

# Analytical determination of the local oxygen structure around $\text{Cr}^{3+}$ in $\text{SnO}_2$ rutile-type crystals by use of electron paramagnetic resonance

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The origin of two distinct electron paramagnetic resonance (EPR) spectra observed in Cr-doped  $\text{SnO}_2$  crystals, i.e.,  $(\text{EPR})_{\text{I}}$  and  $(\text{EPR})_{\text{II}}$ , was investigated using the superposition model specifically developed for rutile-type crystals. Analytical results suggest that these spectra are due to the substitutional  $\text{Cr}^{3+}$  ions having a unique structure with respect to its local surrounding oxygen atoms. The  $(\text{EPR})_{\text{I}}$  spectrum showed that the four nearest-neighbor oxygen atoms on the (110) plane have moved from normal sites toward the  $\text{Cr}^{3+}$  ion by  $0.072 \text{ \AA}$  (3.5%) as a result of a reduction in the metal ionic radius. The  $(\text{EPR})_{\text{II}}$  spectrum showed the  $\text{Cr}^{3+}$  ion to be coupled with the vacancy of the two nearest-neighbor oxygen atoms on the [110] axis. In this case, the ratio of spin-Hamiltonian parameters takes the form  $E/D = -\cos 2\alpha$  from the superposition model, where  $\alpha$  is the angle between the [001] axis and the cation-ligand bonding axis in (110) plane. The theoretical value  $E/D = -0.205$  was obtained from this simple relation, and was in good agreement with the experimental values.

## I. INTRODUCTION

$\text{SnO}_2$  is a transparent *n*-type semiconductor with a wide band gap. It has been considered that its electric conductivity originates from a nonstoichiometric structure containing oxygen vacancies, interstitial Sn ions, or other native defects which form shallow donor centers providing many conduction electrons.<sup>1-7</sup> These phenomena are also found in several excess-type oxide semiconductors such as  $\text{TiO}_2$  or  $\text{ZnO}$ .<sup>2</sup> Although oxygen vacancies were previously suggested to be the most predominant native defect using electrical conductivity temperature-dependent measurements,<sup>7</sup> the nonstoichiometric structure of  $\text{SnO}_2$  crystals has not yet been fully elucidated.

Application of electron paramagnetic resonance (EPR) to  $\text{Cr}^{3+}$ -doped  $\text{SnO}_2$  crystals has shown two distinct spectra, i.e.,  $(\text{EPR})_{\text{I}}$  and  $(\text{EPR})_{\text{II}}$ .<sup>8-11</sup> In addition, an inclusive spectrum  $(\text{EPR})_{\text{III}}$  was found in as-grown crystals.<sup>12</sup> The angular dependence of these spectra,  $(\text{EPR})_{\text{I}}$ ,  $(\text{EPR})_{\text{II}}$ , and  $(\text{EPR})_{\text{III}}$ , are shown in Fig. 1. The origin of the spectrum  $(\text{EPR})_{\text{I}}$  is believed to represent the effect of substitutional  $\text{Cr}^{3+}$  ions,<sup>9-11</sup> whereas  $(\text{EPR})_{\text{II}}$  has been considered to be due to interstitial ones.<sup>9,10</sup> We previously showed, using an analysis of the line intensity ratio of the superhyperfine structure of the Sn ion, that  $(\text{EPR})_{\text{II}}$ , like  $(\text{EPR})_{\text{I}}$ , is attributed to a  $\text{Cr}^{3+}$  ion located at a substitutional site, rather than at an interstitial site.<sup>10</sup> The difference between  $(\text{EPR})_{\text{I}}$  and  $(\text{EPR})_{\text{II}}$  may arise from a particular defect occurring near the Cr ions in  $\text{SnO}_2$  crystals, yet this phenomenon has not been clarified.

An analytical tool was developed to determine the local structure of a crystal's paramagnetic ion from EPR data, i.e., the superposition model.<sup>13-23</sup> This model was originally introduced to analyze spin-Hamiltonian parameters of *S*-state ions in insulators,<sup>3,14</sup> and assumes these parameters can be described by the individual con-

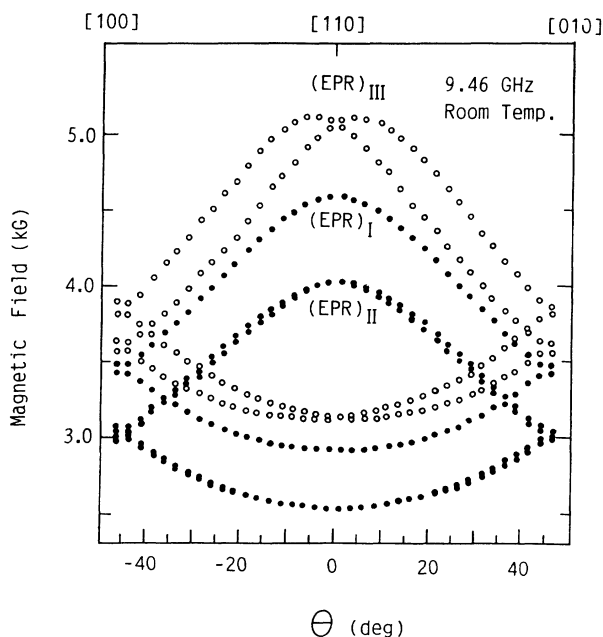


FIG. 1. Angular dependence of EPR spectra of a  $\text{Cr}^{3+}$ -doped  $\text{SnO}_2$  crystal in the (001) plane.

