# Delocalization of the Fe 3d levels in the quasi-two-dimensional correlated insulator FePS<sub>3</sub>

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The degree of spatial localization of the Fe 3d levels in the quasi-two-dimensional correlated insulator iron phosphorus trisulphide (FePS<sub>3</sub>) is probed using resonant and angle-resolved photoemission in the range  $hv=40\sim65$  eV. Our results indicate that the 3d levels in this compound are not as localized as assumed by an existing ionic model. Spectra can be adequately fitted using an atomic multiplet theory for the  $3d^{n-1}$  final state modified by the presence of an octahedral ligand field. However, a relatively low Racah exchange parameter B = 0.075 eV is deduced and is interpreted in terms of greater hybridization with neighboring sulfur atoms than in iron oxides and halides. Resonant photoemission spectra collected near the iron M edge yielded excitation spectra composed of three prominent peaks approximately characterized by Fano line shapes. Systematic variation of the Fano asymmetry parameter q through the 3d multiplet is attributed to differential hybridization of various Fe 3d levels with sulfur 3d orbitals. Finally, we report angle-resolved photoemission results in the mirror symmetry planes, which indicate that some components of the 3d multiplet are substantially delocalized by band formation parallel to the layers. We summarize and discuss these results in terms of the covalency of this material.

### I. INTRODUCTION

The discovery of the high-temperature cuprate superconductors has lead to enormous scrutiny of materials that exhibit reduced dimensionality and have electronic structures in which electron correlation plays a significant role.<sup>1,2</sup>  $FePS_3$ , a prototypical member of the MPX<sub>3</sub> transition-metal phosphorus trichalcogenide series of compounds, bears qualitative similarity to the cuprates in these respects.<sup>3,4</sup> Similar to the cuprates and other systems having correlated electronic structures, an important issue in the  $MPX_3$  compounds concerns the degree of spatial localization of the 3d manifold. This in turn is determined by the relative importance of on-site correlation and exchange interactions, crystal-field splittings, and hybridization with neighboring atoms. Such materials are commonly modeled using simple phenomenological parameters-a correlation energy, a crystal-field parameter, and a hopping or charge-transfer integral, for example. These models mask much of the underlying complexity associated with quenching and/or delocalization of atomic multiplets. This paper presents the results of resonant photoemission (RESPES) and angle-resolved photoemission (ARP) studies of FePS<sub>3</sub> to probe the degree of localization of the 3d levels.

The  $MPX_3$  materials are structurally similar to the  $MX_2$  transition-metal dichalcogenide layered compounds and thus exhibit many quasi-two-dimensional (2D) behaviors.<sup>5</sup> One third of the  $MX_2$  metal atoms are replaced in the  $MPX_3$  compounds by phosphorous dimers. Each trilayer is composed of a covalently bonded hexagonal network of  $(P_2X_6)^{4-}$  ions intersecting a honeycomb of formally divalent  $M^{2+}$  ions. The transition-metal atoms are coordinated to six chalcogen atoms in distorted octahedral symmetry. Unlike the  $MX_2$  compounds where the one-electron approximation provides a reasonable zero-order description of electronic properties, the 3d transition-metal analogs of the  $MPX_3$  series are correlated antiferromagnetic insulators in their ground states.

An ionic model for the electronic structure of the MPX<sub>3</sub> compounds has been developed, largely through the work of Khumalo and Hughes,<sup>6</sup> and Piacentini et al.,<sup>7,8</sup> in which the 3d manifold remains localized and noninteracting. The dominant splittings of the 3d manifold involve the crystal field and multiplets formed by electron correlation. A simplified energy level diagram for FePS<sub>3</sub> is shown in the left part of Fig. 1. The atomic 3d level [panel (c)] is split by a global exchange energy U [panel (b)] and then the  $t_{2g}$  and  $e_g$  levels are further split by a crystal-field 10Dq estimated to be ~10 eV [panel (a)].<sup>9,10</sup> The trigonal distortion to  $D_{3d}$  symmetry further splits the  $t_{2g}$  levels into  $a_{1g}$  and  $e_g$  sets separated by 0.23 eV (not shown in Fig. 1).<sup>10</sup> Local moments on each metal center are weakly ferromagnetically or antiferromagnetically coupled to neighboring sites, leading in all known cases to antiferromagnetic ground states with Néel temperatures of 100-300 K.<sup>11</sup> This model, which successfully explained optical and soft x-ray absorption results,  $6^{-8, 12, 13}$  is consistent with the observed nearly integral magnetic moments on the transition-metal centers in the paramagnetic region, <sup>11,14,15</sup> and has provided useful insight into understanding the systematic variation in the ability of these compounds to intercalate alkali-metal atoms.<sup>14</sup> Lattice-dynamics calculations also suggest the importance of metal- $P_2X_6$  interactions.<sup>16</sup>

The ionic model is not adequate to explain other spectroscopic results, particularly the degree of mixing between transition metal 3*d* and anion ligand states and the structure of the lower conduction band of FePS<sub>3</sub> observed in inverse photoemission results.<sup>17</sup> Also, the 3*d* bandwidths of  $MX_2$  compounds are typically 0.5–1.0 eV, and this should not be dramatically smaller in the  $MPX_3$ compounds. Extended Hückel molecular-orbital calculations<sup>18, 19</sup> indicate significant mixing between M 3*d* and S



FIG. 1. Schematic representation of two simple models for the electronic structure of FePS<sub>3</sub>. Panel (c) represents the unsplit  $3d^6$  level. Moving left from this panel emphasizes electron exchange and correlation. Panels (b) and (a) add an on-site correlation energy U and the crystal-field interaction 10Dq, respectively. Hybridization is emphasized and correlation is neglected in the panels to the right of panel (c). The crystal field first splits the 3d manifold in panel (d), and strong  $e_g$ -S 3p hybridization further splits the  $e_g$  levels into bonding and antibonding sets in panel (e).

