# Thermoluminescence mechanism in CdF<sub>2</sub>:Eu

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A model explaining all the features of the complex thermoluminescence (TL) process in CdF<sub>2</sub>:Eu is presented, based on extensive optical and EPR studies. It is shown that two types of europium centers are active in the TL process: the charge-compensated  $Eu^{3+}-O_s^{2-}$  or  $Eu^{3+}-F_i^{-}$  complexes (the centers dominating the photoluminescence under uv excitation), which act as the source of electrons as well as recombination centers, and the  $Eu^{3+}$  centers with cubic site symmetry, which are the electron traps. The TL excitation proceeds via the allowed intra-impurity transition of the fluorine (oxygen) coactivator, and the electrons are autoionized from the coactivator excited states through a lattice-relaxation-induced potential barrier. The different barriers for electron recapture by the ionized fluorine and oxygen coactivators are shown to be responsible for the different activation energies observed in the thermoluminescence of  $Eu^{3+}-O_s^{2-}$  and  $Eu^{3+}-F_i^{-}$  centers.

### I. INTRODUCTION

The continuous interest in the studies of rare-earth activated wide band-gap compounds is stimulated by their various possible applications. For example, such compounds as  $CaSO_4$  can be widely used in thermoluminescence (TL) dosimetry. It was shown that the TL response of  $CaSO_4$ :Eu to uv radiation is several orders of magnitude greater than that of any other related material.<sup>1</sup> The extremely bright thermoluminescence<sup>2</sup> observed by us in CdF<sub>2</sub>:Eu has, therefore, attracted our interest. In this paper we present a comprehensive study of the thermoluminescence processes in CdF<sub>2</sub>:Eu.

The nature of the complex photoluminescence (PL) in CdF<sub>2</sub>:Eu has been studied in detail by many authors, see, e.g., Refs. 3-5. The general outcome of all these studies is that a whole range of different  $Eu^{3+}$  centers, by which we mean Eu<sup>3+</sup> ions with different local site symmetries, are active in the PL. For example, in the studies of Sun-Il Mho and Wright<sup>5</sup> 17 different Eu<sup>3+</sup> centers have been observed. The reason for the occurrence of such a large number of centers is that the additional positive charge of  $Eu^{3+}$  (which substitutes the  $Cd^{2+}$  ion in the lattice) requires charge compensation, which can be different depending on sample preparation. Typically, europium is introduced as EuF<sub>3</sub> or Eu<sub>2</sub>O<sub>3</sub> and the charge compensation is realized then mainly by interstitial fluorine ions  $(\mathbf{F}_i^{-})$  or by substitutional oxygen ions  $(\mathbf{O}_s^{2-})$ , respectively. In the case when the compensating ions are located close to Eu<sup>3+</sup>, i.e., oxygen is at the nearest anion site in the [111] direction and fluorine is at the nearest interstitial position in the [100] direction, the so-called  $C_{3v}$ and  $C_{4\nu}$  centers of Eu<sup>3+</sup> are formed. These two types of centers together with the  $C_{2\nu}$  center, which consists of a Eu<sup>3+</sup>-Eu<sup>3+</sup> pair with two close-lying interstitial fluorine ions, play a dominant role in the PL in our crystals.

What distinguishes the  $C_{3v}$  and  $C_{4v}$  centers from the other centers observed is that they are most efficiently excited via broad bands in the uv region, whereas other Eu<sup>3+</sup> associates require site-selective excitation. The broad-band excitation process for  $C_{3v}$  centers has been previously studied by one of the authors.<sup>3</sup> It was found that the uv illumination induces the allowed  $2p \rightarrow 3s$  transition  $({}^{1}S_{0} \rightarrow {}^{1}P_{1})$  within the coactivator  $O_{s}^{2-}$  (or  $F_{i}^{-}$ ) and the excitation energy is then transferred to the Eu<sup>3+</sup> ion resulting in Eu<sup>3+</sup> radiative deexcitation. These facts are recalled here because, as it will be shown, the thermoluminescence in our crystals is dominated by the emissions of  $C_{3v}$  and  $C_{4v}$  centers.

Since in the TL process the optically induced electrons are stored at excited metastable states and the process of their release is thermally activated, it should be first of all determined whether the TL process is localized and some metastable excited state of the Eu<sup>3+</sup>-coactivator pair is involved, or nonlocalized, i.e., the Eu<sup>3+</sup>-coactivator pairs are ionized. In the latter case the nature of the electron trap and the mechanism of the thermally activated deexcitation process should be established. These problems will be discussed in Sec. IV. We will show that the TL process in CdF<sub>2</sub>:Eu is activated by charge-transfer processes from PL active  $C_{3v}$  and  $C_{4v}$  Eu<sup>3+</sup> complexes to isolated Eu<sup>3+</sup> centers forming Eu<sup>2+</sup> donor states in the CdF<sub>2</sub> lattice.

We acknowledge here the previous attempts to solve the above-listed problems.<sup>6-11</sup> However, despite intensive studies the mechanism of the CdF<sub>2</sub>:Eu TL has remained unclear. Though most of the results seem to point to a nonlocalized process, with the Eu<sup>2+</sup> donor being the electron trap, the activation energies of the TL were larger than the Eu<sup>2+</sup> activation enthalpy. The second difficulty was the understanding of the TL excitation process.

## **II. EXPERIMENT**

The Eu<sup>3+</sup> PL was excited with a high-pressure mercury lamp and a double-quartz monochromator. The PL and TL spectra were measured using a GDM 1000 monochromator, a Hamamatsu cooled photomultiplier, and a lock-in amplifier. The excitation spectra were recorded in the same experimental setup but using a high-pressure xenon lamp. To measure the TL glow curves the samples were illuminated at 100 K and then heated up to room temperature with the rate of 0.011 K/s. The absorption was measured in the range  $0.2-20 \ \mu m$  with use of Carl-Zeiss-Jena IR and UV-VIS specords, Cary 17 and Hitachi-Perkin-Elmer spectrometers.

The EPR measurements were performed on a standard BRUKER X-band spectrometer. A high-pressure xenon lamp, monochromator, and a set of Carl-Zeiss Jena interference filters were used for sample illumination.

The crystals were grown by the Bridgman-Stockbarger method from powdered  $CdF_2$  purified by several zonemelting runs and mixed with 1 mol % and 0.1 mol % of  $EuF_3$  or  $Eu_2O_3$ . Some of the samples were additionally annealed in  $F_2$  or  $O_2$  vapor at 500 °C to increase the concentration of  $C_{4v}$  and  $C_{3v}$  centers, respectively. Conversion from the 3+ to 2+ charge state of Eu was obtained by annealing the crystals in H<sub>2</sub> atmosphere at temperatures between 300 °C and 600 °C for a few minutes up to 1 h depending on the desired level of conversion.

