VOLUME 51, NUMBER 1

Dimensional crossover field as a function of oxygen stoichiometry in YBa₂Cu₃O_{7- δ} thin films

J. Deak, Lifang Hou, P. Metcalf, and M. McElfresh

Physics Department, Purdue University, West Lafayette, Indiana 47907 (Received 4 August 1994; revised manuscript received 17 October 1994)

The magnetic phase diagram of YBa₂Cu₃O_{7- δ} thin films was studied as a function of anisotropy by systematically changing the oxygen stoichiometry (δ value). For small δ values the vortex-solid phase transition boundary $H_g(T)$ is observed over the full accessible field range (50 kOe) to follow the $(1 - T/T_c)^{-1.5}$ dependence that is expected for an anisotropic superconductor in the three-dimensional regime. As δ increases, a portion of the phase boundary no longer follows the $(1 - T/T_c)^{-1.5}$ dependence making it possible to identify the anisotropy-dependent dimensional crossover field H_0 at which the system begins to behave quasi-two-dimensionally. Plotting $H_g(T)$ normalized by H_0 as a function of $(1 - T/T_c)$ results in a collapse of the phase boundaries onto a single universal curve. Using published values of the anisotropy $\gamma=8.5$ and the upper critical field slope $dH_{c2}/dT=-20$ kOe/K it is possible to determine the specific relation $H_0 \approx 1.2 \phi_0/(d^2 \gamma^2)$, where d is the multilayer spacing, which can be used to determine the δ dependence of γ .

The CuO-based high-temperature superconductors (HTS's) represent a group of highly anisotropic materials that are often described as alternating layers of superconducting and normal, or insulating, layers.¹ Numerous experiments have suggested that superconductivity resides primarily in a layer composed of nearly planar CuO₂ multilayers with the alternate layer functioning as charge-reservoir layer that affects the carrier concentration in the CuO₂ multilayers.² Flux vortices in these materials are often described as supercurrent loops within the CuO₂ multilayers (pancake vortices) strung together into flexible vortex lines.³ The pancake vortices in different CuO₂ multilayers can be coupled via their magnetic interactions or Josephson coupling, with the strength of this coupling depending on the anisotropy of the material.¹

Several theoretical models have been proposed to describe the flux-vortex behavior and its implications for the magnetic phase diagram of anisotropic superconductors like the HTS's.⁴⁻⁶ For the more weakly anisotropic HTS's (e.g., YBa₂Cu₃O₇) the model of Feigel'man, Geshkenbein, and Larkin (FGL),⁵ as well as that of Fisher, Fisher, and Huse (FFH),⁶ describe a phase transition below the upper critical field H_{c2} at which point a liquid of flexible flux vortices becomes a flux-vortex solid (glass or crystal). In the case of strongly disordered materials (e.g., YBa₂Cu₃O₇ thin films) a continuous vortex-glass phase transition is expected and has been observed.⁷ At a sufficiently large applied magnetic field value, the system will behave quasi-two-dimensionally as a result of fluctuations rendering the pancake vortices within a given CuO_2 multilayer independent of the pancake vortices in neighboring CuO_2 multilayers.⁴⁻⁶ The value of this dimensional-crossover field H_0 is expected to be proportional to $\phi_0/(d\gamma)^2$, decreasing with the anisotropy $\gamma = \xi_{ab} / \xi_c$; where d is the distance between CuO₂ multilayers and the coherence lengths ξ_{ab} and ξ_c are in the *ab* plane and along the *c* axis, respectively.⁴⁻⁶ Here we present a specific determination of H_0 and show how it evolves with changes in anisotropy that are produced in epitaxial thin films of YBa₂Cu₃O_{7- δ} (YBCO) as oxygen is systematically removed.

Epitaxial YBCO thin films, with the c axis perpendicular to the film plane, were prepared by pulsed laser deposition on heated (001) LaAlO₃ substrates as previously described.⁸ Each thin-film sample was about 4000 Å thick and initially had a superconducting transition temperature $T_c = 90 \pm 2$ K, with a transition width ΔT_c of about 2 K when measured using ac susceptibility (χ_{ac}) at 1.5 MHz. The oxygen stoichiometry of these films was modified by annealing at 400 °C in a controlled flowing mixture of oxygen and argon gases followed by a rapid quench to room temperature as described previously.⁹ A separate film was prepared for each oxygen stoichiometry. The T_c value for a given δ value correspond closely with previous studies¹⁰ and there is an estimated error of about 0.05 in the values of δ used here.

