# Percolation effects and oxygen inhomogeneities in $YBa_2Cu_3O_{7-\delta}$ crystals

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The magnetization curves of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7- $\delta$ </sub> crystals are widely observed to exhibit a pronounced lowfield minimum in the temperature range 30 K < T < T<sub>c</sub>. We demonstrate that these magnetization anomalies correlate with the *c*-axis lattice parameter, and hence with the specific oxygen deficiency  $\delta$ . We interpret this low-field feature in terms of a field-induced decoupling of regions of oxygen-rich material by boundaries of oxygen-poor material, a phenomenon reminiscent of the behavior in granular superconductors. A "phase diagram" that demarcates the multigrain onset as a function of temperature and  $\delta$  is then constructed. The shape of the "phase boundaries" is described using a percolation model. This analysis demonstrates that magnetization is a very sensitive measure of crystal quality.

#### **INTRODUCTION**

The constant-temperature magnetization curves of single crystals of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-8</sub> (Y-Ba-Cu-O) invariably exhibit anomalous features: a minimum at low magnetic fields (0-2 T) as well as a high-field (2-6 T) maximum. Kupfer et al.<sup>1</sup> asserted that these crystals showed granular behavior in which intergrain  $J_c$ 's were strongly field dependent. Sulpice et al.<sup>2</sup> studied the remnant magnetization of several crystals as a function of crystal radius and did not observe size scaling. By subdividing a crystal using laser ablation, Yeshurun et al.<sup>3</sup> found that the remnant magnetization of samples divided into sections smaller than several hundred micrometers did scale with size at 5 K. This was not true for crystals divided into larger sections. These results suggested the presence of defects impeding the current flow. Daeumling et al.<sup>4</sup> examined the size dependence of the magnetization at various temperatures below  $T_c$  by subdividing individual crystals. They found that the magnetization curves  $(30 \text{ K} \le T \le 80 \text{ K})$  scaled with the sample radius at low fields, but not at high fields, results which are consistent with a granular model. The authors concluded that oxygen defects were the likely source of the granularity. At lower temperatures they saw no evidence for granular behavior. Welp et  $al.^5$  conducted a similar study and saw evidence for scaling with size.

While these experiments suggest that sample inhomogeneities are generally present in crystals of Y-Ba-Cu-O, their origin remains undetermined. Since the coherence length of this system is on the order of tens of Å, these inhomogeneities are likely to influence magnetic and transport properties. Distinguishing such extrinsic effects from intrinsic properties is essential for improving our understanding of superconductivity in the high- $T_c$  materials.

In this paper we present the results of a systematic study of  $YBa_2Cu_3O_{7-\delta}$  crystals employing measurements of x-ray diffraction, magnetization, ac susceptibility, and

electrical resistivity. Our principal finding is that there is an unmistakable correlation between the low-field minimum in the magnetization (at a field  $H_{\min}$ ) and the c-axis lattice parameter. We relate the c-axis parameter to the oxygen-deficiency parameter  $\delta$ , using the results of Parks et al.,<sup>6</sup> and thus derive the dependencies of  $H_{\min}$ on  $\delta$  and T. We confirm that crystals exhibit behaviors characteristic of homogeneous superconductors for  $H < H_{\min}$  and inhomogeneous superconductors for  $H > H_{\min}$ . The granular behavior observed for  $H > H_{\min}$ is attributed to clusters of oxygen defects that restrict supercurrent flow and allows excess flux to enter the crystal. The observed  $H_{\min}(\delta)$  data are then described by a two-dimensional percolation model for oxygen defects. These data demonstrate that magnetization is an especially sensitive measure of crystal homogeneity.

### SAMPLE PREPARATION

Crystals were grown using a self-decanting BaO:CuO flux method<sup>7</sup> adapted from the procedures reported by Sadowski and Scheel.<sup>8</sup> Starting materials were Y<sub>2</sub>O<sub>3</sub>, BaCO<sub>3</sub>, and CuO of 99.99% or higher purity. The composition chosen for the melt was 10.2-wt % YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub> mixture in a BaO:CuO 0.28:0.72-mol eutectic solvent (mp near 890 °C), resulting in an overall molar charge composition of 1:18.4:45.1=[Y]:[Ba]:[Cu]. This particular mixture feaures a relatively large concentration of solvent and was reported<sup>8</sup> to yield thick, multimillimeter-sized  $YBa_2Cu_3O_{7-\delta}$  crystals. The components were mixed by grinding with an agate mortar and pestle for 30 min; reactions were carried out in zirconia crucibles in order to minimize the introduction of impurity ions into the superconducting crystals. Semiquantitative elemental analyses by electron microscopy (combined SEM and EDX), showed that clean crystal surfaces were impurity free, whereas trace levels of zirconium were just detectable in frozen flux droplets. In a typical crystal growth experi-

