

## NMR study of spin dynamics at planar oxygen and copper sites in $\text{YBa}_2\text{Cu}_4\text{O}_8$

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(Received 24 January 1994)

The planar-oxygen Knight shift  $^{17}\text{K}$  and nuclear spin-lattice relaxation rate  $(^{17}\text{T}_1)^{-1}$  have been determined in the superconductor  $\text{YBa}_2\text{Cu}_4\text{O}_8$ . The present oxygen results have been analyzed in connection with the planar-copper relaxation rate  $(^{63}\text{T}_1)^{-1}$  data. In the normal state, both  $^{17}\text{K}$  and  $(^{17}\text{T}_1\text{T})^{-1}$  decrease as the temperature is lowered towards  $T_c = 81$  K, while  $(^{63}\text{T}_1\text{T})^{-1}$  shows a maximum around 160 K. Comparison with  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  data strongly suggests that both the  $q$  and the temperature dependences of the magnetic fluctuations in  $\text{YBa}_2\text{Cu}_4\text{O}_8$  present a similarity to those for the 60-K phase of  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  in the normal state above 110 K. In the superconducting state,  $(^{63}\text{T}_1\text{T})^{-1}$  decreases significantly with decreasing temperature, while the slope for  $(^{17}\text{T}_1\text{T})^{-1}$  shows a slight change near  $T_c$ . The considerable decrease in  $^{17}\text{T}_1/^{63}\text{T}_1$  below  $T_c$  suggests that the loss of antiferromagnetic fluctuations is dominant in the superconducting state.

### I. INTRODUCTION

Nuclear-magnetic-resonance (NMR) and nuclear-quadrupole-resonance (NQR) studies have focused on  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  (Y-1:2:3) in order to investigate the relationship between superconductivity and antiferromagnetic fluctuations in the  $\text{CuO}_2$  plane of high- $T_c$  materials.<sup>1</sup> The distinct temperature dependence of the spin-lattice relaxation rates at planar Cu and O sites has established a picture that the dynamical spin susceptibility in the normal state of Y-1:2:3 is enhanced around the  $q = (\pi, \pi)$  position.<sup>2</sup> The  $T_c$  value for Y-1:2:3 is sensitive to the oxygen population at the CuO chain site. Both NMR and NQR studies have revealed that the oxygen content in superconducting Y-1:2:3 considerably changes both the temperature and the  $q$  dependences of the spin susceptibility in the  $\text{CuO}_2$  plane.<sup>3,4</sup> Rossat-Mignod and co-workers<sup>5</sup> observed a loss of low-energy spin excitations in oxygen-deficient Y-1:2:3 at temperatures higher than  $T_c$  using the neutron inelastic-scattering technique. This observation seems to correspond to a spin-gap behavior proposed from a peak of  $(^{63}\text{T}_1\text{T})^{-1}$  at the planar Cu site as a function of temperature.<sup>6</sup>

The 81-K superconductor  $\text{YBa}_2\text{Cu}_4\text{O}_8$  (Y-1:2:4) also belongs to the Y-Ba-Cu-O family. A high-quality Y-1:2:4 material has been synthesized under a high-oxygen-pressure atmosphere.<sup>7</sup> Y-1:2:4 has a crystal structure parallel to Y-1:2:3 with the exception of double CuO chain sites.<sup>8</sup> Both crystals have  $\text{CuO}_2$  square planes and an apical oxygen related with the square in common. A characteristic feature of Y-1:2:4 is that the removal of oxygen in the double CuO chains is prevented in the range up to 800°C. The oxygen content is fixed for high-pressure synthesized Y-1:2:4. This stability has raised the hope that we can derive the intrinsic nature of the  $\text{CuO}_2$

plane in high- $T_c$  superconductors from NMR and NQR studies on the stoichiometric compound Y-1:2:4. The oxygen spin-lattice relaxation rates  $(^{17}\text{T}_1)^{-1}$  for Y-1:2:4 with  $T_c = 74$  K have been reported by Zheng *et al.*<sup>9</sup> For Y-1:2:4  $(^{17}\text{T}_1\text{T})^{-1}$  are found to be considerably lower than those for the 60 K phase of Y-1:2:3 above 120 K, although the similarity of  $(^{17}\text{T}_1\text{T})^{-1}$  between these materials are noticeable at lower temperatures. Thus their  $(^{17}\text{T}_1)^{-1}$  data suggest that the spin fluctuations in Y-1:2:4 fill a unique position in the Y-Ba-Cu-O family. They also found that the planar-oxygen Knight-shift in the normal state of Y-1:2:4 is higher than that for the 60-K phase of Y-1:2:3. On the other hand, Mangelschots *et al.*<sup>10</sup> showed that the planar-oxygen Knight shift for Y-1:2:4 is similar in behavior to that for oxygen-deficient Y-1:2:3. The point in controversy should be settled by further NMR experiments on Y-1:2:4 with  $T_c = 81$  K.

Previously Machi *et al.*<sup>11</sup> reported the Cu spin-lattice relaxation rates  $(^{63}\text{T}_1)^{-1}$  up to 680 K in this material using the NQR technique. They showed that  $(^{63}\text{T}_1)^{-1}$  in the normal state are divided into  $q = (0, 0)$  and  $q = (\pi, \pi)$  contributions. Their data were consistent with those for Zimmermann *et al.*<sup>12</sup> except for the range above 500 K. The present NMR measurements extend to the planar-oxygen Knight-shift and spin-lattice relaxation rate in Y-1:2:4 with  $T_c = 81$  K. Comparison with Y-1:2:3 NMR data<sup>3</sup> reveals that the normal-state spin fluctuations at planar Cu and O sites for Y-1:2:4 are similar in behavior to those for the 60-K phase of Y-1:2:3 at temperatures above 110 K. Below  $T_c$  the ratio  $^{17}\text{T}_1/^{63}\text{T}_1$  for Y-1:2:4 suggests the suppression of antiferromagnetic fluctuations with decreasing temperature. Magnetic fluctuations observed at both sites in Y-1:2:4 are discussed in conjunction with neutron and NMR experiments on the Y-1:2:3 system.

## II. EXPERIMENTAL PROCEDURE

The Y-1:2:4 materials were synthesized by a high-oxygen-pressure technique. Appropriate mixtures of  $Y_2O_3$ ,  $BaCO_3$ , and  $CuO$  were fired at  $920^\circ C$  in flowing  $O_2$  at one atmosphere for a week. The powders were pressed into pellets and fired at  $940^\circ C$  for two weeks with intermediate grinding. These ceramics were then reacted in a mixed gas of  $O_2$  (20%) and Ar (80%) at 100 MPa and  $1060^\circ C$  for 12 h using a hot isostatic press apparatus. Powder x-ray diffraction for the present samples indicated a single phase of Y-1:2:4. An exchange for  $^{17}O$  was made by annealing the powdered sample at  $500^\circ C$  for 80 h in a  $^{17}O$ -enriched gas. A mixture of Y-1:2:4 powder with epoxy (Stycast 1266) was fixed in an 8-T magnetic field at room temperature to obtain a  $c$ -axis aligned sample.