3p states. This mixing occurs preferentially with  $e_g$  levels since these are directed toward the octahedrally coordinated sulfur ligands. The dominant splitting in these calculations is thus associated with formation of bonding and antibonding Fe  $3d(e_g)$ -S 3p levels, as shown in panels (d) and (e) in Fig. 1, and electron correlation interactions are largely ignored.

It is likely that the true situation lies intermediate between these two models and that correlation, crystal field, and hybridization are all important. In principle, ab initio self-consistent band calculations can help clarify the situation. These order the 3d levels as in panel (a) of Fig. 1 with some additional width due to band formation, in qualitative support of an intermediate model.<sup>20,21</sup> In the calculations, preferential hybridization of the sulfur orbitals with the  $e_g$  relative to the  $t_{2g}$  levels is not readily apparent, since the ordering of the  $t_{2g}$  and  $e_g$  spin-down levels is not reversed due to formation of a strong Fe 3d $(e_g)$ -S 3p bonding level. These calculations were based upon the local-density approximation, and the application of this technique to such highly correlated systems is not without problems. For example, the calculated ground state of FePS<sub>3</sub> is metallic, in gross contradiction of experiment where a correlation gap of  $\sim 1.5$  eV is observed.9,22,23

The most direct probes of electronic structure, photoemission, and inverse photoemission have been usefully applied to try to elucidate the compounds' electronic structures.<sup>9,12,24</sup> Presence of a highly localized 3d shell normally will lead to RESPES at photon energies just above the threshold for 2p or 3p core excitation. This motivated one previous RESPES study and, indeed, some features were observed to resonate in intensity and were assigned to 3d levels and satellites.<sup>24</sup> While these results certainly imply some localized character, the delicate interplay between localized and delocalized effects were not seriously examined. To date, no ARP measurement of any  $MPX_3$  compound has been reported. The primary purpose of the present experiment was to undertake RESPES and ARP measurement of FePS<sub>3</sub> to examine this interplay in detail.

In the following sections, we report the photoemission spectra for  $FePS_3$  and determine the most appropriate model for this compound's electronic structure. We start

by relating our observed spectral features to the various iron-, sulfur-, and phosphorous-derived levels. The ironderived features in the spectra are then modeled in terms of the  $3d^{n-1}$  final-state ionization potentials and the Racah B and C parameters using the Tanabe-Sugano diagram.<sup>25</sup> We find that the spectra can be adequately fitted within this localized model, but that the Racah parameters are substantially smaller than for other more ionic iron compounds. This is consistent with a greater degree of hybridization in FePS<sub>3</sub>. Excitation spectra corresponding to the Fe 3d states, the satellites, and the sulfur 3p states are then presented and are decomposed into Fano resonance lines. Systematic variation of the Fano asymmetry parameter q indicates differential Fe 3d - S 3phybridization. We discuss the relationship between our excitation spectra and recent inverse photoemission (IP) spectra<sup>17</sup> as well as  $M_{2,3}$  absorption-edge spectra<sup>13</sup> to clarify the position of the empty 3d-derived valence states. Finally, we report the quasi-2D electronic structure of FePS<sub>1</sub> determined using ARP along the symmetry lines of the FePS<sub>3</sub> Brillouin zone at various photon energies to provide further information about the localization of the 3d levels. These results also are interpreted in terms of significant delocalization of part of the 3d multiplet. We conclude with a discussion of the covalency of FePS<sub>3</sub> and suggest useful ways to think about its electronic structure. Throughout this analysis, we compare the valence electronic structure and the covalency of FePS<sub>3</sub> to those of other ionic iron compounds to determine the relative extent of localization of the iron levels.

### **II. EXPERIMENTAL PROCEDURES**

The FePS<sub>3</sub> crystals were grown using the chemical vapor transport method<sup>26</sup> and were lustrous black, opaque plates of hexagonal shape. The samples were very flexible and much care was taken to avoid deformation upon mounting. A clean surface of FePS<sub>3</sub> was attained by cleaving *in situ*. In order to establish electrical contact, high purity silver paint (SPI Co.) was daubed between the crystal and sample holder. After curing at 150–180 °C for 30 min, electrical contact was examined and the edges of the crystal were trimmed so that the samples had an

approximately circular shape with a diameter of about 5 mm. The edge of the crystal was prone to bend after cleaving so that photoelectrons were hindered from exiting the surface uniformly. A small percentage of the cleaves provided enough flat space ( $\sim 1 \times 2 \text{ mm}^2$ ) with adequate electrical contact that photoemission experiments could be accomplished. After cleaving, the cleanliness and azimuthal orientation of the crystal were identified using Auger electron spectroscopy and lowenergy electron diffraction, respectively. The surfaces remained clean and ordered for several days in our vacuum system. In order to locate the position of the Fermi level and to investigate the reaction of the Fe 3d state with the adsorption of alkalis, potassium was dosed using a getter evaporation source (SAES, Inc.). It was dosed at room temperature and at a pressure of  $5.5 \sim 6.5 \times 10^{-10}$ torr. The high angular and energy resolution ARP experimental system has been described in detail previously.<sup>27,28</sup> Experiments were accomplished at the National Synchrotron Light Source at Brookhaven National Laboratory, using 6-m toroidal grating monochromator. The total energy and angular resolutions used here were typically less than 150 meV and 1°, respectively, at full width at half maximum.