### **III. RESULTS**

Detailed PL studies revealed that the as-grown samples contained  $Eu^{3+}$  centers of  $C_{2v}$  symmetry ( $Eu^{3+}-Eu^{3+}$ pairs compense ed by two close-lying interstitial fluorine ions), centers if  $C_{3v}$  symmetry ( $Eu^{3+}$  compensated by an oxygen ion eplacing one of the nearest-neighbor fluorine ligands), and centers of  $C_{4v}$  symmetry (Eu<sup>3+</sup> compensated by a fluorine ion at the nearest interstitial site). A weak PL spectrum of isolated  $Eu^{3+}$  centers ( $O_h$  symmetry) could be also observed. The relative concentrations of these centers depend on the sample preparation. The type of center which dominates in the PL could be changed by first converting the crystal and then annealing in  $F_2$  or  $O_2$  atmosphere (to obtain  $C_{4v}$  or  $C_{3v}$  centers, respectively). For illustration the PL spectra corresponding to the strong  ${}^{5}D_{0} \rightarrow {}^{7}F_{1}$  magnetic dipole transition of  $Eu^{3+}$  for all four symmetries, as measured for the asgrown 1 mol % Eu sample, are shown in Fig. 1(a). The figure shows collected data as the centers have different excitation spectra and, in principle, cannot be all observed simultaneously. The number of lines observed for a given symmetry reflects the crystal-field splitting of the  ${}^{7}F_{1}$  state. For the cubic symmetry the  ${}^{7}F_{1}$  state is unsplit whereas for the lowest  $C_{2v}$  symmetry the degeneracy is totally lifted. For the  $C_{4v}$  and  $C_{3v}$  centers the  ${}^7F_1$  state splits into a singlet  $A_2$  and a doublet E. The transition to the E doublet for  $C_{3v}$  centers occurs at a lower energy



FIG. 1. (a) Collected PL spectra corresponding to the strong  ${}^{5}D_{0} \rightarrow {}^{7}F_{i}$  transition of Eu<sup>3+</sup> in the as-grown CdF<sub>2</sub>:Eu 1 mol % sample. The emission lines attributed to Eu<sup>3+</sup> centers of  $C_{2v}, C_{3v}, C_{4v}$ , and  $O_{h}$  symmetries are marked. (b) PL (dashed line) and TL (solid line) spectra observed in the same sample under 265.5-nm (left) and 315-nm excitations.

 $(16\,692\ \mathrm{cm}^{-1})$  and is not shown in the figure.

The  $C_{2v}$  and  $O_h$  centers are excited only by narrow lines corresponding to the intrashell transitions of Eu<sup>3+</sup>, whereas the most efficient excitation of the  $C_{3v}$  and  $C_{4v}$ centers proceeds via broad, Gaussian-shaped bands in the uv region with the maxima at 254 nm (4.88 eV) and 286 nm (4.34 eV), respectively. The same bands can be also observed in the absorption spectra of samples with high concentrations of  $C_{3v}$  and  $C_{4v}$  centers, and have been shown to be due to allowed  $2p \rightarrow 3s$  transitions of the  $O_s^{2-}$  (254 nm) and  $F_i^{-}$  (286 nm) coactivators.<sup>3</sup> In Fig. 2 the absorption and excitation spectra for  $C_{4v}$  and  $C_{3v}$ centers are shown. The measurements have been performed on samples annealed in fluorine and oxygen vapor, respectively.

In the TL spectra only the emission of  $C_{3v}$  and  $C_{4v}$  centers was observed. The brightest TL was obtained in the as-grown CdF<sub>2</sub>:Eu 1% sample. The TL spectra induced by two different illuminations (265.5 and 315 nm) are shown in Fig. 1(b) and compared to the PL spectra observed under the same excitation. It can be seen that no emission of  $C_{2v}$  centers is observed in the TL though it dominates in the PL spectrum. Moreover, the relative intensities of the  $C_{4v}$  and  $C_{3v}$  emissions are different in TL and PL.

To clear up the mechanism of energy storage leading to TL we measured the CdF<sub>2</sub> absorption before and after 15 min of uv excitation at 77 K. We employed a Hitachi-Perkin-Elmer spectrometer with a memory system which allows to measure very small absorption changes. The uv-light-induced changes of the absorption spectra are shown in Fig. 3 for two CdF<sub>2</sub>:Eu 0.1% samples, which were additionally annealed in oxygen but for different periods. Before the treatment both samples contained mainly  $C_{4v}$  centers. After long annealing practically only  $C_{3v}$  centers are present in the sample (Fig. 3 left-hand side), whereas the sample lightly annealed in oxygen contains both  $C_{4v}$  and  $C_{3v}$  centers (right-hand side). It can



FIG. 2. The absorption (solid lines) and PL excitation (dashed lines) spectra of (a)  $C_{4v}$  and (b)  $C_{3v}$  centers measured in CdF<sub>2</sub>:Eu 0.1% crystals annealed in (a) fluorine and (b) oxygen vapor. (c) The spectral dependence of the increase rate,  $\tau_i^{-1}$ , of the Eu<sup>2+</sup> EPR signal intensity under illumination measured in the as-grown CdF<sub>2</sub>:Eu 1 mol% sample. The data have been corrected for constant light intensity.

be seen that uv illumination leads to a decrease in the intensity of the coactivator absorption bands and to the appearance of an additional band, which is due to the  $4f^7 \rightarrow 4f^{6}5d^1$  transition of  $Eu^{2+}$ . The population of  $Eu^{2+}$  states is metastable and decreases with increasing temperature, while the TL intensity increases. The temperature dependence of the  $Eu^{2+}$  absorption is shown in Fig. 4(a) together with the TL glow curves for  $C_{3v}$  and  $C_{4v}$  centers, which were found to be slightly different. The activation energies obtained from the TL increase at low temperatures are  $360\pm15$  and  $440\pm15$  meV, respec-



FIG. 3. The absorption spectrum before illumination (solid line), and the absorption changes after 15 min of uv illumination at 77 K (dashed line) for two  $CdF_2:EuF_3$  0.1 mol % samples heavily (left-hand side) and lightly (right-hand side) annealed in oxygen.



FIG. 4. (a) Top: temperature dependence of the  $Eu^{2+}$  absorption coefficient (solid line) and the TL glow curves of  $C_{3v}$  (full circles) and  $C_{4v}$  (open circles) centers. Bottom: evaluation of the TL activation energies. (b) The temperature dependencies of the decay times  $\tau_d$  of the fast (full circles) and slow (open circles) components of the  $Eu^{2+}$  signal decay observed after the broadband uv illumination was turned off, as well as of the decay after the 254-nm excitation was turned off (triangles).

tively. It was found, moreover, that very long annealing, either in  $O_2$  or in  $F_2$  vapor, leads to a decrease of the efficiencies of both the TL and the  $Eu^{3+} \rightarrow Eu^{2+}$  photoconversion processes.

In all the samples in which TL was observed an EPR spectrum of  $Eu^{2+}$  was detected after illumination of the sample with uv light at low temperature. The same spectrum was observed in crystals converted by annealing in Cd or H<sub>2</sub> vapor. It consists of seven groups of lines, arising from the allowed  $\Delta M = 1$  transitions within the  ${}^{8}S_{7/2}$  ground multiplet of  $Eu^{2+}$ , with a rich hyperfine structure due to  $Eu^{151}$  and  $Eu^{153}$  isotopes with the natural abundances of 47.77% and 52.23%, respectively, both having a nuclear spin of  $I = \frac{5}{2}$ . The angular dependence of this spectrum was measured and is shown in Fig. 5 for the



FIG. 5. The angular dependence of uv-light-induced EPR spectrum of  $Eu^{2+}$  for the magnetic field rotated in the (110) plane. For the sake of simplicity only the center of gravity of each set of the 12 observed hyperfine structure lines is marked. The solid line represents the values calculated with use of the spin-Hamiltonian parameters given in Table I.

magnetic field rotated in the (110) plane.

In the CdF<sub>2</sub>:Eu 1 mol % sample, characterized by the brightest thermoluminescence, a weak EPR signal of  $Eu^{2+}$  was observed prior to illumination. The intensity of this signal was found to increase under illumination with uv light at temperatures below 230 K. The maximal concentration of photogenerated Eu<sup>2+</sup> centers was  $(1.6\pm0.4)\times10^{17}$  cm<sup>-3</sup> and was reached for temperatures below 160 K. In this temperature region the occupancy of  $Eu^{2+}$  states was found to be metastable (no decrease of the signal intensity was observed after the light had been turned off). The kinetics of the EPR signal increase under illumination were measured for various wavelengths of the incident light at 130 K. The increase rate  $\tau_i^{-1}$  of the Eu<sup>2+</sup> EPR signal intensity was determined from the initial rise of the kinetics and normalized to constant light intensity making use of the observed linear dependence of the increase rate on light intensity. As can be seen in Fig. 2(c) the  $Eu^{2+}$  photogeneration spectrum,  $\tau_i^{-1}(\lambda)$ , consists of two bands superimposed on each other, having the maxima at 288 and 254 nm. These bands correspond exactly to the PL excitation spectra of  $C_{4v}$ and  $C_{3v}$  centers, respectively. The relative intensities of these two bands were found to depend on temperature. As it turned out the increase rate of the  $Eu^{2+}$  EPR signal has a different temperature dependence for light energies from the  $C_{4v}$  and  $C_{3v}$  excitation regions.

