# Jahn-Teller mechanism of the half width of the intramolecular vibrational spectrum in doped  $\mathbf{C}_{60}$ : Coupling with  $H_g$ ,  $T_{1u}$ , and  $H_u$  mode

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We have studied the half width of the intramolecular vibrational spectrum of the nonadiabatic electron intramolecular vibration (e-MV) coupling origin in doped  $C_{60}$ . We have also estimated the half width of the adiabatic e-MV coupling origin. We found that along with the two e-MV couplings with  $H<sub>e</sub>$ modes, there are some modes with  $H_u$  and  $T_{1u}$  symmetries that couple with conduction electrons and may have non-negligible phonon widths. This mainly comes from a local symmetry reduction due to the Jahn-Teller distortion. The theoretical results agree with previous experimental results with  $H<sub>g</sub>$  modes and may agree qualitatively with recent experimental findings for the  $H_u$  and  $T_{1u}$  modes. Our e-MV theory based on Jahn-Teller effects explains most of the experimental observations related to the half width of the phonon spectrum in doped  $C_{60}$ . We predict a doping-induced structure for the highest frequency  $H<sub>g</sub>$  mode, which comes from the large coupling constants of both the adiabatic and the nonadiabatic e-MV mode coupling.

#### I. INTRODUCTION

The superconductivity found in  $A_x C_{60}$  has stimulated studies of electron intramolecular vibration (e-MV) couplings in solids.<sup>1</sup> Among them, intramolecular Jahn-Teller (JT) effects have received much attention.<sup>2,3</sup> Inelastic neutron scattering measurements<sup>4,5</sup> and Raman scattering measurements<sup>6,7</sup> supplied important informa tion about e-MV coupling strengths. These measurements showed that the low-frequency tangential  $H<sub>g</sub>$ modes contribute about as much as the higher-frequency radial  $H<sub>g</sub>$  mode. This tendency agrees with some of the common features of previous theoretical results, $8-11$ which were obtained using different theoretical methods.<br>Besides these results, the <sup>13</sup>C isotope effect on  $T_c$ , measured by some groups, supports the idea that there are large contributions of phonons in the mechanism of superconductivity. $12-16$  These results put constraints on some models, which rely entirely on hypothetical magnetic fluctuation in doped  $C_{60}$ .<sup>17</sup> Recent photoemission results exclude the possibility of the formation of the pseudogap in  $K_3C_{60}$ . <sup>18</sup> The other important experimental results obtained recently are the giant vibrational resonance of  $T_{1u}$  modes found in optical measurements<sup>19,20</sup> and the broadenings of  $H_u$  and  $T_{1u}$  modes upon doping found in an inelastic neutron scattering experiment.<sup>21</sup> The gian vibrational resonance was studied phenomenologically by Rice and Choi.<sup>22</sup> We report here that our  $e$ -MV theory including both the adiabatic and the nonadiabatic  $e$ -MV couplings<sup>10</sup> explains experimental observations related to phonon spectrum broadenings qualitatively and that the broadenings observed with some  $H_u$  and  $T_{1u}$  modes may originate entirely from the JT mechanism.

In Sec. II we show rigorously the existence of the nonadiabatic e-MV coupling term. In doped  $C_{60}$  the nonadiabatic e-MV coupling term gives leading contributions to the noadiabatic correction to the phonon self-energy than that from higher-order terms with the adiabatic e-MV coupling beyond the Migdal approximation. In Sec. III we present formulas of the lowest-order phonon selfenergy and half width of the phonon spectrum of a nonadiabatic e-MV origin. In Sec. IV we estimate the width of the  $H_{g}$ ,  $A_{g}$ ,  $H_{u}$ ,  $T_{1u}$ , and  $A_{u}$  modes of doped  $C_{60}$  with both the adiabatic and the nonadiabatic e-MV coupling terms.

#### II. NONADIABATIC e-MV COUPLING TERM

We show rigorously that there exists a nonadiabatic e-MV coupling correction term to the Born-Oppenheimer (BO) adiabatic approximation. In the most rigorous meaning, the correction term cannot be neglected when one uses the BO adiabatic electronic wave function. We may expect that the nonadiabatic e-MV coupling coefficients may be small enough to be neglected in many materials; however, these coefficients are large in doped  $C_{60}$  and they cannot be neglected.