tributions of each nearest-neighbor ligand ion to the paramagnetic ion. The spin-Hamiltonian parameters therefore allow a correlation to be established with the position of the ligand ions; hence enabling the superposition model to be successfully applied to the vacancy free or vacancy associated centers in the perovskite oxides<sup>15-18</sup> and fluorides.<sup>19-22</sup> Consequently, detailed information on the local surroundings of the sixfold coordinated paramagnetic ions has been obtained. It should be noted, however, that only limited research has been directed at using this model to study rutile-type crystals. Recently we proposed the superposition model of  $\text{Cr}^{3+}$  in such crystals.<sup>24</sup> The present study analytically investigates the origin of the  $(\text{EPR})_{\text{I}}$  and  $(\text{EPR})_{\text{II}}$  spectra using the superposition model which is specifically developed for  $\text{Cr}^{3+}$  ions in rutile-type crystals.

## II. SUPERPOSITION MODEL OF $\text{Cr}^{3+}$ IN RUTILE-TYPE CRYSTALS

The superposition model<sup>13-17</sup> assumes that the spin-Hamiltonian parameter  $b_n^m$  can be expressed as a superposition of a single ligand contribution, i.e.,

$$b_n^m = \sum_i \bar{b}_n(R_i) K_n^m(\theta_i, \phi_i), \quad (1)$$

where  $(R_i, \theta_i, \phi_i)$  is the polar coordinate for the  $i$ th ligand ion,  $\bar{b}_n(R_i)$  is an intrinsic parameter which is a function of the metal-ligand distance  $R_i$ , and  $K_n^m(\theta_i, \phi_i)$  is a spherical harmonic function of polar angles. To calculate the spin-Hamiltonian parameter  $b_n^m$  the distance between the metal and ligand must be obtained.

Figure 2 schematically shows the structure of a rutile-type crystal, where the cations have six octahedrally located  $\text{O}^{2-}$  ions giving a rhombic distortion belonging to point symmetry  $D_{2h}$ . The  $[110]$  axis of the crystal is chosen as the  $Z$  axis and the  $[001]$  axis is chosen as the  $X$  axis. The positions of the nearest-neighbor oxygens on the  $Z$  axis " $\text{O}_z$ " have a different symmetry from that of the nearest-neighbor oxygens on the  $XY$  plane " $\text{O}_{xy}$ ." The crystallographic data for rutile-type  $\text{TiO}_2$ ,  $\text{GeO}_2$ , and  $\text{SnO}_2$  were determined by Baur<sup>25</sup> and are summarized in

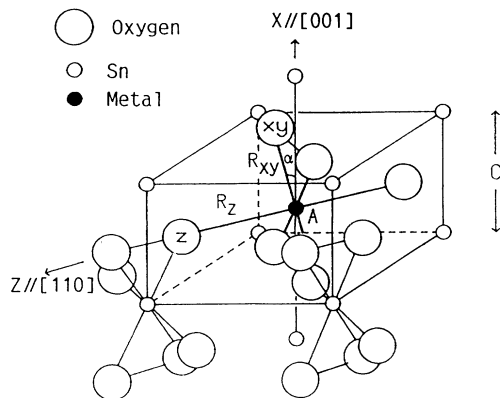


FIG. 2. Crystal structure of rutile-type crystal. The position "A" is a metal ion and the oxygen atoms are represented by large circles. The nearest-neighbor oxygen atoms on the  $Z$  axis are annotated as " $\text{O}_z$ " and ones on the  $XY$  plane as " $\text{O}_{xy}$ ."

Table I. The parameter  $\alpha$  represents the angle between the  $X$  axis and the bonding axis of  $\text{O}_{xy}$ . In rutile-type crystals the host ion is replaced by a  $\text{Cr}$  ion.

The spin-Hamiltonian of a  $\text{Cr}$  ion with  $S = \frac{3}{2}$  in rutile-type crystals is conventionally written as

$$\mathcal{H} = \beta H \cdot g \cdot S + D[S_z^2 - \frac{1}{3}S(S+1)] + E(S_x^2 - S_y^2), \quad (2)$$

where the  $x$ ,  $y$ , and  $z$  axes are the paramagnetic principal axes and the hyperfine interaction with the  $\text{Cr}^{53}$  nuclei is neglected. The spin-Hamiltonian parameters  $D$  and  $E$  for  $\text{TiO}_2:\text{Cr}^{3+}$ ,<sup>26,27</sup>  $\text{TiO}_2:\text{Mn}^{4+}$ ,<sup>28</sup>  $\text{GeO}_2:\text{Cr}^{3+}$ ,<sup>29</sup> and  $\text{SnO}_2:\text{Cr}^{3+}$  (Ref. 11) are listed in Table II. The values of  $D$  and  $E$  in this table were transformed to the coordinate system shown in Fig. 2.