Magnetization measurements were carried out using a superconducting quantum interference device magnetometer. The susceptibility  $\chi$  for the powder sample used for this work was taken under field-cooled (FC) and zero-field-cooled (ZFC) conditions at 10 Oe. As shown in Fig. 1, the present Y-1:2:4 sample indicates a sharp superconducting transition at  $T_c = 81$  K and the 60% Meissner volume at 5 K without any demagnetization correction. Figure 2 shows the normal-state susceptibility at 1 T. The bulk susceptibility  $\chi$  in the normal state decreases gradually with decreasing temperature. This is similar in behavior to  $\chi$  for the oxygen-deficient Y-1:2:3 with  $T_c = 60$  K.<sup>13</sup>

In this paper we use the following notation for each copper and oxygen site. The double Cu(1)-O(1) chains are parallel with the  $b$  axis. The Cu(2)-O(2)-Cu(2) bond axis in the  $CuO_2$  plane is parallel with the  $b$  axis, and the other Cu(2)-O(3)-Cu(2) bond axis is along the  $a$  axis. The apical oxygen O(4) connects Cu(1) and Cu(2) along the  $c$  axis.

The NMR spectra were taken with a standard pulsed NMR apparatus. The spin-echo intensity vs the magnetic field was obtained using a boxcar integrator. Knight

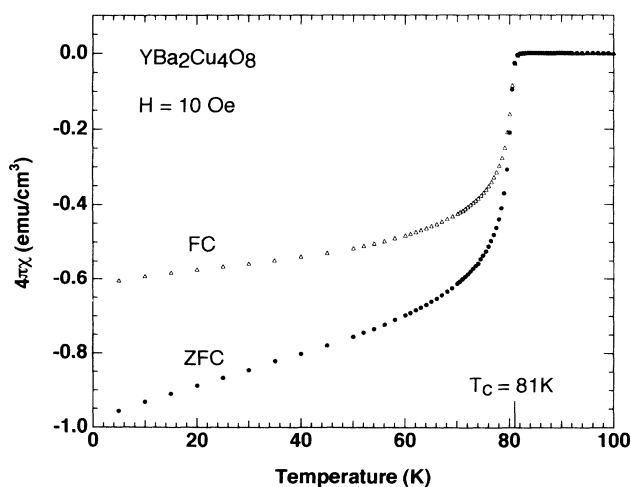


FIG. 1. Temperature dependence of zero-field-cooled (ZFC) and field-cooled (FC) susceptibilities for  $YBa_2Cu_4O_8$  used for the present study. The data were taken at a 10-Oe field.

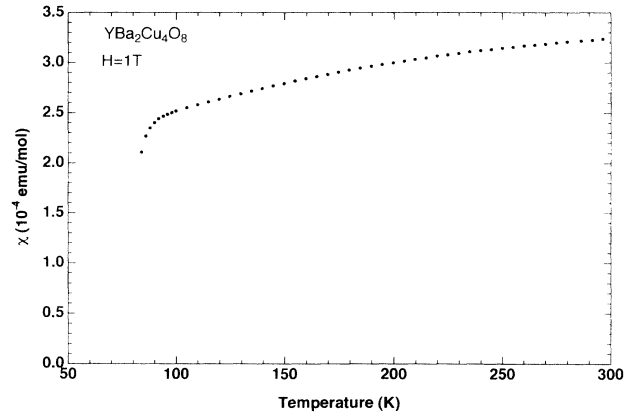


FIG. 2. Normal-state susceptibility for  $YBa_2Cu_4O_8$  sample measured at 1 T.

shifts were determined by using a set of first and second satellite lines at 65.1 MHz. The spin-lattice relaxation rates  $^{17}T_1^{-1}$  for O(2) at 33 MHz in a 5.71-T field parallel to the  $c$  axis were determined by measuring the spin echo from the first higher-field satellite ( $\frac{3}{2} \leftrightarrow \frac{1}{2}$ ) transition. Furthermore, we measured the planar Cu(2) NQR relaxation rate on the same sample up to 300 K and found that the present data are in good agreement with the results reported previously.<sup>11</sup>

## III. OXYGEN NMR SPECTRA AND ELECTRIC-FIELD GRADIENT

Figure 3 shows the  $^{17}O$  NMR spectrum of Y-1:2:4 at 100 K and 65.1 MHz for the applied field along the  $c$  axis ( $H \parallel c$ ). The quadrupole interaction with the nuclear spin  $I = \frac{5}{2}$  should give a set of five resonance lines for each oxygen site. In Fig. 3, four pairs of slightly split satellite lines from O(2,3) indicate a little difference in the electric-field gradient (EFG) between the O(2) and O(3) sites. A similar situation has been found for the planar oxygen in Y-1:2:3 (Ref. 14). We assumed that the absolute value of quadrupole frequency  $\nu_c$  for the O(2) site is larger than for the O(3) site, in view of the Y-1:2:3 re-

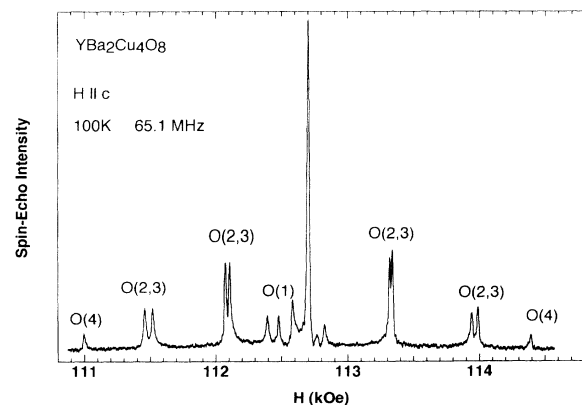


FIG. 3.  $^{17}O$  NMR spectrum taken at 65.1 MHz and 100 K of aligned  $YBa_2Cu_4O_8$  sample with  $c$  axis parallel to applied field.