We start with the following molecular Hamiltonian:

$$
H = \frac{p^2}{M} + V(q) + \int a^+(1)h(1,q)a(1)d(1)
$$
  
+ 
$$
\frac{1}{2} \int \int a^+(1)a^+(2) \frac{e^2}{r_{12}} a(2)a(1)d(1)d(2), \qquad (1)
$$

where  $q$ ,  $p$ , and  $M$  are the normal coordinates of molecular vibration, nuclear momentum, and nuclear mass, respectively. The variables <sup>1</sup> and 2 denote the coordinates of the electrons including the spin variables.  $h(1,q)$ denotes the one-body term for the electrons and  $e^2/r_{12}$ denotes Coulomb repulsion between them. The annihilation operator  $a(1)$  is defined as  $a(1)=\sum_j \psi_j(1;q)c_j$ , where  $c_i$  is the annihilation operator for electrons with orthonormalized molecular orbitals  $\psi_i$ . It should be noted that  $\psi$  depends on q parametrically. As nuclei and electrons

are independent particles, we need the following commu-<br>  $\int X(1,2)\psi_k(2)d(2) = \frac{\partial}{\partial q}\psi_k(1)$ ,<br>  $\int X(1,2)\psi_k(2)d(2) = \frac{\partial}{\partial q}\psi_k(1)$ 

$$
[p, a] = 0 \tag{2}
$$

The parametric dependence of  $\psi$  on q due to the BO adiabatic approximation does not allow  $p$  and  $c_i$  to commute:

$$
[p,c_j] = -i \sum_i \left\langle \frac{\partial}{\partial q} \psi_j \middle| \psi_i \right\rangle c_i \tag{3}
$$

This noncommutation relation makes calculations in the nonadiabatic problem very complicated. We can remedy this difficulty by introducing the function

$$
X(1,2) \equiv \sum_{k} \frac{\partial}{\partial q} \psi_k(1) \psi_k^*(2)
$$
 (4)

and the recoil momentum operator following Fukutome: $^{23}$ 

$$
\pi \equiv -i \int \int a^{+}(1)X(1,2)a(2)d(1)d(2).
$$
 (5)

With the help of the relations

$$
\int X(1,2)\psi_k(2)d(2) = \frac{\partial}{\partial q}\psi_k(1) , \qquad (6a)
$$

$$
\int \psi_k^*(1)X(1,2)d(1) = -\frac{\partial}{\partial q}\psi_l^*(2) , \qquad (6b)
$$

we find the following relation to hold:

$$
[\pi, c_j] = [p, c_j] \tag{7}
$$

If we define a new nuclear momentum  $P$  by

$$
P \equiv p - \pi \; , \tag{8}
$$

we then observe that

$$
[P,c_j]=0\tag{9}
$$

and the commutation relation for  $P$  and  $q$  is preserved. Now we have a set of canonical variables which have desirable communication relations. With the new nuclear momentum P, the molecular Hamiltonian given by Eq. (1) is rewritten as follows:

$$
H = \frac{P^2}{M} + V(q) + \sum_{ij} \langle \psi_i | h | \psi_j \rangle c_i^{\dagger} c_j + \frac{1}{2} \sum_{ijkl} (\left[i | jk \right] - \left\{ i | jk \right\} ) c_i^{\dagger} c_j^{\dagger} c_k c_l + \frac{1}{2} \sum_{ij} i \langle \psi_i | \frac{\partial}{\partial Q} \psi_j \rangle c_i^{\dagger} c_j i \sqrt{\omega/2} (b - b^{\dagger})
$$
  

$$
- \frac{1}{2} \sum_{ij} \left| \langle \frac{\partial}{\partial Q} \psi_i | \frac{\partial}{\partial Q} \psi_j \rangle + \langle \psi_i | \frac{\partial^2}{\partial Q^2} \psi_j \rangle \right| c_i^{\dagger} c_j , \qquad (10a)
$$

$$
[ij|kl] = \int \int \psi_i^*(1)\psi_j^*(2)\frac{e^2}{r_{12}}\psi_k(2)\psi_l(2)d(1)d(2) ,
$$
\n(10b)

$$
\{ij|kl\} = \left\langle \psi_i \left| \frac{\partial}{\partial Q} \psi_l \right\rangle \left\langle \frac{\partial}{\partial Q} \psi_k \right| \psi_j \right\rangle, \tag{10c}
$$

where  $Q$  is the mass-weighted normal coordinate defined where  $Q$  is the mass-weighted normal coordinate define<br>by  $Q = \sqrt{M}q$  and  $\omega$  is the molecular vibrational frequen cy. Equation (10) is the most convenient Hamiltonian to start the nonadiabatic e-MV problem. If one tries to use Eq. (1), one has to deal with the noncommutability of  $p$ and  $c_i$  as shown in Eq. (3). In the adiabatic limit, where the parametric dependence of  $\psi$  on q or Q can be neglected, we may suppose the approximate commutability between  $p$  and  $c_i$  and neglect terms in the second and third lines of Eq. (10a). In doped  $C_{60}$ , we observe, with the help of quantum chemistry, that quantities such as  $\langle \psi_i | (\partial/\partial Q) \psi_i \rangle$  can never be negligible, i.e., doped C<sub>60</sub> is a Jahn-Teller system. On the basis of these arguments, doped  $C_{60}$  may be best described by the following model Hamiltonian:

$$
H = H_0 + H_1 \t\t(11a)
$$

$$
H_1 = H_{11} + H_{12} \t\t(11b)
$$

$$
H_0 = \sum_{i=1}^n \epsilon_l^i n_l^i + \sum_{i}^n \sum_{l \neq m, \sigma} t_{lm}^i c_{il\sigma}^{\dagger} c_{im\sigma} + \sum_l \omega_l (b_l^{\dagger} b_l + \frac{1}{2}) ,
$$
\n(11c)

$$
H_{11} = \sum_{i}^{n} \sum_{l} g_{l}^{i} n_{l}^{i} (b_{l} + b_{l}^{\dagger}) , \qquad (11d)
$$

$$
H_{12} = \sum_{\langle ij \rangle} \sum_{l\sigma} \left\{ i\kappa_{l\sigma}^{ij} c_{il\sigma}^{\dagger} c_{jl\sigma}^{\dagger} (b_l - b_l^{\dagger}) + \text{H.c.} \right\} , \qquad (11e)
$$

where  $c_{il\sigma}^{\dagger}$  and  $b_l^{\dagger}$  are creation operators for electrons with spin  $\sigma$  on the *l*th site of the *i*th band and of molecular vibrational bosons on the *l*th site, respectively.  $\epsilon_l^i$ ,  $t_m^i$ ,  $g_i^i$ , and  $\kappa_i^{ij}$  are the site energy of the *i*th band, the transfer integral of the ith band, the adiabatic e-NV coupling constant of the ith band, and the nonadiabatic e-MV coupling constant between the *i*th and *j*th bands, respectively.  $H_{11}$  and  $H_{12}$  are the adiabatic and the nonadiabatic  $e-MV$  couplings.<sup>10</sup> We have used a Taylor expansion with respect to  $Q$  to take into account the site energy modulation effect by the phonon. The adiabatic e-MV coupling term comes from this efFect and is called Holstein coupling. $24$  Long-range interactions such as the long-range transfer interaction are neglected on the basis of the strong molecularity of  $C_{60}$ . We have estimated g and  $\kappa_l^{ij}$  of  $C_{60}^-$  and found that these are comparable in magnitude of order 0.01.<sup>10</sup> The higher-order correction to the lowest-order phonon self-energy with the adiabatic e-MV coupling  $H_{11}$  is of the order of  $g<sup>4</sup>$ . The cross term

contribution to the phonon self-energy between the adiabatic e-MV coupling term  $H_{11}$  and the nonadiabatic e-MV coupling term  $H_{12}$  is of the order of  $g^2 \kappa^2$ .

We neglect these higher-order contributions expecting that the integral associated with the vertex correction to the lowest-order phonon self-energy is not singular (Migdal approximation).<sup>25,26</sup> If the expectation is valid or not depends on the actual values of the parameters and it is very difficult to know if the approximation works or not in doped C<sub>60</sub>. With the Fermi energy  $\epsilon_F=0.9$  eV and the partial density of state of each  $t_{1u}$  band  $N(0)=2.5$ states/eV  $C_{60}^-$  per spin, we may neglect the higher-order corrections. Justifications should be looked at for comparisons with the calculated results and experiments. The bottom line is that there is the lowest-order phonon self-energy with a novel nonadiabatic e-MV coupling whose prefactor is over  $10<sup>4</sup>$  larger than that of the higher-order corrections which have been believed to

play an exclusive role in the nonadiabatic effects so far. The effect of the nonadiabatic e-MV coupling has not been understood yet and we think it worthwhile to start with the lowest-order contributions. The lowest-order contribution from the nonadiabatic e-MV coupling is independent of the singularity of the integral associated with the vertex correction.