It is generally known that the  $^4F$  state of  $\text{Cr}$  ions with  $d^3$  electrons in a rutile-type crystal can be decomposed into seven singlets by the perturbation potential  $V(D_{2h})$  with orthorhombic  $D_{2h}$  symmetry as shown in the energy diagram of Fig. 3. The probable ground state  $B_1$  is a mixing state of the  $t_2^3$  state and a small portion of the higher  $t_2e^2$  state having the same notation, i.e.,  $\psi(t_2^3) + \lambda\psi(t_2e^2)$ . Such hybridization from a higher state also occurs for  $d^1$  ions as well as for  $d^3$  ions in these crystals.<sup>30-32</sup> Since the mixing parameter  $\lambda$  is dependent on the angle  $\alpha$ , the intrinsic parameter of  $\text{Cr}^{3+}$  in rutile-type crystals with rhombic distortion may have a large anisotropy different from that in cubic crystals. In an octahedron with large anisotropy, even if  $R_z = R_{xy}$ , the intrinsic parameter  $\bar{b}_2(R_z)$  corresponding to  $\text{O}_z$  would be different from  $\bar{b}_2(R_{xy})$  corresponding to  $\text{O}_{xy}$  in symmetry. As a result, the summation in Eq. (1) of intrinsic parameters for ligand oxygens must be divided into two parts according to the rhombic distortion of the octahedron, i.e., one being the sum for the two  $\text{O}_z$  atoms on the  $Z$  axis and the other the sum for the four  $\text{O}_{xy}$  atoms on the  $XY$  plane. The spin-Hamiltonian parameters  $D$  and  $E$  in Eq. (2) can therefore be written for rutile-type crystals as

$$D = b_2^0 = 2\bar{b}_2(R_z) - 2\bar{b}_2(R_{xy}), \quad (3)$$

$$E = \frac{1}{3}b_2^2 = 2\bar{b}_2(R_{xy})\cos 2\alpha. \quad (4)$$

The intrinsic parameter  $\bar{b}_2(R_z)$  is a function of the distance between the  $\text{Cr}^{3+}$  ion and  $\text{O}_z$ , while  $\bar{b}_2(R_{xy})$  is a function of the distance between the  $\text{Cr}^{3+}$  ion and  $\text{O}_{xy}$ . When  $D$  and  $E$  in Eqs. (3) and (4) are set equal to zero, this corresponds to cubic symmetry without the Jahn-Teller effect, where  $R_z = R_{xy}$  and  $\alpha = 45^\circ$ .

Müller *et al.*<sup>16-18</sup> showed that for  $\text{Cr}^{3+}$  ions in cubic

TABLE I. Crystallographic data of  $\text{TiO}_2$ ,  $\text{GeO}_2$ , and  $\text{SnO}_2$ .  $R_z$  is the distance between the cation and  $\text{O}_z$ , and  $R_{xy}$  is the distance between the cation and  $\text{O}_{xy}$ .  $\alpha$  is an angle, less than  $45^\circ$ , between the  $X$  axis and the cation- $\text{O}_{xy}$  bonding axis in the  $XY$  plane.

	$a$ (Å)	$c$ (Å)	$R_z$ (Å)	$R_{xy}$ (Å)	$\alpha$ (°)
$\text{TiO}_2$	4.594	2.959	1.988	1.944	40.44
$\text{GeO}_2$	4.395	2.860	1.91	1.87	39.9
$\text{SnO}_2$	4.737	3.185	2.056	2.052	39.09

TABLE II. Spin-Hamiltonian parameters of  $\text{Cr}^{3+}$  and  $\text{Mn}^{4+}$  in rutile-type crystals. The values for  $|D|$  and  $|E|$  are in units of  $\text{cm}^{-1}$ .

	$g$	$ D $	$ E $	Ref.
$\text{TiO}_2:\text{Cr}^{3+}$	1.97	0.680	0.140 <sup>b</sup>	26,27
$\text{TiO}_2:\text{Mn}^{4+}$	1.9983	0.400	0.139 <sup>a</sup>	28
$\text{GeO}_2:\text{Cr}^{3+}$	1.980	0.634	0.137 <sup>a</sup>	29
$\text{SnO}_2:\text{Cr}^{3+}$				
(EPR) <sub>I</sub>	1.976	0.651	0.174 <sup>b</sup>	11
(EPR) <sub>II</sub>	1.975	0.703	0.146 <sup>b</sup>	11

<sup>a</sup> $E/D < 0$  for all crystals.

<sup>b</sup> $D < 0$ .

crystals, the intrinsic parameter  $\bar{b}_2(R)$  is represented by a Lennard-Jones-type function having a two-term power law with constants  $A$  and  $B$  given as

$$\bar{b}_2(R) = -A \left( \frac{R_0}{R} \right)^n + B \left( \frac{R_0}{R} \right)^m, \quad (5)$$

where  $R_0$  is a reference length and  $R$  is the distance between the metal and ligand. However, Eq. (5) must be modified for rutile-type crystals because of the large rhombic distortion due to  $O_z$  and  $O_{xy}$  having nonsymmetric sites with respect to the metal ion. Equation (5) should then be rewritten as

$$\bar{b}_2(R_z) = -A_1 \left( \frac{R_0}{R_z} \right)^n + B_1 \left( \frac{R_0}{R_z} \right)^m, \quad (6)$$

$$\bar{b}_2(R_{xy}) = -A_2 \left( \frac{R'_0}{R_{xy}} \right)^n + B_2 \left( \frac{R'_0}{R_{xy}} \right)^m, \quad (7)$$

