# Solid-state effects on nonradiative decay of $4d^{9}4f^{1}$ states in barium halides

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The nonradiative decay of  $4d^94f^1$  states in barium halides was investigated by using resonantphotoemission spectroscopy. Constant-final-state spectra with the final state at  $N_{4,5}$ - $O_{2,3}O_{2,3}$  Auger electron peak and constant-initial-state (CIS) spectra with the initial state at Ba 5*p* levels were enhanced in the Ba 4*d* excitation-energy region, indicating Auger and direct recombination decay processes, respectively. The probability of the direct recombination decay was estimated from the CIS and the absorption spectra. At the excitation energy of the  $4d^94f^1$  ( $^3D$ ) state, the intensity ratio of  $5p_{1/2}$  to  $5p_{3/2}$  photoelectrons showed the anomalous increase due to the different branching ratio in the direct recombination process. It was noticed that the decay probability through the direct recombination process and the degree of the anomalous branching ratio increase in the order of BaF<sub>2</sub>, BaCl<sub>2</sub>, and BaBr<sub>2</sub>. This result indicates that the nonradiative decay of the  $4d^94f^1$  states in the barium halides is affected by crystalline environments.

## I. INTRODUCTION

The localization or delocalization of 4f electrons is of much interest, because 4f electrons are closely related to a variety of electrical and magnetic properties of rareearth compounds. There have been many studies to understand the relation between them.<sup>1</sup> On the other hand, 4f electrons in the core excitation have attracted recent interest because they also show a variety of localization or delocalization behaviors. Through the years, there have been many studies on the absorption spectra of atoms or ions with Z = 54-70 in the region of  $4d \rightarrow nf, \epsilon f$  excitations ( $n = 4, 5, \text{ and so on, and } \epsilon$  is the continuum states).<sup>2-13</sup> The absorption spectra are characterized by huge peaks and weak sharp lines. The latter is due to the multiplet structures of  $4d^{9}4f^{m+1}$ states (m is the number of 4f electrons in the ground state), while the former depends on the potential barrier separating inner and outer wells for 4f electrons. The inner well becomes narrower and deeper with increasing nuclear charge Z and then leads to the sudden collapse of the 4f wave functions from the outer into the inner well. The strong absorption peaks are interpreted in terms of delayed onsets of  $4d \rightarrow \epsilon f$  transitions for lighter elements  $[Z \leq 54(Xe)]$ , while for heavier elements  $[Z \geq 56(Ba)]$  the observed absorption peaks arise from the  $4d^{9}4f^{m+1}$ states autoionized in the continuum.

However, these explanations of the observed spectra are not fully satisfactory. Jo<sup>13</sup> has demonstrated the effect of valence mixing on multiplet structures in the Ce 4d photoabsorption spectra for Ce compounds, on the basis of the impurity Anderson model. He showed the deviation of the spectra for CeO<sub>2</sub> from the multiplet structure with integral valence, and attributed it to a strong interference between the  $4d^{10}4f^0 \rightarrow 4d^94f^1$  and  $4d^{10}4f^1v \rightarrow 4d^94f^2v$  photoexcitations (v refers to a hole in the valence state). Miyahara *et al.*<sup>10</sup> have measured the 4d photoabsorption spectra of La, LaF<sub>3</sub>, Ba, and BaF<sub>2</sub>, and found the difference of the absorption structures between metallic Ba and BaF<sub>2</sub>, and between the amorphous and crystalline BaF<sub>2</sub>. They have suggested that the amount of hybridization of 5f or 6f states with a  $4d^94f^1$  (<sup>1</sup>P) state or continuum states is independent on the crystal structure. These results indicate that the decay process of  $4d^94f^{m+1}$  states is not completely interpretable within an atomic picture.

pretable within an atomic picture. Recently we<sup>14,15</sup> have investigated decay processes of 4d excited states in Cs halides and BaF<sub>2</sub> and LaF<sub>3</sub> by means of resonant photoemission spectroscopy, and found that their 4d excited states decay dominantly through the N<sub>4,5</sub>-O<sub>2,3</sub>O<sub>2,3</sub> Auger process, where N<sub>4,5</sub> denotes the initial N<sub>4</sub> or N<sub>5</sub> hole and O<sub>2,3</sub> denotes the final O<sub>2</sub> or O<sub>3</sub> hole state, and that the localization of the 4d excited states is not constant over the 4d excitation region. The purpose of the present study is to examine the decay process of the 4d<sup>9</sup>4f<sup>1</sup> excited states in Ba halides in more detail, because they have no 4f electrons in the ground state, but have a 4f electron with a 4d hole in the excited state as Cs, La, and some Ce compounds.

