# Effect of low-level titanium(IV) doping on the resistivity of magnetite near the Verwey transition

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The effects of Ti substitution for Fe on octahedral sites in magnetite has been investigated through electrical resistivity measurements. In a manner analogous to zinc ferrites, the Verwey transition temperature is depressed with increasing Ti content. The Verwey transition is of first order in  $Fe_{3-y}Ti_yO_4$  in the concentration range  $0 \le y \le y_c = 0.012$ ; for  $y_c \le y \le 3y_c$  the transition is of second order, and for  $y > 3y_c$  the phase transformation is completely eliminated. The data are correlated with comparable work on dilute zinc ferrites and nonstoichiometric magnetite, and the implications of the findings are discussed.

## **INTRODUCTION**

Although the Verwey transition in magnetite has been extensively studied, many aspects of this phase transformation are not yet completely understood. It was recognized quite early that the transition temperature  $T_V$ was strongly affected by variations in oxygen stoichiometry<sup>1-4</sup> and by substitution of iron with other transition metal cations. These matters were not followed up further until their consideration was revived in more recent studies. 5-11 Detailed reports have been published recently on the changes in physical properties concomitant to alterations of the oxygen to iron ratio in  $Fe_{3(1-\delta)}O_4$ , or to the replacement of iron by zinc on tetrahedral cation sites to form  $Fe_{3-x}Zn_xO_4$ , or to the replacement of titanium on octahedral cation sites to form  $Fe_{3-\nu}Ti_{\nu}O_4$ .<sup>12-19</sup> Through heat capacity measurements on magnetite it was demonstrated that in the range  $-0.0005 < \delta < \delta_c = 0.0039$  the Verwey transition is of first order, whereas in the range  $\delta_c \leq \delta \leq 3\delta_c$ , the transformation is of higher order. This feature was independently verified by observation<sup>13</sup> of discontinuities at  $T_V$  in the resistivity  $\rho$  and Seebeck coefficients  $\alpha$  of specimens with  $\delta \leq \delta_c$ , whereas for  $\delta > \delta_c$ ,  $\rho$  and  $\alpha$  exhibited discontinuities in slope at temperatures close to  $T_V$ . Analogous observations of the electrical characteristics have been reported for the  $Fe_{3-x}Zn_xO_4$  system.<sup>18</sup> In both cases, and for both the first- and higher-order regimes,  $T_V$  decreases linearly with increasing cation vacancy density or with Zn substitution, with the correspondence  $x = 3\delta$ , as might be anticipated from the elementary comparison of  $\operatorname{Fe}_{3(1-\delta)}O_4$  with  $\operatorname{Fe}_{3-x}\operatorname{Zn}_xO_4$ : plots of  $T_V$  vs x and  $3\delta$ could be nearly superposed (see also Fig. 5 of the present paper).

For comparison purposes it appeared of interest to undertake studies of the  $Fe_{3-y}Ti_yO_4$  system. As is well established, titanium replaces iron on octahedral interstices for y < 0.2, whereas zinc enters the lattice substitutionally on tetrahedral sites. When  $Ti^{4+}$  substitution occurs, charge balance requires the conversion of a corresponding amount of  $Fe^{3+}$  to  $Fe^{2+}$ . In the range  $0 \le y < 0.2$  the resulting titanomagnetite is characterized by the formula

 $(Fe^{3+})$   $[Fe^{2+}_{1+y}Fe^{3+}_{1-2y}Ti^{4+}_{y}]O_4$ , where the round and square brackets enclose ions located on tetrahedral and octahedral interstices, respectively. By contrast, dilute zinc ferrites are characterized by the formula  $(Zn^{2+}_xFe^{3+}_{1-x})[Fe^{2+}_{1-x}Fe^{3+}_{1+x}]O_4$ , showing that charge balance requires the conversion of  $Fe^{2+}$  to  $Fe^{3+}$  on octahedral sites.

A very elementary analysis<sup>20</sup> shows that when electron transport involves small polarons as charge carriers, the conductivity is given by  $\sigma = Acv\mu$ ; in the present case Ais a collection of parameters, c is the carrier density on octahedral sites (i.e.,  $[Fe^{2+}]$ ), v is the density of vacant octahedral sites (i.e.,  $[Fe^{3+}]$ ), and  $\mu = \mu_0 \exp(-\epsilon_\sigma/k_B T)$ is the mobility, characterized by a conductivity activation energy  $\epsilon_\sigma$ ,  $k_B$  being the Boltzmann constant. In zeroth order, one may therefore anticipate that Ti<sup>4+</sup> and Zn<sup>2+</sup> substitutions should give rise to mirror image effects, so that the variation of  $\sigma$  with the Zn<sup>2+</sup> or Ti<sup>4+</sup> content of the sample should be very nearly the same. These matters are examined below.