# III. LOWEST-ORDER PHONON SELF-ENERGY WITH NONADIABATIC e-MV COUPLING

We derive formulas of the lowest-order phonon selfenergy and the half width of the phonon spectrum with the nonadiabatic e-MV coupling term by use of the standard Feynman diagrammatic technique.<sup>27-29</sup> We define the adiabatic and the nonadiabatic phonon finite temperature Green's functions as follows:

$$
D_q^{\text{ad}}[\tau,\tau'] = -\left\langle TU_{\text{ad}}(\beta)u_q(\tau)u_{-q}(\tau')\right\rangle_0,\tag{12a}
$$

$$
D_q^{\text{nonad}}[\tau,\tau'] = -\langle TU_{\text{nonad}}(\beta)\phi_q(\tau)\phi_{-q}(\tau')\rangle_0,
$$
\n(12b)

$$
U_{\rm ad}(\beta) = 1 + \sum_{n=1}^{\infty} (-1)^n \int_0^{\beta} du_1 \int_0^{u_1} du_2 \cdots \int_0^{u_{n-1}} H_{11}(u_1) \cdots H_{11}(u_n) du_n , \qquad (12c)
$$

$$
U_{\text{nonad}}(\beta) = 1 + \sum_{n=1}^{\infty} (-1)^n \int_0^{\beta} du_1 \int_0^{u_1} du_2 \cdots \int_0^{u_n-1} H_{12}(u_1) \cdots H_{12}(u_n) du_n , \qquad (12d)
$$

where  $\langle \cdots \rangle_0 = \text{Tr}(\cdots e^{-\beta H_0}) / \text{Tr}(e^{-\beta H_0}), \qquad u_q(\tau)$  $= b_q(\tau) + b_{-q}^{\dagger}(\tau), \phi_q(\tau) = b_q(\tau) - b_{-q}^{\dagger}(\tau), \text{ and } \beta = 1/2$  $k_B \dot{T}$ .

We supposed that the cross term between  $H_{11}$  and  $H_{12}$ is much less smaller than the lowest-order contributions. We may use the following approximate Dyson equation in our system:

$$
\mathbf{D}_{\mathbf{q}}(\omega) \simeq \frac{-1}{\left[\mathbf{D}_{\mathbf{q}}^{(0)}(\omega)\right]^{-1} - \mathbf{\Pi}^{(2)}(\mathbf{q},\omega)},
$$
\n(13a)

$$
\mathbf{D}_{\mathbf{q}}(\omega) = \begin{bmatrix} D_{q}^{\mathrm{ad}}(\omega) & 0 \\ 0 & D_{q}^{\mathrm{nonad}}(\omega) \end{bmatrix}, \qquad (13b)
$$

$$
\Pi^{(2)}(\mathbf{q},\omega) = \begin{bmatrix} \Pi^{\mathrm{ad}(2)}(q,\omega) & 0 \\ 0 & \Pi^{\mathrm{nonad}(2)}(q,\omega) \end{bmatrix} . \tag{13c}
$$

This means that frequency shifts and the width of the adiabatic and the nonadiabatic e-MV coupling origins may be approximately independent. The nonadiabatic e-MV coupling gives rise to doping-induced additional fine structure of the phonon spectrum, which might be observed by experiments.

We assume that the *i*th and *j*th bands are separated by a constant energy  $\Delta$  and have the same dispersion, for simplicity:  $\epsilon_{jk} = e_k$ ,  $\epsilon_{ik} = \Delta + e_k$  and  $e_k = k^2 / 2m$ , where m is the effective mass of the band. We neglect the ladder process and use the bare Green's functions to calculate the vertex function and the phonon self-energy. The lowest-order vertex function of the nonadiabatic e-MV coupling in the ground state defined by  $\Gamma^{\text{nonad}} = \kappa_{ij}(1 + \Gamma^{(2)\text{nonad}} + \cdots)$  is estimated as follows:

$$
\Gamma^{(2)\text{nonad}}(q,\omega) \sim \sqrt{1/M} \ln \frac{\Delta + qv_F - \omega - i\delta}{\Delta - qv_F - \omega - i\delta} , \qquad (14)
$$

where  $v_F$  is the Fermi velocity. We may neglect the vertex correction to the phonon self-energy. The lowestorder phonon self-energy of the nonadiabatic e-MV coupling origin is given in the normal ground state as follows:

 $\angle$  4292  $\angle$  493

$$
\Pi^{(2)\text{nonad}}(q,\omega) = -\sum_{\langle ij\rangle} \kappa_{ij}^2 \frac{mk_{Fj}}{2\pi^2} \left[ -\frac{1}{2} - \frac{\tilde{\omega}' - \tilde{\Delta}'}{\tilde{q}'^2} + \frac{1}{2\tilde{q}'} \left\{ 1 - \left( \frac{\tilde{\omega}' - \tilde{\Delta}'}{\tilde{q}'} + \frac{\tilde{q}'}{2} \right)^2 \right\} \ln \left| \frac{1 - \left( \frac{\tilde{\omega}' - \tilde{\Delta}'}{\tilde{q}'} + \frac{\tilde{q}'}{2} \right)}{1 + \left( \frac{\tilde{\omega}' - \tilde{\Delta}'}{\tilde{q}'} + \frac{\tilde{q}'}{2} \right)} \right| \right]
$$
  