The films were patterned using laser ablation into bridges having dimensions of 100 μ m wide by 2000 μ m long. A standard four-point probe technique was used for the temperature-dependent resistivity measurements $\rho(T)$ and electric field as a function of current density E(J) measurements using procedures described previously.¹¹ The dc magnetic field (H), ranging from 0 to 50 kOe, was applied parallel to the crystallographic c axis.

Shown in Fig. 1 are the vortex-glass phase boundaries $H_{\rho}(T)$ for δ ranging from 0.05 to 0.65. The points at 10 and 50 kOe were determined by scaling of E(J) curves, while those at the other fields studied were determined by analyzing $\rho(T)$ using a linear extrapolation to the temperature at which the quantity $[d(\ln\rho)/dT]^{-1}$ equals zero.¹²⁻¹⁵ The H=0 kOe points are the T_c values determined using $\rho(T)$ and χ_{ac} measurements. The $H_g(T)$ curves broaden significantly as δ increases, with the temperature difference $\Delta T = (T_c - T_g)$ at H = 50 kOe equal to about 10 K for δ =0.05 increasing to $\Delta T \sim 35$ K for δ =0.65; where the T_c value at H=0 is used. The temperature dependence of H_g is observed to change with δ . For $\delta < 0.12$, the relation $H_{g}(T) \sim (1 - T/T_{c})^{x}$ with x = 1.3 - 1.5 fits the results, which is consistent with previous observations of $H_{q}(T)$ in anisotropic three-dimensional high-temperature superconductors.¹³ In contrast to this, for $\delta > 0.12$, $H_g(T)$ can no 706



FIG. 1. Vortex-glass phase boundaries $H_g(T)$ determined for YBa₂Cu₃O_{7- δ} thin films with values of δ ranging from 0.05 to 0.65 using a vortex-glass scaling analysis of the electric field as a function of current density data at 10 and 50 kOe and the resistivity as a function of temperature data at all other fields.

longer be described by a simple power-law temperature dependence over the full H range. The behavior in this regime is more consistent with observations of the vortex-glass transition in quasi-two-dimensional superconductors, such as Tl₂Ba₂CaCu₂O₈ (Ref. 14) and Bi₂Sr₂ CaCu₂O_x (Ref. 15), where at high field $H_g(T)$ decreases more rapidly with T.

The observed shift of the $H_g(T)$ phase boundary toward lower temperature is expected when the anisotropy increases.9 A previous analysis of torque magnetometry data on grain-aligned YBCO powder samples¹⁶ has shown γ to increase from about 7 to 32 as δ is increased from 0 to 0.5. These results are similar to the results described below. The increase in δ also corresponds to a decrease in the zerotemperature c-axis coherence length $\xi_c(0)$, which should result in a decrease of the Josephson coupling.⁹ Either effect is consistent with YBCO moving closer to the two-dimensional limit as δ is increased. The FGL and FFH models both describe a dimensional crossover field that depends on the anisotropy γ as $H_0 \propto \phi_0 / (\gamma d)^2$ (Ref. 5). If the δ dependence of $H_{\rho}(T)$ is a direct result of the δ dependence of H_0 , then a plot of $H_{\varrho}(T)/H_0$ as a function of $(1-T/T_c)$, where T_c is the δ -dependent superconducting transition temperature determined for each film, may be universal. By plotting $H_g(T)/H_0$ as a function of $(1-T/T_c)^{1.5}$ the threedimensional portion of the H-T phase diagram that is below H_0 should be linear while the portion of the phase diagram above H_0 , where $H_g(T)$ no longer shows this power-law temperature dependence, should deviate from linearity.