### **II. EXPERIMENTAL PROCEDURES**

Photoelectron experiments were carried out by using synchrotron radiation from an electron storage ring at the Institute for Solid State Physics of the University of Tokyo. The spectral band width of a 2-m grazingincidence monochromator was about 0.18 eV at the photon energy of 90 eV, and the electron-analyzer resolution was constant with a full width at half maximum (FWHM) of 0.4 eV. Barium halides were prepared *in situ* by evaporation onto gold substrates. The absorption measurements were performed by using synchrotron radiation from a 750-MeV storage ring (UVSOR) at the Institute for Molecular Science. A 2-m Grasshopper monochromator was used for the present measurement. The spectral width was set to be the same as that of the monochromator used for the measurement of the photoelectron spectra. The other experimental procedures have been described in detail in Refs. 14 and 15.

# **III. EXPERIMENTAL RESULTS**

Figures 1 and 2 show sets of photoelectron spectra of BaCl<sub>2</sub> and BaBr<sub>2</sub>, respectively, which were obtained with various photon energies around the Ba 4d threshold. The photon energy of 90.5 eV and 94.2 or 94.3 eV corresponds to the excitation energy of the  ${}^{3}P$  and  ${}^{3}D$  multiplet states  $(4d^{9}4f^{1})$ , respectively, while the other photon energies are shown with an equal distance in energy. The binding energies are given relative to the top of the valence band. The ordinate is proportional to the number of photoelectrons per unit incident photon flux. The spectral distribution of incident photon flux was determined from a photoelectric yield spectrum of gold. The valence-band spectrum of BaCl<sub>2</sub> shows a single peak, while that of BaBr<sub>2</sub> consists of a peak and a shoulder on its higher binding-energy side. Two components observed in the valence spectrum of BaBr<sub>2</sub> are attributed to the spin-orbit splitting of Br 4p orbitals. The outermost s level of the halogen was appreciable between the Ba  $5p_{1/2}$ 

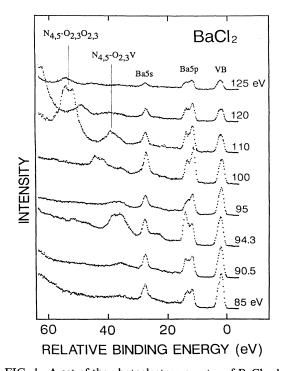


FIG. 1. A set of the photoelectron spectra of  $BaCl_2$  obtained with various photon energies around the Ba 4*d* excitation energy. The binding energy is given relative to the top of the valence band. The intensities are normalized to the incident photon flux.

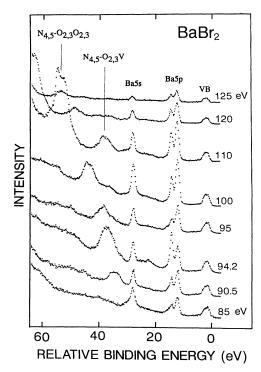


FIG. 2. A set of the photoelectron spectra of  $BaBr_2$  obtained with various photon energies around the Ba 4*d* excitation energy. The binding energy is given relative to the top of the valence band. The intensities are normalized to the incident photon flux.

and Ba  $5p_{3/2}$  spectra in BaCl<sub>2</sub>, but could not be clearly observed in BaBr<sub>2</sub>. By taking account of the binding energy, it is supposed that the Br 4s level is buried in the tail of the Ba  $5p_{3/2}$  spectrum in BaBr<sub>2</sub>. The binding energies of the valence band and the inner-core levels in the energy-distribution curves are listed in Table I (see Fig. 2 and Table I in Ref. 15 for BaF<sub>2</sub>).

The  $N_{4,5}$ - $O_{2,3}$  and  $N_{4,5}$ - $O_{2,3}V$  Auger electron peaks are observed when the excitation-photon energy is beyond 90 eV. Kinetic energies of the Auger electron peaks, which

TABLE I. The binding energies of valence-band and innercore levels, as well as the kinetic energies of Auger electrons observed at 110 eV. Energies are relative to the top of the valence band and are given in electron volts.