The kinetics of  $Eu^{2+}$  photogeneration were measured as a function of temperature for two different illuminations coinciding with the excitation of  $C_{4v}$  centers (300 nm) and  $C_{3v}$  centers (254 nm). The temperature range was chosen so that no thermal depopulation of  $Eu^{2+}$ centers was taking place. The temperature dependence of the increase rates (determined from the initial rise of each kinetics) is shown in Fig. 6. The open and full circles denote the experimental values obtained for the 300- and

1000

 $\begin{array}{c} 800^{-} \\ 600^{-} \\ \hline \\ \\ 600^{-} \\ \hline \\ \\ 600^{-} \\ \hline \\ \\ 0^{-} \\ \hline \\ 0^{-} \\ \hline \\ 0^{-} \\ \hline \\ \\ 0^{-} \\ \hline \\ \\ 0^{-} \\ \hline 0^{-} \\ \hline \\ 0^{-} \\$ 

FIG. 6. The temperature dependence of the increase rate of the  $Eu^{2+}$  EPR signal intensity for two different excitations: 300 nm (open circles) and 254 nm (full circles).

254-nm excitations, respectively. It can be seen that for both illuminations the increase rate has a thermally activated character, however, the activation energies are different and equal to  $13\pm2$  meV for the light energy from the  $C_{4v}$  PL excitation region and  $56\pm7$  meV for the  $C_{3v}$  excitation. This implies that the ionization processes of  $F_i^-$  and  $O_s^{2-}$  coactivators are thermally activated with different activation energies.

At temperatures above 160 K the occupancy of lightinduced  $Eu^{2+}$  centers is no longer metastable and a slow decrease of the EPR signal intensity is observed after the light is turned off. It was found that after a broadband uv excitation the kinetics of the EPR signal decrease consisted of a sum of two exponential decays: a "fast" one, the contribution of which increases with increasing temperature, and a "slow" one. The temperature dependencies of the decay times  $\tau_d$  of the fast (full circles) and slow (open circles) components of the decrease are shown in Fig. 4(b). The two components are found to be exponentially dependent on temperature but are characterized by different activation energies: 451±28 meV for the fast component and  $352\pm17$  meV for the slow one. This indicates the existence of two different recombination centers and is consistent with the results of TL measurements. The two activation energies observed in the thermal depopulation of  $Eu^{2+}$  centers are close to the TL activation energies of  $C_{3v}$  (440±15 meV) and  $C_{4v}$  (360±15 meV) centers. When a selective excitation was used the kinetics of  $Eu^{2+}$  EPR signal decrease after the light was turned off showed a single-exponential behavior. The temperature dependence of the decay time after 254-nm excitation is shown in Fig. 4(b) (triangles). The decay time as well as the activation energy of this decay  $(440\pm17 \text{ meV})$  are comparable to those of the fast component observed when a broadband excitation was applied.

#### **IV. DISCUSSION**

### A. The nature of the thermoluminescence emission

As it is demonstrated in Fig. 1(b) the TL spectra are dominated by the emissions of  $C_{3v}$  and  $C_{4v}$  centers, those excited via coactivators. There is no emission of  $C_{2v}$ centers, though they are found to be the dominant centers in PL measured under the same excitation (the 315.5-nm excitation applied coincides with the  ${}^7F_J \rightarrow {}^5H_6$ intrashell transition of Eu<sup>3+</sup> in  $C_{2v}$  symmetry<sup>11</sup>). This fact indicates that the  $O_s^{2-}$  and  $F_i^-$  coactivators may play a decisive role in the TL process.

Figure 1(b) proves that the radiative deexcitation of  $C_{3v}$  and  $C_{4v}$  centers in both the TL and PL processes is identical, except that in the case of TL the radiative deexcitation process is thermally activated. On the other hand the results depicted in Fig. 3 show directly that after illumination with uv light at low temperature the intensities of the  $O_s^{2-}$  and  $F_i^{-}$  absorption bands are reduced and an absorption band appears,<sup>12</sup> which is due to the  $4f^7 \rightarrow 4f^{6}5d^{1}$  transition of Eu<sup>2+</sup>. This proves that during uv illumination oxygen and fluorine coactivators are ionized and the electrons are trapped by Eu<sup>3+</sup>

centers. At first view, this result seems to contradict earlier findings. It was previously shown that the broad, Gaussian-shaped band with the maximum at 254 nm is due to the internal  $2p^6 \rightarrow 2p^{5}3s^1$  transition of the oxygen coactivator, and does not have a photoionizing character.<sup>3</sup> Moreover, it was shown that recombination from the excited  $2p^{5}3s^1$  state results in very efficient energy transfer to  $Eu^{3+}$  within the  $C_{3v}$  complex. Now, it appears that the same transition induces free electrons which populate the  $Eu^{2+}$  centers. The only possible explanation of this puzzle is the possibility of ionization (autoionization) of the excited state of the coactivator, which would require its location close to the continuum of the conduction-band states. This model will be further confirmed in the following sections of this paper.

As can be seen in Fig. 4(a) the TL process and the population of the  $Eu^{2+}$  state are correlated. This opens the fundamental question what is the nature of the  $Eu^{3+}$ states which capture the electrons, are they isolated "cubic"  $Eu^{3+}$  centers or those constituting the  $Eu^{3+}$ coactivator pair. Some of the experimental results seem to point to the latter possibility. The TL activation energies of  $C_{4v}$  and  $C_{3v}$  centers are different and larger than the activation energy of the conductivity in chemically converted  $CdF_2$ :Eu crystals (which contain cubic Eu<sup>2+</sup> centers). This might be explained by the presence of close-lying coactivator ions disturbing the activation enthalpy of  $Eu^{2+}$ . Therefore, before further discussion of the TL nature the local symmetry of  $Eu^{2+}$  ions has to be determined. To this end we employed the EPR technique. The analysis of the EPR spectrum of the lightinduced  $Eu^{2+}$  centers is presented in Sec. IV B.

### B. The nature of the electron trap

Europium ions in CdF<sub>2</sub> can be incorporated in two charge states, Eu<sup>3+</sup> and Eu<sup>2+</sup>. The ground state of Eu<sup>3+</sup>, <sup>7</sup>F<sub>0</sub>, is diamagnetic and cannot be studied by means of the EPR technique. It is not the case for Eu<sup>2+</sup>, for which the ground state ( ${}^{8}S_{7/2}$ ) is easily observed. The EPR spectrum of Eu<sup>2+</sup> observed in our crystals after excitation with uv light is identical to the one observed after thermal conversion and agrees well with the spectrum reported previously<sup>13,14</sup> for cubic Eu<sup>2+</sup> centers in CdF<sub>2</sub>. The experimental results are well described with the spin Hamiltonian for a  ${}^{8}S_{7/2}$  octet ( $S = \frac{7}{2}$ ) in a crystal field of cubic symmetry:

$$H_{S} = g\beta \overline{S} \ \overline{B} + \frac{1}{60} b_{4} (O_{4}^{0} + 5 \ O_{4}^{4}) + \frac{1}{1260} b_{6} (O_{6}^{0} - 21 \ O_{6}^{4}) + \sum_{i} A_{i} \overline{S} \ \overline{I} ,$$

where g is the isotropic g factor,  $\beta$  is the Bohr magneton,  $A_i$  (i=151,153) are the hyperfine structure constants of the two Eu<sup>151</sup> and Eu<sup>153</sup> isotopes, and the two terms with  $b_4$  and  $b_6$  constants are the crystal-field terms. The parameters obtained from the fit of the above spin Hamiltonian to the experimental spectrum are summarized in Table I. For comparison the spin-Hamiltonian parameters as derived from previous studies<sup>14-16</sup> are also given. Moreover, there is a perfect agreement of the measured angular dependence of the spectrum with the one calculated using the same parameters and the formulas given by Lacroix<sup>17</sup> (see Fig. 5). All this proves that the Eu<sup>2+</sup> centers populated during uv excitation are isolated substitutional europium ions well separated from the  $F_i^-$  and  $O_s^{2-}$  coactivators.