Figure 2 shows normalization of the $H_g(T)$ curves in Fig. 1, with a break from linearity at $H_g(T)/H_0 \approx 1$. Data collapse was accomplished by first determining the anisotropy value $\gamma = 8.5$ for the film with $\delta = 0.05 \pm 0.05$ ($T_c = 89.4$ K). This analysis was originally attempted using γ in the range of 5–6 previously reported for stoichiometric YBCO crystals and powders,¹⁶ however, this range of γ values was found to yield unreasonably large values for dH_{c2}/dT . Considering the fact that stoichiometric YBCO typically has a $T_c \approx 92$ K, it is likely that the 89.4 K thin film is not at the optimal oxygen content, and is thus likely to have a greater aniso-



FIG. 2. The $H_g(T)$ boundaries shown in Fig. 1 normalized by the dimensional crossover field H_0 and plotted against $[1-T/T_c(\delta)]^{1.5}$. The universal $H_g(T)$ boundary in this plot deviates from linearity at the crossover between three-dimensional and quasi-two-dimensional behavior, which is found to occur at $H_g(T)/H_0=1$. This normalization procedure allows the determination of H_0 and the relative values of anisotropy $\gamma = \xi_{ab}/\xi_c$ for all δ values studied.

tropy value. The anisotropy value for this film was thus determined using the relation $\gamma = \{\phi_0 / [2\pi\xi_c(0)^2T_c] dH_{c2} /$ $dT|]\}^{1/2}$ along with the upper critical field slope $dH_{c2}/dT = -20$ kOe/K determined for a YBCO thin film with $\delta = 0.05$ (Ref. 17) and the zero-temperature *c*-axis coherence length $\xi_c(0)$ previously determined for this film to be 1.6 Å (Ref. 9) using the crossover temperature T_{23} from two- to three-dimensional fluctuations above T_c and the relation $\xi_c(0) = d/2(T_{23}/T_c - 1)^{1/2}$ (Ref. 18). The quantity $H_g(T)/H_0$ was then determined for each of the other YBCO thin films by adjusting the γ value for each of these $H_g(T)/H_0$ curves in order that these curves collapsed onto the universal $H_g(T)/H_0$ versus $(1-T/T_c)^{1.5}$ curve determined for the film with $T_c = 89.4$ K. The value of d for all films was fixed at 11.7 Å since x-ray-diffraction measurements on these films indicate that d varies from 11.70 to 11.77 Å as δ changes from 0.05 to 0.65. It was then found that this universal $H_g(T)/H_0$ versus $(1-T/T_c)^{1.5}$ curve deviates from linearity (no longer shows threebehavior) at $H_g(T)/H_0 = 1$, dimensional if H_0 = $1.2\phi_0/(\gamma d)^2$. This relation is consistent with the models of FFH and FGL, which give order of magnitude estimates for H_0 of $\phi_0/(d\gamma)^2$ and $4\phi_0/(d\gamma)^2$, respectively, and it may apply to all high-temperature superconductors.^{5,6} The $H_{g}(T)$ phase boundary determined using $\rho(T)$ data for a $Tl_2Ba_2CaCu_2O_8$ (Tl-2212) thin film was scaled onto the $H_g(T)/H_0$ curve in Fig. 2 with a value of $\gamma=42$ by first fixing d = 14.7 Å (the *c*-axis length divided by the number of multilayers per unit cell) and then varying γ . This is in agreement with previous observations for TI-2212 which show anisotropy values ranging from about 5 to 70.19

The values of the anisotropy γ and the dimensional crossover field H_0 determined using this scaling analysis are shown as a function of δ in Fig. 3. The γ values are consistent with previous measurements. For example, the value $\gamma=30$ for the $\delta=0.65$ sample is close to the previously reported value of $\gamma\approx32$ determined from an analysis of torque magnetometry measurements on the grain-aligned YBCO



FIG. 3. The anisotropy γ and dimensional crossover field H_0 values, determined using the normalization procedure shown in Fig. 2, plotted as a function of δ for several oxygen-deficient YBa₂Cu₃O_{7- δ} thin films.

powder sample with $\delta \approx 0.5$ (Ref. 16). Note, however, that in previous analyses of γ as a function of δ on grain-aligned YBCO powder samples, γ increases slowly for $\delta = 0-0.25$ (Ref. 16). In contrast to this, the results in Fig. 3 indicate that for thin films prepared under the conditions utilized here, γ increases quickly in the range $\delta = 0-0.25$ and then plateaus in the range $\delta = 0.25-0.35$ coincident with the 60 K T_c plateau. The $H_0(\delta)$ plot in Fig. 3 also shows a rapid decrease with δ in the range $\delta = 0-0.25$, dropping from about 260 kOe to about 30 kOe. The small values determined for H_0 when $\delta > 0.25$ are consistent with the work of Welp *et al.*, which found that the M(T) isochamps measured from H = 10 to 50 kOe for YBCO with $\delta \approx 0.35$ are better described by a twodimensional, rather than a three-dimensional, fluctuation scaling analysis.²⁰

