# Ni<sup>3+</sup>-Ni<sup>3+</sup> pair transitions in highly doped LiNbO<sub>3</sub>:Ni

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We report on the EPR  $Ni^{3+}$ - $Ni^{3+}$  pair transitions in highly doped LiNbO<sub>3</sub>:Ni. It is found that there are nine absorption peaks at 640, 1200, 1460, 1520, 3040, 3160, 3380, 7800, and 10 600 G in the range 0–12 000 G in highly doped LiNbO<sub>3</sub>:Ni (0.8 wt. %). The spectra were interpreted as both the  $Ni^{3+}$  single-ion transitions and  $Ni^{3+}$ - $Ni^{3+}$  pair transitions. In addition, it is found that many superhyperfine lines exist in the range 3000–3500 G which is not yet understood. Their origin is possibly an electron-phonon disturbance.

## I. INTRODUCTION

The ferroelectric behavior and related properties in crystalline LiNbO<sub>3</sub> have been investigated in part by substituting a paramagnetic impurity such as  $Cu^{2+}$ ,  $Cr^{3+}$ ,  $Fe^{3+}$ ,  $Mn^{2+}$ , or Ni<sup>2+</sup> for a small fraction of the positive ions. The paramagnetic impurity ions, such as  $Fe^{3+}$ , then serve as a sensitive probe for investigating the crystalline environment and its response to ambient changes.<sup>1</sup> In studying the electron paramagnetic resonance (EPR) spectra of LiNbO<sub>3</sub>:Cu<sup>2+</sup>, LiNbO<sub>3</sub>:Cr<sup>3+</sup>, and YAG:Cr<sup>3+</sup> where YAG is yttrium aluminum garnet, it is noticed that the low-field transition intensity increases with paramagnetic-impurity-ion doping and this has led to consideration of the interaction of neighboring Cu<sup>2+</sup>, or Cr<sup>3+</sup> ions by Zhao and Yan,<sup>2</sup> Zhao,<sup>3</sup> and Siu and Zhao.<sup>4</sup>

With a frequency-tunable EPR spectrometer Mirzakhanyan<sup>5</sup> identified the two possible  $\Delta m_s = \pm 1$  transitions of Ni<sup>2+</sup> signal ions in LiNbO<sub>3</sub>:Ni. The splitting *D* was derived to be 152.1±0.3 GHz and  $g_{11} = 2.24\pm0.03$ . Thiemann and Schirmer<sup>6</sup> have found that there is a  $\Delta m_s = \pm 2$  transition of Ni<sup>2+</sup> ions in LiNbO<sub>3</sub>:Ni.

Here, we report EPR transitions observed at 9.553 GHz in LiNbO<sub>3</sub> doped with Ni (0.8 WT %). We will show that these transitions are induced by Ni<sup>2+</sup> single ions, Ni<sup>3+</sup> single ions, and the Ni<sup>3+</sup>-Ni<sup>3+</sup> pair.

### **II. MEASUREMENTS AND RESULTS**

A single crystal of LiNbO<sub>3</sub>:Ni(0.8 wt %) was grown by the Czochralski technique. The crystal axes were

dx/dH 10600 7800 Ŷ የ 1200 2400 3600 4800 6000 7200 8400 9600 10800 12000 H(G)

checked by x-ray analysis.

The EPR spectra were recorded on an x-band Brucker ER-200D spectrometer with 100 kHz field modulation. The spectra are shown in Figs. 1 and 2. Since D = 152GHz) >> f (=9.553 GHz), the present spectra show no detectable signals of  $\Delta m_s = \pm 1$  transitions of Ni<sup>2+</sup> ions in the range  $0-12\,000$  G. It can be seen from the figures that there are many resolved strong superhyperfine lines and nine absorption peaks at 640, 1200, 1460, 1620, 3040, 3160, 3380, 7800, and 10 600 G in the range 0-12 000 G in highly doped LiNbO<sub>3</sub>:Ni. From the similarity between the EPR spectra of  $LiNbO_3$ :Cr<sup>3+</sup>(3d<sup>3</sup>) with sixcoordination  $C_3$  symmetry<sup>4</sup> and the EPR spectra of LiNbO<sub>3</sub>:Ni, we suggest that the absorption peaks are due to Ni<sup>3+</sup>(3d<sup>7</sup>) with the ground state  ${}^{4}A_{1}(F)$  which indicates that the impurity  $Ni^{3+}$  ions have the axially symmetric four-coordination (i.e., the  $60^{2}$ - $20^{2-}$  vacancy) site rather than the six-coordination site. This is apparently to be expected in LiNbO<sub>3</sub>, which generally has a rather imperfect crystal structure due to high doping.