	BaCl <sub>2</sub>	BaBr <sub>2</sub>
Valence band	2.0	1.2/2.4
Ba $5p_{3/2}$	11.4	12.2
$5p_{1/2}$	13.6	14.3
Ba 5s	27.0	27.8
Br $3d_{5/2}$		66.2
$3d_{3/2}$		67.0
Ba $4d_{5/2}$	87.0	87.8
$4d_{3/2}$	89.6	90.4
N <sub>4,5</sub> -O <sub>2,3</sub> V	71.2	71.4
N <sub>4,5</sub> -O <sub>2,3</sub> O <sub>2,3</sub>	56	55.4
	58.4	57.8

were measured at an excitation-photon energy of 110 eV, are also shown in Table I with respect to the top of the valence band for convenience. The Auger electron peaks and Ba 5p photoelectron peaks are enhanced beyond the threshold of the Ba 4d excitation. In order to see the photon-energy dependence of these enhancements in more detail, the constant-final-state (CFS) spectra with the final state corresponding to the kinetic energy of the  $N_{4,5}$ - $O_{2,3}O_{2,3}$  Auger electron and the constant-initialstate (CIS) spectra with the initial states at the peak of the Ba 5p level were observed. The results are shown in Figs. 3 and 4, together with the Ba- $N_{4,5}$  absorption spectra, whose absorption coefficient is given on the righthand side of the figures.

As seen in Figs. 3 and 4, absorption spectra of BaCl<sub>2</sub> and BaBr<sub>2</sub> show sharp lines A and B due to the  $4d^94f^{\tilde{1}}$ multiplet  $({}^{3}P$  and  ${}^{3}D)$  and structures C through H originating from the  $4d^94f^{1}P$  states. The other states such as  $4d^9nf^1$  states (n = 5, 6, and so on) may mix into the structures. The CFS spectra with the final state at the  $N_{4,5}$ - $O_{2,3}O_{2,3}$  Auger electron peak and the  $5p_{1/2}$ -CIS spectrum (the CIS spectrum with the initial state at the Ba  $5p_{1/2}$  level) show sharp lines and structures corresponding to the absorption lines and structures in Ba halides. Strictly speaking, the kinetic energy of the N4,5-O<sub>2,3</sub>O<sub>2,3</sub> Auger electron shifts due to a two-hole-andone-electron interaction<sup>14</sup>) and the CFS spectra contain the background due to the inelastic scattering of Ba 5p, Ba 5s, halogen s, and valence-band photoelectrons. However, the amount of the energy shift is small (less than 1.2

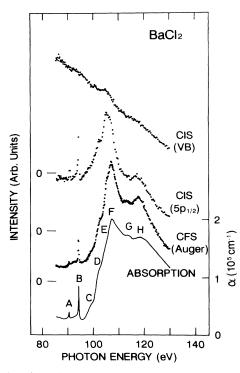


FIG. 3. The valence-band CIS, Ba  $5p_{1/2}$  CIS, CFS, and absorption spectra of BaCl<sub>2</sub>. The absorption coefficient is given on the right-hand side of the figure.

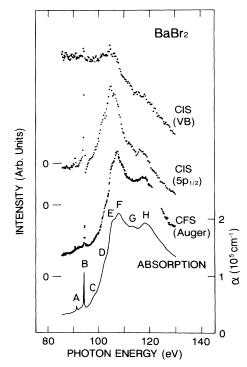


FIG. 4. The valence-band CIS, Ba  $5p_{1/2}$  CIS, CFS, and absorption spectra of BaBr<sub>2</sub>. The absorption coefficient is given on the right-hand side of the figure.

eV) relative to the bandwidth of Auger electrons (the full width at half maximum is about 5 eV), and the background due to the inelastic scattered electrons is smooth and small in comparison with the Auger electron intensity, and then these do not change drastically the spectral feature of the observed CFS spectra.

Intensity distributions of the CFS and absorption spectra in BaCl<sub>2</sub> and BaBr<sub>2</sub> are similar to each other, while the intensity distribution of the 5*p*-CIS spectra is much different from that of the absorption spectra. These results are in good agreement with that for BaF<sub>2</sub> reported in Ref. 15. It should be noted that the enhancement of the  $5p_{1/2}$ -CIS spectra is remarkable for peak *B*, due to the  $4d^94f^1$  (<sup>3</sup>*D*) state, and the enhancement becomes larger in the order of BaF<sub>2</sub>, BaCl<sub>2</sub>, and BaBr<sub>2</sub>. On the other hand, the valence-band intensity of BaCl<sub>2</sub> decreases with little enhancement for peak *E*, as the photon energy is increased, while that of BaBr<sub>2</sub> shows the enhancement for peaks *B* and *F*. This is in contrast to the valence-band CIS spectrum of BaF<sub>2</sub>, which does not show any enhancement around the Ba 4*d* excitation photon energy.

