear



FIG. 2. The  $AR_t$  vs bilayer number *N* for Au/Cu, Ag/Au, and Ag/Cu multilayers sputtered at standard (diamonds) or half (squares) rates. Open symbols are for samples with  $t_T$ =360 nm; filled ones are for  $t_T$ =540 nm. The solid lines are "square" interface profile fits to the  $t_T$ =360 nm data. The broken curve for Au/Cu is an extension of the parameters for the solid line to  $t_T$ =540 nm. The dashed curves are for linear interface profiles with the same slopes and saturation values as for the solid lines. The black bars just left of the ordinate axes indicate the ranges of allowed intercepts given the uncertainties in the first six terms in Eq.  $(1)$ .

slope of Eq.  $(1)$  intersects the saturation value of  $AR_t$ . This value occurs at  $t_1 \approx 2/3t_1'$ . As noted above, such a profile is still nonuniform for layers thinner than  $t<sub>I</sub>$ , and thus still gives x-ray satellites.

In Sec. IV, we fit each data set with both a square profile and a linear profile having the same slope and same saturation value of  $AR_t$  as the square one.

### **IV. DATA**

Figure 2 shows  $AR_t$  versus N for our three metal pairs using the two sputtering rates listed above. For each pair, the samples were sputtered in several separate runs. Where their data overlap, we found no obvious differences in  $AR<sub>t</sub>$  for samples sputtered at "standard" (diamonds) or half rates (squares). The dark bands on the ordinate axes indicate the ranges of allowed sums of the constant terms in Eq.  $(1)$ , for  $t_T$ =360 nm, from the values given above.

The data of Fig. 2 are qualitatively consistent with Eq.  $(1)$ for each metal pair—they initially increase linearly with *N* and the data for  $t_T$ =360 nm eventually level off as expected for overlapping interfaces. In the linear regions, we see no systematic differences between data for  $t_T$ =360 nm (open symbols) or 540 nm (filled symbols). There, the data for 540 nm should be only  $1-2$  f $\Omega$  m<sup>2</sup> higher than for 360 nm, comparable to our measuring uncertainty. The linear regimes for 540 nm extend to larger *N*, because each *N* involves 50% thicker layers.

Since our interface alloying profiles are unlikely to be perfectly square, our data ought to approach saturation gradually instead of abruptly. In Fig. 2, the data for Au/Cu

TABLE II. Estimates and measurements of  $AR_{N1N2}$ .

Metals	Ag(1)/Cu(2)	Ag(1)/Au(2)	Au(1)/Cu(2)
$1^{\text{a}}$ AR $_{\text{N1N2}}^{LB} = \rho_{BE}$ (50%) $t_{Ix}$ (fΩ m <sup>2</sup> )	$0.021 \pm 0.005$	$0.045 \pm 0.005$	$0.056 \pm 0.01$
$2^{\rm b}$ AR <sup>est</sup> <sub>N1N2</sub> = $\rho_{BE}$ (50%) $t_{If}$ (f $\Omega$ m <sup>2</sup> )	$0.038 \pm 0.015$	$0.054 \pm 0.015$	$0.17 \pm 0.05$
$3^c AR_{N1N2}^{exp}$ (f $\Omega$ m <sup>2</sup> )	$0.044 \pm 0.003$	$0.050 \pm 0.004$	$0.149 \pm 0.006$

a Lower bound estimate: calculated from rows 8 and 9 in Table I.

<sup>b</sup>Estimate: calculated from rows 8 and 10 in Table I.

c Experimental: calculated from solid lines in Fig. 2.

require such a gradual approach, but those for Ag/Au and Ag/Cu can be either gradual or abrupt, depending upon the maximum value of *N* chosen for the linear regime. We examine both possibilities.

