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Inelastic exchange scattering in electron-energy-loss spectroscopy: Localized excitations in transition-metal and rare-earth systems

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Cross sections for quasiatomic excitation by exchange scattering of electrons are calculated in the Born-Ochkur approximation for 3p-3d and 3d-3d transitions in transition-metal systems, and for 4d-4f and 4f-4f transitions in rare earths. The energy dependence of the spin polarization of 3p-3d and 4d-4f losses in reflection electron-energy-loss spectroscopy from ferromagnetic surfaces involves a balance of small-angle spin-dependent inelastic processes accompanied by a high-angle elastic scattering, and large-angle spin-flip exchange scattering without the need for elastic scattering. Both 3d-3d excitations, e.g., in transition-metal compounds, and 4f-4f excitations in rare earths involve spin-flip transitions whose scattering amplitudes g fall off with momentum transfer q such that the full width at half maximum $q_{1/2}$ (in a.u.) is given by $q_{1/2} \langle r_{nl} \rangle \sim 2$, where $\langle r_{nl} \rangle$ is the expectation value of r for the 3d or 4f electron. The angular width of the spin-flip differential cross section is then much greater than for dipole transitions, a pattern that helps to account for how these intra-atomic transitions compete with dipole processes for primary energies in excess of 100 eV.

For primary electron energies significantly larger than the excitation or loss energy, electron-energy-loss spectroscopy is usually dominated by dipolar processes involving scattering of the incident electrons through a small angle: observation of the loss electron in reflection mode then requires an additional large-angle elastic scattering. This single stage process [Fig. 1(a)] is generally much less probable than an inelastic + elastic scattering [Fig. 1(b)] due to the dominance of near forward inelastic scattering. When electrons interact with an atom having a net spin, the outcome of the scattering process will depend on whether the spin of the incoming electron is parallel or antiparallel to the atomic spin: if atomic spins near a surface are aligned as in a ferromagnetic system, the electron scattering cross sections will produce both spin polarization in the scattered beam if the incident beam is unpolarized (see, for example, $3p \rightarrow 3d$ in the electron energy losses of amorphous Fe alloys¹) and spin asymmetry in the scattering of spin-up and spindown electrons.

These phenomena arise from exchange terms in the inelastic-scattering cross sections. Treating the scattering of the incident electron and the promotion of an oriented electron into an empty state as a two-electron problem, i.e., neglecting multiplet effects in the partially filled shell, the scattering may be described in terms of a direct amplitude $f(\theta)$ and an exchange amplitude $g(\theta)$, where θ is the scattering angle. For $3p \rightarrow 3d$ transitions in ferromagnetic Fe or Mn¹ or $4d \rightarrow 4f$ transitions in ferromagnetic rare earths, the polarization is then given by

$$P = \frac{|f|^2 + |g|^2 - |f - g|^2}{|f|^2 + |g|^2 + |f - g|^2} .$$
 (1)

In systems with open shells it is also possible for incident electrons to induce dipole forbidden intermultiplet excitations, e.g., $3d^{n}-3d^{n}$ or $4f^{n}-4f^{n}$ transitions, which



FIG. 1. (a) A large-angle inelastic-scattering event; (b) a small-angle inelastic scattering followed by large-angle elastic scattering.

require a spin flip.²⁻⁵ The differential cross section is then proportional to $|g|^2$.

THEORY

In this paper, we examine the properties of f and g for $3p \rightarrow 3d$ transitions in Fe and $4f^7 \cdot 4f^7$ transitions in Gd within a simple quasiatomic scattering model, the Born-Ochkur approximation,^{6,7} where for incident energy $E_p = k_i^2/2$ a.u. and incident wave vector \mathbf{k}_i ; f and g are given by

$$f = -\frac{2}{q^2}l(q) , \qquad (2a)$$

$$g = -\frac{2}{k_i^2} l(q) , \qquad (2b)$$

where $\mathbf{q} = \mathbf{k}_i - \mathbf{k}_f$ is the momentum transfer and l(q) the transition amplitude, is given by

$$l(q) = \int \psi_{nl'}^* e^{i\mathbf{q}\cdot\mathbf{r}} \psi_{nl} \,\mathrm{d}\mathbf{r} , \qquad (3)$$

where $\psi_{nl(n'l')}$ is the initial (final) state wave function. The excitation energy $\Delta E = (k_i^2 - k_f^2)/2$, and the approximation is valid for $E_p \gg \Delta E$. When the scattering angle is small,

$$P \simeq \frac{g(\theta)}{f(\theta)} = \frac{1}{4} \left(\frac{\Delta E}{E_p} \right)^2.$$
(4)