This conclusion explains why only a small fraction (approximately 1%) of the  $C_{3v}$  and  $C_{4v}$  sites observed in the PL measurements were found to be active in TL. The TL efficiency is limited by the concentration of cubic  $(O_h)$  Eu<sup>3+</sup> centers acting as electron trap. This fact could not be understood in the case of an intrasite charge transfer.

## C. The activation enthalpy of the $Eu^{2+}$ electron trap

In order to construct the model of the thermoluminescence process the activation enthalpy (thermal-ionization energy at T=0 K) of the electron trap should be known. It has been previously found that after thermal conversion the CdF<sub>2</sub>:Eu crystals are conducting, with the dc conductivity characterized by a 330-meV activation energy.<sup>18</sup> However, since only the conductivity has been measured the exact value of the Eu<sup>2+</sup> activation enthalpy remained unknown. This is because the transport mechanism in the CdF<sub>2</sub> lattice is still not clear. The same difficulty will arise when discussing the emission and capture processes. The problem of appropriate descriptions of the  $\sigma_{dc}(T)$  dependence for different conductivity mechanisms is discussed, e.g., in Ref. 19.

The EPR technique would provide, apparently, a simple method to determine the ionization enthalpy of  $Eu^{2+}$ , by studying the temperature dependence of the  $Eu^{2+}$ EPR signal intensity, which is directly proportional to the concentration of  $Eu^{2+}$  centers. In conducting samples, however, the thermal depopulation of a center affects the signal intensity in two ways: directly, and indirectly—by effectively changing the sample volume penetrated by microwave radiation due to the increase of conductivity (the so-called skin effect). As it turns out, even in samples with relatively low  $Eu^{2+}$  concentration  $(10^{17} \text{ cm}^{-3})$  both these effects are of the same order of

TABLE I. Spin-Hamiltonian parameters for Eu<sup>2+</sup> in CdF<sub>2</sub>.

T (K)	g factor	$b_4$ (10 <sup>-4</sup> cm <sup>-1</sup> )	$b_6$ (10 <sup>-4</sup> cm <sup>-1</sup> )	$A_{151}$ (10 <sup>-4</sup> cm <sup>-1</sup> )	$A_{153}$ (10 <sup>-4</sup> cm <sup>-1</sup> )	Ref.
280	1.9918±0.0005	$-51.4{\pm}0.5$	0.24±0.2	$-33.9{\pm}0.2$	$-15.0\pm0.2$	this work
300	$1.9918 {\pm} 0.0005$	$-52.37{\pm}0.1$	$0.24{\pm}0.05$	$-33.9{\pm}0.15$	$-15.05{\pm}0.15$	Ref. 14
77	$1.9923 {\pm} 0.0006$	$-56.04{\pm}0.15$	$0.28 {\pm} 0.1$	$-34.15{\pm}0.15$	$-15.15{\pm}0.15$	Ref. 14
300	$1.9885 {\pm} 0.001$	$\pm 51.94 {\pm} 0.5$				Ref. 15
				$-34.2153{\pm}0.0007$	$-15.1865{\pm}0.0007$	ENDOR data (Ref. 16)



FIG. 7. The temperature dependence of the Eu<sup>2+</sup> EPR signal intensity in the CdF<sub>2</sub>:Eu 1% sample (without illumination). Eu<sup>2+</sup> concentration at 250 K was  $1.3 \times 10^{17}$  cm<sup>-3</sup>. The solid line is the calculated dependence for the sample with use of formulas given in Ref. 20.

magnitude and their influence on the signal intensity cannot be easily separated. In samples with higher  $Eu^{2+}$ concentration the skin effect is the dominating mechanism and though one can determine the conductivity from the data<sup>20</sup> the whole information on the source of the free carriers may be lost.

The decisive argument that the  $Eu^{2+}$  centers observed in absorption, EPR, and transport measurements are the same centers comes from the analysis of the temperature dependence of the Eu<sup>2+</sup> EPR signal intensity,  $I_{EPR}(T)$ , shown in Fig. 7. The data have been corrected for the temperature changes of the Zeeman-level occupation as well as the decrease of the cavity quality factor with increasing temperature.<sup>20</sup> These effects were controlled by the use of a probe sample measured together with the crystal studied. As already mentioned the  $I_{\rm EPR}(T)$ dependence is governed both by  $Eu^{2+}$  depopulation and by the skin effect. Making use of the information obtained from absorption studies we estimated the number of electrons ionized to the conduction band from  $Eu^{2+}$ and hence, taking the typical mobility in CdF<sub>2</sub> (10  $cm^2/Vs$ ) and assuming acoustic-phonon scattering, we estimated the sample conductivity  $\sigma(T)$ . Since in presence of the skin effect the decay of  $I_{EPR}(T)$  is a function<sup>20</sup> of  $\sqrt{\sigma(T)}$ , we were able to estimate the expected changes of  $I_{EPR}(T)$  due to the center depopulation and the skin effect. Such a procedure, which is based on the assumption that the sample conductivity is due to  $Eu^{2+}$  thermal ionization, allowed us to explain very well the  $I_{EPR}(T)$ experimental data. It can be seen that the calculated  $I_{\text{EPR}}(T)$  dependence (solid line in Fig. 7) follows the  $I_{\rm EPR}(T)$  changes. This result is the final verification that Eu<sup>2+</sup> centers are thermally ionized and that the activation enthalpy of this process is close to 330 meV.

#### D. Emission and capture processes of the coactivator

The formulas describing the emission and capture processes are well known.<sup>21-23</sup> The relation between the

emission  $(e_n)$  and capture  $(c_n)$  rates is obtained from the detailed balance condition and is given by

$$e_n = X_n c_n N_c \exp\left[-\frac{\Delta H_n}{kT}\right],$$
 (4.1)

where

$$X_n = \exp\left[\frac{\Delta S_n}{k}\right] \tag{4.2}$$

is the "entropy factor" containing the total change in entropy (due to the change of the vibrational frequency and electronic degeneracy) taking place when electrons are excited from donors to the conduction band. For the polar lattice of  $CdF_2$  the entropy factor cannot be simply partitioned into the vibronic and electronic components.  $\Delta H_n$  in Eq. (4.1) is the enthalpy needed to emit an electron from the donor to the conduction band, which may be called the activation enthalpy.<sup>24</sup>

The unknown entropy factor is not the only problem encountered in the analysis of emission and capture processes in CdF<sub>2</sub>. The concept of the emission and capture rate as defined above has been introduced for standard conduction-band transport and may not apply to the ionic CdF<sub>2</sub> compound. For example, the results of ac conductivity studies<sup>25</sup> may be interpreted by impurity band transport. Furthermore, the carrier mobility in CdF<sub>2</sub> (of the order of 10 cm<sup>2</sup>/V s) is in the range of typical mobilities in amorphous semiconductors.<sup>19</sup> For this reason the experimental results are analyzed in two approaches, one of which is based on formulas (4.1) and (4.2) and leads to the classical Arrhenius plots.