First, we force linear fits up to the largest values of *N* consistent with the scatter in the data, and determine the "saturation values" of  $AR_t$  by simply linearly averaging the values of  $AR_t$  for those data points that are consistent with saturation. As indicated in Sec. III, the values of *N* where the linear regimes intersect the saturation values of  $AR_t$ —which we designate by *N*<sub>I</sub>—yield values of  $t_{Ie} = t_T/2N_I$  that should approximate  $t_I$ . The solid lines in Fig. 2 are such fits for  $t_T$ =360 nm for Ag/Au (up to *N* = 257–*N<sub>I</sub>*=311), Ag/Cu (up to  $N=200-N_I=208$ , and Au/Cu (up to  $N=120-N_I=151$ ). Their intercepts and slopes (with least-squares fit uncertainties) are  $(11.4\pm0.5)+(0.088\pm0.005)N$  fΩ m<sup>2</sup> for Ag/Cu,  $(13.1 \pm 1.0) + (0.100 \pm 0.008)N$  fΩ m<sup>2</sup> for Ag/Au and (14.1)  $\pm 0.8$  + (0.298 $\pm$ 0.012)*N* fΩ m<sup>2</sup> for Au/Cu. Half the slopes give the values of  $AR_{\text{N1}/\text{N2}}$  listed in row 3 of Table II. The best fit intercepts lie near or above the upper bounds estimated in Sec. III (11.4 f $\Omega$  m<sup>2</sup> for Ag/Cu, 12.9 f $\Omega$  m<sup>2</sup> for Ag/Au, and 12.6 f $\Omega$  m<sup>2</sup> for Au/Cu) from independent measurements of the first six terms in Eq.  $(1)$ . However, including uncertainties gives overlap with the independent values, except for Au/Cu. An analysis of these slopes and intercepts using Eq.  $(1)$  is, thus, just internally consistent. We do not know if this bias toward high intercepts is due to slight variation of the "constant" terms of Eq.  $(1)$  with decreasing layer thickness, or if our choices of maximum *N* for the linear fits are too large. The values of  $t_{Ie}$  (listed in row 10 of Table I) found from the intercepts of the straight lines with the saturation values of  $AR_t$  are larger than the "lower bound" x-ray estimates of  $t_{Ix}$  given in row 9 of Table I, but are comparable to what we would have expected based upon the limitations of sputtering and measurements on other multilayers sputtered in our system.<sup>13</sup>

Second, we assume that all three sets of data approach saturation gradually, and fit the linear model noted in Sec. III  $(dashed curves in Fig. 2)$  to the same slopes and saturation values as for the square model. This model fits the Au/Cu data better than the square model does, and is consistent with the Ag/Cu and Ag/Au data sets to within their uncertainties.

Lastly, the parameters for  $t_T=360$  nm let us predict square and linear profile behaviors for the  $t_T$ =540 nm Au/Cu data (broken and dashed curves, respectively), where those data extend farther in *N* than the  $t_T$ =360 nm data. The linear profile fits the  $t_T$ =540 nm data better.

#### **V. ANALYSIS**

We wish to examine how well interface alloying alone can account for the values of  $AR_{\text{N1}/\text{N2}}$  listed in row 3 of Table II. More specifically, we ask what fractions of the values of  $AR_{\text{N1/N2}}$  are given by Eq. (3). For this comparison, we need "best values" of  $\rho$ (50%) and  $t_I$ . We make four separate estimates of  $\rho$ (50%).

The first involves independent measurements of  $\rho$ (50%) for these alloys by others, as listed in row 4 of Table  $I<sup>18</sup>$ . The values for Ag/Au and Au/Cu should be reliable, as they represent true alloys. That for Ag/Cu is much less sure, as it represents a two phase mixture.

Alternatively, we can estimate  $\rho(50\%) = 25(\Delta \rho_0/\Delta c)_{avg}$  by combining Eq. (4) with the average of the  $\Delta \rho_0 / \Delta c s$  for N1 and N2 given in row 3 of Table  $I<sup>10</sup>$  These estimates are listed in row 5 of Table I. Again, those for Ag/Au and Au/Cu should be reliable, as there are consistent independent measurements of  $\Delta \rho_0 / \Delta c$ , while that for Ag/Cu is uncertain since the few independent measurements of  $(\Delta \rho_0/\Delta c)$  scatter widely.<sup>10</sup>

Thirdly, we have approximated 50%/50% alloys experimentally ourselves by sputtering, onto silicon substrates, multilayer films with intended layer thicknesses of only 0.5– 1.0 ML, thin enough to minimize any effects of layering. This process required reducing our sputtering rates to about 1/5 standard, which led to higher average resistivities for single metal films sputtered at similarly slow rates. Our best estimates of  $\rho$ (50%) for these films, after subtracting  $\rho_{\text{avg}}t_I$ for the two metallic constituents to correct for additional defects in the sputtered alloy films,<sup>16</sup> are given in row 6 of Table I. Here, the estimates for Ag/Cu and Ag/Au should be reliable, as they involve averages over several films each, whereas that for Au/Cu is less sure, as it is based on only a single film.

Lastly, we estimate  $\rho(50\%)$ , by combining the data of Fig.  $2$  with Eq.  $(2)$ . These estimates, which are independent of the interface profile, are given in row 7 of Table I.