### **III. RESULTS AND DISCUSSION**

Figure 2 provides normal emission energy distribution curves (EDC's) of  $FePS_3$  collected at a variety of photon



FIG. 2. Normal emission energy distribution curves of the valence bands of FePS<sub>3</sub> at several photon energies hv in the vicinity of the Fe 3*p* threshold energy. The different vertical lines correspond to the assignments after Ref. 24. Features D-G are discussed in more detail in Ref. 24.

energies near the 3p threshold. The intensities of all EDC's are normalized to the photon current. That little dispersion is observed in these features as a function of photon energy reflects the 2D character of these materials. The high-energy onset of the spectra [i.e., the valence-band maximum (VBM)], was located at a binding energy (BE) of ~1.5 eV relative to  $E_F$ . As is normally done in photoemission studies of traditional semiconductors, we measure the binding energies of various spectral features relative to the VBM.

#### A. Photoemission peak assignments

Our spectra are largely consistent with Piacentini's results,<sup>24</sup> albeit with slightly better definition of some features. Some small differences may be attributed to the different angular acceptance of their energy analyzer. Piacentini et al., assigned most features observed in the valence band by comparison to a calculated densities of states, and we adopt their assignments and lettering. The peaks  $A_1$ ,  $A_2$ , and  $A_3$  are similar to features on ionic iron oxides and chlorides<sup>29,30</sup> and are taken to be primarily derived from the final-state multiplet splitting of the Fe 3d states. Peaks B,  $C_1$ , and  $C_2$  are located where the sulfur and phosphorous 3p bonding manifolds are expected. However, the large intensity variation of the peak  $C_1$ is more characteristic of an Fe 3d-related feature. The ratio of the calculated atomic subshell photoionization cross sections is small  $(\sigma_{3p} / \sigma_{3d}) = 0.07 \sim 0.1)$  in the range of  $40 \sim 60 \text{ eV}$ , <sup>31</sup> so that the contribution of 3d electrons should dominate the EDC's. Piacentini et al. concluded that peak  $C_1$  is a satellite of the main lines.<sup>24</sup> We caution, however, that the significant energy dispersion of this feature reported in Sec. III C is contrary to this conclusion. Other sulfur and phosphorous levels are observed (but not shown) at higher binding energy, in accord with Piacentini's results.<sup>24</sup>

The P  $3p_z$  level primarily responsible for the covalent bonding of  $P_2$  dimer is not easily associated with features in any of our spectra. This level, which must play a crucial role in determining the structural stability of these phases, was suggested to lie at the top of the valence band in the ionic model.<sup>8</sup> In calculations,<sup>21</sup> however, the crystal-orbital overlap population curve for P - P shows that one peak among three P - P bonding levels is located in the region containing strong metal  $t_{2g}$  orbitals. In either case, emission from this feature would probably be masked by the more intense and overlapping Fe 3d features.

### 1. Fe 3d main lines and satellites

Distinct changes in the shape of the EDC's in Fig. 2 occur near the Fe 3p threshold at hv=55 eV. These arise from the resonance between the 3p inner shell excitation and the valence 3d- and 4s-shell excitations. Peaks  $A_3$ and  $C_1$  resonate in intensity most prominently relative to other peaks in the EDC's. The behavior of such features can be analyzed to provide additional information about the material's electronic structure, as discussed in Sec. III B. As discussed above, the peak  $C_1$  lies well below the VBM and is probably not associated with direct emission from a predominantly Fe 3d level since this would require a 3d bandwidth in excess of 10 eV. The 3d-related character in  $C_1$  must arise from another cause, i.e., multielectron shake up. Similar satellites were observed in x-ray photoemission spectroscopy (XPS) studies of the Ni 2p level in NiPS<sub>3</sub> located 5 and 10 eV below the main line.<sup>7,32</sup> The Fe 2p XPS spectrum of FePS<sub>3</sub> exhibits a broad and strong satellite at each spin-orbit component and the two main lines themselves appear quite asymmetric and broad.<sup>7</sup>

These kinds of satellites can be ascribed to either a multielectron excitation (shake up) process<sup>33</sup> or anion ligand-to-metal monopole charge-transfer transitions.<sup>34,35</sup> In the former process, the satellites are caused by simultaneous excitation of a second 3*d* electron to unoccupied 4*s*, 4*p*, or 3*d* levels upon photoemission. Charge-transfer transitions are often invoked to explain the observed satellites of the less ionic transition-metal oxides like NiO and CoO. Given the close proximity of the chalcogen levels and the low ionicity of the *MPX*<sub>3</sub> phases relative to, e.g., oxides and halides, we believe that this satellite is probably of the charge-transfer variety.

### 2. Multiplet splittings in the Fe 3d manifold

The qualitative analysis in the previous section begged the issue of the precise relationship between the spectral features in Fig. 2 and final state Fe 3d multiplet splittings. We now attempt to apply a relatively straightforward model to our spectra with the goal of achieving this relationship.<sup>36,37</sup> The model treats the iron centers to be isolated, yet subject to an octahedral crystal field characterized by the parameter 10Dq. We neglect the splitting of the  $t_{2g}$  manifold due to the small trigonal distortion, and the multiplet splittings of the  $e_g$  and  $t_{2g}$  manifolds are evaluated for the final state (i.e., Fe<sup>3+</sup>) in terms of the Racah B and C Coulomb and exchange parameters.