where  $A_1$  and  $B_1$  denote the constants for  $\bar{b}_2(R_z)$ , and

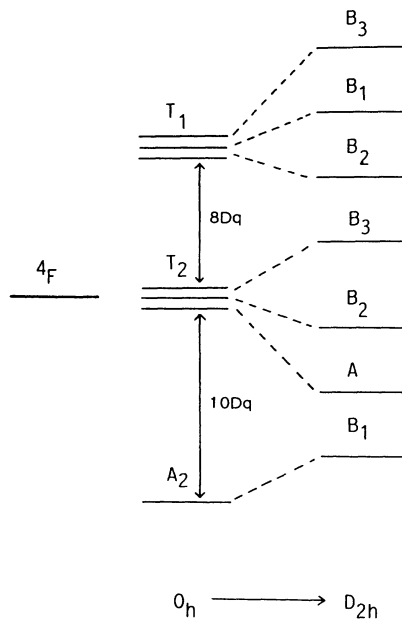


FIG. 3. Schematic energy level diagram for a  $\text{Cr}^{3+}$  ion in a rutile-type crystal.

TABLE III. Calculated superposition model parameters for  $\text{Cr}^{3+}$  in rutile-type crystals and those from the cubic crystals  $\text{SrTiO}_3$  and  $\text{MgO}$  (Ref. 16).

	Rutile type		$\text{SrTiO}_3$	$\text{MgO}$
	(z)	(xy)		
$R_0$ ( $\text{\AA}$ )	2.056	2.052	1.952	2.101
$R_m$ ( $\text{\AA}$ )	2.003	1.932	1.967	2.102
$A$ ( $\text{cm}^{-1}$ )	-0.375	-1.074	-10.6	-8.8
$B$ ( $\text{cm}^{-1}$ )	-0.278	-0.717	-8.2	-6.5
$n$	12	12	$\sim 10$	$\sim 10$
$m$	15	15	$\sim 13$	$\sim 13$

$A_2$  and  $B_2$  for  $\bar{b}_2(R_{xy})$ .  $R_0$  and  $R'_0$  are, respectively, set equal to the reference length of 2.056 and 2.052  $\text{\AA}$  from the  $\text{SnO}_2$  crystal. The exponents  $n$  and  $m$  are on the order of 10, and the constraint  $m - n = 3$  is imposed.<sup>16</sup> The intrinsic parameters in Eqs. (6) and (7) have extremal values at

$$R_m = R_0 \left( \frac{mB_1}{nA_1} \right)^{1/(m-n)} \quad (8)$$

$$R'_m = R'_0 \left( \frac{mB_2}{nA_2} \right)^{1/(m-n)}, \quad (9)$$

where the distance  $R_m$  on the  $Z$  axis gives the extremal value of  $\bar{b}_2(R_z)$  and  $R'_m$  on the  $XY$  plane gives those for  $\bar{b}_2(R_{xy})$ .

The experimental values of  $\bar{b}_2(R_z)$  and  $\bar{b}_2(R_{xy})$  for rutile-type crystals were obtained from Eqs. (3) and (4) using the spin-Hamiltonian parameters  $D$  and  $E$  in Table II. The constants  $A_1$ ,  $B_1$ ,  $A_2$ ,  $B_2$ ,  $n$ , and  $m$  in Eqs. (6) and (7) were determined from the intrinsic parameters of rutile-type crystals  $\text{GeO}_2$  and  $\text{TiO}_2$ . Table III lists the calculated values of these constants, and for reference the constants for the cubic crystals  $\text{SrTiO}_3$  and  $\text{MgO}$  are shown.<sup>16</sup> Notice that these constants of rutile-type crystals are about  $\frac{1}{10}$  those of cubic crystals. In addition,  $A_1$

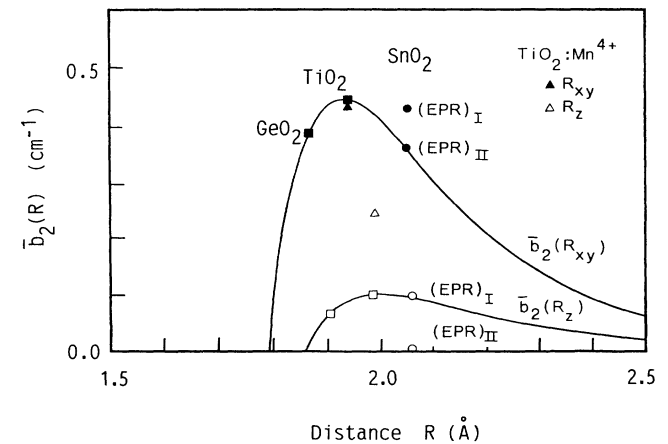


FIG. 4.  $\bar{b}_2(R_z)$  and  $\bar{b}_2(R_{xy})$  vs distance. Experimental values of  $\bar{b}_2(R_z)$  and  $\bar{b}_2(R_{xy})$  of  $\text{GeO}_2:\text{Cr}^{3+}$ ,  $\text{TiO}_2:\text{Cr}^{3+}$ , and  $\text{SnO}_2:\text{Cr}^{3+}$  are also indicated.

and  $B_1$  for  $R_z$  are approximately three times smaller than  $A_2$  and  $B_2$  for  $R_{xy}$ . Figure 4 shows curves of the intrinsic parameters using these calculated constants as a function of the distance between the  $\text{Cr}^{3+}$  ion and oxygen atom. The experimental values of  $\bar{b}_2(R_z)$  and  $\bar{b}_2(R_{xy})$  obtained from the  $D$  and  $E$  in Table II are also shown. It should be noted that the intrinsic parameter for  $R_z$  of  $\text{TiO}_2:\text{Mn}^{4+}$  is twice as large as that of  $\text{Cr}^{3+}$  in rutile-type crystals, possibly a result of the interaction of  $\text{Mn}^{4+}$  with the oxygen atom on the  $[110]$  axis being different from the interaction of  $\text{Cr}^{3+}$  with oxygen atoms.