- 
$$
\sum_{\langle ij\rangle} \kappa_{ij}^2 \frac{mk_{Fi}}{2\pi^2} \left[ -\frac{1}{2} + \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}^2} - \frac{1}{2\tilde{q}} \left\{ 1 - \left( \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}} - \frac{\tilde{q}}{2} \right)^2 \right\} \ln \left| \frac{1 - \left( \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}} - \frac{\tilde{q}}{2} \right)}{1 + \left( \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}} - \frac{\tilde{q}}{2} \right)} \right| \right| + i \sum_{\langle ij\rangle} \kappa_{ij}^2 \frac{m^2 \omega}{2\pi q} ,
$$
(15)

where  $\tilde{\omega} \! \equiv \! m \, \omega / k_{Fi}^2, \, \tilde{q} \! \equiv \! q \, / k_{Fi}, \, \tilde{\Delta} \! \equiv \! m \, \omega / k_{Fi}^2, \, \tilde{q}' \! \equiv \! m \, \omega / k_{Fi}^2, \, \tilde{q}' \! \equiv \! q \, / k_{Fi},$  and  $\tilde{\Delta}' \! \equiv \! m \, \omega / k_{Fi}^2.$  Here we assumed both the *i*th where  $\omega = m\omega/\kappa_{Fi}$ ,  $q = q/\kappa_{Fi}$ ,  $\Delta = m\omega/\kappa_{Fi}$ ,  $\omega = m\omega/\kappa_{Fj}$ ,  $q = q/\kappa_{Fj}$ , and  $\Delta = m\omega/\kappa_{Fj}$ . Here we assumed both the following for-<br>and jth bands cross the Fermi level. If the band splitting energy  $\Delta$  is smal mulas for the frequency shift and the Lorentz half width of intramolecular vibration:

$$
\left(\frac{\Delta\omega_{\text{vib}}}{\omega_{\text{vib}}}\right)_{\text{nonad}} = -\frac{1}{2}\lambda_{\text{nonad}}/d\tag{16a}
$$

$$
\gamma_{\text{nonad}} = \frac{\pi}{2} N(0) \lambda_{\text{nonad}} \omega_{\text{vib}}^2 / d \tag{16b}
$$

$$
\lambda_{\text{nonad}} = N(0)\kappa^2/\omega_{\text{vib}} \tag{16c}
$$

where  $N(0)$ , d, and  $\kappa^2$  are the partial density of state at the Fermi level per each band, which is supposed to be identical for the ith and jth bands, the degeneracy of the molecular vibrational modes, and the sum of the square of the nonadiabatic e-MV coupling constants over the degenerate vibrational modes, respectively. In the case where the ith band crosses the Fermi level but the jth band does not, the lowest-order phonon self-energy of the nonadiabatic e-MV coupling origin is given as follows:

$$
\Pi^{(2)\text{nonad}}(q,\omega) = -\sum_{\langle ij\rangle} \kappa_{ij}^2 \frac{mk_{Fi}}{2\pi^2} \left[ -\frac{1}{2} + \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}^2} - \frac{1}{2\tilde{q}} \left\{ 1 - \left( \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}} - \frac{\tilde{q}}{2} \right)^2 \right\} \ln \left| \frac{1 - \left( \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}} - \frac{\tilde{q}}{2} \right)}{1 + \left( \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}} - \frac{\tilde{q}}{2} \right)} \right| \right]
$$
  
+  $i \sum_{\langle ij\rangle} \kappa_{ij}^2 \frac{mk_{Fi}}{4\pi\tilde{q}} \left[ 1 - \left( \frac{\tilde{\omega} - \tilde{\Delta}}{\tilde{q}} - \frac{\tilde{q}}{2} \right)^2 \right].$  (17)

This leads to a very approximate formula of the Lorenzian half width of intramolecular vibration:

$$
\gamma_{\text{nonad}} \simeq \frac{\epsilon_F}{\omega_{\text{vib}}} \frac{\pi}{2} N(0) \lambda_{\text{nonad}} \omega_{\text{vib}}^2 / d \quad , \tag{18}
$$

where  $\epsilon_F < \Delta \ll 4\epsilon_F$ . For solids with strong molecularity like C<sub>60</sub>, the factor  $\epsilon_F/\omega_{\rm vib}$  may take a value of about 2—20. One can find corresponding formulas for the adiabatic e-MV coupling in the literature.<sup>2,8,30</sup>