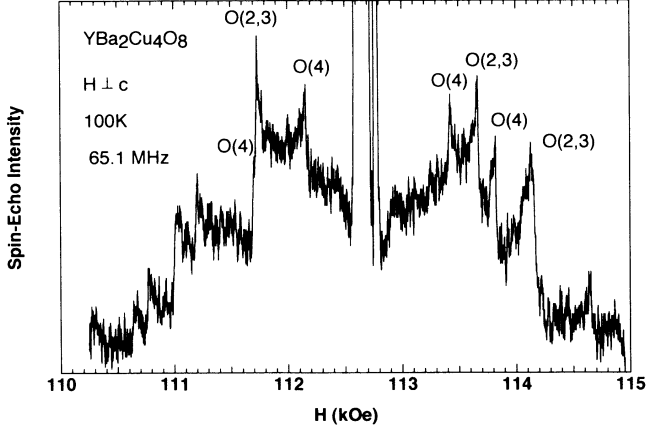


FIG. 4.  $^{17}\text{O}$  NMR spectrum taken at 65.1 MHz and 100 K of aligned  $\text{YBa}_2\text{Cu}_4\text{O}_8$  sample with  $c$  axis perpendicular to applied field.

sult.<sup>14</sup> Figure 4 shows the  $^{17}\text{O}$  spectrum of Y-1:2:4 at 100 K and 65.1 MHz with the field perpendicular to the  $c$  axis ( $H \perp c$ ). A two-dimensional powder spectrum should exhibit two sets of five singularities for each oxygen site, corresponding to the condition that the external field  $H$  is parallel or perpendicular to the Cu-O-Cu bond axis. In Fig. 4, the O(2) resonance lines for  $H \parallel b$  overlap with the O(1) lines for  $H \parallel b$ , indicating that the quadrupole frequency  $\nu_b$  for the O(2) site is nearly equal to that for the O(1) site. A detail analysis of this spectrum will be published elsewhere.<sup>15</sup>

We derive the quadrupole frequencies  $\nu_\alpha$  from the first ( $\frac{1}{2} \leftrightarrow \frac{3}{2}$ ) and the second ( $\frac{3}{2} \leftrightarrow \frac{5}{2}$ ) satellite lines. Here  $\nu_\alpha$  is expressed as  $\nu_\alpha = \frac{3}{20} |eQ| V_{\alpha\alpha}$ , where  $Q$  is the nuclear electric quadrupole moment, and  $V_{\alpha\alpha}$  is the EFG with respect to the  $\alpha$  direction. The  $\nu_\alpha$  values in Table I are obtained using the relation  $\nu_a + \nu_b + \nu_c = 0$ . The present data in Table I are in good agreement with the results of Mangelschots *et al.*<sup>10</sup> The  $\nu_c$  values at the O(2,3) and the O(4) sites for Y-1:2:4 are comparable to those for Y-1:2:3 (Refs. 4 and 14). The structural difference at the chain site has a slight influence on EFG at the other oxygen positions.

The present  $\nu_\alpha$  data for Y-1:2:4 are consistent with the EFG calculation made by Ambrosch-Draxl, Blaha, and Schwarz.<sup>16</sup> The EFG at the O site of high- $T_c$  materials is mainly dominated by an asymmetric internal charge distribution around the nucleus. The EFG calculation

TABLE I. Quadrupole frequency components (in MHz) at oxygen sites for  $\text{YBa}_2\text{Cu}_4\text{O}_8$  and  $\text{YBa}_2\text{Cu}_3\text{O}_7$ . The  $\text{YBa}_2\text{Cu}_3\text{O}_7$  data were taken from Takigawa *et al.* (Ref. 14).

Position	$\text{YBa}_2\text{Cu}_4\text{O}_8$			$\text{YBa}_2\text{Cu}_3\text{O}_7$		
	$\nu_a$	$\nu_b$	$\nu_c$	$\nu_a$	$\nu_b$	$\nu_c$
O(1)	0.845	0.905	-0.0641	-0.484	1.629	-1.145
O(2,3)	0.909	-0.558	-0.349	0.986	-0.598	-0.387
			-0.365	0.966		-0.369
O(4)	-0.366	-0.612	0.978	-0.375	-0.721	1.096

shows that the axis for the maximum EFG component at each O site is parallel to the Cu-O  $dp$ - $\sigma$  bonding axis.<sup>16,17</sup>

#### IV. OXYGEN KNIGHT SHIFT

Figure 5 shows the temperature dependence of the oxygen Knight shifts for  $H \parallel c$ ,  $^{17}K_{i,c}$ , where  $i$  denotes the oxygen site. Here we derived the  $^{17}K_{i,c}$  value from a set of resonance lines except for the central line. In the normal state,  $^{17}K_{2,c}$  for the planar O(2) site decreases gradually with decreasing temperature. Note that  $^{17}K_{2,c}$  is slightly higher than  $^{17}K_{3,c}$  below 175 K. The existence of double CuO chains along the  $b$  axis appears to induce the Knight-shift difference between the two planar-oxygen sites. The  $^{17}K_{2,c}$  value at 100 K is in agreement with the value reported by Mangelschots *et al.*<sup>10</sup> The present data, however, are different from those reported by Zheng *et al.*<sup>9</sup> in a wide temperature range. This discrepancy may be related to the fact that their Y-1:2:4 sample has a lower superconducting temperature ( $T_c = 74$  K).

The O(2,3) hyperfine interaction between the  $^{17}\text{O}$  nuclear spin  $I$  and the Cu electron spin  $S$  is expressed as

$$H_O = \sum_{\alpha,j} C_\alpha I_\alpha S_{\alpha,j}, \quad (1)$$

where  $C_\alpha$  is the transferred hyperfine coupling. The Knight shift  $^{17}K_{2,c}$  consists of the spin and orbital parts,

$$^{17}K_{2,c} = ^{17}K_{2,c}^{\text{spin}} + ^{17}K_{2,c}^{\text{orb}}, \quad (2)$$

where  $^{17}K_{2,c}^{\text{orb}}$  is temperature independent. The spin part is related to the spin susceptibility  $\chi^{\text{spin}}$  by

$$^{17}K_{2,c}^{\text{spin}} = C_\alpha \chi^{\text{spin}} / \mu_B N, \quad (3)$$

where  $\mu_B$  is the Bohr magneton, and  $N$  is the Avogadro's number. The Knight shift  $^{17}K_{2,c}$  is plotted in Fig. 6 as a function of bulk susceptibility  $\chi$ . The temperature-

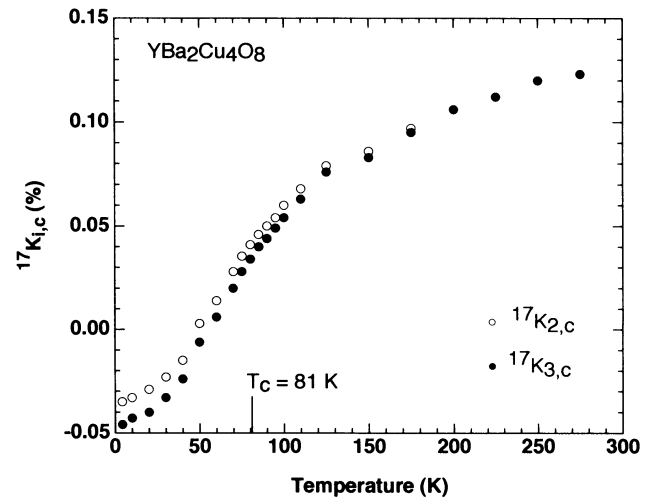


FIG. 5. Temperature dependence of  $^{17}K_{i,c}$  for O( $i$ ) site in  $\text{YBa}_2\text{Cu}_4\text{O}_8$ . The superconducting-state data are plotted without any diamagnetic field correction.