The direct photoionization of a 3d electron leaves an  $Fe^{3+}$  ion with a sextet ground state  ${}^{6}S({}^{6}A_{1g})$  and three lowest quartet excited states,  ${}^{4}G$ ,  ${}^{4}D$ ,  ${}^{4}P$ .  ${}^{38}$  In an octahedral field, the  ${}^{4}G$  state of the free ion splits into two threefold-degenerate states  ${}^{4}T_{1g}(t_{2g}^{4}e_{g}^{1})$  and  ${}^{4}T_{2g}(t_{2g}^{4}e_{g}^{1})$ , a doubly degenerate state  ${}^{4}E_{g}(t_{2g}^{3}e_{g}^{2})$ , and a nondegenerate state  ${}^{4}A_{1g}(t_{2g}^{3}e_{g}^{2})$ . The  ${}^{4}D$  state of the free ion splits into a doubly degenerate state  ${}^{4}E_{g}(t_{2g}^{3}e_{g}^{2})$  and a triply degenerate state  ${}^{4}T_{1g}(t_{2g}^{3}e_{g}^{2})$  and a triply degenerate state  ${}^{4}T_{1g}(t_{2g}^{3}e_{g}^{2})$  and a triply degenerate state  ${}^{4}T_{1g}(t_{2g}^{3}e_{g}^{2})$ . The photoemission selection rules allow final states to have the above symmetries in the  $3d^{5}$  high-spin configuration, and these states lie within the expected energy window of our experiment.<sup>38</sup> In the absence of any trigonal distortion, the levels  ${}^{4}A_{1g}$  and  ${}^{4}E_{g}$  are exactly degenerate. Although this degeneracy will be lifted by the trigonal distortion in FePS<sub>3</sub>, the magnitude of the splitting of 60 meV (Ref. 39) is so small that the separation was neglected. In addition, the  ${}^{4}E_{g}(t_{2g}^{3}e_{g}^{2})$  multiplet of  ${}^{4}D$  free-ion state was excluded from the final states since it is forbidden by the exclusion principle, at least for an octahedral crystal field.

In treating the data, smooth backgrounds were first subtracted from the raw EDC's. Thereafter the spectral feature B was removed from the curves by subtraction of a simple Lorentzian line. In this way, multiplets derived from iron 3d states and p-band structure (dotted lines in the top panel of Fig. 3) were approximately separated and could be modeled without consideration of atomic subshell cross-section variation. The decomposed multiplet structures extend  $5 \sim 6$  eV below the VBM, comparing well with a width of  $5 \sim 7$  eV ultraviolet photoemission spectroscopy studies of similar iron compounds.<sup>29,30,40</sup> Multiplet curves were considered to be composed of purely 3d final states and were fitted using the Tanabe-Sugano diagram.<sup>25</sup> The well-resolved peak around 1-eV BE spectra can be interpreted to be mainly the  ${}^{6}A_{10}$ ground state. The integrated intensity of this peak relative to that of the rest of the final states, i.e., sextet to quartet states, is 1:3.78, comparing well to the statistical ratio of 1:4.

The spectrum was fitted as Racah parameters and crystal-field parameter  $(10Dq, B, \gamma = C/B)$  were varied. The widths of all spectral features were fixed to the same value, and this value was also optimized in the fit. The relative intensities of the multiplets were fixed at statistical values. The resulting best fit of the spectrum at hv=40 eV is shown in the bottom panel of Fig. 3. The



FIG. 3. Energy distribution curve of FePS<sub>3</sub> at hv=40 eV. Upper panel: The two dotted lines correspond to the contribution of Fe 3d states and sulfur 3p band, while the dash-dotted line is an approximate background. The solid curve is the best fit to the spectrum. Bottom panel: Best fit to the Fe 3d multiplet using the model described in the text. The vertical lines show the calculated  $3d^{n-1}$  final-state ionization potentials and intensities for a crystal-field splitting 10Dq = 1.4 eV, Racah parameters B = 605 cm<sup>-1</sup>, and C = 2662 cm<sup>-1</sup>. Best fit is for a linewidth of 0.98 eV for each multiplet.

derived parameters,  $B = 605 \text{ cm}^{-1}$  (0.075 eV),  $\gamma = 4.4$ , and 10Dq = 1.4 eV, are all quite reasonable as compared to previous results on related systems. These parameters lead to the following set of final-state ionization potentials (energies in eV with respect to  ${}^{6}A_{1g}$  level):  ${}^{6}A_{1g} [\equiv 0$ eV],  ${}^{4}T_{1g} [1.27]$ ,  ${}^{4}T_{2g} [1.74]$ ,  ${}^{4}A_{1g} [2.4]$ ,  ${}^{4}E_{g} [2.4]$ ,  ${}^{4}T_{2g} [2.72]$ , and  ${}^{4}T_{1g} [3.49]$ . A linewidth of 0.98 eV for all multiplets gives the best fit to the spectrum.

Given that this is a simplistic model and also that there are obvious limitations with our treatment of the data (e.g., the background subtraction and removal of the spectral feature B), one should not place too much emphasis on the quantitative results given above. It is interesting, however, to compare the derived value of the Racah parameter B with that of other formally divalent iron oxide and halide compounds and the  $Fe^{3+}$  free-ion value. These are given in Table I. The value of the B parameter in  $FePS_3$  is 60% of  $Fe^{3+}$  free-ion value and is systematically smaller than that of other ionic iron compounds. A parameter  $\beta$  is often defined as the ratio of B in a compound to  $B_0$  in the free ion.<sup>41</sup> The  $\beta$  values, also given in Table I, decrease in magnitude successively. These observations suggest that a larger S 3p - Fe 3d hybridization exists in FePS<sub>3</sub>, since this would delocalize the 3d electrons and thereby reduce the associated Coulomb and exchange integrals. We thus conclude that the 3d orbitals in FePS<sub>3</sub> are less localized than these other formally  $Fe^{2+}$  compounds.