Shown in Fig. 4 are the values of dH_{c2}/dT plotted as a function of δ for YBCO thin films with H parallel to the c axis using the Ginzburg-Landau relation $-dH_{c2}/dT = \phi_0/dt$ $\left[2\pi\xi_{ab}^{2}(0)T_{c}\right]$ (Ref. 20) and the definition of anisotropy $\gamma = \xi_{ab}/\xi_c$. The values of dH_{c2}/dT represented by the solid diamonds were determined using the γ values plotted in Fig. 3 and the $\xi_c(0)$ values determined for the same films using a zero-magnetic-field fluctuation conductivity analysis.⁹ The hollow circles represent dH_{c2}/dT values determined by Ossandon et al. for $\delta < 0.2$ using the Hao-Clem magnetization analysis, which is based on the anisotropic Ginburg-Landau theory.^{17,21} These different determinations of dH_{c2}/dT indicate that the magnitude of dH_{c2} decreases as δ increases to 0.2. However, the present analysis extends the range over which dH_{c2}/dT has been determined and indicates that dH_{c2}/dT exhibits a minimum between the 90 and 60 K pla-



FIG. 4. The slope at T_c of the upper critical field as a function of δ . Solid diamonds represent values determined using $-dH_{c2}/dT = \phi_0[2\pi\gamma^2\xi_c(0)^2T_c]$, with $\xi_c(0)$ determined from the zero-field fluctuation conductivity at $T > T_c$ and γ values determined from the $H_g(T)/H_0$ analysis. Hollow circles are values determined by Ossandon *et al.* (Ref. 17) using a three-dimensional scaling analysis for $\delta=0$ and the hollow squares are values determined by Welp *et al.* (Ref. 20) using a two-dimensional scaling analysis for $\delta=0.35$.

teaus. These results are in agreement with both the twodimensional scaling analysis of Welp *et al.* (Ref. 20) at large δ values $(dH_{c2}/dT \approx -12 \text{ kOe/K} \text{ for } \delta \approx 0.35)$ as well as the values of dH_{c2}/dT determined at small δ ($\delta < 0.2$) by Ossandon *et al.*¹⁷

In summary, the temperature dependence of the vortex glass transition $[H_g(T)]$ was studied in thin films of YBa₂Cu₃O_{7- δ} as a function of δ . The dimensional crossover field H_0 was identified using the deviation in the temperature dependence from $H_g \sim (1 - T/T_c)^{1.5}$ expected in the three-dimensional regime. The $H_g(T)$ curves at all δ values could be collapsed onto one another by appropriate normalization of both the T scale and the H scale. Using the relation $H_0 \sim \phi_0 / (\gamma d)^2$ with values of γ and d determined for nearly fully oxygenated YBCO thin films, it was possible to determine relative values of the anisotropy γ as a function of δ . There is a notable generality of the phase diagram and an attempt to collapse the $H_g(T)$ curve of TI-2212 onto the YBCO results met with success. It is possible that the specific relation $H_0 \approx 1.2 \phi_0 / (\gamma d)^2$ determined may be generally applicable to CuO-based HTS materials, thereby providing a general method for determining the anisotropy in HTS materials from transport data.

This work was supported by the Director for Energy Research, Office of Basic Energy Sciences through the Midwest Superconductivity Consortium (MISCON) DOE Grant No. DE-FG02-90ER45427.

- ¹J. R. Clem and M. W. Coffey, Phys. Rev. B **42**, 6209 (1990); J. R. Clem, *ibid.* **43**, 7837 (1991).
- ²R. J. Cava, Science 247, 656 (1990).
- ³S. Doniach, in *The Phenomenology of Flux Motion in High Temperature Superconductors*, Proceedings of the Los Alamos Symposium—1989, edited by K. S. Bedell, D. Coffey, D. E.
- Meltzer, D. Pines, and J. R. Schrieffer (Addison-Wesley, Reading, MA, 1989), p. 406.
- ⁴L. I. Glazman and A. E. Koshelev, Phys. Rev. B 43, 2835 (1991).
- ⁵ M. V. Feigel'man, V. B. Geshkenbein, and A. I. Larkin, Physica C 167, 177 (1990).
- ⁶M. P. A. Fisher, Phys. Rev. Lett. **62**, 1415 (1989); D. S. Fisher, M.