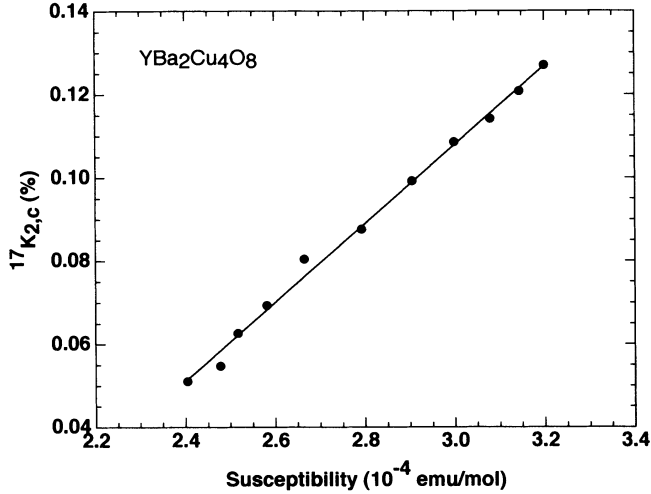


FIG. 6. Knight shift  $^{17}K_{2,c}$  vs bulk susceptibility  $\chi$  in  $\text{YBa}_2\text{Cu}_4\text{O}_8$ . The line is a linear fit.

dependent part of the bulk susceptibility  $\chi$  originates from the spin susceptibility  $\chi_{\text{spin}}$ . In Y-1:2:4 the spin susceptibility is given by  $\chi^{\text{spin}} = 2\chi_1^{\text{spin}} + 2\chi_2^{\text{spin}}$ , where  $\chi_i^{\text{spin}}$  stands for the Cu(*i*) site spin susceptibility. In the normal state  $^{63}K_{1,c}$  has a slight decrease with decreasing temperature, while  $^{63}K_{2,ab}$  shows a marked decrease.<sup>18</sup> Room-temperature value for  $^{63}K_{1,c}$  is two-thirds of that for  $^{63}K_{2,ab}$ . We evaluate  $C_c = 140 \text{ kOe}/\mu_B$  from the slope  $dK_{2,c}/d\chi$  in Fig. 6, on the following assumptions. (1) The orbital Knight-shift components are the same as in Y-1:2:3 (Ref. 19). (2) In the normal state  $\chi_1^{\text{spin}}$  is proportional to  $\chi_2^{\text{spin}}$  and the ratio  $\chi_1^{\text{spin}}/\chi_2^{\text{spin}}$  is equal to  $^{63}K_{1,c}^{\text{spin}}/^{63}K_{2,ab}^{\text{spin}}$ . Here we estimate  $^{63}K_{1,c}^{\text{spin}} = 0.10\%$  and  $^{63}K_{2,ab}^{\text{spin}} = 0.24\%$  at room temperature from the Y-1:2:4 data.<sup>18</sup> On the other hand, Yoshinari *et al.*<sup>4</sup> obtained that the  $C_c$  value for Y-1:2:3 is of the order of 100  $\text{kOe}/\mu_B$ . They made two assumptions; (1)  $\chi_1^{\text{spin}}$  at the fourfold Cu(1) site is equal to  $\chi_2^{\text{spin}}$  and (2)  $\chi_1^{\text{spin}}$  at the two- or threefold Cu(1) site is zero. Although all the Cu(1) sites in Y-1:2:4 are surrounded by four neighbor O(1) sites, the assumption that  $\chi_1^{\text{spin}}$  is equal to  $\chi_2^{\text{spin}}$  is not applicable to the case of Y-1:2:4. The role of the Cu(1) spin should be clarified to compare the  $C_c$  value for Y-1:2:4 with that for the 60-K phase of Y-1:2:3.

## V. RELAXATION RATES AT THE PLANAR-OXYGEN AND COPPER SITES

### A. Relaxation rates above $T_c$

Figure 7 shows the temperature dependence of  $(^{17}T_1T)^{-1}$  for the O(2) sites and  $(^{63}T_1T)^{-1}$  for the Cu(2) sites in Y-1:2:4. For O(2),  $(^{17}T_1T)^{-1}$  decreases with decreasing temperature, changes the slope at temperatures just below  $T_c$ , and then decreases gradually below 50 K. Our  $(^{17}T_1T)^{-1}$  data above 160 K are considerably higher than the values measured by Zheng *et al.*<sup>9</sup>

For Cu(2),  $(^{63}T_1T)^{-1}$  increases with decreasing tem-

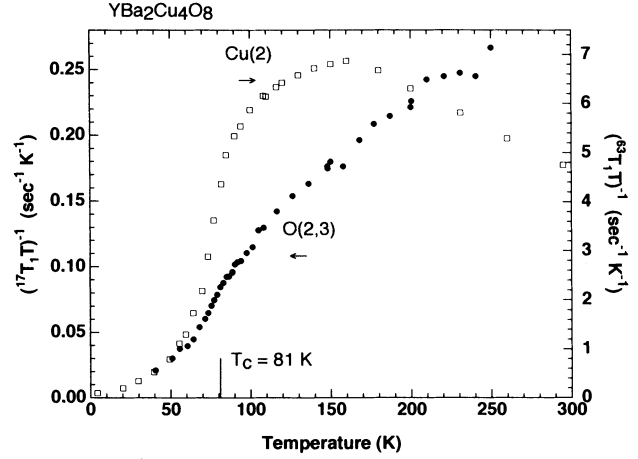


FIG. 7. Temperature dependence of  $(^{17}T_1T)^{-1}$  for O(2) sites and  $(^{63}T_1T)^{-1}$  for Cu(2) sites in  $\text{YBa}_2\text{Cu}_4\text{O}_8$ .

