PHYSICAL REVIEW B VOLUME 51, NUMBER 8 15 FEBRUARY 1995-II

## Charge-conjugation symmetry breaking and the absorption spectra of polyphenylenes

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(Received 13 October 1994)

The effects on the absorption spectra of polyphenylenes of charge-conjugation symmetry breaking are studied within the framework of a recently introduced microscopic model. Breaking of this symmetry is shown to result in the appearance of a fourth distinct absorption band in the spectra of derivatized and atomically bridged polyphenylenes, providing further direct experimental information on the intramonomer contribution to the effective electron-hole interaction.

A fundamental problem in conjugated polymers, particularly in the polyphenylenes, $<sup>1</sup>$  is understanding the origin and</sup> nature of their absorption bands. The crucial factor in this problem is the magnitude of the effective Coulomb interaction  $H_{e-h}$  between an electron and a hole relative to the  $\pi$ -electron bandwidth W. Practically, conclusions on this relative magnitude are made on the basis of indirect experimental evidence and are frequently controversial. A good example of the latter is the current intense debate on the nature of the lowest energy absorption band in poly(phenylene vinylene) (PPV), $2-5$  for which estimates of the excitonic binding energy range from thermal energies,  $k_BT$ , <sup>3</sup> to the order of 1 eV.<sup>4,5</sup>

Recently, two of the present authors have introduced<sup>6</sup> a simplified but analytically explicit microscopic model (hereafter referred to as RG), which we believe elucidates the essential physics of the photoexcitations of the polyphenylenes. Since these polymers are essentially chains of linked phenylene monomers, the model recognizes that their singlet excitations are derived from the four singlet  $(e_{1g} \rightarrow e_{2u})$  excitations of the local phenylene monomer. If the polyphenylene possesses charge-conjugation symmetry  $(CCS)$ , that is, electron-hole symmetry, the model leads to the generic appearance of three principal absorption bands. The relative spacings and intensities of these bands are set by W and key parameters specifying the magnitude of  $H_{e-h}$ , thereby establishing direct experimental access to these microscopic parameters. Very interestingly, there is a fourth, dipole forbidden, singlet excitation band which is rendered allowed if the CCS of the polyphenylene is broken. The RG model has been studied analytically<sup>6</sup> and numerically for oligomers<sup>8,9</sup> and approximate fits to the three main absorption bands of PPV (Refs. 10—12) have indicated that the lowest energy exciton in PPV is weakly bound in the sense that the *relevant part* of  $H_{e-h}$  is small by comparison to W.

Here, we explicitly consider CCS-breaking terms in the RG model and demonstrate the appearance of the fourth absorption band as a natural consequence of them. We do this for derivatized polyphenylenes, where CCS is violated by side groups attached to the phenylene monomer, and atomically bridged polyphenylenes, where the electron-hole symmetry is broken by the presence of the bridging atoms [see examples in Figs.  $1(a)$  and  $1(b)$ ]. Importantly, the appearance of the fourth peak in PPV derivatives can be explained consistently with the estimates of the microscopic parameters deduced from our previous analysis $6.8$  of the three main absorption bands in this polymer. This is in sharp contrast to the consideration of Ref. 5, where the appearance of the fourth peak in the spectrum of MEH-PPV (Ref. 13) was attributed entirely to the strength of electron-electron correlations exceeding a threshold value in a Pariser-Parr-Poplelike model of PPV which, because it preserves CCS, makes no allowance whatsoever for the substitution of the phenylene monomer. Recently, a fourth peak in the absorption spectrum has also been observed $14$  in alkoxysulfonatesubstituted poly(paraphenylene) (PPP),<sup>15</sup> confirming that the symmetry-breaking-induced transition dipole moment we describe here is a general characteristic of substituted polyphenylenes.