#### **IV. DISCUSSION**

Absorption spectra from 4d levels in Xe and Xe-like ions are characterized by huge peaks and weak sharp lines. These structures have been explained within an atomic picture,<sup>2-13</sup> and the huge peaks observed in Ba<sup>++</sup> (Z = 56) and La<sup>+++</sup> (Z = 57) have generally been attributed to a  $4d^94f^1$  (<sup>1</sup>P) state autoionized into the continuum, while sharp lines have been considered to be due to the multiplet structures of  $4d^{9}4f^{1}$  states located below the ionization threshold. Previously the present authors<sup>14,15</sup> investigated the nonradiative decay of the 4dexcited states in Cs halides, BaF2, and LaF3, and proposed the following nonradiative decay processes as dominant ones: (1) The N<sub>4,5</sub>-O<sub>2,3</sub> direct-recombination process, where an excited electron and a 4d hole recombine, resulting in the excitation of the 5p electron. The finalstate configuration of this direct recombination process is the same as that of the direct photoexcitation of the 5pelectron, and thus this process causes the enhancement of the 5p-CIS spectrum. (2) The  $N_{4,5}$ - $O_{2,3}O_{2,3}$  Auger process, where a 4d hole and a 5p electron recombine with the energy transferring to another 5p electron. This Auger decay process creates the N4,5-O2,3O2,3 Auger electrons.

As seen in Figs. 3 and 4, the 5*p*-CIS and CFS spectra of  $BaCl_2$  and  $BaBr_2$  show enhancements in the energy range of Ba 4*d* excitation, indicating that the above nonradiative decay processes exist in these compounds. It should be noted that the CFS spectra are similar in shape to corresponding absorption spectra. This indicates that 4*d*-excited states in  $BaCl_2$  and  $BaBr_2$  decay dominantly through the N<sub>4,5</sub>-O<sub>2,3</sub>O<sub>2,3</sub> process [process (2) mentioned above], and is consistent with the fact that strong Auger peaks are observed in Figs. 1 and 2. This result is the same as in cesium halides,  $BaF_2$ , and  $LaF_3$  (Refs. 14 and 15).

In contrast, the spectral features of the 5*p*-CIS spectra of BaCl<sub>2</sub> and BaBr<sub>2</sub> are much different from those of the absorption spectra. This indicates that the probability of the 4*d*-excited states through the N<sub>4,5</sub>-O<sub>2,3</sub> decay process is not constant over the Ba N<sub>4,5</sub> excitation region. The decay probability of the N<sub>4,5</sub>-O<sub>2,3</sub> process can be estimated from the 5*p*-CIS and the absorption spectra according to the following formula:

$$P = \frac{\Delta I_{5p}(hv) / I_{5p}(hv)}{\alpha_{4d}(hv) / \alpha_{5p}(hv)} , \qquad (1)$$

where  $\Delta I_{5p}$  and  $I_{5p}$  are the incremental enhancement of the Ba 5p photoelectron intensity due to the N<sub>4,5</sub>-O<sub>2,3</sub> process and the Ba 5p photoelectron intensity without any resonant enhancement, respectively. Also,  $\alpha_{4d}$  and  $\alpha_{5p}$  are parts of the absorption coefficient due to the formation of 4d-excited states and due to the transition from the Ba 5p level to the continuum, respectively. The derivation of the formula has been reported in detail elsewhere.<sup>14</sup>

The estimated decay probability of peak B due to the  $4d^94f^1$  (<sup>3</sup>D) state in BaF<sub>2</sub>, BaCl<sub>2</sub>, and BaBr<sub>2</sub> is 1%, 3.5%, and 12%, respectively, while that of peak E at 103 eV (the <sup>1</sup>P state) is 0.8%, 2%, and 6%, respectively. It is noteworthy that the decay probability of the <sup>3</sup>D state is larger than that of the <sup>1</sup>P state in all of the barium halides. This is consistent with the idea that the <sup>3</sup>D state is well localized below the ionization threshold, while the <sup>1</sup>P state above the threshold must be extended to be autoionized.<sup>2,14</sup>

Figure 5 shows the detailed comparison of the Ba 5p photoelectron spectra around the excitation photon ener-