## **III. INTERPRETATION OF EPR SPECTRA**

With consideration of the exchange (or superexchange) interaction, the perturbation Hamiltonian for  $Ni^{3+}$ -ion pairs takes the form, for J much greater than the other terms,

$$\mathcal{H}_{s} = \mathcal{H}_{s}(1) + \mathcal{H}_{s}(2) + J\mathbf{S}_{1} \cdot \mathbf{S}_{2} + DS_{z}^{2}$$
  
$$= g_{z}(1)\mu_{B}HS_{z}(1) + g_{z}(2)\mu_{B}HS_{z}(2) + D(1)S_{z}^{2}(1)$$
  
$$+ D(2)S_{z}^{2}(2) + J\mathbf{S}_{1} \cdot \mathbf{S}_{2} + DS_{z}^{2} , \qquad (1)$$

FIG. 1. EPR  $d\chi/dH$  spectrum of a LiNbO<sub>3</sub>:Ni crystal (5×5×1.5 mm<sup>3</sup>). f=9.553GHz; gain 2.5×10<sup>4</sup>; test temperature, 77 K;  $H//C_3$ ;  $\leftrightarrow$ , pair transition.

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dχ dĤ

- <mark>d'</mark>X

400

800



FIG. 2. EPR spectra of LiNbO<sub>3</sub>: Ni crystal  $(5 \times 5 \times 1.5 \text{ mm}^3)$ . f=9.553 GHz; gain,  $4 \times 10^4$  for  $d\chi/dH$  (top spectrum),  $2 \times 10^5$  for  $-d^2\chi/dH^2$ (bottom spectrum); test temperature, 77 K;  $H//C_3$ ;  $\rightarrow$  singleion transition;  $\rightarrow$ , pair transition. The upper part is the same as Fig. 1 on an expanded scale.

where *H* denotes the applied magnetic field, S=S(1)+S(2), S(i) is the spin of the single ion Ni<sup>3+</sup>(*i*),  $g_z(i)$  and D(i) are the *g* factor and zero-field splitting parameter of the single ion Ni<sup>3+</sup>(*i*), respectively, and *J* is the exchange integral. *D* is the zero-field splitting parameter of the Ni<sup>3+</sup>-Ni<sup>3+</sup> pair which has a spin *S* due to the combination of the exchange (or superexchange) interaction, the magnetic dipole-dipole interaction, the spinorbit coupling, and the low-symmetric crystal field, which can be expected to be different for the various values of *S*.  $z ||C_3||$  pair axis was used.

1200

1600

2000

H(G)

2400

2800

3200

3600

4000

Since

$$\mathbf{S}_1 \cdot \mathbf{S}_2 = \frac{1}{2} [S(S+1) - S_1(S+1) - S_2(S_2+1)],$$

where S is the total effective spin of the final states of the two ions, the centers of gravity of the four spectroscopic states with S=3, 2, 1, and 0 are at energies  $\frac{9}{4}J$ ,  $-\frac{3}{4}J$ ,  $-\frac{11}{4}J$ , and  $-\frac{15}{4}J$  at zero magnetic field, respectively; i.e., the largest term in Eq. (1), the exchange interaction, is diagonalized first. Resonance transitions are allowed only between states having the same total spin.

The resulting states are  $|(\frac{3}{2}, m_s; \frac{3}{2}, m_s)S, Ms\rangle$  (the single-ion state symbols will be neglected in the coupled states). The resulting states are as follows:

$$|3,3\rangle = |\frac{3}{2}, \frac{3}{2}, \frac{3}{2}, \frac{3}{2}\rangle,$$
  

$$|3,2\rangle = \frac{1}{\sqrt{2}} [|\frac{3}{2}, \frac{3}{2}; \frac{3}{2}, \frac{1}{2}\rangle + |\frac{3}{2}, \frac{1}{2}; \frac{3}{2}, \frac{3}{2}\rangle],$$
  