708

P. A. Fisher, and D. A. Huse, Phys. Rev. B 43, 130 (1991).

- ⁷R. H. Koch, V. Foglietti, W. J. Gallagher, G. Koren, A. Gupta, and M. P. A. Fisher, Phys. Rev. Lett. **64**, 2586 (1990).
- ⁸ R. E. Muenchausen, K. M. Hubbard, S. R. Foltyn, R. C. Estler, and N. S. Nogar, Appl. Phys. Lett. 56, 578 (1990); X. D. Wu, R. E. Muenchausen, S. R. Foltyn, R. C. Estler, R. C. Dye, C. Flamme, N. S. Nogar, A. R. Garcia, J. Martin, and J. Tesmen, *ibid.* 56, 1481 (1990).
- ⁹L. Hou, J. Deak, P. Metcalf, and M. McElfresh, Phys. Rev. B 50, 7226 (1994).
- ¹⁰ R. J. Cava, A. W. Hewat, E. A. Hewat, B. Batlogg, M. Marezio, K. M. Rabe, J. J. Krajewski, W. F. Peck, Jr., and L. W. Rupp, Jr., Physica C 165, 419 (1990); E. Osquiguil, M. Maenhoudt, B. Wuyts, and Y. Bruynseraede, Appl. Phys. Lett. 60, 1627 (1992); E. C. Jones, D. K. Christen, J. R. Thompson, R. Feenstra, S. Zhu, D. H. Lowndes, J. M. Phillips, M. P. Siegal, and J. D. Budai, Phys. Rev. B 47, 8986 (1993).
- ¹¹ J. Deak, M. McElfresh, J. R. Clem, Z. Hao, M. Konczykowski, R. Muenchausen, S. Foltyn, and R. Dye, Phys. Rev. B 47, 8377 (1993).
- ¹²J. Deak and M. McElfresh, Phys. Rev. B 48, 1337 (1993).
- ¹³P. L. Gammel, L. F. Schneemeyer, and D. J. Bishop, Phys. Rev. Lett. **66**, 953 (1991).

- ¹⁴J. Deak, M. McElfresh, D. W. Face, and W. L. Holstein (unpublished).
- ¹⁵H. Safar, P. L. Gammel, D. J. Bishop, D. B. Mitzi, and A. Kapitulnik, Phys. Rev. Lett. **68**, 2672 (1992).
- ¹⁶B. Janossy, D. Prost, S. Pekker, and L. Fruchter, Physica C 181, 51 (1991).
- ¹⁷J. G. Ossandon, J. R. Thompson, D. K. Cristen, B. C. Sales, H. R. Kerchner, J. O. Thompson, Y. R. Sun, K. W. Lay, and J. E. Tkaczyk, Phys. Rev. B **45**, 12 534 (1992); E. C. Jones, D. K. Christen, J. R. Thompson, J. G. Ossandon, R. Feenstra, Julia M. Philips, and M. P. Siegal, *ibid.* **49**, 572 (1994).
- ¹⁸B. Oh, K. Char, A. D. Kent, M. Naito, M. R. Beasley, T. H. Geballe, R. H. Hammond, A. Kapitulnik, and J. M. Graybeal, Phys. Rev. B **37**, 7861 (1988).
- ¹⁹J. H. Kang, K. E. Gray, R. T. Kampwirth, and D. W. Day, Appl. Phys. Lett. **53**, 2560 (1988); H. Mukaida, K. Kawaguchi, M. Nakao, H. Kumakura, D. R. Dietderich, and K. Togano, Phys. Rev. B **42**, 2659 (1990).
- ²⁰U. Welp, S. Fleshler, W. K. Kwok, R. A. Klemm, V. M. Vinokur, J. Downey, and G. W. Crabtree, *Reversible Magnetization of Copper Oxide Superconductors in the Mixed State*, in *High Temperature Superconductivity*, edited by S. K. Malik and S. S. Shah (Nova Science, New York, 1992).
- ²¹Z. Hao, J. R. Clem, M. McElfresh, L. Civale, A. P. Malozemoff, and F. Holtzberg, Phys. Rev. B 43, 2845 (1991).