## **B.** Excitation spectra

Figure 4(b) presents excitation spectra, defined as the excitation-energy dependence of the photoemission intensity, for various structures in the EDC's in Fig. 2. The partial-yield spectrum, which represents the optical-absorption spectrum, is shown for comparison in Fig. 4(a).<sup>24</sup> The intensities in the spectra shown in Fig. 4(b) are obtained as the heights of each structure in the raw EDC's after subtracting smooth backgrounds represented by dotted line shown in Fig. 2. Undoubtedly, some errors arise from overlap of adjacent structures and uncertainty in the background subtraction. This is particularly true for features  $A_3$  and B. However, a careful decomposition of the overlapping band using a nonlinear fit to the EDC's could not be achieved without comparable uncertainty.

The five excitation spectra in Fig. 4(b) exhibit distinct similarities to the yield spectrum in Fig. 4(a) and also to recent IP spectra.<sup>17</sup> A subset of three prominent peaks

TABLE I. The Racah parameters *B* and *C*, their ratio  $\gamma$ , and the ratio of the Racah *B* parameter to the free-ion value ( $\beta$ ) for the octahedrally coordinated Fe<sup>3+</sup> ion in different compounds.

Fe <sup>3+</sup> in:	$B  (cm^{-1})$	$C \ (cm^{-1})$	γ	β	Ref.	
Free ion	1015	4800	4.73	1.0	38	
$Fe_xO$	913	4320	4.73	0.9	49	
	800	3737	4.67	0.78	40	
	629	2805	4.46	0.62	29	
FeCl <sub>2</sub>	661	2962	4.48	0.65	30	
FePS <sub>3</sub>	605	2662	4.4	0.6	present work	

 $(\gamma, \delta, \eta)$  above and two minor peaks  $(\alpha, \beta)$  below  $h\nu = 54$ eV is observed in each spectrum. Here we focus on the prominent peaks since these provide the most useful information and are the best-characterized in our spectra. Some of the excitation spectra do not exhibit all five peaks, and in some instances (e.g., the  $\gamma$  and  $\delta$  peaks for curve  $A_1$ ) the spectra show one broad peak ( $\gamma \delta$ ) instead of two. IP spectra of FePS<sub>3</sub>, which probe the unoccupied valence bands, exhibited two peaks, which were assigned to 3d states.<sup>17</sup> One was close to  $E_F$  and was assumed to have  $t_{2g}$  orbital symmetry and the other was about 2 eV higher and was assumed to have mixed  $e_{g}$  and S 3p character. These two peaks should correspond to the  $\gamma$  and  $\delta$ in our excitation spectra, and the separation of 2 eV in energy agrees very well with our results. The relationship of the third feature above threshold  $(\eta)$  to the inverse photoemission spectrum is not apparent. Given the analysis in the previous section, these features ought to be interpreted in terms of the multiplet structures for the  $d^{n+1} = d^7$  system since an electron has been added to the valence band. We have not attempted to undertake this analysis.

The resonance in the intensity of the satellite structure



FIG. 4. Bottom panel: Excitation spectra for the main structures in the energy distribution curves of  $FePS_3$  in Figs. 1 and 2. Notation is the same as in Fig. 2. For comparison we show the Fe 3*p* partial yield spectrum of  $FePS_3$  from Ref. 24 in the upper panel.

 $C_1$  in Fig. 2 is closely related to a Koster-Kronig or super-Koster-Kronig Auger transition following dipole excitation of a 3*p* core electron:  $3p^{6}3d^{N}\underline{nl}$  $\rightarrow 3p^{5}3d^{N}nl \rightarrow 3p^{6}3d^{N-1}nl + \in .^{42}$  This autoionization process interferes with the direct double excitation photoemission process  $(3p^{6}3d^{N}nl \rightarrow 3p^{6}3d^{N-1}nl + \epsilon)$  and hence the satellite peak is enhanced through a Fano-like process. The structures seen in the excitation spectra discussed later show asymmetric line shapes and are explained by the Fano line shape induced by this interference effect. We also note that an  $M_{2,3}$  VV Auger peak having the same final state as the super-Koster-Kronig transition could not be detected in the valence band near or above the resonant photon energy. This result contradicts the mode by Dietz et al.<sup>43</sup> for elemental transition metals that the resonance of the satellite is generally enhanced due to the overlap with the Auger emission. It does, however, coincide with the fact that  $M_{2,3}$  VV Auger emission is absent in most insulating transition-metal compounds.44

In order to model these excitation spectra from first principles, we would need to calculate the line-shape function and the ratio of transition moments of a 3p electron to  $e_g$  versus  $t_{2g}$  orbitals. The difficulty of this approach leads us to analyze the excitation spectra in Fig. 4(b) in terms of phenomenological Fano interactions. According to Davis and Feldkamp,<sup>42</sup> the excitation spectra can be expressed as

$$N(\varepsilon) = A(\varepsilon) + \sum_{j} K_{j} f_{j}(\varepsilon) .$$
 (1)

Here,  $\varepsilon$  represents the normalized excitation energy and  $A(\varepsilon)$  is a smoothly varying background. The second term is the resonant part where  $K_j$  is the amplitude and  $f_j(\varepsilon)$  is the line shape of resonance line. The analytical form of function  $f_j(\varepsilon)$  cannot be easily determined, but the physical origin of some structures observed in x-ray absorption<sup>45</sup> and excitation spectra<sup>46</sup> for the transition-metal compounds have been related to Fano interaction phenomena. The Fano-type interaction produces a spectral line with its typical resonance and antiresonance features for energies above and below the resonance, and is expressed by the following functional form:

$$f_j(\varepsilon) = \frac{(\varepsilon + q_j)^2}{(\varepsilon^2 + 1)^2} , \qquad (2)$$

where

$$\varepsilon = (hv - hv_i) / \Gamma_i . \tag{3}$$

In these formulas,  $hv_j$  is the resonance energy for transition j,  $\Gamma_j$  is the spectral half-width of the autoionized state, and  $q_j$  is the asymmetry parameter, respectively. We have fitted our excitation spectra to Eq. (1). We assume the background is constant and a constant q value is used for each spectral feature. Features in each excitation spectrum are extracted and labeled by different  $hv_j$ and  $\Gamma_j$ . The result of this fitting procedure for the case of  $A_3$  is shown in Fig. 5.