The model of RG explicitly regards each phenylene monomer as providing two hole states, labeled  $a$  and  $c$ , and two electron states, labeled  $b$  and  $d$ . In an undistorted phenyl ring under an assumed local  $D_{6h}$  symmetry, the states in each pair are degenerate and have  $e_{1g}$  and  $e_{2u}$  orbital batterns.<sup>16</sup> Explicitly, their respective molecular orbitals<br>(MO's) are  $\psi_a = (12)^{-1/2} \times (2,1,-1,-2,-1,1)$ ,  $\psi_b = (12)^{-1/2}$  $X(-2,1,1,-2,1,1), \psi_c = 2^{-1} \times (0,-1,-1,0,1,1),$  and  $\psi_d = 2^{-1} \times (0,-1,-1,0,1,1)$  $\times (0,-1,1,0,-1,1)$ , where each component of the MO specifies the atomic  $C(2p)$  site amplitude in the order of the numbering of the carbon atoms given in Fig. 1. The corresponding singlet excitations of the monomer are described by the operators  $B_{j\sigma}^{\dagger} = b_{j\sigma}^{\dagger} a_{j,-\sigma}^{\dagger}$ ,  $D_{j\sigma}^{\dagger} = d_{j\sigma}^{\dagger} c_{j,-\sigma}^{\dagger}$ ,  $A_{j\sigma}^{\dagger} = d_{j\sigma}^{\dagger} a_{j,-\sigma}^{\dagger}$ ,



FIG. 1. Schematic structures of (a) dimethoxy PPV and (b) an atomically bridged polyphenylene. The numbering of carbon atoms used in the text is shown.

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and  $C_{j\sigma}^{\dagger} = b_{j\sigma}^{\dagger} c_{j,-\sigma}^{\dagger}$ , where the fermion operators  $a_{j\sigma}^{\dagger}$ ,  $b_{j\sigma}^{\dagger}$ ,  $c^{\dagger}_{i\sigma}$ , and  $d^{\dagger}_{i\sigma}$  create, respectively, an electron or hole with spin polarization  $\sigma$  in the specified orbitals of the monomer j  $(j=1, \ldots, N)$ . These excitations may be combined to form the four  $(n= 1,2,3,4)$  following singlet excitations of the phenylene monomer:<sup>17</sup>

$$
P_{j,1}^{\dagger} = \sum_{\sigma} (B_{j\sigma}^{\dagger} - D_{j\sigma}^{\dagger})/2, \quad E_{1u}(x), \tag{1} \qquad (1)
$$

$$
P_{j,2}^{\dagger} = \sum_{\sigma} (A_{j\sigma}^{\dagger} + C_{j\sigma}^{\dagger})/2, \quad E_{1u}(y), \tag{2}
$$

$$
P_{j,3}^{\dagger} = \sum_{\sigma} (B_{j\sigma}^{\dagger} + D_{j\sigma}^{\dagger})/2, \quad B_{1u}, \tag{3}
$$

$$
P_{j,4}^{\dagger} = \sum_{\sigma} (A_{j\sigma}^{\dagger} - C_{j\sigma}^{\dagger})/2, \quad B_{2u}.
$$
 (4)

The excitations of Eqs. (1) and (2) have transition dipole moments in the monomer  $x$  and  $y$  directions, respectively, while the excitations of Eqs. (3) and (4) are dipole forbidden under  $D_{6h}$  symmetry.<sup>16</sup>

In a general form, the Hamiltonian  $H$  defining the RG model $<sup>6</sup>$  is</sup>

$$
H = \sum_{j\sigma} \{ E_h^a a_{j\sigma}^\dagger a_{j\sigma} + E_h^c c_{j\sigma}^\dagger c_{j\sigma} + E_e^b b_{j\sigma}^\dagger b_{j\sigma} + E_e^d d_{j\sigma}^\dagger d_{j\sigma} \} + H_d + H_{e-h},
$$
\n
$$
(5)
$$

where the  $E$ 's are the excitation energies of electrons and holes in the orbitals mentioned,

$$
H_{d} = -\sum_{j\sigma} \{t_{bb}(b_{j+1,\sigma}^{\dagger}b_{j\sigma} + \text{H.c.}) + t_{aa}(a_{j+1,\sigma}^{\dagger}a_{j\sigma} + \text{H.c.}) + t_{ab}((b_{j+1,\sigma}^{\dagger} - b_{j-1,\sigma}^{\dagger})a_{j,-\sigma}^{\dagger} + \text{H.c.})\}
$$
(6)