# IV. HALF WIDTH OF THE PHONON SPECTRUM IN DOPED C<sub>60</sub>

We calculate the half width of the phonon spectrum of the  $H_{g}$ ,  $A_{g}$ ,  $H_{u}$ ,  $T_{1u}$ , and  $A_{u}$  modes in doped  $C_{60}$  with both the adiabatic and the nonadiabatic e-MV coupling terms. We have adopted the modified neglect of

differential overlap  $(MNDO)$  approximation<sup>31</sup> for the molecular electronic wave function to calculate coupling constants with the  $H_g$ ,  $A_g$ ,  $H_u$ ,  $T_{1u}$ , and  $A_u$  modes using  $C_{60}^-$  as a model of  $A_3C_{60}^-$ . The details of the quantum chemical calculation are similar to those in a previous paper.<sup>10</sup> It should be noted that calculations of the  $e$ -MV coupling constants appearing in Eq. (11) are done with one of the distorted structures located in a drainlike structure of the potential energy surface (PES} of (a Goldstone-like mode)  $C_{60}^{-32}$  Changes of the C-C bond lengths from the neutral molecule are of order 0.01  $\rm \AA$ .<sup>10</sup> The adiabatic e-MV coupling brings about interactions between the  $H_g$  and  $A_g$  vibrational modes (JT active) and intraband scattering. The nonadiabatic e-MV couplin with the  $H_g$  and  $A_g$  modes brings about interactions with interband mixing between the  $t_{1u}$  derived bands. The nonadiabatic e-MV coupling with the  $H_u$ ,  $T_{1u}$ , and  $A_u$ 

TABLE I. Assignments, calculated frequencies  $\omega$  (cm<sup>-1</sup>), and half width of the phonon spectrum (cm<sup>-1</sup>) of  $H_g$  and  $A_g$  modes of  $C_{60}^-$ . The widths of both the adiabatic e-MV origin  $\gamma_{ad}$  and nonadiabatic e-MV origin  $\gamma_{\text{nonad}}$  are tabulated. We have assumed  $\epsilon_F=0.9$ eV and  $N(0) = 2.5$  states/eV C<sub>60</sub> per spin for each  $t_{1u}$  band.

| Mode              | 1H., | $2H_{\circ}$ | $\Delta H_{\rm m}$ | $3H_{\sim}$ | 4H <sub>a</sub> | 5H.  | 6H,  | 1110 | $4\pi$ | 8H <sub>a</sub> |
|-------------------|------|--------------|--------------------|-------------|-----------------|------|------|------|--------|-----------------|
| $\omega$          | 264  | 452          | 611                | 770         | 926             | 1262 | 1408 | 1585 | 1661   | 1709            |
| $\gamma$ nonad    | 0.0  | 0.8          | 0.5                | 7.2         | J. 1            | 9.9  | 6.6  | 11.9 | 9.4    | 61.7            |
| $\gamma_{\rm ad}$ | 9.4  | 16.3         | 15.1               | 84.7        | 25.4            | 55.9 | 25.8 | 70.1 | 21.1   | 185.4           |

[Herzberg-Teller (HT) active] modes brings about interactions with interband mixing between the  $t_{1u}$  and the  $t_{1g}$  derived bands. The symmetry reduction due to the JT effect<sup>32,33</sup> and a pseudorotation along the Goldstone-like mode makes this group theoretical argument less rigorous. We have included both the  $t_{1u} - t_{1u}$  phononinduced interband mixing and the  $t_{1u} - t_{1g}$  phononinduced interband mixing to calculate nonadiabatic e-MV coupling contribution to the half width of the phonon spectrum of the  $H_g$ ,  $A_g$ ,  $H_u$ ,  $T_{1u}$ , and  $A_u$  modes. We have used Eq. (16) for the former case and Eq. (18) for the latter case. In adopting these equations, we ignored for simplicity liftings of degeneracies of vibrational modes. We used the parameters  $\epsilon_F=0.9$  eV and  $N(0)=2.5$ states/eV per spin  $C_{60}$ . This corresponds to a total density of state 15 states/eV per C<sub>60</sub>. The other parameters  $\lambda$ and  $\omega$  were calculated from the electronic wave function of  $C_{60}^-$  obtained with the MNDO approximation.

The calculated half width of the nonadiabatic e-MV coupling origin  $\gamma_{\rm nonad}$  and of the adiabatic e-MV coupling origin  $\gamma_{ad}$  are summarized in Tables I and II. In Table I we found a substantial width of the highest-frequency  $H<sub>o</sub>$ mode of the nonadiabatic e-MV coupling origin. The other nonadiabatic e-MV coupling origin widths of the  $H_g$ ,  $A_g$ ,  $H_u$ ,  $T_{1u}$ , and  $A_u$  modes are relatively small. Along with the adiabatic e-MV coupling origin width of the highest-frequency  $H<sub>g</sub>$  mode, we may be able to observe doping-induced formation of the structure of the highest-frequency  $H<sub>g</sub>$  mode, which should be assigned to the strong coupling constants of both the adiabatic and the nonadiabatic e-MV couplings in this mode. The highest-frequency  $H<sub>e</sub>$  modes have very large widths of the adiabatic e-MV coupling origin. We also found large widths of the  $3H_g$ ,  $5H_g$ , and  $7H_g$  modes. (We numbered the vibrational modes in ascending manner with frequencies.) These results are in one of the best agreements with experiments among  $e$ -MV theories.<sup>5-7</sup> The agreement suggests that there is no serious breakdown of our lowest-order arguments.