### III. ANALYSIS OF THE $(\text{EPR})_I$ AND $(\text{EPR})_{II}$ SPECTRA

#### A. $(\text{EPR})_I$

The experimental intrinsic parameter for  $R_z$  from  $(\text{EPR})_I$  correlates well with the theoretical  $\bar{b}_2(R_z)$  function as shown in Fig. 4. In contrast, however, the corresponding value for  $R_{xy}$  does not fit the  $\bar{b}_2(R_{xy})$  function. This subsequently indicates that the  $\text{O}_{xy}$  atoms moved from their normal sites toward the central  $\text{Cr}^{3+}$  ion while the  $\text{O}_z$  atoms have remained stationary. If the displaced oxygen atoms leave the crystal axes, then the magnetic principal axes would shift from these axes. However, the magnetic principal axes of  $(\text{EPR})_I$  coincide with the orientation of the crystal axes of the octahedron; hence the displaced  $\text{O}_{xy}$  atoms would lie on the  $\text{Cr}-\text{O}_{xy}$  bonding axis. The distance from the  $\text{Cr}$  ion to the  $\text{O}_z$  and  $\text{O}_{xy}$  atoms is, respectively, expressed as

$$R_z = R_0, \quad (10)$$

$$R_{xy} = R'_0 + \Delta_{xy}, \quad (11)$$

where  $\Delta_{xy}$  is the displacement of the  $\text{O}_{xy}$  atoms from the reference length  $R'_0$  on the  $\text{Cr}-\text{O}_{xy}$  bonding axis. The spin-Hamiltonian parameters  $D$  and  $E$  in Eqs. (3) and (4) can then be represented as a function of  $\Delta_{xy}$ . It is convenient to use the ratio  $\Delta_{xy}/R'_0$  in Eqs. (6) and (7) to represent the displacement from the normal site. Figure 5 shows the variation of the spin-Hamiltonian parameters  $D$  and  $E$  in Eqs. (3) and (4) versus  $\Delta_{xy}/R'_0$ , where two points on the  $D$  and  $E$  curves, i.e.,  $\Delta_{xy}/R'_0 = -0.078$  and  $-0.035$ , corresponded with the experimentally obtained  $(\text{EPR})_I$  parameters. As shown by Table IV, the radius of  $\text{Cr}^{3+}$ ,  $R(\text{Cr}^{3+})$ , is  $0.08 \text{ \AA}$  less than that of  $\text{Sn}^{4+}$ ,  $R(\text{Sn}^{4+})$ . At  $\Delta_{xy}/R'_0 = -0.078$ ,  $\Delta_{xy} = -0.16 \text{ \AA}$ ; thus, the displacement of the  $\text{O}_{xy}$  atoms towards the central  $\text{Cr}^{3+}$  ion is much larger than the reduction of the metal-ionic radius [ $R(\text{Cr}^{3+}) - R(\text{Sn}^{4+}) = -0.08 \text{ \AA}$ ] and electrons in the outer shell of  $\text{O}^{2-}$  would then overlap onto the  $\text{Cr}^{3+}$  ion. Such a large displacement in  $\text{O}_{xy}$  atoms can obviously be excluded. On the other hand, when  $\Delta_{xy}/R'_0 = -0.035$ , then  $\Delta_{xy} = -0.072 \text{ \AA}$ , being in

TABLE IV. Ion radii of  $\text{Sn}^{4+}$ ,  $\text{Ti}^{4+}$ ,  $\text{Ge}^{4+}$ ,  $\text{Cr}^{3+}$ , and  $\text{O}^{2-}$ . Units of  $\text{\AA}$  are used.

$\text{Sn}^{4+}$	$\text{Ti}^{4+}$	$\text{Ge}^{4+}$	$\text{Cr}^{3+}$	$\text{O}^{2-}$
0.84	0.77	0.69	0.76	1.22

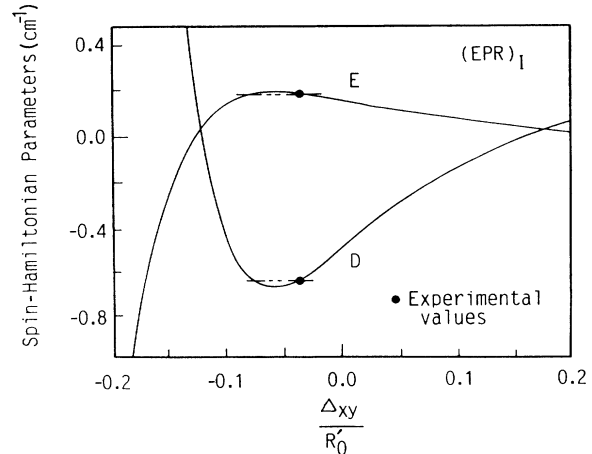


FIG. 5. Spin-Hamiltonian parameters vs  $\Delta_{xy}/R'$  when the two nearest-neighbor oxygen atoms on the  $Z$  axis are located at their normal sites. Experimental values of  $D$  and  $E$  for  $(\text{EPR})_I$  are also indicated.