describes the delocalization of the b and a orbitals due to the intermolecular hopping integrals  $t$  (the  $c$  and  $d$  orbitals remain localized), while

$$
H_{e-h} = -\sum_{jn} U_{n} P_{jn}^{\dagger} P_{jn} + V_{dd} + V_{e-h}
$$
 (7)

specifies the leading contributions arising from Coulomb interactions. The first term in Eq. (7) defines the energy gain  $U_n$  when an electron and a hole in a singlet state are simultaneously present on the *same* monomer in the symmetry combination n.  $V_{dd} = -\sum_{jnm} V_{nm} (P_{j+1,n}^{\dagger} + P_{j+1,n}) (P_{jm}^{\dagger}$  $+P_{im}$ ) describes the delocalization of the charge-neutral intramonomer excitations via the dipole-dipole interaction. In this paper we will use the simplified structure of PPP, in which case  $V_{11} = V$ ,  $V_{22} = -V/2$ , while  $V_{nm} = 0$  otherwise.<sup>6</sup> The long-range Coulomb interaction is introduced as  $V_{e-h} = V_C \sum_{j \neq l} \rho_j \rho_l/2|j - l|$ , where  $\rho_j = \sum_{\sigma} (a_{j\sigma}^\dagger a_{j\sigma} + c_{j\sigma}^\dagger c_{j\sigma})$  $V_{e-h} = V_C \sum_{j \neq l} \rho_j \rho_l/2|j - l|$ , where  $\rho_j = \sum_{\sigma} (a_{j\sigma}^{\dagger} a_{j\sigma} + c_{j\sigma}^{\dagger} c_{j\sigma} - b_{j\sigma}^{\dagger} b_{j\sigma} - d_{j\sigma}^{\dagger} d_{j\sigma})$  is the net charge density on the monomer

The interband transition dipole moments relevant to the optical absorption are discussed in Ref. 6 and, for the model in which the  $x$  axis of the phenylene monomer coincides with the polymer axis, are given by

$$
P_j^x = \mu_0 (P_{j,1}^\dagger + P_{j,1}) + (\mu_1/2) \sum_{\sigma} [(b_{j+1,\sigma}^\dagger + b_{j-1,\sigma}^\dagger) a_{j,-\sigma}^\dagger + \text{H.c.}],
$$
  

$$
P_j^y = \mu_0 (P_{j,2}^\dagger + P_{j,2})
$$

for the x and y directions, respectively. Here  $\mu_0$  arises from the transition dipole moments of the local  $E_{1u}$  excitations while  $\mu_1$  arises from the "oblique" interband hopping terms in  $H_d$ . The  $B^{\dagger}$  and  $D^{\dagger}$  transitions are polarized along the chain, while the  $A^{\dagger}$  and  $C^{\dagger}$  transitions are polarized perpendicular to it.

CCS is broken in the model of Eq. (5) when (a) the local monomer energies E satisfy  $E_e^d - E_e^b \neq E_h^c - E_h^a$ , and (b) the hopping integrals  $t_{aa}$  and  $t_{bb}$  are different.