Figure 2 plots P as a function of θ for $3p \rightarrow 3d$ transitions in Fe($\Delta E = 56 \text{ eV}$) at $E_p = 90$, 227, and 1321 eV. At small scattering angles, P is small and arises from differences in the direct scattering amplitudes for spins parallel (f - g)or antiparallel (f) to the oriented atom direction¹ rather than spin-flip transitions. $P \rightarrow 1$ in the range $60^{\circ}-75^{\circ}$, corresponding to conditions when $|\mathbf{q}| = |\mathbf{k}_i|$ and f = g. This is an artifact of the simplification implicit in the



FIG. 2. The spin polarization P versus scattering angle for $3p \rightarrow 3d$ transitions in ferromagnetic iron for primary energies 90, 227, and 1321 eV.

Born-Ochkur exchange correction, and higher-order theories will yield somewhat smaller values. In addition, the first Born approximation is known to be erratic in its prediction at high scattering angles. However, Born-Ochkur gives a good approximation to the spin asymmetry in H ionization⁸ by electrons for $E_p \ge 80$ eV, and this simple theory gives general insight into the spin dependence of scattering. When P is large $(g \sim f)$, spinflip transitions have assumed considerable importance, but the peak in P contrasts strongly with the rapid falloff in the conventional first-order Born cross section

$$\frac{d\sigma}{d\Omega} \propto (\theta^2 + \theta_0^2)^{-1} , \qquad (5)$$

where $\theta_0 = \Delta E / (2E_p)$. $(d\sigma/d\Omega)_{3p \to 3d}^{1\text{ST BORN}}$ has fallen to half its maximum value at $\theta = 18^\circ$, 7°, and 1.2°, respectively, at the energies shown, so that high polarization events have low cross section even at $E_p = 90$ eV. The pattern is then one of low polarization with a high inelastic forward scattering cross section and of high polarization and low inelastic cross section at higher scattering angle. This implies that the balance between low-angle loss accompanied by a single high-angle elastic scattering [Fig. 1(b)] or multiple elastic scattering, and high-angle losses is delicate and highly dependent on both experimental geometry and the state of order at the surface. This is discussed in detail by Porter and Matthew⁹ for $p \to d$ and $d \to f$ transitions in transition-metal systems and rare earths, respectively.

For spin-flip transitions within a configuration, e.g., 4f-4f transitions in the rare earths, Born-Ochkur leads to

$$\frac{d\sigma}{d\Omega} \propto \left| \int |\psi_{nl}|^2 e^{i\mathbf{q}\cdot\mathbf{r}} \mathbf{dr} \right|^2.$$
(6)

Here the one-electron wave function ψ_{nl} of both the initial and final states is the same, and so $d\sigma/d\Omega$ is proportional to the x-ray atomic scattering for the excited electron. The differential cross section peaks in the forward direction as for dipolar losses but falls off much more slowly with angle. Expanding $e^{iq \cdot r}$ and approximating the matrix element by a parabolic function of q, $d\sigma/d\Omega$ falls off to half its maximum value at $\theta_{1/2}$ given by

$$\theta_{1/2} \approx 2 \arcsin \left[\left[\frac{3(1-2^{-1/2})}{4E_p \langle r_{nl}^2 \rangle} \right]^{1/2} \right],$$
(7)