We find in Table II that the symmetry unfavorable  $1H_u$ ,  $2T_{1u}$ , and  $3T_{1u}$  modes have large widths of the adiabatic e-MV coupling origin. The contribution from the nonadiabatic e-MV coupling is very small. The large gap between  $t_{1u}$  and  $t_{1g}$  derived bands makes it hard to mix these bands via virtual exchange of nuclear momentum. The large contribution from the adiabatic e-MV coupling of some of the ungerade modes indicates that the symmetry reduction by the JT distortion of the order of 0.01 A changes of C-C bonds puts very dramatic effects on mixing among  $t_{1u}$  and  $t_{1g}$  derived bands. Experimentally, Kato et al. observed the JT distortion of isolated  $C_{60}^{-33}$ . It may be difficult to observe the distortion directly in solids, but our results may suggest indirectly the existence of the JT distortion in doped  $C_{60}$ . Experimental observation of doping-induced changes of the phonon half width of the ungerade modes is one of the criteria of the JT distortion.

Coupling with  $T_{1u}$  modes has been studied by infrared absorption spectroscopy<sup>19,20</sup> and was studied theoretical ly with the charged-phonon model by Rice and Choi.<sup>22</sup> Recently Prassides et al. have observed a broadening of the  $H_u$  mode upon doping in the range of 60-70 meV in addition to a  $T_{1u}$  mode in that energy region.<sup>21</sup>

The  $1H<sub>u</sub>$  mode has the largest width of the phonon spectrum among all HT active modes of  $C_{60}^-$ . The  $2T_{1u}$ and  $3T_{u1}$  modes also have substantial width. These results are in qualitative agreement with the experimental results obtained by Prassides *et al.* for the lower-<br>frequency  $1H_u$  and  $2T_{1u}$  modes.<sup>21</sup> Our results also suggest the coupling with the higher-frequency  $3T_{1u}$  mode, which does not contradict another inelastic neutron scattering experimental result by White et  $al.^{34}$ 

These agreements may indicate the validity of our e-MV theory and are indicative of the JT distortion in doped  $C_{60}^-$ . The e-MV couplings of the  $H_u$  and  $T_{1u}$ modes can contribute to the electron-phonon mechanism of superconductivity along with the e-MV couplings with  $H<sub>g</sub>$  modes.

TABLE II. Assignments, calculated frequencies  $\omega$  (cm<sup>-1</sup>), and half width of the phonon spectrum (cm<sup>-1</sup>) of  $H_u$ ,  $T_{1u}$ , and  $A_u$ modes C<sub>60</sub>. The widths of both adiabatic e-MV origin  $\gamma_{ad}$  and nonadiabatic e-MV origin  $\gamma_{\text{nonad}}$  are tabulated. We have assumed  $\epsilon_F = 0.9$  eV and  $N(0) = 2.5$  states/eV  $C_{60}^-$  per spin for each  $t_{1u}$  band.

|                           |       |      |     |      |      |         |      | Mode $1H_u$ $2H_u$ $1T_{1u}$ $2T_{1u}$ $3H_u$ $H_u$ $A_u$ $5H_u$ $3T_{1u}$ $6H_u$ $4T_{1u}$ $7H_u$ |      |      |           |                  |
|---------------------------|-------|------|-----|------|------|---------|------|--|------|------|-----------|------------------|
| $\omega$                  | 406   | 564  | 575 | 700  | 706  |         |      | 818 970 1331 1351  |      | 1470 | 1561 1679 |                  |
| $\gamma$ <sub>nonad</sub> | 1.3   | 2.9  | 5.0 | 3.5  |      | 1.8 1.7 | 3.2  | 12.2   | 3.5  | 3.3  | 18.5      | 13.4             |
| $\gamma_{\rm ad}$         | 150.9 | 29.6 | 7.2 | 91.8 | 17.6 | 3.6     | 25.5 | 2.6  | 82.9 | 0.3  | 10.9      | $\overline{0.1}$ |