It is easy to understand why the structures of Fig. 1 lead to breakdown of CCS. In the case of Fig.  $1(a)$  we may, most simply, represent a side group by one electron level with energy  $E<sub>s</sub>$  with respect to the atomic  $C(2p)$  energy and introduce the matrix element  $t_s$  for the hopping of an electron between this level and the neighboring carbon atom. The perturbation Hamiltonian for a single monomer is then  $V_p = V_{p2} + V_{p5}$ , where  $V_{p2} = t_s(a_2^{\dagger}s_2 + \text{H.c.}) + E_s s_2^{\dagger}s_2$ ,  $a_2^{\dagger}$ being the electron site creation operator for the carbon site 2, while  $s_2^{\dagger}$  is the site creation operator for the side group 2 spin indices omitted). ( $V_{p5}$  is analogous to  $V_{p2}$  with indices 2 being replaced by 5.) Assuming the corrections to the energies  $E$  to be small, second-order perturbation theory in  $t_s$ yields them as  $\delta E_h^a = \epsilon_1/6$ ,  $\delta E_h^c = \epsilon_1/2$ ,  $\delta E_e^b = \epsilon_2/6$ ,  $\delta E_e^d = \epsilon_2/2$ , where  $\epsilon_1 = t_s^2/(\alpha_0 + E_s)$  and  $\epsilon_2 = t_s^2/(\alpha_0 - E_s)$ . It is important to note the following: (1) Electron and hole excitation energies within pairs of localized  $(c \text{ and } d)$  and delocalizable  $(a \text{ and } b)$  states are shifted by different amounts  $(\epsilon_1 \neq \epsilon_2)$ . This results in either positive  $(|E_s| < \alpha_0)$  or negative  $(|E_s| > \alpha_0)$  shifts of the band absorption edges for  $x$ -polarized transitions. (2) Within each pair of electron ( $b$  and  $d$ ) and hole ( $a$  and  $c$ ) states, the corrections are different. This results in shifts and splitting of the band edges for y-polarized transitions. Note that the second effect also occurs if  $t_s = 0$  but the energies of the  $C(2p)$  orbitals on sites 2 and 5 are inductively modified by amounts  $\Delta E$  $\neq$  0. If the intermonomer hopping in Eq. (6) is a stronger interaction than the coupling to the side groups, the perturbing effect of the latter on the band states derived from the a and b orbitals must be calculated. Since the band levels closer to  $E<sub>s</sub>$  experience larger shifts in energy, this can lead to different effective bandwidths for the conduction and vaence bands. [Of course, in detailed calculations more than one energy level associated with a side group can be involved. See, e.g., the quantitative results of valence effective  $Hamiltonian<sup>19</sup>$  and intermediate neglect of differential overlap<sup>20</sup> calculations for oligomers of PPV derivatives.] The principal effects of side groups in the model of Eq. (5) therefore may, in general, be taken into account by setting  $t_{aa}$  $\neq t_{bb}$  and

$$
E_e^b = E_h^a = \alpha_1, \quad E_e^d = \alpha_2 + \delta, \quad E_h^c = \alpha_2 - \delta, \tag{8}
$$

where in Eq.  $(8)$  we have redefined the zero of energy. Consequently, already in a band picture with  $H_{e-h} = 0$ , four, rather than three, absorption bands occur in the polymer, and at the following threshold energies:  $2\alpha_1 - 2(t_{aa} + t_{bb})$  for the  $B^{\dagger}$  transitions,  $\alpha_1 + \alpha_2 - \delta - 2t_{bb}$  for the  $C^{\dagger}$  transitions,  $\alpha_1 + \alpha_2 + \delta - 2t_{aa}$  for the  $A^{\dagger}$  transitions, and  $2\alpha_2$  for the  $D^{\dagger}$  transitions.

The case of atomically bridged polyphenylenes [Fig.  $1(b)$ ] can be treated analogously. If  $E_s$  is now the pertinent energy level of the bridging atom and  $t_s$  is the hopping integral between the phenylene end carbons and this atom, then corrections to the excitation energies occur only for the delocalizable states:  $\delta E_e^b = 2\epsilon_2/3$  and  $\delta E_h^a = 2\epsilon_1/3$ . The importance of this effect in understanding the C(1s)- $\pi$ <sup>\*</sup> excitation spectra of these polyphenylenes has been stressed by Crecelius et  $al$ .<sup>22</sup> Of course, CCS is also broken through  $t_{aa} \neq t_{bb}$  and the perturbation calculation yields  $t_{aa} = |\epsilon_1|/3$  and  $t_{bb} = |\epsilon_2|/3$ .