$$|3,1\rangle = \frac{1}{\sqrt{5}} [|\frac{3}{2}, \frac{3}{2}; \frac{3}{2}, -\frac{1}{2}\rangle + \sqrt{3} |\frac{3}{2}, \frac{1}{2}; \frac{3}{2}, \frac{1}{2}\rangle + |\frac{3}{2}, -\frac{1}{2}; \frac{3}{2}, \frac{3}{2}\rangle],$$
  

$$|3,0\rangle = -\frac{1}{\sqrt{5}} [|\frac{3}{2}, \frac{3}{2}, \frac{3}{2}, -\frac{3}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{1}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, \frac{1}{2}\rangle$$
  

$$|3,0\rangle = -\frac{1}{\sqrt{5}} [|\frac{3}{2}, \frac{3}{2}, \frac{3}{2}, -\frac{3}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{1}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, \frac{1}{2}\rangle$$
  

$$|3,0\rangle = -\frac{1}{\sqrt{5}} [|\frac{3}{2}, \frac{3}{2}, \frac{3}{2}, -\frac{3}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{1}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, \frac{1}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{1}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, \frac{1}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{3}{2}, \frac{1}{2}\rangle + 2|\frac{3}{2}, \frac{1}{2}, \frac{1}{2},$$

$$|3,0\rangle = \frac{1}{\sqrt{20}} \left[ \left| \frac{3}{2}, \frac{3}{2}; \frac{3}{2}, -\frac{3}{2} \right\rangle + 3 \left| \frac{3}{2}, \frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle + 3 \left| \frac{3}{2}, -\frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle + 3 \left| \frac{3}{2}, -\frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle - \left| \frac{3}{2}, -\frac{3}{2}; \frac{3}{2}, \frac{3}{2} \right\rangle \right],$$

$$|2,2\rangle = \frac{1}{\sqrt{2}} \left[ \left| \frac{3}{2}, \frac{3}{2}; \frac{3}{2}, \frac{1}{2} \right\rangle - \left| \frac{3}{2}, \frac{1}{2}; \frac{3}{2}, \frac{3}{2} \right\rangle \right],$$

$$|2,1\rangle = \frac{1}{\sqrt{2}} \left[ \left| \frac{3}{2}, \frac{3}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle - \left| \frac{3}{2}, -\frac{1}{2}; \frac{3}{2}, \frac{3}{2} \right\rangle \right],$$

$$|2,0\rangle = \frac{1}{2} \left[ \left| \frac{3}{2}, \frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle + \left| \frac{3}{2}, -\frac{3}{2}; \frac{3}{2}, \frac{3}{2} \right\rangle \right],$$

$$|1,1\rangle = \frac{1}{\sqrt{5}} \left[ \sqrt{\frac{3}{2}} \left| \frac{3}{2}, \frac{3}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle - \sqrt{2} \left| \frac{3}{2}, \frac{1}{2}; \frac{3}{2}, \frac{1}{2} \right\rangle \right],$$

$$|1,1\rangle = \frac{1}{\sqrt{5}} \left[ \sqrt{\frac{3}{2}} \left| \frac{3}{2}, \frac{3}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle - \sqrt{2} \left| \frac{3}{2}, \frac{1}{2}; \frac{3}{2}, \frac{1}{2} \right\rangle \right],$$

$$|1,0\rangle = \frac{1}{\sqrt{20}} \left[ 3 \left| \frac{3}{2}, \frac{3}{2}; \frac{3}{2}, -\frac{3}{2} \right\rangle - \left| \frac{3}{2}, \frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle - \left| \frac{3}{2}, -\frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle - \left| \frac{3}{2}, -\frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle \right],$$

$$(4)$$

$$|1,0\rangle = \frac{1}{\sqrt{20}} \left[ 3 \left| \frac{3}{2}, \frac{3}{2}; \frac{3}{2}, -\frac{3}{2} \right\rangle - \left| \frac{3}{2}, \frac{1}{2}; \frac{3}{2}, -\frac{1}{2} \right\rangle - \left| \frac{3}{2}, -\frac{1}{2}; \frac{3}{2}, \frac{3}{2} \right\rangle \right],$$