We have calculated the Lorenzian half widths of intramolecular vibrations of doped  $C_{60}$ , which are brought about by adiabatic and the nonadiabatic e-MV coupling. We have succeeded in explaining qualitatively most of the experimental observations related to phonon broadenings with use of the JT mechanism. We have obtained direct theoretical evidence of the non-negligible contributions of the  $H_u$  and  $T_{1u}$  modes in addition to the  $H_g$  modes. We also obtained a substantial width of the phonon spectrum of the nonadiabatic e-MV coupling origin with the highest-frequency  $H_g$  mode. The theoretical result agrees with the inelastic neutron scattering results qualitatively. This indicates the vital role of the JT mechanism (includ-

- <sup>1</sup>A. F. Hebard, Phys. Today 45 (x), 26 (1992).
- <sup>2</sup>C. M. Varma, J. Zaanen, and K. Raghavachari, Science 254, 989 (1991).
- $3M$ . Schlüter et al., Phys. Rev. Lett. 68, 526 (1992).
- 4K. Prassides et al., Nature (London) 354, 462 (1991).
- 5K. Prassides et al., Europhys. Lett. 19, 629 (1992).
- <sup>6</sup>M. G. Mitch, S. J. Chase, and J. S. Lannin, Phys. Rev. Lett. 68, 883 (1992).
- <sup>7</sup>V. N. Denisov et al., in Clusters and Fullerenes, edited by V. Kumar, T. P. Martin, and E. Tosatti (World Scientific, Singapore, 1992).
- $8M$ . Schlüter et al., J. Phys. Chem. Solids 53, 1473 (1992); (unpublished).
- <sup>9</sup>R. A. Jishi and M. S. Dresselhaus, Phys. Rev. B 45, 2597 (1992).
- $10Y$ . Asai and Y. Kawaguchi, Phys. Rev. B 46, 1265 (1992).
- <sup>11</sup>J. C. R. Faulhaber, D. Y. K. Ko, and P. R. Briddon, Phys. Rev. B48, 661 (1993).
- <sup>12</sup>A. P. Ramirez et al., Phys. Rev. Lett. 68, 1058 (1992).
- <sup>13</sup>C.-C. Chen and C. M. Lieber, J. Am. Chem. Soc. **114**, 3141 (1992).
- <sup>14</sup>P. Auban-Senzier et al., Synth. Met. 55-57, 3027 (1993).
- <sup>15</sup>A. A. Zakidov et al., Phys. Lett. A 164, 355 (1992).
- <sup>16</sup>T. W. Ebbesen et al., Nature 355, 620 (1992).
- <sup>17</sup>R. W. Lof et al., Phys. Rev. Lett. 68, 3924 (1992).
- <sup>18</sup>J. H. Weaver et al., J. Phys. Chem. Solids 53, 1707 (1992).

ing the nonadiabatic e-MV coupling) of superconductivity in doped  $C_{60}$ .

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- $^{19}$ K.-J. Fu et al., Phys. Rev. B 46, 1937 (1992).
- <sup>20</sup>T. Pichler, M. Matus, and H. Kuzmany, Solid State Commun. 86, 221 (1993).
- $21$ K. Prassides *et al.* (personal communication).
- <sup>22</sup>M. J. Rice and H.-Y. Choi, Phys. Rev. B **45**, 10 173 (1992).
- <sup>23</sup>H. Fukutome, Prog. Theor. Phys. **64**, 1931 (1980).
- 24T. Holstein, Ann. Phys. (N.Y.) 8, 325 (1959).
- 25A. B. Migdal, Zh. Eksp. Teor. Fiz. 34, 1438 (1958) [Sov. Phys. JETP 7, 996 (1958)].
- L. Pientronero, Europhys. Lett. 18, 627 (1992).
- <sup>27</sup>A. A. Abrikosov, L. P. Gorkov, and I. E. Dzyaloshinski, Methods of Quantum Field Theory in Statistical Physics (Dover, New York, 1975).
- <sup>28</sup>A. L. Fetter and J. D. Walecka, *Quantum Theory of Many*-Particle Systems (McGraw-Hill, New York, 1971).
- <sup>29</sup>J. W. Negele and H. Orland, *Quantum Many-Particle Systems* (Addison-Wesley, Redwood City, CA, 1988).
- 30P. B. Allen, Phys. Rev. B 6, 2577 (1972).
- M. J. Dewar, J. A. Harshmall, and C. G. Venier, J. Am. Chem. Soc. 90, 1953 (1968).
- <sup>32</sup>N. Koga and K. Morokuma, Chem. Phys. Lett. 196, 191 (1992).
- 33T. Kato et al., Chem. Phys. Lett. 186, 35 (1991); (personal communication).
- 34J. W. White et al., Chem. Phys. Lett. 191, 92 (1992).