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ment, a 20-25-g charge was packed into a 10-ml roundbottom zirconia crucible and heated in a muffle furnace according to the following schedule: heat to 990 °C in 3.5 h, soak 20-24 h, step cool to 950°C, cool at 0.4°C/h to 870 °C, cool in 96 h to room temperature. Crystals grew as projections from the crucible walls and were easily extracted mechanically. Post-growth anneals were carried out under flowing oxygen at 1 atm. In a typical annealing procedure, the crystals were first heated over several hours to 800-850°C, cooled in 24 h to 700°C, soaked 96 h at 700 °C, cooled over 24 h to the annealing temperature, soaked for various times, and then finally cooled in 24 h to room temperature. Annealing temperatures ranged from 420-565 °C; soak times from several days to a month (see Table I). In general, the preheating step at 700-850 °C seemed to produce a greater number of samples with sharper superconducting transitions and higher onset temperatures.

The oxygen content of each crystal was estimated from its measured c-axis lattice parameter using the data reported by Parks et al.;<sup>6</sup> in that work, c-axis determinations from refined x-ray powder diffraction data were correlated with oxygen content obtained by iodometric titration. To this data set were added two additional data points for (1) tetragonal YBa2Cu3O6.0 from a singlecrystal x-ray-diffraction structure determination [a=3.863(2) Å, c=11.830(4) Å],<sup>9</sup> and (2) a near fully oxygenated, high-quality (purity and  $T_c$ ) polycrystalline sample that was synthesized and chemically analyzed by bromo/iodometric titration<sup>10</sup> in this study [a=3.8838(8)]Å, b = 3.8164(4) Å, c = 11.664(1) Å;  $YBa_2Cu_3O_{6.98\pm0.01}$ ]. A linear fit of these data yields the relation

c = 12.8714 - 0.1728x Å, where  $x = 7 - \delta$  as it appears in YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7- $\delta$ </sub>.

To determine the c-axis length, each crystal was mounted and aligned on an automated four-circle diffractometer. The (0,0,11) and (0,0,11) diffraction peaks, excited with Cu  $K\alpha$  radiation, were each centered using a standard centering procedure. The  $K\alpha_1$ - $K\alpha_2$ doublets were then measured by step scanning in  $\pm 2\theta$  in  $0.02^\circ$  steps. These data were then least-squares fitted to double-Gaussian curves to determine centroids of all four peaks, from which c was calculated. The scatter in the values of the c axis was typically about  $\pm 0.003\%$ , which corresponds to an uncertainty in oxygen content of about  $\pm 0.03\%$ . This uncertainty is much smaller than the scatter in the c axis versus  $\delta$  data of Ref. 6 which yields an uncertainty in  $\delta$  of approximately  $\pm 0.03-0.04$ .

## MAGNETIZATION

Magnetization data, M(H), were obtained at several temperatures for each crystal in a Quantum Design SQUID magnetometer. The samples were cooled in a  $0\pm 30$ -G field and warmed above the superconductive transition temperature,  $T_c$ , between each temperature run. In all cases the field was oriented along the crystalline c axis so that the M(H) data reflect shielding currents which flow in the a-b plane. Figures 1(a) and 1(b) show the dip at  $H_{\min}$  for several temperatures for a crystal with a nominal deficiency,  $\delta \sim 0.17$ . At this nominal oxygen composition,  $H_{\min}$  increases with decreasing temperature. Whenever possible, the value for  $H_{\min}$  is determined from the initial ascending field sweep to avoid

TABLE I. List of the last stage of the sample anneals, their resulting *c*-axis lattice parameters, and corresponding oxygen content as determined in the text. Anneals were performed in oxygen unless otherwise stated.