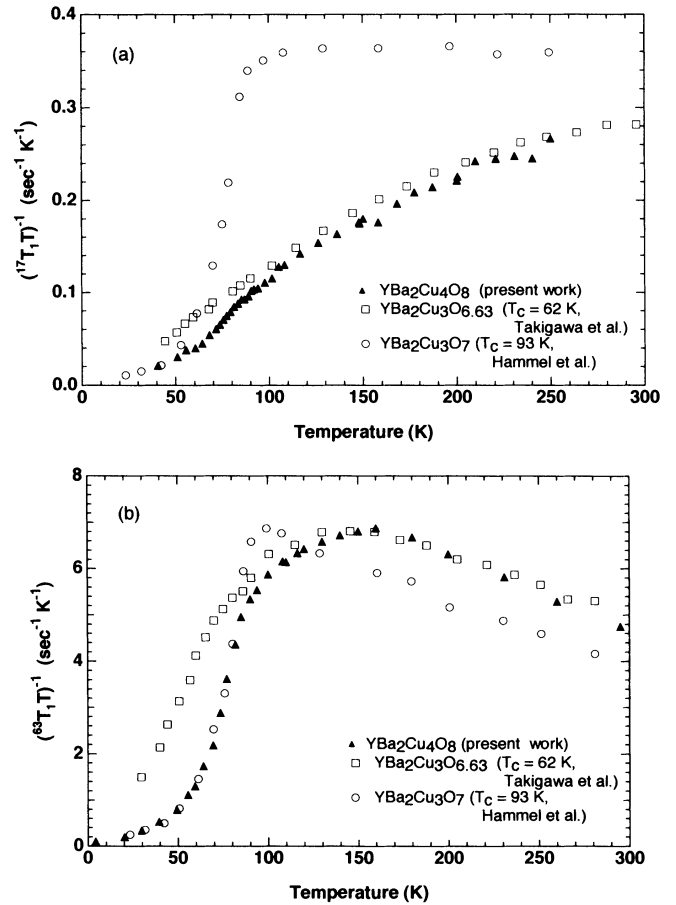


FIG. 8. Comparison of present  $(^aT_1T)^{-1}$  data for  $\text{YBa}_2\text{Cu}_4\text{O}_8$  (triangles) with those for  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ . The data for the 90-K phase (circles) and the 60-K phase (squares) of  $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$  were taken from Hammel *et al.* (Ref. 2) and Takigawa *et al.* (Ref. 3), respectively. (a)  $(^{17}T_1T)^{-1}$  at the O(2,3) site. (b)  $(^{63}T_1T)^{-1}$  at the Cu(2) site.

perature, exhibits a broad peak near 160 K and then decreases drastically in the vicinity of  $T_c$ . The present  $({}^\alpha T_1 T)^{-1}$  data for Y-1:2:4 are compared with the Y-1:2:3 data of Hammel *et al.*<sup>2</sup> and Takigawa *et al.*<sup>3</sup> in Fig. 8. Note that the normal state  $({}^{17}T_1 T)^{-1}$  for Y-1:2:4 is nearly equal to that for the oxygen-deficient Y-1:2:3 in a wide temperature range above 110 K. A similar situation is found for  $({}^{63}T_1 T)^{-1}$  in the same range between the two materials.

In general,  $({}^\alpha T_1 T)^{-1}$  for the nucleus  $\alpha$  is expressed in terms of the imaginary part of the spin susceptibility  $\text{Im}\chi(q, \omega)$

$$({}^\alpha T_1 T)^{-1} = \frac{{}^\alpha \gamma^2 k_B}{2\mu_B^2} \sum_q |{}^\alpha A(q)|^2 \frac{\text{Im}\chi(q, \omega)}{\omega}. \quad (4)$$

Here,  $\omega$  is the nuclear Larmor frequency and  ${}^\alpha \gamma$  is the nuclear gyromagnetic ratio. The form factor  ${}^\alpha A(q)$  represents the Fourier transform of the hyperfine coupling. Under the present experimental condition, these are given by

$${}^{17}A(q) = 2C \cos(q_x/2), \quad (5)$$

$${}^{63}A(q) = A_{ab} - 2B(\cos q_x + \cos q_y), \quad (6)$$

where  $A_{ab}$  is the direct hyperfine coupling of the  ${}^{63}\text{Cu}$  nuclei, and  $B$  is the transferred hyperfine coupling to the nearest-neighbor Cu spins.<sup>20</sup> The O(2) nuclei have the form factor  ${}^{17}A(q)$  that filters antiferromagnetic fluctuations in the neighboring Cu sites. Thus the O(2) relaxation rate is dominated by spin fluctuations in a broad  $q$  space around  $q=(0,0)$ . On the other hand, the form factor  ${}^{63}A(q)$  has double peaks at  $q=(0,0)$  and  $q=(\pi, \pi) \equiv Q$ .

First, we consider the Cu(2) relaxation behavior in the normal state. We have found that  $({}^{63}T_1 T)^{-1}$  above 250 K are well described by a Curie-Weiss form

$$({}^{63}T_1 T)^{-1} = a + \frac{b}{(T + \theta)}, \quad (7)$$

where the first term is the contribution around  $q=(0,0)$ , and the second term is the contribution from antiferromagnetic spin fluctuations. The solid line in Fig. 9 is the fit to the data with  $a=0.28(\text{sec}^{-1} \text{K}^{-1})$ ,  $b=1454 \text{ sec}^{-1}$  and  $\theta=29 \text{ K}$ . The agreement is quite good. This means that the normal-state Cu(2) relaxation rate is dominated by antiferromagnetic fluctuation near  $Q$ .

The normal-state  $({}^{63}T_1 T)^{-1}$  in Y-1:2:4 deviates from the Curie-Weiss law at lower temperatures, as shown in Fig. 9. The gradual decrease behavior of  $({}^{63}T_1 T)^{-1}$  is also recognized for oxygen-deficient Y-1:2:3 in a broader range between 160 K and  $T_c=60 \text{ K}$ . This anomaly has been discussed in connection with the existence of a spin gap above  $T_c$ .<sup>6</sup> Here we argue that the spin gap opens at the temperature  $T^*$  where  $({}^{63}T_1 T)^{-1}$  reaches the maximum in the normal state. Rossat-Mignod *et al.*<sup>5</sup> pointed out that the  $\text{Im}\chi(q, \omega)$  vs  $\omega$  relationship deduced from neutron scattering for the oxygen-deficient Y-1:2:3 is consistent with the temperature dependence of  $({}^{63}T_1 T)^{-1}$  determined from NMR experiments. The deviation from the Curie-Weiss law implies that the low-energy spectral

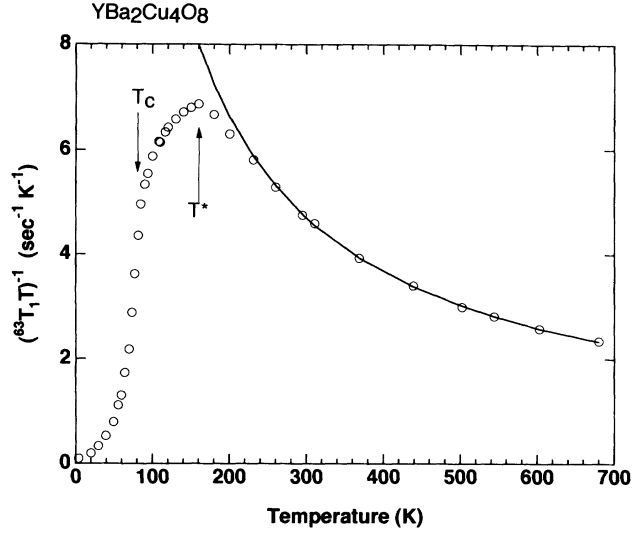


FIG. 9. Temperature dependence of  $({}^{63}T_1 T)^{-1}$  for Cu(2) sites in  $\text{YBa}_2\text{Cu}_4\text{O}_8$  up to 680 K. The data above 250 K are taken from Machi *et al.* (Ref. 11). The line is a fit to the data above 250 K with Eq. (7).