The expressions for the energy levels are as follows (i) For single-ion transitions when  $\Delta m_s = \pm 1$ ,

$$-\frac{1}{2} \rightarrow \frac{1}{2}; \quad f = g_z \mu_B H ,$$
  

$$-\frac{1}{2} - \frac{3}{2}; \quad f = \pm 2D(i) \mp g_z(i) \mu_B H ,$$
  

$$\frac{1}{2} - \frac{3}{2}; \quad f = \pm 2D(i) \pm g_z(i) \mu_B H ;$$
  
(5)

and when  $\Delta m_s = \pm 2$  (forbidden transitions),

$$-\frac{3}{2} \underbrace{\longleftrightarrow}_{2}^{1}, \quad f = \mp 2D(i) \pm 2g_{z}(i)\mu_{B}H \quad . \tag{6}$$

(ii) For pair transitions with  $\Delta Ms = \pm 1$  and S=1,

$$|1,0\rangle \rightarrow |1,1\rangle; \quad f = \frac{1}{2}[g_{z}(1) + g_{z}(2)]\mu_{\beta}H + D$$
  
+  $\frac{3}{5}[D(1) + D(2)],$   
 $|1,1\rangle \rightarrow |1,0\rangle; \quad f = -\frac{1}{2}[g_{z}(1) + g_{z}(2)]\mu_{\beta}H - D$   
-  $\frac{3}{5}[D(1) + D(2)],$  (7)  
 $|1,-1\rangle \rightarrow |1,1\rangle; \quad f = [g_{z}(1) + g_{z}(2)]\mu_{B}H;$   
with  $S=2,$ 

TABLE I. Calculated and observed bands.

Single-ion transitions				
$g_z(1) = g_z(2) = 2.019,$	$D(1) = -170  \mathrm{G},$	D(2) = -110  G		
$ \frac{3}{2},m_s\rangle \rightarrow  \frac{3}{2},M'_s\rangle$	H (G) (calc)	H (G) (obs)		
$\frac{1}{\left \frac{3}{2},-\frac{1}{2}\right\rangle} \rightarrow \left \frac{3}{2},\frac{1}{2}\right\rangle}$	3380; 3380	3380; 3380		
$\left \frac{3}{2},-\frac{3}{2}\right\rangle \rightarrow \left \frac{3}{2},-\frac{1}{2}\right\rangle$	3040; 3160	3040; 3160		
$\left \frac{3}{2},-\frac{3}{2}\right\rangle \rightarrow \left \frac{3}{2},\frac{1}{2}\right\rangle$	1520: 1580	1520: 1520		

Pair transitions				
D(S=1)=-3852 G				
$ 1,M'_s angle \rightarrow  1,Ms angle$	H (G) (calc)	H (G) (obs)		
$ 1,0\rangle \rightarrow  1,1\rangle$	7400	7800		
$ 1,1\rangle \rightarrow  1,0\rangle$	640	640		

Pair transitions D(S=2) = -4524 G			
$ 2,M_s\rangle \rightarrow  2,M_s'\rangle$	H (G) (Calc)	H (G) (obs)	
$ 2,2\rangle \rightarrow  2,1\rangle$	10 192	10 600	
$ 2,0\rangle \rightarrow  2,1\rangle$	3 380	3 380	

 Pair transitions

 D (S = 2) = D (S = 3) = -4524 G

  $|3, M_s \rangle \rightarrow |3, M'_s \rangle$  H (G) (calc)
 H (G) (obs)

  $|3, 1 \rangle \rightarrow |3, 0 \rangle$  1 200
 1 200

  $|3, 0 \rangle \rightarrow |3, 1 \rangle$  7 960
 7 800

  $|3, 2 \rangle \rightarrow |3, 1 \rangle$  10 360
 10 600

$$\begin{aligned} |2,1\rangle \to |2,2\rangle; \quad f &= \frac{1}{2} [g_z(1) + g_z(2)] \mu_\beta H + 3D , \\ |2,2\rangle \to |2,1\rangle; \quad f &= -\frac{1}{2} [g_z(1) + g_z(2)] \mu_\beta H - 3D , \\ |2,0\rangle \to |2,1\rangle; \quad f &= \frac{1}{2} [g_z(1) + g_z(2)] \mu_\beta H ; \\ \text{and with } S &= 3, \\ |3,3\rangle \to |3,2\rangle; \quad f &= -\frac{1}{2} [g_z(1) + g_z(2)] \mu_\beta H - 5D \\ &- [D(1) + D(2)] , \\ |3,1\rangle \to |3,0\rangle; \quad f &= -\frac{1}{2} [g_z(1) + g_z(2)] \mu_\beta H - D \\ &- \frac{1}{5} [D(1) + D(2)] , \\ |3,0\rangle \to |3,1\rangle; \quad f &= \frac{1}{2} [g_z(1) + g_z(2)] \mu_\beta H + D \\ &+ \frac{1}{5} [D(1) + D(2)] , \end{aligned}$$
(9)