Comparing the four estimates of  $\rho(50%)$  in rows 4–7, we find that they all agree well for Ag/Au, are roughly consistent for Au/Cu, and divide into two groups for Ag/Cu. From these observations, we infer that  $\rho(50\%)=90\pm10$  n $\Omega$  m for Ag/Au and  $140\pm20$  n $\Omega$  m for Au/Cu should be reliable approximations. For Ag/Cu, the values from our measurements on sputtered films with very thin layers (row  $6$ ) and on our multilayers (row  $7$ ) are about twice those estimated from the independent measurements on alloys (row 4) and from Nordheim's rule (row 5). However, the  $\rho$ (50%) in row 5 is for a two-phase mixture,<sup>18</sup> and the estimates for  $(\Delta \rho_0/\Delta c)$  used in Eq. (4) are not well reproduced.<sup>10</sup> We thus weight the other two values most heavily and choose  $\rho(50\%) = 42 \pm 10 \text{ n}\Omega \text{ m}.$ Our three ''best estimates'' are given in row 8.

Turning now to  $t_I$ , in Sec. II we estimated from x-ray studies the lower bound values of  $t_{Ix}$  listed in row 9 of Table I, and in Sec. IV we estimated from the data of Fig. 2 the value of  $t_{Ie}$  given in row 10 of Table I. Combining the lower bound estimates of  $t_{Ix}$  with our best estimates of  $\rho(50%)$  in row 8 of Table I gives the lower bound estimates of  $AR_{\text{N1}/\text{N2}}$ listed in row 1 of Table II. These estimates account for 40– 90 % of our best values for  $AR_{\text{N1/N2}}$ . We conclude that at least 40–90 % of the respective values of  $AR_{\text{N1/N2}}$  are due simply to interface alloying. If, instead, we combine the values of  $t_{Ie}$  in row 10 of Table I with our best estimates for  $\rho$ (50%) in row 8, we obtain the  $AR_{\text{N1/N2}}$  predictions listed in row 2 of Table II. These predictions overlap our best values of  $AR_{\text{N1/N2}}$  in row 3.

## **VI. SUMMARY AND CONCLUSIONS**

In summary, our measurements of the increase in perpendicular specific resistance, *AR<sub>t</sub>*, of sputtered N1/N2 multi-<br>layers yield interface specific resistances of resistances  $AR_{\text{Ag/Cu}} = 0.044 \pm 0.003$  fΩ m<sup>2</sup>,  $AR_{Ag/Au} = 0.050 \pm 0.004$  $f\Omega$  m<sup>2</sup>, and  $AR_{Au/Cu}$ =0.149±0.006 f $\Omega$  m<sup>2</sup>. From independent estimates of  $\rho(50\%)t_I$ , we find that interface alloying accounts for 40–100 % of  $AR_{Au|Cu}$ , 50–100% of  $AR_{Ag|Cu}$ , and 90–100% of  $AR_{Ag/Au}$ . For multilayers in which such a large fraction of  $AR<sub>N1/N2</sub>$  is due to interface alloying, there is no unique interface specific resistance, in that different preparation conditions can give different interface thicknesses.

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We end by comparing our values of  $AR_{\text{N1/N2}}$  for Ag/Cu, Ag/Au, and Au/Cu with those for the S/F pair Nb/Co  $(AR_{Nb/C_0}\cong 3 \text{ f}\Omega \text{ m}^2)$  and for three F/N metal pairs, Co/Cu, Co/Ag, and Py/Cu.<sup>19</sup>  $AR_{\text{N1/N2}}$  is much smaller than  $AR_{\text{Nb/Co}}$ , where the physics determining *AR* is presumably quite different.<sup>15</sup> The comparisons with the  $F/N$  pairs can only be rough, since an F/N interface does not have a unique specific resistance; rather, there are separate *AR*'s for majority and minority carriers, and different combinations for different magnetic structures of the multilayer. As the noble metals have high conductivities, we choose  $AR\uparrow_{FN}$  for the highest conductivity electrons.  $4,14,19$  This is the lowest possible value for the comparison. We also reduce the values of  $AR\uparrow_{FN}$  by half, assuming that they are due to only half the conduction electrons. The resulting values of  $(AR \uparrow_{\text{Co/Cu}}/2) \cong 0.13 \text{ f}\Omega \text{ m}^2$ ,  $(AR \uparrow_{\text{Co/Ag}}/2) \approx 0.1 \text{ f}\Omega \text{ m}^2$ , and  $(AR \uparrow_{\text{Py/Cu}}/2) \approx 0.09 \text{ f}\Omega \text{ m}^2$ , are comparable to those for  $AR_{\text{N1/N2}}$  for our noble-metal pairs. Further investigations must determine if the physics underlying them is also the same.

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