where $\langle r_{nl}^2 \rangle$ is the expectation value of r^2 for the electron in both its initial and final state. Higher order terms in the expansion increase this value slightly (by ~10% for $E_p = 100 \text{ eV}$ in Gd). Figure 3 compares the differential cross sections for 4f - 4f transitions in Gd at three typical primary energies. $(d\sigma/d\Omega 0)_{\theta=0}$ varies as E_p^{-2} , and the total 4f - 4f cross section varies as E_p^{-3} as noted by Joachain.¹⁰ In contrast to the $4f^7 - 4f^{71}G$ loss ($\Delta E = 4.5$ eV), dipolar losses at the same ΔE have fallen to half maximum by 1° for $E_p = 100$ eV so that in a reflection loss experiment these will again be a balance between doubleand multiple-scattering (loss + elastic) and single inelastic-scattering events. The sensitivity of the ratio of $4f^7 - 4f^7$ losses in Gd to geometry, primary energy, and surface order is consistent with this conclusion. Only for inelastic low-energy electron-diffraction events are the low angle exchange events, i.e., non-spin-flip processes, likely to predominate.

For the corresponding spin-flip cross sections for $3d \cdot 3d$ transitions in ionic Mn compounds ($\Delta E = 3 \text{ eV}$), $(d\sigma/d\Omega)_{\theta=0}$ is lower than for Gd (five electrons instead of seven) and $(d\sigma/d\Omega)$ falls off more quickly with angle since $\langle r_{Mn}^2 \rangle = 1.64 \text{ a.u.}^2$ is greater then $\langle r_{Gd4f}^2 \rangle = 0.89$ a.u.²—see Froese Fischer.¹¹ In terms of momentum transfer the results may be expressed by a kind of "uncertainty" style relationship

$$\Delta q_{1/2} \langle r_{nl} \rangle \sim 2 , \qquad (8)$$

where $\Delta q_{1/2}$ is the momentum transfer at which the transition *amplitude* g has fallen to half its $\theta = 0$ value and $\langle r_{nl} \rangle$ is a measure of the size of the electron orbital. These results are also relevant to d-d transitions involving spin flip where the levels are further split by a crystal field.¹²⁻¹⁵ Indeed the recent results of Gorschlüter and Merz¹³ on d-d excitations in NiO(100) and CoO(100) are consistent with significant contributions from high-angle losses without elastic scattering.

Although higher order theories would modify the simple pattern outlined here, the Born-Ochkur model provides a good general guide to the angular distribution of electron exchange scattering for quasiatomic 3p-3d and 4d-4f excitations in transition metals and rare earths. Likewise, 4f - 4f transitions in rare earths and 3d - 3dtransitions in ionic transition-metal compounds should be reasonably well described provided $E_p \gg \Delta E$. Although Stoner excitations^{16,17} and $d \cdot d$ transitions in paramagnetic model systems¹⁸ are less quasiatomic and show marked bandlike character, the results presented here usefully complement the dielectric descriptions of spin-flip processes developed, for example, by Modesti et al.¹⁷ and Mills.¹⁹ It must, however, be emphasized that this simple model does not treat the behavior of the individual multiplet transitions and a more detailed theory would predict some differences in the variation of cross sections with energy and angle for different loss components, as is indeed observed by Matthew et al.³ and Kolaczkiewicz and Bauer et al.⁴ The pioneering calculations of Moser and Wendin²⁰ using the distorted-wave approximation



FIG. 3. The differential scattering cross section versus scattering angle for 4f-4f transitions in Gd at $E_p = 100$, 200, 300 eV.

predict L-S resolved results for La $4d \rightarrow 4f$ and $3d \rightarrow 4f$ transitions and Th $4d \rightarrow 5f$ and 4f - 5f transitions, but make no explicit spin-polarization predictions. Clearly such approaches provide a way forward for the problems investigated here, but the simple scaling patterns inherent in the Born-Ochkur approximation provide useful initial tests of spin-polarized loss data.

SUMMARY

The Born-Ochkur approximation is shown to give useful insights into exchange scattering in electron-energyloss spectroscopy in the reflection mode. Both the polarization induced in dipolar transitions and spin-flip transitions are much less forward scattering dominated than for nonexchange scattering and as a result experimental observations will include both single inelastic-scattering events and multiple-scattering events where low-angle inelastic scattering is combined with elastic scattering.

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