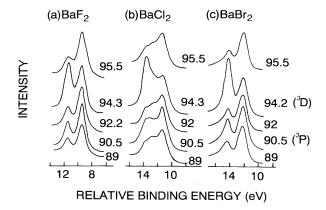


FIG. 5. Detailed comparison of Ba 5p photoelectrons around the excitation photon energy of the  ${}^{3}P$  and  ${}^{3}D$  states.

gy for  ${}^{3}P$  and  ${}^{3}D$  states. The intensity ratio between Ba  $5p_{1/2}$  and  $5p_{3/2}$  photoelectrons changes remarkably in Ba halides, although the Cl 3s photoelectron appears between Ba  $5p_{1/2}$  and  $5p_{3/2}$  photoelectrons in BaCl<sub>2</sub>. The intensities of Ba  $5p_{1/2}$  and  $5p_{3/2}$  photoelectrons, which were derived from the set of photoelectron spectra by subtracting the contributions of the background and Cl 3s photoelectrons, are shown in Fig. 6. The intensity of the Ba  $5p_{1/2}$  photoelectron is normalized at 89 eV in the figure. The contribution of photoelectrons from the Br 4s level could not be subtracted, since it is buried under the Ba  $5p_{3/2}$  level. As seen in these figures, the intensity ratio of the  $5p_{1/2}$  to  $5p_{3/2}$  photoelectrons deviates from the statistical weight  $(\frac{1}{2})$  at 90.5 and 94.3 eV, which correspond to the excitation photon energy of the  ${}^{3}P$  and  ${}^{3}D$ states, respectively. This anomalous intensity ratio can be interpreted in terms of the different branching ratio in nonradiative decay of  $4d^94f^1$  states into  $5p_{1/2}^{-1}6d^1$  and  $5p_{3/2}^{-1}6d^1$  states. Recently, Ogasawara *et al.*<sup>17</sup> have succeeded in explaining the anomalous intensity ratio between La  $5p_{1/2}$  and  $5p_{3/2}$  photoelectrons in LaF<sub>3</sub> by taking account of the multiplet dependence of the transition probabilities for the direct-recombination process. Their calculation agrees qualitatively with the present results for Ba halides.

Previously, Miyahara *et al.*<sup>10</sup> found the difference in the giant Ba 4d absorption structures between metallic

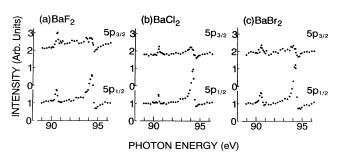


FIG. 6. Detailed comparison of Ba  $5p_{3/2}$  and  $5p_{1/2}$  photoelectron intensities derived from a set of photoelectron spectra. The Ba  $5p_{1/2}$  intensity obtained with 89 eV is normalized.

Ba and BaF<sub>2</sub>, and between amorphous and crystalline BaF<sub>2</sub>. They suggested that the amount of hybridization of 5f or 6f states with the  $4d^94f^{1}P$  state or continuum states are dependent on the crystal structure. As mentioned above, the nonradiative decay probability of  ${}^{3}D$ and  ${}^{1}P$  states through the N<sub>4,5</sub>-O<sub>2,3</sub> process increases in the order of BaF<sub>2</sub>, BaCl<sub>2</sub>, and BaBr<sub>2</sub>. This result shows that the solid-state effects occur for the  ${}^{3}D$  state below the 4d threshold as well as the  ${}^{1}P$  state autoionized into the continuum. Moreover, as shown in Fig. 6, the anomalous intensity ratio of  $5p_{1/2}$  to  $5p_{3/2}$  photoelectrons becomes larger in the order from  $BaF_2$  to  $BaBr_2$ . As mentioned above, the calculation by Ogasawara *et al.*<sup>17</sup> agrees qualitatively with the observed anomalous intensity ratio. Although their calculation cannot explain the observed difference in the intensity ratio among barium halides since their calculation is limited within an atomic picture, the matrix elements for direct recombination decay depend on the radial integrals of  $4d^94f^1$  and  $5p^5\epsilon d^1$  states. Thus we suggest that the spatial distribution as well as the nonradiative decay probability of  $4d^94f^1$  states are affected not only by the atomic-wave-function collapse due to a 4d hole, but also by the crystalline field in barium halides.