#### **EXPERIMENT**

Single crystals of  $Fe_{3-y}Ti_yO_4$  with y < 0.05 were grown from 99.999%  $Fe_2O_3$  and 99.95%  $TiO_2$  under a  $CO_2$  atmosphere in a skull melter.<sup>21,22</sup> The charge was maintained above its melting point for several hours; convective stirring optimized the uniform distribution of Ti<sup>4+</sup> in the host. After cooling the boule, suitable single crystals were analyzed for titanium and iron composition by electron microprobe techniques. All precautions called for were properly observed, so as to optimize the uniformity of the Ti distribution. While the Ti content varied considerably with depth in the boule, the composition variable y tended to be quite uniform in the single crystals. Fifteen of these were selected and analyzed by microprobe techniques. Those with the most uniform Ti distribution were annealed as described below, cut to the appropriate geometry, and reanalyzed; these samples were more homogeneous in Ti content after the anneal than before. For the specimens used in the measurements the uncertainty in y remained in the range  $\pm 0.0007$  to  $\pm 0.0009$ , except for one sample with y = 0.0206 where the

uncertainty was  $\pm 0.0016$ .

Once the titanium-iron stoichiometry was known, the crystals were annealed under the appropriate CO-CO<sub>2</sub> buffer gas<sup>9</sup> using a zirconia transfer cell<sup>23</sup> to monitor the oxygen fugacity. The ideal 4:3 oxygen to cation ratio was attained<sup>24,25</sup> within 48 h at temperatures in the range 1200 °C-1400 °C. At higher temperatures annealing was more rapid, but upon quenching these specimens tended to shatter. Considerable difficulty was experienced in obtaining high-quality single crystals in the composition range 0.012 < y < 0.025, where the titanium distribution tended to be nonuniform. Measurements were carried out on the best specimen for this composition range.

The crystals were trimmed with a diamond saw to remove outer layers of different composition produced during quenching, and cut into bars of approximately 2 mm $\times$ 2 mm  $\times$ 10 mm. Four-probe leads were soldered ultrasonically and dc resistivity measurements were made from room temperature to liquid helium on both cooling and heating cycles.

## **RESULTS AND DISCUSSION**

The resistivity data for  $\operatorname{Fe}_{3-y}\operatorname{Ti}_y O_4$  are shown in Figs. 1 and 2 as plots of  $\log \rho$  vs 1/T for the compositional ranges  $0 \le y \le 0.0100$  and  $0.0206 \le y \le 0.0380$ , respectively. It is immediately evident that samples in these two ranges of y undergo a first- and a higher-order transition, respectively. No anomaly in electrical properties is encountered in the low-temperature range for titanomagnetites with y > 0.0380.<sup>26</sup>

One should note that the plots in Figs. 1 and 2 are highly nonlinear and that the anomaly at  $T_V$  involves a semiconductor-semiconductor transition. Also, all data in the temperature range  $T > T_V$  fall essentially on a universal curve, whereas for a fixed T in the range  $T < T_V$  the resistivities assume steadily lower values as y is increased. Thus there is a significant spread in resis-

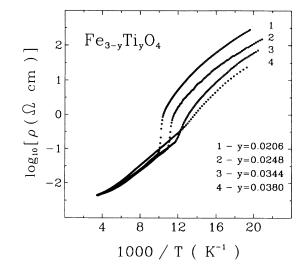


FIG. 2. Plot of  $\log_{10}\rho$  vs 1/T for dilute titanomagnetites in the composition range of the higher-order Verwey transition.

tivity values below 120 K as the titanium content in magnetite is increased. Both  $T_V$  and the magnitude  $\Delta\rho$  of the discontinuity diminish as y is increased. This latter trend is clearly displayed in Figs. 3 and 4, which show the smooth variation of  $\Delta\rho$  with y. For samples undergoing the higher-order transition  $\Delta\rho$  was computed from the region of the rapid change of  $\rho$  with T centered on  $T_V$ . In conformity with earlier practice, <sup>13,18</sup>  $T_V$  was identified with the inflection point in the curves of Fig. 2.

There is a remarkable similarity of the present data with the electrical properties of  $Fe_{3(1-\delta)}O_4$  and of  $Fe_{3-x}Zn_xO_4$  reported earlier.<sup>13,18</sup> This is also illustrated in Figs. 3 and 4, which show a detailed comparison of the electrical properties of the titanomagnetites with nonstoichiometric magnetite in the vicinity of  $T_V$ . These

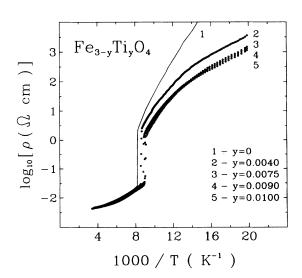


FIG. 1. Plot of  $\log_{10}\rho$  vs 1/T for dilute titanomagnetites in the composition range of the first-order Verwey transition.