weight in  $\chi(Q, \omega)$  shifts to the high-energy part with decreasing temperature. For Y-1:2:4 with  $T_c=81 \text{ K}$  and the 60-K phase of Y-1:2:3,  $({}^{63}T_1 T)^{-1}$  has a broad peak at  $T^* \approx 160 \text{ K}$ . On the other hand,  $({}^{63}T_1 T)^{-1}$  for the 90-K phase of Y-1:2:3 has not a clear peak above  $T_c$ . These results imply that  $T^*$  for the development of a spin gap has little correlation with  $T_c$ .

Second, we discuss the  $({}^{17}T_1 T)^{-1}$  data in the normal state. For noninteracting conduction electrons, both  ${}^\alpha K^{\text{spin}}$  and  $({}^\alpha T_1 T)^{-1}$  obey the Korringa relation

$$[{}^\alpha T_1 T ({}^\alpha K^{\text{spin}})^2]^{-1} = \frac{{}^\alpha \gamma_e^2 4\pi k_B}{\gamma_e^2 \hbar} \equiv S, \quad (8)$$

where  $\gamma_e$  is the electronic gyromagnetic ratio. The Korringa value  $S$  is estimated to be  $6.98 \times 10^4 \text{ sec}^{-1} \text{K}^{-1}$  for an oxygen nucleus. In Fig. 10 we plot  $({}^{17}T_1 T {}^{17}K_{2,c}^{\text{spin}})^{-1}$  and  $[{}^{17}T_1 T ({}^{17}K_{2,c}^{\text{spin}})^2]^{-1}$  for the O(2) site in Y-1:2:4 as a function of temperature. Here we use  ${}^{17}K_{2,c}^{\text{orb}} = -0.014\%$  for Y-1:2:4, assuming that  ${}^{17}K_{2,c}^{\text{orb}}$  is the same as in Y-1:2:3 (Ref. 3). The quantity  $[{}^{17}T_1 T ({}^{17}K_{2,c}^{\text{spin}})^2]^{-1}$  is practically constant in the range above 150 K. However, deviation from the Korringa relation  $T_1 T K^2 = \text{const}$  is found in the vicinity of  $T_c$ . This is similar in behavior to the result for the 60-K phase of Y-1:2:3 (Ref. 3). As shown in Fig. 10,  $[{}^{17}T_1 T ({}^{17}K_{2,c}^{\text{spin}})^2]^{-1}$  is weakly temperature dependent near  $T_c$ . Comparison with the data for the oxygen-efficient Y-1:2:3 (Ref. 3) suggests that  $({}^{17}T_1 T)^{-1}$  is roughly proportional to  ${}^{17}K_{2,c}^{\text{spin}}$  in the vicinity of  $T_c$  in the two materials.

As shown in Fig. 8(a), the normal-state  $({}^{17}T_1 T)^{-1}$  values for Y-1:2:4 and the 60-K phase of Y-1:2:3 are considerably lower than for the 90 K phase of Y-1:2:3.

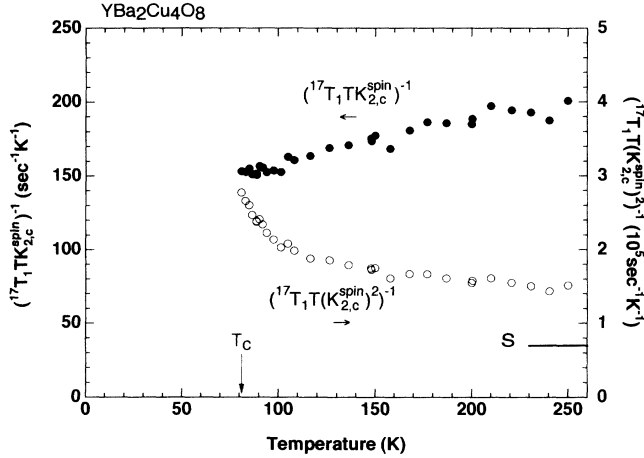


FIG. 10. Plots of  $(^{17}T_1T)^{-1}$  and  $[^{17}T_1T(K_{2,c}^{\text{spin}})^2]^{-1}$  for O(2,3) sites in  $\text{YBa}_2\text{Cu}_4\text{O}_8$  as a function of temperature. The line indicates the Korringa value  $S$  for an oxygen nucleus.

Moreover,  $(^{17}T_1T)^{-1}$  for Y-1:2:4 exhibits a steady decline as the temperature is lowered toward  $T_c$ . The temperature dependent  $(^{17}T_1T)^{-1}$  remains an unsolved problem of cuprate superconductors. Based on Eq. (4), the  $(^{17}T_1T)^{-1}$  data indicate the decrease in  $\text{Im}\chi(q, \omega)$  around  $q = (0, 0)$  with decreasing temperature.

One possibility is that the appearance of a spin gap at  $q = Q$  disturbs the  $\text{Im}\chi(q, \omega)$  spectrum around  $q = (0, 0)$ . For Y-1:2:4 and the oxygen-deficient Y-1:2:3, the gap is created at  $T^* = 160$  K. Figure 7 illustrates that  $(^{17}T_1T)^{-1}$  starts to decrease at a high-temperature region where the spin gap disappears. Tanamoto, Kuboki, and Fukuyama<sup>21</sup> calculated the dynamical spin susceptibility  $\chi(q, \omega)$  based on the  $t$ - $J$  model. According to this model, the maximum of  $(^{63}T_1T)^{-1}$  is due to the spin gap near 0.1 J. The calculated  $\chi(q, \omega)/\omega$  shows that the suppression of the peak at  $q = Q$  gives rise to an anomaly along the diagonal line joining  $q = (0, 0)$  and  $q = Q$ . The temperature-independent  $(^{17}T_1T)^{-1}$  is predicted in a highly doped region. Their calculation, however, shows that  $(^{17}T_1T)^{-1}$  in a lightly doped region increases gradually with decreasing temperature, in contrast to the observed behavior. Subsequently Tanamoto, Kohno, and Fukuyama<sup>22</sup> proposed the concept that singlet resonating-valence-bond (RVB) pairing is responsible for the decrease in  $\chi(q)$  at  $q = 0$  and  $q = Q$  for the lightly doped region. Bucher *et al.*<sup>23</sup> found that the  $\text{CuO}_2$  plane resistivity along the  $a$  axis in Y-1:2:4 exhibits a strong correlation with the spin dynamics. The normal-state resistivity deviates from the linear temperature dependence below  $T^*$ . Furthermore, the Hall coefficient  $R_H$  in Y-1:2:4 varies inversely as the temperature above  $T^*$  and increases considerably in the range between  $T_c$  and  $T^*$ .<sup>23,24</sup> Thus the opening of the spin gap appears to have an influence on these transport properties of Y-1:2:4. The transport behavior connected with the spin gap seems consistent with the theoretical prediction.<sup>22</sup> From the experimental point of view, it is still open to question whether an RVB state exists in high- $T_c$  superconductors or not.