# 1. Photoexcitation of Eu<sup>2+</sup> centers. Ionization of the coactivator

It was shown in Secs. IV A and IV B that electrons induced in the conduction band during uv excitation are ionized from the excited states of oxygen and fluorine coactivators, and then captured by isolated  $Eu^{3+}$  centers. The kinetics of this process can be studied by measuring the increase of the EPR signal intensity of  $Eu^{2+}$ . The reverse process, i.e., the recapture of electrons thermally released from  $Eu^{2+}$  traps via the coactivator excited states, is responsible for the thermoluminescence. In this section the former process will be analyzed in detail. The latter will be discussed in Sec. IV D 2.

The uv-light-induced population of the  $Eu^{2+}$  states can be described by the following kinetics equations:

$$\frac{d}{dt}N_{(\mathrm{Eu}^{2+})} = nc_{\mathrm{Eu}}(N_{\mathrm{Eu}} - N_{(\mathrm{Eu}^{2+})}) - e_{\mathrm{Eu}}N_{(\mathrm{Eu}^{2+})}, \qquad (4.3)$$

$$\frac{d}{dt}n = e_{\mathrm{Eu}}N_{(\mathrm{Eu}^{2+})} - nc_{\mathrm{Eu}}(N_{\mathrm{Eu}} - N_{(\mathrm{Eu}^{2+})}) + p_{i,X}N_{(X^*)} - nc_XN_{(X^+)}, \qquad (4.4)$$

$$\frac{d}{dt}N_{(X^*)} = I\sigma_0(N_X - N_{(X^+)} - N_{(X^*)}) - (p_{i,X} + p_{r,X})N_{(X^*)} + nc_X N_{(X^+)} , \qquad (4.5)$$

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$$\frac{d}{dt}N_{(X^+)} = p_{i,X}N_{(X^*)} - nc_XN_{(X^+)}, \qquad (4.6)$$

and

$$N_{(X^+)} = N_{(Eu^{2^+})} - (N_{Eu} - N_A) + n$$
 (4.7)

In the Eqs. (4.3)–(4.7) the following notation is used.  $N_X$ is the concentration of  $F_i^-$  or  $O_s^{2-}$  centers prior to illumination;  $N_{(X^*)}$  is the light-induced population of the excited states of  $\mathbf{F}_i^{-}$  or  $\mathbf{O}_s^{2-}$ ;  $N_{(X^+)}$  is the concentration of the ionized coactivator centers  $(F_i^0 \text{ or } O_s^-)$ ; I is the light intensity;  $\sigma_0$  is the optical cross section for intraion excitation of the coactivators;  $p_{r,X}$  is the recombination rate of the europium-coactivator pair;  $p_{i,X}$  is the ionization rate of the excited state of the coactivator. If the process is thermally activated  $p_{i,X} = p'_{i,X} \exp(-E_{b1}/kT)$ , where  $E_{b1}$  is the effective height of the energy barrier for ionization;  $c_X$  is the electron capture rate by ionized coactivators, given by  $c_{\chi} = c'_{\chi} \exp(-E_{b2}/kT)$  when the capture process is thermally activated;  $E_{h2}$  is the effective height of the energy barrier for the process; n is the freeelectron concentration;  $N_{\rm Eu}$  is the total concentration of cubic Eu centers, whereas  $N_{({\rm Eu}^{2+})}$  is the concentration of  $Eu^{2+}$  centers;  $e_{Eu}$  is the electron emission rate from  $Eu^{2+}$ centers given by Eq. (4.1);  $c_{Eu}$  is the electron capture rate by cubic Eu<sup>3+</sup> centers. For classical conduction-band transport the  $e_{Eu}, c_{Eu}, c_X$ , and  $p_{i,X}$  terms are temperature dependent and are equivalent to the discussed above emission and capture rates connected by Eq. (4.1). In the Eqs. (4.3)-(4.7) we assume that the illumination which excites the coactivators does not ionize Eu<sup>2+</sup> states, which will be confirmed further on.

Before solving Eqs. (4.3)-(4.7) under the equilibrium condition we give a simple description of the Eu<sup>2+</sup> EPR signal rise after the light is turned on at low temperature. When the temperature is low enough the thermal emission of electrons from Eu<sup>2+</sup> states can be neglected, moreover, it can be assumed that electrons ionized to the conduction band are primarily captured by Eu<sup>3+</sup> centers and the term describing their recapture by ionized coactivators can be omitted (the validity of the latter assumption will be proved in the following section). Assuming that the concentrations of excited coactivator states and of photogenerated free electrons reach equilibrium much faster than the concentration of Eu<sup>2+</sup>

$$\left\lfloor \frac{d}{dt} N_{(X^*)} = \frac{d}{dt} n = 0 \right\rfloor,$$

which seems to be justified seeing that the typical increase rate of the  $Eu^{2+}$  EPR signal is about  $10^{-2} s^{-1}$ , the initial rise of the  $Eu^{2+}$  concentration can be approximated by

$$N_{(\mathrm{Eu}^{2+})}(t) - N_{(\mathrm{Eu}^{2+})}(0) \simeq [N_{\mathrm{Eu}} - N_{(\mathrm{Eu}^{2+})}(0)] \left[ \frac{t}{\tau_i} \right],$$

where

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$$N_{(\mathrm{Eu}^{2+})}(0) = N_{\mathrm{Eu}} - N_{A}$$

and

$$\tau_i^{-1} = \frac{I\sigma_0 N_X p_{i,X}}{N_A (p_{r,X} + p_{i,X})} .$$
(4.8)

The validity of the proposed approximation is confirmed by the observed linear dependence of the increase rate of the Eu<sup>2+</sup> EPR signal intensity  $\tau_i^{-1}$  on light intensity *I*.

According to Eq. (4.8)  $\tau_i^{-1}$  is proportional to the optical cross section for the coactivators excitation. The spectral dependence of  $\tau_i^{-1}$  should, therefore, reflect the excitation spectrum of the thermoluminescence. As can be seen in Fig. 2(c) the spectral dependence of the initial increase rate of the Eu<sup>2+</sup> EPR signal as measured for the CdF<sub>2</sub>:Eu 1% sample consists of two superimposed bands which are identical with the excitation bands of the  $C_{4v}$ and  $C_{3v}$  PL. The third weak band at lower energies indicates that there are some other centers in the sample which can be ionized, however, the process does not lead to Eu<sup>3+</sup> TL.

Equation (4.8) can be further simplified if we recall that the uv excitation results in a very strong photoluminescence and only a small number of the coactivators is ionized, hence  $p_{r,X} \gg p_{i,X}$ . Since I,  $N_X$ , and  $N_A$  are temperature independent, and the temperature dependencies of  $p_{r,X}$  and  $\sigma_0$  should be very weak, the exponential temperature dependence of  $\tau_i$  (see Fig. 6) indicates that the ionization of the coactivator is temperature activated,  $\tau_i^{-1} \propto p_{i,X} = p'_{i,X} \exp(-E_{b1}/kT)$ . The activation energy obtained is, therefore, equivalent to the effective height of the energy barrier  $E_{b1}$  for the ionization process. However, the magnitudes of the appropriate  $E_{b1}$  energies for fluorine and oxygen coactivators are uncertain. If we assume that  $p'_{i,X}$  is temperature independent these energies are  $13\pm 2$  meV for  $C_{4v}$  and  $56\pm 7$  meV for  $C_{3v}$  centers, as given in Table II. However, if we consider the classical description of the emission process  $p_{i,X}$  is equivalent to the emission rate and then  $p'_{i,X}$  depends on temperature as  $T^2$ . In such an approach the ionization of  $C_{4v}$  centers is not thermally activated, while in the case of  $C_{3\nu}$ centers the  $E_{b1}$  energy is reduced to 30 meV.