good agreement with

$$\frac{R(\text{Cr}^{3+}) - R(\text{Sn}^{4+})}{R'_0} = -0.039. \quad (12)$$

In this case the displacement of the  $\text{O}_{xy}$  atoms corresponds to the reduction of the metal-ionic radius. The distance between the  $\text{O}_{xy}$  atoms and the  $\text{Cr}$  ion in the  $XY$

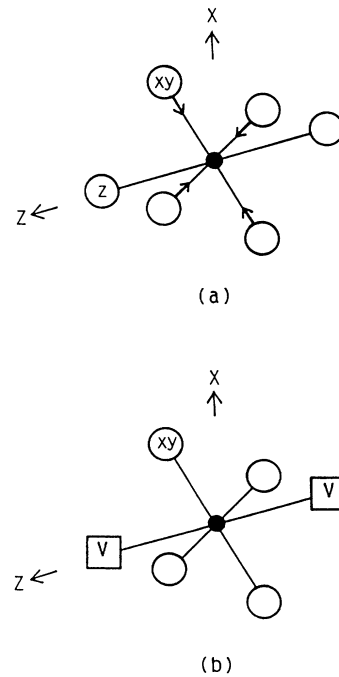


FIG. 6. Local structure of oxygen atoms around a  $\text{Cr}^{3+}$  ion for  $(\text{EPR})_I$  and  $(\text{EPR})_{II}$ . (a) Representation of  $(\text{EPR})_I$  in which the nearest-neighbor oxygen atoms on the  $XY$  plane move toward the  $\text{Cr}^{3+}$  ion in the octahedron. (b) Representation of  $(\text{EPR})_{II}$  in which the nearest-neighbor oxygen atoms on the  $Z$  axis are vacant.

plane would decrease by 0.072 Å, or 3.5%, in the direction of the Cr-O<sub>xy</sub> bond due to the small ion radius of Cr<sup>3+</sup>, i.e., O<sub>xy</sub> atoms are 1.980 Å away from Cr<sup>3+</sup> on the XY plane and O<sub>z</sub> atoms are at their normal sites as shown in Fig. 6(a).

If the presented superposition model was incorrect, then the value  $\Delta_{xy}/R'_0$  for the experimental values of  $D$  would not correlate with one for the experimental  $E$ . Experimental data of  $D$  and  $E$ , shown in Fig. 5, however, show good agreement at the same ratio  $\Delta_{xy}/R'_0$ . It is therefore concluded that the spin-Hamiltonian parameters  $D$  and  $E$  for (EPR)<sub>I</sub> are only a function of  $\Delta_{xy}/R'_0$  at a constant  $R_z$ .

### B. (EPR)<sub>II</sub>

As shown in Fig. 4, the experimental intrinsic parameter  $\bar{b}_2(R_z)$  for (EPR)<sub>II</sub> is near zero, thus suggesting it is negligible, and thereby allowing Eqs. (3) and (4) to be rewritten as

$$D_v = -2\bar{b}_2(R_{xy}), \quad (13)$$

$$E_v = 2\bar{b}_2(R_{xy})\cos 2\alpha, \quad (14)$$

where  $D_v$  and  $E_v$  denote the theoretical spin-Hamiltonian parameters for  $\bar{b}_2(R_z)=0$ . Note, if  $R_z$  in Eq. (6) goes to infinity, then the intrinsic parameter for  $R_z$  approaches zero. Therefore, Eqs. (13) and (14) represent the vacancies of two O<sub>z</sub> atoms [Fig. 6(b)]. The spin-Hamiltonian parameters  $D_v$  and  $E_v$  having the two O<sub>z</sub> vacancies are shown in Fig. 7. For reference, parameter  $D$  from Eq. (3) having two O<sub>z</sub> atoms at  $R_0=R_z$  is also shown (see Fig. 5). On the  $D_v$  and  $E_v$  curves, two points, i.e.,  $\Delta_{xy}/R'_0 = -0.096$  and 0, corresponded with the experimentally obtained  $D$  and  $E$  values, respectively. The experimental values of  $D$  and  $E$  are particularly shown as  $D_{\text{exp}}$  and  $E_{\text{exp}}$  at  $\Delta_{xy}/R'_0=0$ , respectively. As indicated in Fig. 7,  $D_{\text{exp}}$  does not agree with  $D$  from Eq. (3). When