When  $H_{e-h} \neq 0$ , the four independent transitions of the simple band picture are profoundly modified: they couple to each other and at the same time transfer oscillator strength to excitons.<sup>6</sup> If the long-range Coulomb interaction  $V_{e-h}$  is neglected analytical expressions for the frequency-  $(\omega)$  and wave-vector- (Q) dependent conductivity  $\sigma_{\alpha\alpha}(Q,\omega)$  ( $\alpha=x$ or  $y$ ) of an infinite polymer chain may be derived from the Kubo formula. The result for  $\sigma_{vv}(Q,\omega)$  is

$$
\sigma_{yy}(Q,\omega) = (e^2/2Abi\omega)[F_y(Q,\omega+i\Gamma) +F_y(-Q,-(\omega+i\Gamma))],
$$
 (9)

where

$$
F_y = [v_A^2 R_A + v_C^2 R_C + 2v_A v_C V_{y,Q} \chi_A \chi_C]/D_y, \qquad (10)
$$

$$
D_y = (1 - U_{y,Q} \chi_A)(1 - U_{y,Q} \chi_C) - (V_{y,Q})^2 \chi_A \chi_C. \quad (11)
$$

In Eq.  $(9)$ , b is the lattice constant of the chain, A is the transverse area corresponding to one chain, and  $\Gamma$  is a phenomenologically introduced broadening parameter:

$$
R_A = \chi_A (1 - U_{y,Q} \chi_C), \quad R_C = \chi_C (1 - U_{y,Q} \chi_A).
$$

In Eqs. (10) and (11),  $\chi_A(\omega)$  and  $\chi_C(\omega)$  are the propagators for the  $A^{\dagger}$  and  $C^{\dagger}$  interband transitions:

$$
\chi_A = N^{-1} \sum_k \left[ \alpha_1 + \alpha_2 + \delta - 2t_{aa} \cos(kb) - \omega \right]^{-1}
$$

$$
= \left[ (\alpha_1 + \alpha_2 + \delta - \omega)^2 - (W_a/2)^2 \right]^{-1/2}
$$

and

$$
\chi_C = [(\alpha_1 + \alpha_2 - \delta - \omega)^2 - (W_b/2)^2]^{-1/2},
$$

The where  $W_a = 4t_{aa}, W_b = 4t_{bb}.$ velocities  $v_A = \mu_0(\alpha_1 + \alpha_2 + \delta)/e\hbar$  and  $v_C = \mu_0(\alpha_1 + \alpha_2 - \delta)/e\hbar$ . The function  $D_{\nu}(Q,\omega)$ , in which

$$
U_{y,Q} = (U_2 + U_4)/2 - V \cos(Qb)/2,
$$
  
\n
$$
V_{y,Q} = (U_2 - U_4)/2 - V \cos(Qb)/2,
$$

expresses the coupling between  $A^{\dagger} + C^{\dagger}$  and  $A^{\dagger} - C^{\dagger}$  transitions. Its zeros as a function of  $\omega$  determine the energies  $\hbar \omega_0$  of the  $E_{1u}(y)$ - and  $B_{2u}$ -derived excitons. In systems where CCS is preserved  $v_A = v_C$  both propagators are equal,<br> $\chi_A = \chi_C$ , and Eq. (10) is simplified:  $F_y = 2v_A^2 \chi_A$ /  $(1 - \tilde{U}\chi_A)$ , where  $\tilde{U} = U_2 - V \cos(Qb)$ , so that the resulting absorption is a single band, corresponding to  $A^{\dagger} + C^{\dagger}$  excitations [Eq. (2)], while the  $A^{\dagger} - C^{\dagger}$   $B_{2u}$ -derived excitations [Eq. (4)] have vanishing transition dipole moment. The energy of the allowed  $E_{1\mu}(y)$ -derived exciton is<br>  $\hbar \omega_3 = \alpha_1 + \alpha_2 - [\tilde{U}^2 + (W/2)^2]^{1/2}$  while the energy of the forbidden  $B_{2u}$ -derived exciton is  $\hbar \omega_4 = \alpha_1 + \alpha_2 - [U_4^2 + (W/2)^2]^{1/2}$ . Both exciton bands become allowed when  $\chi_A \neq \chi_C$ . In this case the function  $F_y$  shows that the  $B_{2u}$ -derived excitations borrow oscillator strength from the  $E_{1u}$ -derived excitations. If CCS is only weakly broken  $(\delta \approx 0, W_a \approx W_b = W)$  the energy of the  $B_{2u}$ -derived exciton is just  $\hbar \omega_4$ .