Equations (4.3)-(4.7) can be solved at the equilibrium condition:

$$\frac{d}{dt}N_{(Eu^{2+})} = \frac{d}{dt}n = \frac{d}{dt}N_{(X^*)} = \frac{d}{dt}N_{(X^+)} = 0.$$

For low excitation powers, as used in the experiment, the number of excited or ionized coactivators is much smaller than their total concentration, and hence  $N_X - N_{(X^*)} - N_{(X^+)} \cong N_X$ . Moreover, the light- and temperature-induced concentration of free electrons is small enough to be omitted in the charge neutrality equation (4.7) which can be approximated by  $N_{(X^+)} \cong N_{(Eu^{2+})} - (N_{Eu} - N_A) = N_{(Eu^{2+})} - N_{(Eu^{2+})}(0)$ . After applying these two approximations to Eqs. (4.3)-(4.7) we obtain

		$C_{4v}$ (meV)		$C_{3v}$ (meV)		
Activation energy		I	II	I	II	$O_h$ (meV)
$ au_i$	$E_{b1}$	13±2	0	56±7	30	
$ au_d$	$E_{\rm Eu}+E_{b2}$	352±17	317	450±28	414	
				440±17	407	
TL	$E_{\rm Eu} + E_{b2}$	360±15	335	440±15	415	
$I_{\rm EPR}$	$E_{\rm Eu} + E_{b2} - E_{b1}$	350±10	350 <sup>a</sup>			
$\sigma_{ m dc}{}^{ m b}$	$E_{\rm Eu}$					330
$\sigma_{ m ac}$	$E_{Eu}$					334±9°
						$326 \pm 9^d$
	$E_{b1}$	13	0	56	30	
	$E_{b2}$	33 <sup>e</sup>	0 <sup>f</sup>	110	80	

TABLE II. Summarized results of photo-EPR, thermoluminescence, and transport experiments. The activation energies were determined (I) disregarding any temperature dependence of the preexponential factors, (II) assuming standard conduction-band transport.

<sup>a</sup>This result is unaffected by any temperature-dependent preexponential factors whatever the transport mechanism.

<sup>b</sup>Reference 18.

<sup>c</sup>Measured in a CdF<sub>2</sub>:Eu sample which contained predominantly  $C_{4v}$  centers before annealing in Cd vapor.

<sup>d</sup>Measured in a CdF<sub>2</sub>:Eu sample which contained predominantly  $C_{3v}$  centers before annealing in Cd vapor.

<sup>e</sup>Obtained from  $\tau_i$  and  $I_{EPR}$  data as more accurate.

<sup>f</sup>This set of values is less consistent than (I), e.g., it follows from the TL activation energy as well as the EPR decay kinetics that  $E_{b2}=0$ , however, from  $I_{EPR}(T)$  we obtain  $E_{b2}$  20 meV.

$$\frac{N_{\rm Eu} - N_{(\rm Eu^{2+})}}{N_{(\rm Eu^{2+})} [N_{(\rm Eu^{2+})} - N_{(\rm Eu^{2+})}(0)]} = \frac{C}{I} \exp\left[-\frac{E_{\rm Eu} + E_{b2} - E_{b1}}{kT}\right], \quad (4.9)$$

where C is given by

$$C = \frac{e'_{\rm Eu}c'_X p_{r,X}}{\sigma_0 N_X p'_{i,X} c'_{\rm Eu}}$$
(4.10)

and is temperature dependent (if we disregard the weak temperature dependencies of  $\sigma_0$  and  $p_{r,X}$ ) even for standard conduction-band transport. In (4.9)  $E_{\rm Eu}$  is the activation enthalpy of Eu<sup>2+</sup>, denoted as  $\Delta H_n$  in Eq. (4.1).

The temperature and light-intensity dependencies of the saturation amplitude of the  $Eu^{2+}$  EPR signal under illumination from the  $C_{4v}$  excitation region are shown in Fig. 8. The activation energy obtained from the fit of the temperature dependence with formula (4.9) is  $(E_{\rm Eu}+E_{b2}-E_{b1})=350\pm10$  meV. The fitting parameters found to be the best for the description of the temperature dependence were then used to calculate the lightintensity dependence. The very good agreement of the experimental and calculated values [shown in Fig. 8(b)] confirms the applicability of formula (4.9) to the description of the experimental results. The above-discussed experiment can provide the decisive argument for the existence of the  $E_{b1}$  energy barrier in the case of  $C_{4v}$ centers. As the activation energy governing the temperature dependence of the saturation amplitude is equal to  $E_{\rm Eu} + E_{b2} - E_{b1}$ , by comparing it to the activation energy

derived from the thermoluminescence studies (which in our notation is given by  $E_{\rm Eu} + E_{b2}$ ) the value of  $E_{b1}$  can be determined. The  $E_{\rm Eu} + E_{b2}$  energy can be also established independently from the kinetics of the Eu<sup>2+</sup> EPR signal decay after the light is turned off. Therefore, before further discussion of the activation character of the coactivators ionization processes the capture process will be described.



FIG. 8. (a) Temperature and (b) light-intensity dependencies of the saturation amplitude of the Eu<sup>2+</sup> EPR signal observed under 333-nm illumination. The lines represent the fit to the data with use of Eqs. (4.9) and (4.10) for the following parameters:  $E_{\rm Eu} + E_{b2} - E_{b1} = 354$  meV;  $C/I = 1.08 \times 10^{-7}$  cm<sup>3</sup>. The light-intensity scale in (b) is a relative one,  $I = 440I_0$  is the intensity applied in (a).

## 2. The kinetics of the thermoluminescence process

The results discussed in the preceding sections prove that during uv excitation electrons are ionized from  $F_i$ and  $O_s^{2-}$  coactivators of the  $C_{4v}$  and  $C_{3v}$  PL, and captured by cubic  $Eu^{3+}$  centers. We propose that the reverse process, i.e., the recapture of electrons thermally released from the populated  $Eu^{2+}$  centers by the ionized coactivators, proceeds via the coactivator excited states. The subsequent deexcitation within the  $C_{4v}$  and  $C_{3v}$ centers results in the observed TL emission. Such a model of the thermoluminescence process we base on the fact that (i) the TL emission is similar to the photoluminescence hence the radiative deexcitation is analogous (see Fig. 1); (ii) the temperature range in which the depopulation of the light-induced Eu<sup>2+</sup> centers is observed is correlated with the range in which thermoluminescence occurs (Figs. 4 and 8).

In consequence, the decay of the  $Eu^{2+}$  EPR signal after the light is turned off should monitor directly the kinetics of the thermoluminescence process. The appropriate kinetics equations can be derived from Eqs. (4.3)-(4.6) by omitting the excitation term  $I\sigma_0(N_X - N_{(X^*)} - N_{(X^*)})$ . Moreover, since  $p_{r,X} \gg p_{i,X}$ most of the electrons captured by the coactivators on their excited states recombine immediately within the oxygen-europium or fluorine-europium pairs and the ionization term  $N_{(X^*)}p_{i,X}$  can be omitted as well. We utilize also the  $N_{(X^+)} \cong N_{(Eu^{2+})} - (N_{Eu} - N_A)$  approximation used in Sec. IV D 1. A further simplification results from the fact that in the temperature range in which the decay of the  $Eu^{2+}$  EPR signal is observed the light-induced concentration of Eu<sup>2+</sup> is much smaller than  $(N_{\rm Eu} - N_{\rm A})$ and, consequently, the free-electron concentration is value: dominated by its equilibrium  $n \approx e_{\rm Eu}(N_{\rm Eu} - N_A)/(c_{\rm Eu}N_A)$ . The solution is then easily found and takes the simple exponential form:

$$N_{(\mathrm{Eu}^{2+})} - (N_{\mathrm{Eu}} - N_{A})$$
  
=  $[N_{(\mathrm{Eu}^{2+})}(0) - (N_{\mathrm{Eu}} - N_{A})] \exp(-t/\tau_{d})$ ,

where

$$\tau_{d} = \frac{c_{\rm Eu}N_{A}}{c_{X}e_{\rm Eu}(N_{\rm Eu}-N_{A})} = \frac{c_{\rm Eu}N_{A}}{c_{X}'e_{\rm Eu}'(N_{\rm Eu}-N_{A})} \exp\left[\frac{E_{\rm Eu}+E_{b2}}{kT}\right].$$
 (4.11)

Here  $N_{(Eu^{2+})}(0)$  is the  $Eu^{2+}$  concentration at the moment when the light is turned off, and  $E_{Eu}$  denotes the activation enthalpy  $\Delta H_n$  in Eq. (4.1). As can be seen the decay time  $\tau_d$  depends exponentially on temperature, however, in the "classical" description the  $T^2$  preexponential factor should be taken into account.