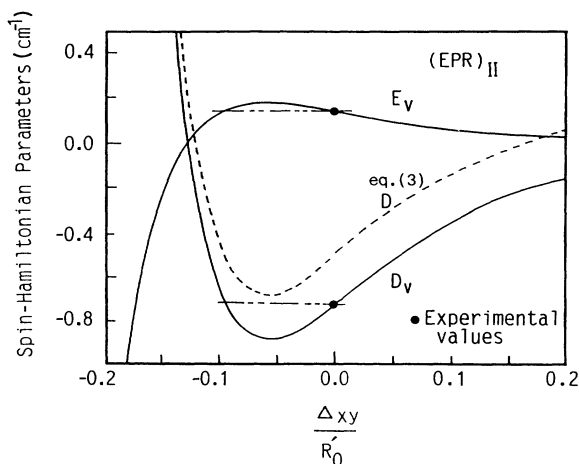


FIG. 7. Spin-Hamiltonian parameters vs  $\Delta_{xy}/R'$  when the two nearest-neighbor oxygen atoms are vacant. The spin-Hamiltonian parameter  $D$  from Eq. (3) is as shown. Experimental values of  $D$  and  $E$ , i.e.,  $D_{\text{exp}}$  and  $E_{\text{exp}}$ , are also indicated by solid circles.

$\Delta_{xy}/R'_0 = -0.096$ , then  $\Delta_{xy} = -0.20$  Å; and the displacement of the O<sub>xy</sub> atoms is too large for the Cr<sup>3+</sup> ion to easily replace the Sn<sup>4+</sup> one. It therefore seems reasonable that

$$\Delta_{xy}/R'_0 = 0, \quad \Delta_{xy} = 0.$$

This implies that the four O<sub>xy</sub> atoms remain at their normal sites and that the two O<sub>z</sub> atoms are vacant as schematically shown in Fig. 6(b). The vacant O<sub>z</sub> atoms in (EPR)<sub>II</sub> would then compensate for the trivalent ion charges if the O<sub>xy</sub> atoms stayed in their normal sites.

From Eqs. (13) and (14), a simple theoretical ratio for the spin-Hamiltonian parameters can be obtained as follows:

$$\frac{E_v}{D_v} = -\cos 2\alpha, \quad (15)$$

where the ratio  $E_v/D_v$  depends only on the angle  $\alpha$ . A comparison of the theoretical  $E_v/D_v$  using the value of  $\alpha = 39.09^\circ$  from Table I and the experimental value  $E_{\text{exp}}/D_{\text{exp}}$  from (EPR)<sub>II</sub> shows good agreement, i.e.,

$$E_v/D_v = -0.205, \quad E_{\text{exp}}/D_{\text{exp}} = -0.208.$$

The ratio  $E_{\text{exp}}/D_{\text{exp}}$  can also be directly determined from the experiment of the angular dependence of (EPR)<sub>II</sub> by

$$\frac{E_{\text{exp}}}{D_{\text{exp}}} = \frac{1 - 3 \cos^2 \theta}{3 \sin^2 \theta}, \quad (16)$$

where  $\theta$  is the angle at which the allowed and forbidden transition energies are equal in the resonance magnetic field on the [001] plane. Equation (16) also provides a means for checking the ratio  $E_v/D_v$  using an experimentally obtained value of  $\theta = 66^\circ$ . This large angle is actually located outside Fig. 1. The experimental study for this angle would be published elsewhere by us. By substituting  $\theta = 66^\circ$  into Eq. (16), the ratio  $E_{\text{exp}}/D_{\text{exp}} = -0.201$  is obtained, a value which correlates well with  $E_v/D_v$  in both magnitude and sign.

The spin-Hamiltonian parameters for an interstitial Cr<sup>3+</sup> ion can be calculated from Eqs. (3) and (4). The conventional SnO<sub>2</sub> lattice constants give  $R_z = 1.718$  Å,  $R_{xy} = 2.342$  Å, and  $\alpha = 47.2^\circ$ , with  $D = -1.99$  cm<sup>-1</sup>,  $E = -0.02$  cm<sup>-1</sup>, and  $E/D = 0.01$ . However, it should be noted that these values are significantly different from those of (EPR)<sub>II</sub>, especially the positive sign for the ratio  $E/D$ . It is consequently concluded that the (EPR)<sub>II</sub> spectrum does not apply to the interstitial Cr<sup>3+</sup> ion, but instead indicates a substitutional Cr<sup>3+</sup> ion, being consistent with an analysis of the line intensity ratio of the superhyperfine structure.<sup>12</sup>

Hou, Summitt, and Tucker<sup>9</sup> obtained the (EPR)<sub>II</sub> spectrum for Cr<sup>3+</sup> in reduced SnO<sub>2</sub> crystals and no (EPR)<sub>I</sub> spectrum was observed. Furthermore, in reoxidized crystals the opposite phenomenon occurred. We consider that these phenomena are associated with the existence of oxygen atom vacancies for (EPR)<sub>II</sub>. These vacancies in SnO<sub>2</sub> crystals would be an essential defect in its non-stoichiometry structure. In fact, if many Sn<sup>4+</sup> ions exist

in SnO<sub>2</sub> crystals which are coupled nonstoichiometry with the two oxygen vacancies on the Z axis, then these Sn<sup>4+</sup> ions can easily be substituted for by the Cr<sup>3+</sup> ions.