The corresponding formula for  $\sigma_{xx}(Q,\omega)$  is given in Ref. 8 and expresses  $\sigma_{xx}$  in terms of the propagators  $\chi_B$  and  $\chi_D$ for the  $B^{\dagger}$  and  $D^{\dagger}$  transitions:

$$
\chi_B = N^{-1} \sum_k \left[ 2\alpha_1 - 2(t_{aa} + t_{bb}) \cos(kb) \cos(Qb/2) - \omega \right]^{-1}
$$
  
= 
$$
[(2\alpha_1 - \omega)^2 - W_Q^2]^{-1/2},
$$
  

$$
\chi_D = (2\alpha_2 - \omega)^{-1}.
$$

Here  $W_O = W \cos(Qb/2)$  and the bandwidth  $W = (W_a$  $+W_b/2$ . The energies of the two excitons  $\hbar \omega_1$  and  $\hbar \omega_2$ associated with these transitions are given by the zeros of the function  $D_x(Q,\omega)$ ,

$$
D_x = (1 - U_{x,Q} \chi_B)(1 - U_{x,Q} \chi_D) - (V_{x,Q})^2 \chi_B \chi_D, \quad (12)
$$



FIG. 2. Analytically calculated absorption spectra of a long polymer chain. The parameters used are listed in the text. The peak close to 3.7 eV arises as a consequence of broken chargeconjugation symmetry. The dash-dotted line is for the  $x$ -polarized absorption, the dashed line for the y-polarized one, and the solid line gives their sum representing unpolarized absorption. The inset shows an absorption spectrum of dimethoxy PPV taken from Ref. 20.

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in which

$$
U_{x,Q} = (U_1 + U_3)/2 + V \cos(Qb),
$$

$$
V_{x,Q} = (U_1 - U_3)/2 + V \cos(Qb).
$$

Thus the energies of the polymer's family of four excitons are determined by Eqs. (11) and (12).

Figure 2 shows the absorption spectrum calculated from the analytical formulas for  $\sigma_{yy}$  and  $\sigma_{xx}$  employing the parameter values  $\alpha_1 = 3.35$  eV,  $\alpha_2 = 3.25$  eV,  $t_{aa} = t_{bb} = 1$  eV,  $U_1 = U_2 = 0.2$  eV,  $U_3 = 1$  eV,  $U_4 = 2$  eV,  $\mu_1 / \mu_0 = 0.45$ ,  $\Gamma = 0.25$  eV, and  $V = 0$ . The CCS-breaking parameter is taken to be<sup>21</sup>  $|\delta|$  = 0.4 eV and leads to the "fourth" absorption band close to 3.7 eV. The former set of parameter values is close to that of our previous analysis $<sup>8</sup>$  of the absorption spec-</sup> trum of PPV. Note that the energy difference between the two central peaks is essentially determined by  $t$ ,  $U_4$ , and  $U_2$ . The finite value of  $\delta$  does correct this quantity but the main effect of  $\delta$  is to provide the *intensity*, i.e., the transition dipole moment, of the "fourth" absorption band. For comparison, in the inset of Fig. 2, the experimental spectrum<sup>20</sup> of