Millis and Monien<sup>25</sup> calculated  $(^aT_1T)^{-1}$  based on the spin Hamiltonian including a large exchange interaction within the  $\text{CuO}_2$  planes,  $J_1$ , and a small exchange interaction between nearest-neighbor  $\text{CuO}_2$  planes,  $J_2$ . According to their model, the decrease in  $(^{17}T_1T)^{-1}$  is governed by  $J_2$ , and the  $(^{63}T_1T)^{-1}$  peak is determined by the interplay between  $J_1$  and  $J_2$ . For the 90-K phase of Y-1:2:3,  $(^{17}T_1T)^{-1}$  is temperature independent. Above 110 K the  $(^{17}T_1T)^{-1}$  data for Y-1:2:4 are nearly equal to those for the 60-K phase of Y-1:2:3. In view of these results, the model should satisfy the following two conditions. (1)  $J_2$  is sensitive to the hole population in the  $\text{CuO}_2$  plane, and (2) the hole population in the  $\text{CuO}_2$  plane of Y-1:2:4 is comparable to that for the 60-K phase of Y-1:2:3.

The Hall coefficient  $R_H$  for Y-1:2:4 is about 15% of that for Y-1:2:3 at room temperature.<sup>26,27</sup> The large difference in  $R_H$  appears to be unfavorable for the picture that  $\chi(q, \omega)$  for the Y-Ba-Cu-O family is determined by the average hole concentration. To be consistent with the picture we interpret that the excess holes in the double  $\text{CuO}$  chain of Y-1:2:4 contribute to  $R_H$ . The anisotropic resistivity data in the  $ab$  plane suggest that some part of the mobile holes is distributed at the  $\text{CuO}$  chain sites.<sup>23,27</sup>

Third, we consider the ratio of the relaxation rate at the Cu(2) site to that at the O(2,3) site,  $^{17}T_1/^{63}T_1$ , in the normal state. In Fig. 11, the present  $^{17}T_1/^{63}T_1$  data for Y-1:2:4 are compared with those for the Y-1:2:3 system obtained by Yoshinari, Yasuoka, and Ueda.<sup>28</sup> For Y-1:2:4,  $^{17}T_1/^{63}T_1$  increases with decreasing temperature, reaches a peak just above  $T_c$ . A similar behavior has been found for the 60-K phase of Y-1:2:3 in the range above 100 K. The maximum  $^{17}T_1/^{63}T_1$  value for Y-1:2:4 is considerably higher than that for the 90-K phase of Y-1:2:3.

Based on the antiferromagnetic Fermi-liquid model proposed by Millis, Monien, and Pines (Ref. 29)  $^{17}T_1/^{63}T_1$  is approximately proportional to  $(1 + \xi^2)$  where  $\xi$  is the antiferromagnetic correlation length. Thus the Y-1:2:4 data in Fig. 11 suggest that the normal-state  $\xi$

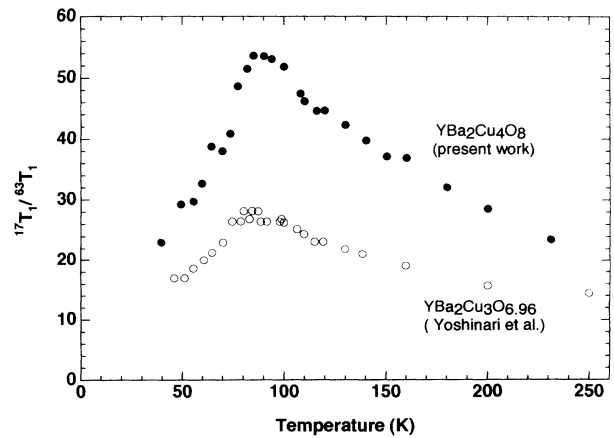


FIG. 11. Temperature dependence of ratio  $^{17}T_1/^{63}T_1$  for  $\text{YBa}_2\text{Cu}_4\text{O}_8$  and  $\text{YBa}_2\text{Cu}_3\text{O}_{6.96}$ . The  $\text{YBa}_2\text{Cu}_3\text{O}_{6.96}$  data with  $T_c = 87$  K are taken from Yoshinari, Yasuoka, and Ueda (Ref. 28).

increases gradually with decreasing temperature. In addition, the opening of the spin gap near  $T^* = 160$  K appears to have no effect on the gradual increase in  $\xi$ . Neutron-scattering studies on the Y-1:2:3 system, however, have suggested that  $\xi$  derived from  $\chi(q, \omega)$  is essentially independent of temperature in a wide temperature range.<sup>5,30</sup> Millis and Monien<sup>31</sup> pointed out the possibility that the half-width of the peak in  $\text{Im}\chi(q, \omega)$  is independent of  $\xi$  at high  $\omega$  even if  $\xi$  is temperature dependent. Tranquada *et al.*<sup>30</sup> have shown that the  $q$  dependence of  $\text{Im}\chi(q, \omega)$  around  $Q$  is anisotropic in the  $ab$  plane of Y-1:2:3. Furthermore, the  $q$  width of the  $\text{Im}\chi(q, \omega)$  peak is  $\omega$  dependent. This complicated situation presents difficulty in comparing  $\xi$  deduced from the  $^{17}\text{T}_1/^{63}\text{T}_1$  data with  $\xi$  determined by neutron experiments.

Note that the normal-state ratio  $^{17}\text{T}_1/^{63}\text{T}_1$  saturates in the vicinity of  $T_c$  where  $(^{63}\text{T}_1 T)^{-1}$  decreases rapidly. A saturation behavior was also observed for the ratio for the 90-K phase of Y-1:2:3 (Ref. 3). The  $^{17}\text{T}_1/^{63}\text{T}_1$  peak means that the temperature derivative  $d\text{Im}\chi(q, \omega)/dT$  is essentially  $q$  independent near  $T_c$ .