#### IV. CONCLUSIONS

The origin of the EPR spectra, (EPR)<sub>I</sub> and (EPR)<sub>II</sub>, for Cr-doped SnO<sub>2</sub> crystals was investigated by applying the superposition model specifically developed for Cr<sup>3+</sup> ions in rutile-type crystals. The results suggested that these spectra originated from the substitutional Cr<sup>3+</sup> having the different local structure of its surrounding oxygen atoms. The (EPR)<sub>I</sub> spectrum showed that the four nearest-neighbor oxygen atoms on the XY plane moved toward the central substitutional Cr<sup>3+</sup> ion by 0.072 Å

(3.5%) in comparison to the normal oxygen octahedron. This decrease of the distance between Cr<sup>3+</sup> and oxygens corresponds to the reduction in the metal-ionic radius. On the other hand, the (EPR)<sub>II</sub> spectrum showed the Cr<sup>3+</sup> ion to be coupled with the vacancy of two nearest-neighbor oxygen atoms on the Z axis. The ratio  $E/D = -0.205$  was theoretically obtained from the superposition model, and showed in good agreement with the experimental  $E/D$  in both magnitude and sign.

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- <sup>1</sup>M. Nagasawa, S. Shionoya, and S. Makishima, *Jpn. J. Appl. Phys.* **4**, 195 (1965).  
<sup>2</sup>M. Nagasawa and S. Shionoya, *Jpn. J. Appl. Phys.* **10**, 472 (1971).  
<sup>3</sup>M. Nagasawa and S. Shionoya, *J. Phys. Soc. Jpn.* **30**, 1118 (1971).  
<sup>4</sup>Z. M. Jarzebski and J. P. Marton, *J. Electrochem. Soc.* **123**, 199C (1976).  
<sup>5</sup>Z. M. Jarzebski and J. P. Marton, *J. Electrochem. Soc.* **123**, 299C (1976).  
<sup>6</sup>Z. M. Jarzebski and J. P. Marton, *J. Electrochem. Soc.* **123**, 333C (1976).  
<sup>7</sup>S. Samson and C. G. Fonstad, *J. Appl. Phys.* **44**, 4618 (1973).  
<sup>8</sup>W. H. From, *Phys. Rev.* **131**, 961 (1963).  
<sup>9</sup>S. L. Hou, R. W. Summitt, and R. F. Tucker, *Phys. Rev.* **154**, 258 (1967).  
<sup>10</sup>W. Rhein, *Z. Naturforsch. Teil A* **27**, 741 (1972).  
<sup>11</sup>H. Hikita, K. Takeda, Y. Kimura, and T. Kurose, *J. Phys. Soc. Jpn.* **57**, 2529 (1988).  
<sup>12</sup>H. Hikita, K. Takeda, and Y. Kimura, *Phys. Status Solidi A* **119**, 251 (1990).  
<sup>13</sup>D. J. Newman and W. Urban, *Adv. Phys.* **24**, 793 (1975).  
<sup>14</sup>D. J. Newman and E. Siegel, *J. Phys. C* **9**, 4285 (1976).  
<sup>15</sup>E. Siegel and K. A. Müller, *Phys. Rev. B* **20**, 3587 (1979).  
<sup>16</sup>K. A. Müller and W. Berlinger, *J. Phys. C* **16**, 6861 (1983).  
<sup>17</sup>K. A. Müller, W. Berlinger, and J. Albers, *Phys. Rev. B* **32**, 5837 (1985).  
<sup>18</sup>K. A. Müller, *J. Phys. Soc. Jpn.* **55**, 719 (1986).  
<sup>19</sup>M. Arakawa, H. Aoki, H. Takeuchi, T. Yosida, and K. Horai, *J. Phys. Soc. Jpn.* **51**, 2459 (1982).  
<sup>20</sup>H. Takeuchi and M. Arakawa, *J. Phys. Soc. Jpn.* **53**, 376 (1984).  
<sup>21</sup>M. Arakawa, H. Ebisu, and H. Takeuchi, *J. Phys. Soc. Jpn.* **55**, 2853 (1986).  
<sup>22</sup>M. Arakawa, H. Ebisu, and H. Takeuchi, *J. Phys. Soc. Jpn.* **57**, 2801 (1988).  
<sup>23</sup>C. Rudowicz, *Phys. Rev. B* **37**, 27 (1988).  
<sup>24</sup>H. Hikita, K. Takeda, and Y. Kimura, *Solid State Commun.* **74**, 1241 (1990).  
<sup>25</sup>W. H. Baur, *Acta Crystallogr.* **9**, 515 (1956).  
<sup>26</sup>H. J. Gerritsen, S. E. Harrison, H. R. Lewis, and J. P. Wittke, *Phys. Rev. Lett.* **2**, 153 (1959).  
<sup>27</sup>H. J. Gerritsen, S. E. Harrison, and H. R. Lewis, *J. Appl. Phys.* **31**, 1566 (1960).  
<sup>28</sup>H. G. Andresen, *J. Chem. Phys.* **35**, 1090 (1961).  
<sup>29</sup>P. P. Madacsi, M. Stapelbroek, and O. R. Gilliam, *Phys. Rev. B* **9**, 2023 (1974).  
<sup>30</sup>C. Kikuchi, I. Chen, W. H. From, and P. W. Dorain, *J. Chem. Phys.* **42**, 181 (1965).  
<sup>31</sup>T. Shimizu, *J. Phys. Soc. Jpn.* **23**, 848 (1967).  
<sup>32</sup>D. P. Madacsi and O. R. Gilliam, *Phys. Lett.* **41A**, 63 (1972).