The Fano line parameters for the prominent excita-



FIG. 5. Decomposition of the  $A_3$  excitation spectrum of FePS<sub>3</sub> near the Fe 3*p* threshold. Curve *A* is the excitation spectrum as measured. The solid curves at the bottom represent the Fano line shapes and a small background, as discussed in the text. Curve *A* is the sum of these curves and indicates the quality of the fit to the spectrum.

tions and the main spectral features are tabulated in Table II. While the resonant energies of the peaks  $\gamma$  and  $\delta$  are fairly consistent, there is measurable discrepancy for  $\eta$ . This difference may be due to ambiguities in the background subtraction as well as to errors caused by not using the integrated intensities for each peak. The most relevant comparison is among the q parameters for the nearly pure and well-resolved Fe 3d feature  $A_1$ , the over-

TABLE II. Parameters representing the Fano line shapes obtained by fitting the excitation spectra in Fig. 4. Capital letters correspond to a subset of the peaks in Fig. 2, while Greek letters indicate the prominent peaks in each excitation spectrum.

FePS <sub>3</sub>							
		q	<u>Г</u>	h v <sub>i</sub>	R		
$A_1$	γδ	1.01	1.13	54.88	2.02		
	η		1.06	59.95	2.02		
<i>A</i> <sub>2</sub>	Ŷ	1.33	0.34	54.45	1.12		
	δ		0.86	56.20	1.52		
<i>A</i> <sub>3</sub>	η		0.60	60.89	1.39		
	β	1.44	2.08	51.56	2.40		
	γ		0.76	54.48	2.54		
	δ		0.66	56.54	2.57		
	η		0.95	60.34	2.05		
B	β	1.46	0.94	52.59	2.87		
	Ŷ		0.39	54.71	2.98		
	δ		1.00	56.42	3.00		
	η		1.71	59.73	2.80		
<i>C</i> <sub><i>i</i></sub>	δ	2.80	1.32	56.33	4.75		
	η		0.47	60.33	3.77		

lapping Fe 3d, S 3p features  $(A_3+B)$ , and the satellite  $C_1$ . Table II indicates that the q value is larger for the last of these and smallest for the first. This observation can be reasoned qualitatively by the involving hybridization effects. In fact, Kakizaki *et al.*,<sup>46</sup> applied this interpretation to transition-metal chlorides such as FeCl<sub>2</sub>, NiCl<sub>2</sub>, and MnCl<sub>2</sub>. In Eq. (2), the q parameter is given, in the absence of hybridization, as

$$q = \frac{\langle 3p|r|3d \rangle}{\pi V_E \langle \varepsilon l|r|3d \rangle} , \qquad (4)$$

where  $|\varepsilon l\rangle$  is the basis function of the unbound electron, r indicates dipole matrix element, and  $V_E$  is the Auger matrix element for autoionization process. Imagine that one sharp state in the multiplet is composed of the hybridization of one Fe 3d state and one S 3p. Then<sup>46</sup>

$$\Psi \approx \frac{1}{(a^2 + b^2)} (a|d\rangle + b|L\rangle) , \qquad (5)$$

where  $|d\rangle$  is one of Fe 3d orbitals  $(e_g, t_{2g})$  and  $|L\rangle$  is a sulfur S 3p ligand orbital combination. If this wavefunction form in Eq. (5) is inserted in Eq. (4), the resulting q value is approximately

$$q' = q(1+\gamma) , \qquad (6)$$

where the covalency parameter  $\gamma$  is defined as  $\gamma = b^2/a^2$ and is related to the magnitude of hybridization, but does not represent exactly the degree of covalency. Equation (6) predicts that the q' value should become larger as hybridization increases. The greater q value for the satellite structure than for those derived for Fe 3d levels can be also attributed to an increase in the covalency parameter by the inner-core-hole-induced covalency, as discussed previously.<sup>47</sup>

Once again this is a simplistic model and there are obvious limitations with our treatment of the data. Any quantitative conclusions should be viewed with some suspicion. Nonetheless, we find additional qualitative evidence for Fe 3d - S 3p hybridization, that is, the 3d orbitals are not so localized as implied by the ionic model. More importantly, this hybridization appears to be different for the different 3d-related features. We will return to these issues after presenting and discussing ARP results for this compound.

## C. ARP studies

The most direct probe of spatial delocalization of the Fe 3d orbitals in FePS<sub>3</sub> is to search for energy dispersion associated with band formation. For this reason we have measured ARP spectra, a sampling of which is shown in Figs. 6(a) and 6(b). FePS<sub>3</sub> adopts a monoclinic crystal structure, but the structure of each layer is hexagonal, with two metal atoms per unit cell in a honeycomb lattice. The spectra in Fig. 6 were collected at momenta along the symmetry lines of this hexagonal unit cell, as shown in the inset in Fig. 6(a). The dimensions of this 2D Brillouin zone (BZ) are 0.703 and 0.608 Å<sup>-1</sup> along  $\Gamma A$  and  $\Gamma Y$ , respectively. The vertical curves through the spectra indicate the dispersion of the primary spectral

features  $A_1$ ,  $A_2$ ,  $A_3$ , B, and  $C_1$ . A summary of the derived dispersion relations is given in Fig. 7.