### B. Relaxation rates below $T_c$

Here we discuss the Cu(2) and the O(2) relaxation behaviors in the superconducting state. Note in Fig. 8(b) that the superconducting-state  $(^{63}\text{T}_1 T)^{-1}$  in Y-1:2:4 is almost the same as that for the 90-K phase of Y-1:2:3. The similarity below 80 K is in marked contrast to the distinct temperature dependences of the normal state  $(^{63}\text{T}_1 T)^{-1}$ . Therefore the appearance of superconductivity makes essentially no difference in magnetic fluctuations near  $q = Q$  between Y-1:2:4 and the 90-K phase of Y-1:2:3. As shown in Fig. 8(a), there is a large difference in the superconducting state  $(^{17}\text{T}_1 T)^{-1}$  between these materials. The slope of  $(^{17}\text{T}_1 T)^{-1}$  just below  $T_c$  for Y-1:2:4 is smaller than that for the 90-K phase of Y-1:2:3. The decrease in  $(^{17}\text{T}_1 T)^{-1}$  in the normal state of Y-1:2:4 appears to reduce the superconducting effect on magnetic fluctuations around  $q = (0, 0)$ .

Figure 12 shows  $(^{17}\text{T}_1 T)^{-1}$  normalized to the value at  $T_c$  as a function of reduced temperature  $T/T_c$  in Y-1:2:4. Both  $(^{63}\text{T}_1 T)^{-1}$  and  $(^{17}\text{T}_1 T)^{-1}$  change their slopes near  $T_c$ . In the superconducting phase, there is a difference in the slope between the Cu(2) and O(2) sites. Figure 11 indicates that the superconducting state  $^{17}\text{T}_1/^{63}\text{T}_1$  shows a marked decrease with decreasing temperature. These results suggest that antiferromagnetic fluctuations are suppressed considerably compared with the spin fluctuations around  $q = (0, 0)$ . The decrease in  $^{17}\text{T}_1/^{63}\text{T}_1$  has also been observed for the 90-K phase of Y-1:2:3 reported by Yoshinari, Yasuoka, and Ueda<sup>28</sup> and Martindale *et al.*<sup>32</sup> On the other hand, Hammel *et al.*<sup>2</sup> found that the ratio  $^{17}\text{T}_1/^{63}\text{T}_1$  is temperature independent in the superconducting state of Y-1:2:3. The reason for this discrepancy in the Y-1:2:3 materials is unexplained.

The pairing symmetry in cuprate superconductors is still in controversy. Bulut and Scalapino<sup>33</sup> pointed out that an  $s$ -wave pairing has a difficulty in explaining the absence of the Hebel-Slichter peak just below  $T_c$ . They interpreted the temperature-independent  $^{17}\text{T}_1/^{63}\text{T}_1$

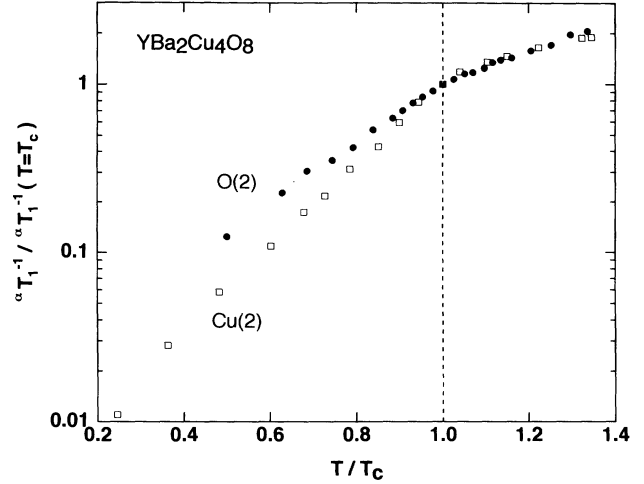


FIG. 12.  $(^{17}\text{T}_1 T)^{-1}$  normalized to the value at  $T_c$  as a function of reduced temperature  $T/T_c$  in  $\text{YBa}_2\text{Cu}_4\text{O}_8$ .

below  $T_c$  as the evidence for a  $d$ -wave pairing state. Thelen, Pines, and Lu<sup>34</sup> showed that a  $d$ -wave pairing state is in favor of the decrease in  $^{17}\text{T}_1/^{63}\text{T}_1$  below  $T_c$  for the 90-K phase of Y-1:2:3. The pronounced decrease in  $^{17}\text{T}_1/^{63}\text{T}_1$  is found for Y-1:2:4. In view of the similarity in  $(^{63}\text{T}_1 T)^{-1}$  between Y-1:2:4 and Y-1:2:3, the difference in the slope of  $^{17}\text{T}_1/^{63}\text{T}_1$  implies that the temperature dependence of magnetic fluctuations around  $q = (0, 0)$  is sensitive to the hole concentration even below  $T_c$ .

## VI. CONCLUSION

The planar-oxygen Knight shift in Y-1:2:4 shows the decrease as the temperature is lowered toward  $T_c$ . In the normal state  $(^{17}\text{T}_1 T)^{-1}$  at the O(2,3) site is roughly proportional to  $^{17}K_{2,c}$  near  $T_c$ . On the other hand,  $(^{63}\text{T}_1 T)^{-1}$  at the Cu(2) site shows a maximum around  $T^* = 160$  K. Comparison with the Y-1:2:3 data strongly suggests that both the  $q$  and the temperature dependences of magnetic fluctuations in Y-1:2:4 present an almost complete similarity to those for the 60-K phase of Y-1:2:3 in the normal state above 110 K. In the normal state, the ratio  $^{17}\text{T}_1/^{63}\text{T}_1$  increases with decreasing temperature, and reaches a broad peak near  $T_c$ . The absence of anomaly in  $^{17}\text{T}_1/^{63}\text{T}_1$  around 160 K suggests that the appearance of the spin gap has no influence on the antiferromagnetic correlation length.

In the superconducting state,  $(^{63}\text{T}_1 T)^{-1}$  decreases dramatically with decreasing temperature. Below  $T_c$  there is a striking similarity in  $(^{63}\text{T}_1 T)^{-1}$  between Y-1:2:4 and the 90-K phase of Y-1:2:3. The antiferromagnetic fluctuations in the superconducting phase of Y-1:2:4 appear to be unaffected by the development of the spin gap observed at temperatures up to  $T^* = 160$  K. The slope for  $(^{17}\text{T}_1 T)^{-1}$  shows a slight change in the vicinity of  $T_c$ . Magnetic fluctuations around  $q = (0, 0)$  in the superconducting state of Y-1:2:4 are smaller than those for the

90-K phase of Y-1:2:3. The significant decrease in  $^{17}\text{T}_1/^{63}\text{T}_1$  suggests that the loss of antiferromagnetic fluctuations are dominant in the superconducting state of Y-1:2:4.

#### ACKNOWLEDGMENTS

We wish to thank Y. Ito, T. Miyatake, and J. O. Willis for their stimulating discussions.

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