Sample	Batch	Anneal	c (Å)	δ
1	A	565°C, 14 days	11.696	0.20
2	A	565 °C, 21 days <sup>a</sup>	11.695	0.19
3	A	565 °C, 21 days <sup>a</sup>	11.691	0.17
4	A	565°C, 21 days	11.693	0.18
5	В	440°C, 7 days	11.689	0.16
6	A	565° C, 28 days	11.691	0.17
7	С	475°C, 8.3 days	11.687	0.15
8	С	565 °C, 96 h	11.692	0.18
9	В	475°C, 8.3 days	11.684	0.13
10	В	475 °C, 8.3 days	11.672	0.06
11	D	515°C, 3 days	11.695	0.19
12	D	515°C, 3 days	11.693	0.18
13	Ε	565°C, 96 h	11.698	0.21
14	F	540°C, 6 days	11.695	0.19
15	Ε	unannealed	11.703	0.25
15 <i>A</i>	E	460°C, 15.5 days	11.685	0.14
16	G	505 °C, 8 days	11.683	0.12
17	H	475°C, 8 days	11.686	0.14
18	D	450°C, 8 days	11.682	0.12
19	Ε	450°C, 16 days <sup>a</sup>	11.6858	0.15
20	Ι	420°C, 10 days	11.681	0.11

<sup>a</sup>+460 °C, 5 min in air for detwinning.

field offsets due to flux trapped in the sample. In some samples the initial dip is at such a low field that it is not observed.

Figures 2(a) and 2(b) show the magnetization curves taken at a temperature of 60 K for a crystal before and after a 200-h, 460 °C oxygen anneal, with calculated  $\delta$ values of 0.25 and 0.14, respectively. These curves demonstrate that the magnetization features observed are controlled by the oxygen content as suggested earlier.<sup>1,4</sup> The resistivity and ac susceptibility of the unannealed crystal showed the broad transitions typically observed in oxygen-poor samples [Fig. 3(a)]. After the anneal, the transitions were 300 mK wide [Fig. 3(b)]. Details of these measurements are presented in Ref. 7.

Even though long oxygen anneals dramatically improve the crystals, full oxygenation is never achieved and a magnetization dip (at least at 60 K) is always observed. There are clearly still inhomogeneities present. This observation brings into question whether large single crystals can ever be fully oxygenated, possibly because of the limitations imposed by the kinetics of the system at the low oxygenation temperatures. Another possible explanation is that these residual crystal inhomogeneities are due to cation disorder which would distort the c axis versus  $\delta$  relationship and would be unaffected by the oxygen anneals.

Figures 4(a) and 4(b) show data for three different crystals with different oxygen content, demonstrating the qualitative features of the magnetization that change with  $\delta$ . Three striking features of these curves are (1) the shift in the position of the low-field magnetization dip,  $H_{\min}$ , (2) the shift in the high-field magnetization maximum,  $H_{\rm max}$ , and (3) the overall change in the magnitude of the magnetization. The second two features are due to the pinning behavior of vortices<sup>1,4</sup> and will not be discussed here.

In the critical state, the magnetization reflects the critical current density,  $J_c$ , which may be expressed in the standard Bean model form<sup>11</sup>  $J_c \approx (M_+ - M_-)/2r$ , where r is the radius of the region through which the screening currents flow. For a homogeneous material, r is identical to the radius of the sample, R, and the derived  $J_c$  will be independent of R. For an inhomogeneous material r < R, and the derived  $J_c$  depends on R. Thus, the homogeneity of a crystal can be tested by cleaving it and examining the magnetization as a function of R.

The size scaling data of Ref. 4 suggest that crystals are homogeneous for  $H < H_{\min}$  and inhomogeneous (or granular) for  $H > H_{\min}$ . Welp et al.<sup>5</sup> performed a fracture experiment and claimed that the magnetization roughly scaled with size and was, therefore, homogeneous.

YBa<sub>2</sub>Cu<sub>3</sub>O

2

Н (T) 3

Unannealed: δ~0.25

Annealed: δ-

-0.1

Jnannealed:

δ~0.25

5

1.5

1

0.5

-0.5

-1.5

1.5

1

0.5

0

-0.5

- 1

-1.5

M (10<sup>5</sup> A/m)

0

1

M (10<sup>5</sup> A/m)

a)

Annealed:

 $\delta \sim 0.14$ 

60K

(b)

н (T) FIG. 1. Magnetization loop of crystal no. 3 with  $\delta \approx 0.17$  at several temperatures showing the change of  $H_{\min}$  with temperature. (b) expands the low-field region of (a) and the arrows indicate the positions of  $H_{\min}(T)$ .