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- <sup>1</sup> For a review, see, e.g., R. L. Elsenbaumer and L. W. Shacklette, in Handbook of Conducting Polymers, edited by T. A. Skotheim (Dekker, New York, 1986), Vol. 1, pp. 213—263.
- <sup>2</sup> See, e.g., U. Rauscher *et al.*, Phys. Rev. B 42, 9830 (1990); M. Gailberger and H. Bässler, ibid. 44, 8643 (1991); K. Pichler et al., J. Phys. Condens. Matter 5, 7155 (1993); P. Gomes da Costa and E. M. Conwell, Phys. Rev. B 48, 1993 (1993).
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- ${}^{6}$ M. J. Rice and Yu. N. Gartstein, Phys. Rev. Lett. 73, 2504 (1994).
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- <sup>9</sup>In oligomers, additional peaks are present in the spectra due to finiteness effects. These must not be confused with the four bands discussed in the text.
- <sup>10</sup>D. D. C. Bradley, J. Phys. D **20**, 1389 (1987).
- $^{11}$ D. A. Halliday et al., Synth. Met. 55-57, 954 (1993).
- <sup>12</sup> See also N. F. Colaneri et al., Phys. Rev. B 42, 11 670 (1990); B. R. Hsieh, Polym. Bull. 25, 177 (1991); J. Bullot, B. Dulieu, and S. Lefrant, Synth. Met. 61, 211 (1993).
- <sup>13</sup>MEH refers to the two substituents (2-methoxy) and  $(5-(2'-ethyl)-hexoxy)$ .
- $14$  S. Kim and J. R. Reynolds (unpublished).

dimethoxy PPV is shown. The experimental spectrum of MEH-PPV is very similar.<sup>5</sup> It is apparent that the gross features of the experimental spectrum are well reproduced by the theoretical calculations. We have also performed numerical calculations for finite chains, which include the longrange Coulomb interaction  $V_{e-h}$  not taken into account in the analytical theory. For a chain of  $N = 10$  monomers, e.g., we find that the calculated absorption spectrum closely resembles the analytic spectrum of Fig. 2.

The appearance of a fourth distinct band in the absorption spectra of derivatized polyphenylenes<sup>5,14,20</sup> has therefore a natural explanation in terms of the breaking of the CCS of the unsubstituted polymer. The appearance of additional structure in the spectra of atomically bridged polyphenylenes observed by Crecelius et  $al.^{22}$  can similarly be interpreted as a signature of CCS violation in these systems. For them, the difference between the electron and hole bandwidths,  $W_a - W_b$ , is an important CCS-breaking parameter in addition to  $\delta$ . Finally, we mention that an indistinct absorption from to *b*. Finany, we include that an indistinct absorption relative at  $\sim$  3.7 eV in unsubstituted PPV,<sup>11</sup> if unambiguously established as such,  $^{23}$  may reflect weak CCS breaking occuring in the real polymer, e.g., due to interchain interactions.<sup>24</sup>

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- $^{16}$ L. Salem, The Molecular Orbital Theory of Conjugated Systems (Benjamin, Reading, MA, 1966).
- <sup>17</sup>M. Goeppert-Mayer and A. L. Sklar, J. Chem. Phys. 6, 645 (1938).
- <sup>18</sup>In fact, the perturbation also induces transitions between  $b \leftrightarrow d$ and  $a \leftrightarrow c$  intramonomer orbitals, which is beyond H in the form of Eq. (5) and will therefore be ignored in the present paper. The effects of such transitions can be found in Refs. 19 and 20.
- <sup>19</sup> F. Meyers, A. J. Heeger, and J. L. Brédas, J. Chem. Phys. 97, 2750 (1992).
- $^{20}$  J. Cornil et al., Chem. Phys. Lett. 223, 82 (1994).
- <sup>21</sup> According to Fig. 5 of Ref. 19, the splitting of the  $A^{\dagger}$  and  $C^{\dagger}$ band gaps for dimethoxy PPV can be of the order 1 eV.
- <sup>22</sup>G. Crecelius et al., Phys. Rev. B **28**, 1802 (1983).
- $23$  We warn of a possible source of confusion on this point which arises from the results of recent calculations (Ref. 20) on PPV oligomers. Cornil et aL (Ref. 20) find a small "fourth" peak both in underivatized and derivatized PPV. The main point to realize here is that in their calculations the "fourth" peaks obtained in underivatized and derivatized PPV have entirely different origins: compare the assignments for peak II in Tables 1 and 2 in Ref. 20. Most probably, the peak they find for underivatized PPV is due to the short length of the oligomer ("finite-box" effect).
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