The decay kinetics of the  $Eu^{2+}$  EPR signal intensity after the light was turned off was measured in the temperature range 180–230 K. Since the concentration of lightinduced  $Eu^{2+}$  centers decreases with increasing temperature (see Fig. 8) in the experiment an efficient broadband

illumination was applied. The kinetics of the EPR signal decay was found to be described by a sum of two exponential functions. The temperature dependencies of the decay time constants for the fast and slow components of the decay [shown in Fig. 4(b)] are distinctly different and yield the activation energies of 451±28 and  $352\pm17$  meV, respectively. These energies are similar to those found in thermoluminescence experiments for  $C_{3\nu}$ (440±15 meV) and  $C_{4v}$  (360±15 meV) emissions. Therefore, we propose that the fast and slow components of the decay relate to the capture of electrons thermally released from Eu<sup>2+</sup> traps on two different kinds of centers: the  $O_s^{-1}$  ionized coactivator in the  $C_{3v}$  center and  $F_i^{0}$  in the  $C_{4v}$  center, respectively. Such a capture process involving two centers is possible since the broadband uv illumination employed in the discussed experiment ionized both  $C_{4v}$  and  $C_{3v}$  centers. The different decay rates of the two capture processes are a direct consequence of the fact that  $\tau_d^{-1}$  is proportional to the electron capture rate of the coactivator. Hence, the ratio of the capture rates by the ionized oxygen and fluorine coactivators,  $c'_{(O^{-})}/c'_{(F^{0})}$ , can be estimated and is found to be of the order of  $2 \times 10^3$ . This value also gives the ratio of the capture cross sections,  $\sigma$ , independent of the transport mechanism in  $CdF_2$ . To determine their absolute magnitudes, however, some assumptions are required. If we take the entropy factor<sup>26</sup> as  $18\pm 2$  we obtain  $\sigma_{(\Omega^{-})} \approx 10^{-18}$  cm<sup>2</sup>. This seems to be rather small for an electron attractive center.

The above-mentioned two components of the Eu<sup>2+</sup> EPR signal decay will be observed only in crystals in which both types of Eu<sup>3+</sup> complexes are present and their concentrations are similar. For example, in the previous studies of von Bardeleben<sup>27</sup> only the slow component of the decay was observed. The hypothesis that the fast and slow components in the decay of  $Eu^{2+}$  are connected with electron capture by  $O_s^{-1}$  and  $F_i^{0}$  coactivators is verified by the experiment in which the 254-nm excitation was applied. This excitation ionizes primarily the  $C_{3v}$  centers. Indeed, only one type of center was found to be active in the capture process and the activation energy obtained from the plot of  $\ln \tau_d$  vs  $10^3/T$ shown in Fig. 4(b)  $(440\pm17 \text{ meV})$  agrees very well with the activation energy for capture by  $C_{3n}$  centers [see the bottom of Fig. 4(a)].

#### E. The model of the thermoluminescence process

The experimental results discussed in Sec. IV D are summarized in Table II. Because of the unknown transport mechanism in the  $CdF_2$  lattice it is not clear how to determine properly the activation energies from the experimental data. Therefore, in Table II two sets of activation energies are given—the first one obtained assuming temperature-independent emission and capture rates (apart from the exponential dependence) and the second obtained assuming standard conduction-band transport [with the capture and emission rates related via the detailed balance equation (4.1)]. Though the validity of the latter description cannot be formally excluded, the first set of data seems to be more consistent. For example, the  $(E_{\rm Eu} + E_{b2})$  energies established from the decay kinetics of the Eu<sup>2+</sup> EPR signal agree in that approach with the activation energies obtained from thermoluminescence data, which in our notation should also be equal to  $(E_{\rm Eu} + E_{b2})$ . Furthermore, the activation energy  $(E_{\rm Eu} + E_{b2} - E_{b1})$  determined from the saturation amplitude of the Eu<sup>2+</sup> EPR signal  $[I_{\rm EPR}(T)]$  under illumination which ionizes  $C_{4v}$  centers agrees with other data only for  $E_{b1}$  and  $E_{b2}$  energies taken from the first set of the data. Moreover, the  $E_{b2}$  energy agrees very well with the 32-meV activation energy obtained from thermostimulated current studies by de Murcia *et al.*<sup>10</sup> and interpreted as the effective height of the energy barrier for electron capture by the fluorine coactivator.

The logical consequence of our supposition that the transport mechanism in CdF<sub>2</sub> is not a pure conduction band one is the possibility of electron diffusion between the Eu<sup>2+</sup> trap and the Eu<sup>3+</sup>-O<sub>s</sub><sup>-</sup> and Eu<sup>3+</sup>-F<sub>i</sub><sup>0</sup> com-plexes being thermally activated. If such an activation energy  $(E_{diff})$  exists it will affect all the activation energies obtained from kinetics experiments. For example, the increase kinetics should be governed by the  $E_{b1} + E_{diff}$ energy instead of  $E_{b1}$ . As can be seen in Table II the upper limit of  $E_{\text{diff}}$  is 13 meV, i.e., the energy obtained from the Eu<sup>2+</sup> increase rate for  $C_{4v}$  center ionization. It seems that if the diffusion activation energy were not negligible a difference in the activation energies for dc and ac transport should be expected (as in dc transport the highest resistivity paths decide about the conductivity magnitude, whereas in the case of ac measurements the low resistivity paths are dominating). However, the temperature dependencies of ac conductivity measured for two types of CdF<sub>2</sub>:Eu crystals (one containing mainly  $C_{4v}$ centers and the other  $C_{3v}$  centers before thermal conversion) yield the activation energies of  $334\pm9$  and  $326\pm9$ meV, respectively (Fig. 9), which agree (within the experimental error) with the 330-meV activation energy of dc transport established by Trautweiler, Moser, and Khos-



FIG. 9. Temperature dependence of ac conductivity measured in two thermally converted CdF<sub>2</sub>:Eu samples containing mainly  $C_{3v}$  (full circles) and  $C_{4v}$  (open circles) centers before the conversion process.

la.<sup>18</sup> We can, therefore, assume that if the  $E_{\text{diff}}$  energy exists, it is fairly small and should not disturb appreciably the energies given in Table II.

Up to now we have disregarded the possibility that the electron capture by cubic  $Eu^{3+}$  centers may be also thermally activated. The existence of an energy barrier for the process  $(E_{b(Eu)})$  should be the more carefully verified since such a barrier is known to occur in the case of the indium impurity in  $CdF_2$ . Moreover, this barrier is responsible for the population inversion between In<sup>2+</sup> localized and  $\ln^{3+} + e^{-}$  hydrogeniclike donor states.<sup>28</sup> In order to verify the presence of the  $E_{b(Eu)}$  energy barrier the following experiment was performed. A converted CdF<sub>2</sub>:Eu sample, containing only Eu<sup>2+</sup> centers was illuminated with light inducing the  $4f^7 \rightarrow 4f^65d^1$ -allowed transition of Eu<sup>2+</sup>. This illumination was shown previously<sup>11</sup> to lead to a very effective ionization of  $Eu^{2+}$ centers, which can be observed as a quenching of the  $Eu^{2+}$  EPR signal in crystals with other than Eu trap centers present. In the converted crystal, however, the electrons induced in the conduction band were found to be immediately recaptured by Eu centers and no  $Eu^{2+}$ photoquenching was observed, even at 4.2 K. This allows us to conclude that there is no significant energy barrier for the capture of electrons by Eu centers.