As seen in Figs. 3 and 4, and Fig. 4 in Ref. 15, the  $N_{4.5}$ -V decay process, where a 4d hole and an excited electron recombine with the energy being transferred to valence electrons, is not appreciable in BaF<sub>2</sub>, but is weakly observed in BaCl<sub>2</sub> and clearly seen in BaBr<sub>2</sub>. The decay probability of the  ${}^{3}D$  state (the peak B) through the N<sub>4.5</sub>-V process in BaF<sub>2</sub>, BaCl<sub>2</sub>, and BaBr<sub>2</sub> is 0%, 0%, and 1.3%, respectively, while that of peak E is 0%, 1%, and 2%, respectively. This shows that the mixing of the barium and halogen wave functions in the valence band becomes larger in the order from BaF<sub>2</sub> to BaBr<sub>2</sub>. This is consistent with the fact that the ionicity of the halogen ion is in the order from  $Br^-$  to  $F^-$ . As mentioned above, the decay probability of <sup>1</sup>P through the  $N_{4,5}$ - $O_{2,3}$  process is smaller than that of  ${}^{3}D$  in barium halides. This is consistent with the above idea based on the wave-function mixing between barium and halogen ions, since the  $P^{-1}$ state spreads spatially more than the  $^{3}D$  state, resulting in the wave-function mixing. The anomalous increase in the branching ratio between  $5p_{1/2}$  and  $5p_{3/2}$  photoelectrons is also consistent with this idea, since the mixing of barium and halogen wave functions may change the matrix elements for direct recombination decay through the  $N_{4,5}$ - $O_{2,3}$  process, resulting in an increase in the intensity ratio of  $5p_{1/2}$  to  $5p_{3/2}$  photoelectrons.

On the other hand, the fact that the decay probability of the  $N_{4,5}$ - $O_{2,3}$  process increases in the order of BaF<sub>2</sub>,

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BaCl<sub>2</sub>, and BaBr<sub>2</sub> is not easily understood in terms of the mixing of barium and halogen wave functions. One might imagine that, as the mixing is increased from BaF<sub>2</sub> to BaBr<sub>2</sub>, the  $4d^94f^1$  states become delocalized, to result in the decrease in the  $N_{4,5}$ - $O_{2,3}$  decay process. This is not the case. Then we suggest that if the mixing of the wave functions decreases the  $N_{4,5}$ - $O_{2,3}O_{2,3}$  process more than the  $N_{4,5}$ - $O_{2,3}$  process, the decay probability of the  $N_{4,5}$ -O<sub>2,3</sub> process may increase as the present experimental result. This is because the decay probability is determined by the competition between various decay processes. In fact, the ratio of the integrated intensity of the  $N_{4.5}$ -O<sub>2,3</sub>O<sub>2,3</sub> Auger electron peak to the incremental enhancement of Ba 5p photoelectrons  $(\Delta I_{5p})$  decreases in going from  $BaF_2$  to  $BaBr_2$  (see Figs. 1 and 2, and Fig. 3 in Ref. 15). Further theoretical studies, however, are needed to confirm the present suggestion.

In conclusion, the nonradiative decay of  $4d^{9}4f^{1}$  states in Ba halides was investigated by using resonant photoemission spectroscopy with synchrotron radiation. It was found that the CFS spectra agree in shape with the absorption spectra, indicating that the  $4d^{9}4f^{1}$  states decay dominantly through the Auger process. On the other hand, the CIS spectra with the initial states at the Ba 5plevel and the valence band were also found to be enhanced around the Ba N<sub>4,5</sub> excitation energy region, indicating the decay processes through a direct recombination between a 4d hole and an excited electron. Spectral features of the 5p-CIS spectra did not coincide with those of the absorption spectra. The intensity ratio of  $5p_{1/2}$  to  $5p_{3/2}$  photoelectrons showed the anomalous increase for the  ${}^{3}D$  state. Moreover, the probability through the direct recombination process and the degree of the anomalous branching ratio showed the increase in the order from BaF<sub>2</sub> to BaBr<sub>2</sub>. From these results, we suggested that the localization of  $4d^94f^1$  states is not constant over the Ba N<sub>4.5</sub> excitation energy region, and that the spatial distribution as well as the nonradiative decay probability of  $4d^94f^1$  states are affected by the crystalline field, as well as the atomic-function collapse due to a 4d hole.

### ACKNOWLEDGMENTS

The authors would like to express their sincere thanks to the staffs of the INS-SOR facility of the University of Tokyo, and members of the UVSOR facility of the Institute of Molecular Science, who helped them conduct photoelectron and absorption experiments. They also thank Professor A. Kotani of the University of Tokyo for discussions.

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