The Fe 3d features exhibit different dispersive behaviors. The highest lying feature  $A_1$  is clearly visible in all spectra and exhibits small dispersion (<0.2 eV)throughout the BZ. Feature  $A_2$  also shows little measurable dispersion, although it can be clearly observed only over a narrow range of momenta near the center of the BZ. The primary reason for this is that the more intense feature  $A_3$  exhibits pronounced upward dispersion by nearly 1 eV away from normal emission in both azimuthal directions. The feature labeled  $C_1$  also disperses upward in energy away from zone center and appears to track the energy of feature  $A_3$ . That is, there is a roughly constant energy difference of  $4.6\pm0.2$  eV between these two features in all spectra. The observed dispersion of feature  $C_1$  contradicts its assignment as a satellite in Sec. III A. The simultaneous observation of a resonance, which implies main-line bandlike character, is an enigma



FIG. 6. ARP spectra of FePS<sub>3</sub> collected at hv=56 eV at emission angles in the (a)  $\Gamma$ -A-Y and (b)  $\Gamma$ -Y- $\Gamma$  directions of the quasihexagonal Brillouin zone. This zone is shown schematically in the inset in panel (a). The wave vectors given are for electrons emitted near the VBM. The vertical lines are included to indicate the dispersion of the primary spectral features.



FIG. 6. (Continued).

that emphasizes the subtle interplay between localized and delocalized phenomena in this compound. A possible explanation is that feature  $C_1$  is actually composed of two features, one of a nondispersive satellite and the other dispersive phosphorous-sulfur band. However, the satellite intensity should be independent of momentum and



FePS<sub>3</sub> Energy Bands

FIG. 7. Summary of the dispersion relations for the primary spectral features in Fig. 6. Bands are labeled as in Fig. 2.

one should then presumably see a doubled feature at momenta near the zone boundary. Instead, one sees a single feature with a slowly declining intensity away from zone center.

We make one further observation about feature  $A_1$ . In several spectra this feature appears asymmetric. This results from the overlap of more than one peak, as indicated in Fig. 8. This shows a high-resolution spectrum collected at normal emission at hv = 56 eV where the asymmetry is most pronounced and two peaks are clearly resolved. There are several possible explanations for this doubling. From the perspective of atomic multiplet theory, it could result from splitting of the  ${}^{6}A_{1g}$  multiplet by the deviation from octahedral to trigonal symmetry. The observed magnitude of the splitting (0.2 eV) is in good accord with optical measurements.<sup>10</sup> An alternative explanation is based upon the fact that there are two iron atoms per geometric unit cell and more than two for the magnetic unit cell. In terms of hybridization and band formation, one thus naturally expects splitting of the iron-derived bands into bonding and antibonding combinations. Finally, in the phenomenological theories discussed in the Introduction and further in Sec. IV, the splitting could be attributed to a separate 3d component produced by crystal-field and exchange splittings. Unfortunately, the splitting was most apparent over a narrow range of momenta and a systematic study was not possible.

# IV. DELOCALIZATION OF THE 3d ORBITALS IN FePS<sub>3</sub>

# A. Initial and final states

The discussion in Secs. III A and III B implies some level of applicability of a localized model for the Fe 3d



FIG. 8. High-resolution spectrum of the Fe 3*d*-derived feature  $A_1$  near the VBM collected at normal emission and a photon energy of 56 eV. Note the presence of two well-resolved peaks in this feature.

levels in FePS<sub>3</sub> since the spectra are adequately reproduced using atomic multiplet theory and the observation of **RESPES** is closely related to atomic autoionization. Thus it is tempting to relate the three predominantly Fe 3d spectral features  $A_1$ ,  $A_2$ , and  $A_3$  to the three lowest levels on the left part of Fig. 1, that is, to  $t_{2g}(\downarrow)$ ,  $e_g(\uparrow)$ , and  $t_{2g}(\uparrow)$ , respectively. In the ground state, which is calculated from first principles, associations like this may have some validity. However, the discussion of Sec. III A 2 indicates that this is not really a valid assignment of the photoemission spectra. The spectral features should be considered to arise from the final state  $3d^{n-1}$ multiplets, as shown in Fig. 3. In the presence of large on-site correlation and exchange energies, the  $t_{2g}$  and  $e_g$ designations may not be very useful since combinations of these orbitals form each multiplet.

It is useful to try to forge a connection between phenomenological ground-state labels like  $t_{2g}(\downarrow)$  and finalstate multiplets. In the case of  $t_{2g}(\downarrow)$  there is an obvious connection. When the  $t_{2g}(\downarrow)$  electron is photoemitted from the left panel in Fig. 1, the final state is the high spin  $d^5$  configuration and this is simply the  ${}^6A_{1g}$  multiplet as shown in Fig. 3. In the same way, the  $e_g(\uparrow)$ ground state maps into the  ${}^4A_{1g}$ , the  ${}^4T_{2g}$ , and the  ${}^4T_{1g}$ final-state multiplets. These are the three lowest energy multiplets after the  ${}^6A_{1g}$  ground state. Finally, the higher energy  ${}^4T_{1g}$  and  ${}^4T_{2g}$  multiplets are associated with emission from the  $t_{2g}(\uparrow)$  state. In this way, we see that the left panel in Fig. 1 apparently can maintain some validity in interpreting the photoemission spectra.

#### B. Limitations of the localized model

The above description does not argue against the local model, but it does suggest redefinition of terminology. However, we distinguish five pieces of evidence that indicate the limitations of the ionic model.