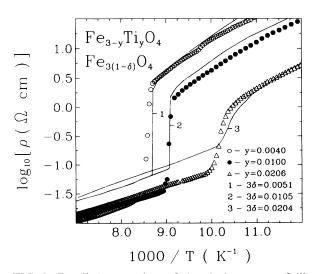


FIG. 3. Detailed comparison of electrical property of dilute titanomagnetites and nonstoichiometric magnetite near the Verwey transition; note the correspondence  $y = 3\delta$ .

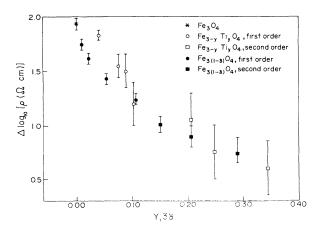


FIG. 4. Variation in the rapid change in resistivity near the Verwey transition,  $\Delta \log_{10}\rho$  vs 3 $\delta$  or y for nonstoichiometric magnetite or dilute titanomagnetite.

curves are representative of data for all other samples. It is evident that the correspondence  $y = 3\delta$  applies to the variation of  $T_V$  with deviations from the parent composition Fe<sub>3</sub>O<sub>4</sub>, just as the  $x = 3\delta$  correspondence held for the zinc ferrite-nonstoichiometric magnetite system.<sup>18</sup> Moreover, for  $T < T_V$  the resistivity data for  $Fe_{3(1-\delta)}O_4$  and for  $Fe_{3-\nu}Ti_{\nu}O_4$  can be very nearly superposed. By contrast, the data for  $T > T_V$  fall on two sets of very closely spaced curves. In this temperature range the resistivities of the various  $Fe_{3(1-\delta)}O_4$  specimens are roughly half an order of magnitude larger than those of the  $Fe_{3-\nu}Ti_{\nu}O_4$ samples. Similarly, for  $T > T_V$  the resistivity curves of  $Fe_{3(1-\delta)}O_4$  had been shown<sup>18</sup> to lie somewhat above those of  $Fe_{3-x}Zn_xO_4$ . These findings are consistent with the elementary concept that the presence of cation vacancies is more deleterious to the electron transfer process than is the incorporation of  $Ti^{4+}$  ions, for which the radial extension of the orbitals is larger than that of the  $Fe^{3+}$  ions. Likewise, the incorporation of  $Zn^{2+}$  is far less damaging to electron transfer than the presence of vacancies.

Finally, we show in Fig. 5 a plot of the variation of  $T_V$  with x, y, and 3 $\delta$ . The data for nonstoichiometric magnetite were read off from both heat capacity and resistivity measurements; heat capacity data are presently unavailable for the other systems. One clearly sees that data for all these systems superpose very well. Also, one can readily distinguish the first-order from the higher-order regimes. In both cases  $T_V$  changes linearly with sample composition; the ratio of the two slopes is R ln2, which fact can be rationalized by an elementary approach dealt with elsewhere.<sup>27</sup>

A comparison of  $Fe_{3-\nu}Ti_{\nu}O_4$  with the properties of

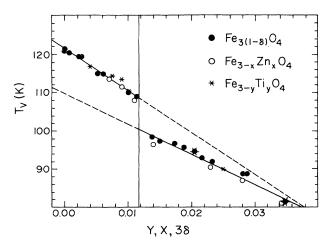


FIG. 5. Variation of Verwey transition temperature against sample composition for dilute titanomagnetite, zinc ferrite, or nonstoichiometric magnetite. The regions of first- and higherorder transitions are clearly delineated.

 $Fe_{3-x}Zn_xO_4$  reported earlier<sup>18</sup> shows that in the range  $0 \le x, y \le 0.04$  both systems display very similar electrical characteristics. In zeroth order the mirror symmetry referred to in the Introduction is satisfied. One should note that iron on the tetrahedral sites is exclusively in the trivalent state for nonstoichiometric (vacancy-containing) magnetite, zinc ferrites, and titanomagnetites, in the dilute concentration range; this fact has been established by appropriate saturation magnetization studies.<sup>28</sup> The striking electrical similarities of all three classes of materials derived from the parent Fe<sub>3</sub>O<sub>4</sub> suggest that conduction occurs via charge fluctuations among the cations in octahedral interstices without involving  $(Fe^{3+})$  on tetrahedral sites. The "mirror-image" properties further suggest that charge transport likely involves small polarons as carriers, since in such a regime  $\sigma \sim cv \approx c(1-c)$ , where c is the charge carrier density.

In conclusion, we have shown that the electrical properties of  $Fe_{3(1-\delta)}O_4$ ,  $Fe_{3-x}Zn_xO_4$ , and  $Fe_{3-y}Ti_yO_4$  are very similar in their dependence on 3 $\delta$ , x, or y, and in their variation with temperature. These findings are consistent with charge transport by thermal activation involving charge fluctuations among ferrous and ferric ions on octahedrally coordinated interstices.

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