<sup>2</sup>M. G. Zhao and Q. L. Yang, Phys. Rev. B 39, 862 (1989).

<sup>3</sup>M. G. Zhao, Phys. Rev. B 40, 2543 (1989).

$$|3,1\rangle \rightarrow |3,2\rangle: f = \frac{1}{2}[g_{z}(1) + g_{z}(2)]\mu_{\beta}H + 3D + \frac{3}{5}[D(1) + D(2)] , |3,2\rangle \rightarrow |3,1\rangle: f = -\frac{1}{2}[g_{z}(1) + g_{z}(2)]\mu_{\beta}H - 3D - \frac{3}{5}[D(1) + D(2)] .$$

Here f denotes the absorption frequency in the EPR measurement, f=9.553 GHz.

Both the calculated and experimental data are listed in Table I. It can be seen from Table I that the calculation is in good agreement with the experimental data.

# IV. DISCUSSION AND CONCLUSIONS

(a) This work is a report on the Ni<sup>3+</sup>-Ni<sup>3+</sup> EPR pair transitions. It should be noted that, in contrast with the case of YAG:Cr<sup>3+</sup>,<sup>3</sup> the EPR lines at 3160, 3380, 7800, and 10 600 G extend below the zero signal level, although all other lines observed showed the typical phase of a derivative EPR absorption spectrum. This behavior of LiNbO<sub>3</sub>:Ni<sup>3+</sup> resonance is not yet understood. Possibly it is due to electron-phonon disturbances in the piezoelectric LiNbO<sub>3</sub>.

(b) There exist many resolved strong superhyperfine lines in the range of 3000-3500 G. This is not yet understood because the nuclear spin I ( $^{58}$ Ni)=0. Possibly, it is again an electron-phonon disturbance in the piezoelectric LiNbO<sub>3</sub>.

(c) The absorption intensity at 1460 G is larger than that at 1520 G. It is probably the  $\Delta m_s = 2$  transition of Ni<sup>2+</sup>. According to the work by Müller,<sup>7</sup> Williams,<sup>8</sup> and Thiemann and Schirmer,<sup>6</sup> the  $\Delta m_s = 2$  transition is induced by the electric part of the microwave electric field.

(d) LiNbO<sub>3</sub> is a dielectric crystal that is of particular interest because of the photorefractive effect observed in these crystals. The photorefractive effect, which can be used for the storage of volume phase holograms, seems to be correlated to the presence of transition-metal impurities. For an understanding of the role of impurities in the photorefractive effect on a microscopic scale, it is necessary to know the valence state, and the sites of these impurities in the lattice. Therefore the discovery of both the Ni<sup>3+</sup>-Ni<sup>3+</sup> pair and four-fold-coordinated Ni<sup>3+</sup> sites in the LiNbO<sub>3</sub> crystal seem to be significant findings.

(e) Models that have a correct and clear physical meaning will be those which agree well with experimental results. Therefore it is safe to say that the present model is reasonable.

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<sup>&</sup>lt;sup>4</sup>G. G. Siu and M. G. Zhao, Phys. Rev. B 43, 13 575 (1991).

<sup>&</sup>lt;sup>5</sup>A. A. Mirzakhanyan, Sov. Phys. Solid State 23, 1434 (1981).

<sup>&</sup>lt;sup>6</sup>O. Thiemann and O. F. Schirmer, Phys. Status Solidi B 143, K115 (1987).

<sup>&</sup>lt;sup>7</sup>K. A. Muller, Phys. Rev. **171**, 350 (1968).

<sup>&</sup>lt;sup>8</sup>F. I. B. Williams, Proc. Phys. Soc. London 91, 111 (1967).