(a) The finite Néel temperatures for  $\text{FePS}_3$  and other  $MPX_3$  compounds implies that intersite exchange interactions are small but not negligible. It is not clear whether the magnetic interactions are direct or indirect (i.e., superexchange). However, they imply significant hybridization of some sort.

(b) The calculated valence of FePS<sub>3</sub>,<sup>21</sup> which matches the experimentally observed magnetic structure,<sup>14</sup> is  $Fe^{0.95+}P^{1.47+}S_1^{0.70-}(S_2^{0.86-})_2$  (S<sub>1</sub> ion has no spin polarization, while S<sub>2</sub> does). The calculated self-consistent Mulliken's charges thus deviate substantially from the ionic model  $M_2^{2+}$  (P<sub>2</sub>S<sub>6</sub>)<sup>4-</sup>.

(c) The Racah B and C parameters are smaller than for other more ionic iron compounds. The degree of covalency between Fe 3d and ligand p orbitals cannot be precisely determined. However, a larger degree of covalency in FePS<sub>3</sub> compared to iron compounds having more electronegative ligands would imply that the mean radial displacement of the Fe 3d electrons and thus the overall ionic size would increase. This will naturally decrease the Racah B and C parameters, which are governed by interelectron repulsion. In other words, a decrease in B and C is explicitly connected to delocalization of the 3d orbitals. (d) The Fano asymmetry parameters vary systematically through the 3d manifold. This can be described in terms of hybridization of the multiplets with anion 3p orbitals and thus in terms of 3d delocalization.

(e) Significant dispersion is observed in the lowest of the Fe 3d features,  $A_3$ . This can only result through hybridization with neighboring ligands, or possibly with neighboring iron atoms. The overall bandwidth of roughly 1 eV is comparable to the multiplet splittings, which in turn are related to the phenomenological on-site correlation energy U.

Unlike the first three arguments, which do not inherently distinguish the localization of one 3d level from another and thus relate to "central-field covalency," the differential interaction implied by the last two is of relevance to "symmetry-restricted covalency." This was the primary conclusion of the extended Hückel calculations, i.e., that the interaction between the  $e_g$  orbitals and the sulfur ligands was large, while the  $t_{2g}$  orbitals remained nonbonding.<sup>18,19</sup> The different overlap between the  $t_{2g}$  and  $e_g$  orbitals with ligands will cause differential d-electron delocalization effects and hence possibly different effective Racah parameters for the different symmetry 3d orbitals.<sup>41</sup> These two covalency mechanisms are summarized to the nephelauxetic effect<sup>48</sup> which increases as  $(1-\beta)$  increases in Table I. There is a close parallel between the nephelauxetic effect and Pauling's electronegativities. As the electronegativity of O, Cl, and S atoms decrease in sequence, the nephelauxetic effect increases.

#### C. Models for the electronic structure of FePS<sub>3</sub>

We are left with a fairly complicated situation in which all interactions-the on-site correlation energy, the crystal-field interaction, multiplet splittings, and the bandwidth-are of comparable magnitude. More precisely, the interplay between these depends sensitively upon the 3d-derived feature being considered. It is probably a good approximation to consider  $A_1$  to be the  $t_{2g}(\downarrow)$  level or  ${}^{6}A_{1g}$  multiplet, perhaps split by the trigonal distortion. This assignment is valid since the band exhibits a bandwidth that is small compared to multiplet and crystal-field splittings. For this reason, the local model will adequately represent this feature. Given that  $A_3$  is the most dispersive feature, it is natural, based upon symmetry-restricted covalency, to associate it with a hybrid band formed between the  $e_g(\uparrow)$  and S 3p orbitals. This assignment is more problematic since the observed bandwidth for  $A_3$  is comparable to the multiplet splittings and thus an assignment in terms of a particular local orbital is dubious. All multiplets contain some  $e_g$ character, and the concept of symmetry-restricted covalency may not be useful in this circumstance. By default,  $A_2$  is assigned to the  $t_{2g}(\uparrow)$  band and is apparently fairly localized, as expected based upon symmetry and as evidenced by its on dispersive nature. This model thus inverts the ordering of the  $t_{2g}(\uparrow)$  and  $e_g(\uparrow)$  orbitals in the left panel of Fig. 1. The fit in Fig. 3, coupled to the correlation between these orbitals and their final-state

multiplets discussed in Sec. IV A implies that this assignment is not valid.

These complications suggest consideration of different models for the electronic structure of FePS<sub>3</sub>. It is useful to consider a purely energetic mechanism to explain the different degrees of localization in the 3d manifold. The electronic structure of FePS<sub>3</sub> can be considered to combine a strongly bonded P, S 3p manifold having a gap  $\sim$  3 eV in magnitude with quasilocalized Fe 3d levels in and near the gap. The degree of localization of a particular multiplet will depend on its position in the gap: those far from the band edges (e.g.,  $A_1$ ) will be highly localized, while those close to the band edges or even outside the gap (e.g.,  $A_3$ ) will interact more strongly. This makes sense from a molecular orbital point of view because levels that are widely separated in energy generally mix less strongly than those that are nearly degenerate. This argument correctly predicts the qualitative observation that  $A_3$  shows significant dispersion while  $A_1$  and  $A_2$  do not.

The above comments provide insight into the best way to think qualitatively about the electronic structure of these interesting, quasi-2D materials. They also indicate

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possible directions for future attempts to model their electronic structures. For example, in future calculations it would make sense to construct a basis set for the 3d levels starting from atomic multiplets, the splitting of which is governed by Racah parameters. The primary difficulty in such an approach is that the importance of the correlation interactions should be measured against solid-state hybridization effects, which apparently are very different for the different multiplets.

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