Though the values given in Table II should be considered only as the upper limits of the effective barrier heights (resulting from the competition between the thermally activated transition over the barrier and tunneling), for further discussion it is pertinent that for both types of centers  $(C_{4v}, C_{3v})$  the  $E_{b2}$  barrier is higher than  $E_{h1}$ . It means that the activation energy for carrier capture is larger than the appropriate energy for its thermal release. It can be readily shown that such a situation occurs only when the excited states of the coactivators are degenerate with the continuum of conduction-band states. The carrier emission process is, in fact, an autoionization process. Its activation character is due to the lattice-relaxation-induced energy barrier which separates the excited and ionized states of the coactivator. This is schematically shown in Fig. 10(a). The model shown in this figure also allows us to explain the thermally activated character of the capture process (governed by the  $E_{b2}$  barrier). It is clear that the activation energy determined from either TL or photo-EPR decay studies is larger than the  ${\rm Eu}^{2+}$  activation enthalpy  $(E_{\rm Eu})$  and equal to  $E_{\rm Eu} + E_{b2}$ .

In the model shown in Fig. 10(a) we assume that the excited state from which the electrons are ionized and on which they are captured is the same. However, previous luminescence studies of one of the authors<sup>3</sup> suggest that in the case of the oxygen coactivator a different situation is possible. While the excitation process (at 4.8 eV) was shown to be due to the  ${}^{1}S_{0}(2p^{6}) \rightarrow {}^{1}P_{1}(2p^{5}3s^{1})$  transition of  $O_{s}{}^{2-}$ , the energy transfer to  $Eu^{3+}$  was suggested to occur from the lower triplet state  ${}^{3}P_{J}(2p^{5}3s^{1})$ . Since the  ${}^{3}P_{J} \rightarrow {}^{1}S_{0}$  transition is forbidden, energy transfer to the  $Eu^{3+}$  center can be more efficient than direct radiative deexcitation. In fact, the  ${}^{3}P_{J} \rightarrow {}^{1}S_{0}$  emission of oxygen (at 2.7 eV) is only observed for oxygen-rich CdF<sub>2</sub> crystals



FIG. 10. The configuration coordinate diagram of the position of the coactivator excited states with respect to the conduction band for the following cases: (a) The barriers for autoionization  $E_{b1}$  and capture  $E_{b2}$  relate to the  ${}^{1}P_{1}$  excited state of the coactivator; (b) the  $E_{b1}$  barrier is connected with the  ${}^{1}P_{1}$  state, but the  $E_{b2}$  barrier occurs at the  ${}^{3}P_{J}$  state; (c) both barriers relate to the  ${}^{3}P_{J}$  state.

not codoped with europium. In consequence, we should distinguish among three possible situations: when the  $E_{b1}$  and  $E_{b2}$  barriers relate to the  ${}^{1}P_{1}$  state [Fig. 10(a)]; the  $E_{b1}$  barrier is connected with the  ${}^{1}P_{1}$  state, but the  $E_{b2}$  barrier occurs at the  ${}^{3}P_{J}$  state [Fig. 10(b)]; both barriers relate to the  ${}^{3}P_{J}$  state [Fig. 10(c)].

It is evident that in the last case a broad photoionizatoin band should be observed starting at an energy lower than that of the  ${}^{1}S_{0} \rightarrow {}^{1}P_{1}$  transition of  $O_{s}{}^{2-}$ . Since in the TL excitation spectrum such a band has not been observed this case can be immediately rejected. The experimental results do not allow, however, to distinguish between the other two cases. It is only certain that the  ${}^{1}P_{1}$ state undergoes autoionization. As the location of this state in respect to the conduction-band edge is unknown we cannot exclude the possibility that in the capture process the  ${}^{3}P_{J}$  state of the oxygen coactivator is active. The situation for the fluorine coactivator is more clear. No emission suggesting that the energy transfer might proceed from the  ${}^{3}P_{J}$  state has been observed for isolated  $F_i^-$  ions. Moreover, the studies of maxue  $Cd_{1-x}Ca_xF_2$ : Eu crystals<sup>29</sup> indicate that both the autoionization and capture processes most probably involve only the  ${}^{1}P_{1}$  state of  $F_{i}^{-}$ . By analogy, we propose that the same [the model shown in Fig. 10(a)] occurs also for the oxygen coactivator, but this cannot be considered as a proven fact.

# V. CONCLUSIONS

The model presented in Figs. 10(a) and 10(b) allows us to explain all the features of the complex thermoluminescence process in the CdF<sub>2</sub>:Eu lattice. It is shown that two types of europium centers are active in this process: the charge-compensated Eu<sup>3+</sup>-O<sub>s</sub><sup>2-</sup> or Eu<sup>3+</sup>-F<sub>i</sub><sup>-</sup> associates (the centers which dominate the photoluminescence under broadband uv excitation), and the cubic  $Eu^{3+}$ centers without any close charge compensation (which are the electron traps). The presence of cubic centers is necessary for the thermoluminescence to occur and their concentration controls the intensity of this process. The  $\mathrm{Eu}^{3+}$ - $\mathrm{O_s}^{2-}$  ( $C_{3v}$  symmetry) and  $\mathrm{Eu}^{3+}$ - $\mathrm{F_i}^{-}$  ( $C_{4v}$  symmetry) centers play a double role. First of all they are a source of electrons due to the autoionization of their excited states. On the other hand, the electrons thermally released from  $Eu^{2+}$  donors are retrapped by the  $O_s^{-}$  and  $\mathbf{F}_i^0$  ionized coactivators in the  $C_{3v}$  and  $C_{4v}$  complexes. The deexcitation process within the oxygen-europium and fluorine-europium centers is identical to the one governing the photoluminescence. It means that the energy of the coactivator, which is in the excited state after electron capture, is transferred to Eu<sup>3+</sup>, and then Eu<sup>3+</sup> radiative recombination follows. Therefore, the emission spectra in the PL and TL processes are identical, as well as their excitation spectra.

The CdF<sub>2</sub> thermoluminescence is a good example of demonstrating the role of lattice relaxation in electronic transitions. The existence of an energy barrier for the autoionization process explains two of the strange features of the CdF<sub>2</sub>:Eu thermoluminescence: the fact that the excitation spectra of the PL and TL processes are the same, and that the autoionization process is thermally activated. On the other hand, the lattice-relaxationinduced energy barrier for the capture process explains another puzzle encountered when studying CdF<sub>2</sub>:Eu TL, i.e., the spread of the activation energies established from the thermoluminescence studies. They were different for different emitting centers and larger than Eu<sup>2+</sup> activation enthalpy. This suggested that the electrons might be captured by Eu<sup>3+</sup> ions within the various associates as the close-lying coactivator could affect the activation enthalpy of such  $Eu^{2+}$  traps. We reject such a model of the thermoluminescence on the basis of very detailed photo-EPR studies. It is unambiguously shown that the spread of the TL activation energies is due to the presence of energy barriers for the electron capture process.

The fact that the experimental data are more consistently described when we neglect the temperature corrections resulting from the "classical" conductionband transport description seems to indicate that the transport mechanism in  $CdF_2$  might not be a standard conduction-band one, as observed in less ionic crystals. The problem of an appropriate description of the  $CdF_2$ transport cannot be, however, solved on the basis of the presented studies and further investigations are necessary.

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