0 0.5 1.5 2 н (T) FIG. 2. The 60 K magnetization loop of crystal no. 15 before and after annealing demonstrating that  $H_{\min}$  is controlled by oxygen content. (b) expands the low-field region of (a) and the arrows indicate the positions of  $H_{\min}(\delta)$ .





FIG. 3. Resistivity and ac susceptibility of the crystal in Fig. 2, (a) before and (b) after annealing.



FIG. 4. Magnetization loops of crystals 3, 10, and 13 with  $\delta = 0$ , 17, 0.06, and 0.21, respectively, at 60 K showing the dependence of  $H_{\min}$  on oxygen content. (b) expands the low-field region of (a) and the arrows indicate the positions of  $H_{\min}(\delta)$ .

We conducted similar breaking studies on several crystals in order to explore their homogeneity. The results of a breaking experiment on a crystal with  $\delta \sim 0.16$  and  $H_{\min} \sim 1$  T are shown in Fig. 5(a). The data are presented in the standard Bean model form with  $R = \frac{3}{2}w[1-(w/3l)]$  for the crystal face of length l and width w.<sup>11</sup> We see that for this specimen  $J_c$  is approximately independent of R at low fields with deviations becoming evident in the range  $H \approx 1-2$  T. Thus, the breakdown of scaling occurs at a field value close to  $H_{\min}$ .

Figure 5(b) shows similar data for a crystal with  $\delta \sim 0.21$  which shows neither the low-field decrease nor size scaling at any field. The raw magnetization data for this crystal look similar to that of Welp et al.,<sup>5</sup> where the magnetic moment of a crystal was measured before and after fracturing. They found that the samples' magnetic moment, m, approximately scaled with the mean fragment size and thus concluded that there was no evidence of granular behavior. This interpretation can be misleading since the magnetization does decrease with R. but not as predicted by the Bean model. This partial scaling of the magnetization implies that there is a distribution of current paths, some of which are smaller than the sample radius, rather than isolated current loops flowing around decoupled "grains." This result is consistent with earlier work<sup>2,3</sup> and is predicted for a percolating system.<sup>12</sup>

There is a degree of uncertainty in the relationship between the onset of granularity and the position  $H_{\min}$ 



FIG. 5. Results of the breaking experiment on (a) crystal no. 5 with  $\delta \sim 0.16$  and  $H_{\min} \sim 1$  T and (b) crystal no. 13 with  $\delta \sim 0.21$  and  $H_{\min} \sim 0$  presented in the standard Bean model form,  $J_c \approx (M_+ - M_-)/2R$ , where  $R = \frac{3}{2}w[1 - (w/3l)]$  is the radius of the crystal face of length *l* and width *w*.

since the dip is the result of the interplay between the magnitude of the intrinsic pinning and the intergranular coupling.<sup>4</sup> Therefore, as  $\delta$  decreases, the coupling improves, the pinning (which is most likely at the defects) decreases, and the minimum becomes less well defined (Fig. 4). However, the size scaling results clearly show the onset of granular behavior at fields near  $H_{\min}$ .

Figure 6(a), summarizing the  $H_{\min}(\delta, T)$  results, resembles a phase diagram with  $H_{\min}$  representing a phase boundary which determines whether or not a crystal is "granular" for a given  $\delta$  and T. These curves reflect the  $J_c(T)$  behavior for the microscopic oxygen-defect regions which define "grain boundaries." For temperatures near  $T_c$ ,  $H_{\min}(T)$  is almost independent of temperature and increases with decreasing  $\delta$ . As the temperature decreases,  $H_{\min}(T)$  increases rather sharply. This behavior is consistent with the relatively large intergranular  $J_c$ 's expected for well-oxygenated crystals and the increase in  $J_c$  (and subsequent loss of "granularity") anticipated at low temperatures.

### **DISCUSSION AND INTERPRETATION**

One significant difference between high- $T_c$  superconductors (HTS) and classical, low-temperature supercon-



FIG. 6. (a) Summary of the  $H_{\min}(\delta, T)$  results which resembles a phase diagram with  $H_{\min}$  representing a phase boundary which determines whether a crystal is "granular" or not for a given  $\delta$  and T. (b) Plot of  $H_{\min}$  as a function of  $\delta$  revealing curves for each of three temperatures converging near  $H_{\min} \sim 0$  at  $\delta \sim 0.20$ . The lines are linear fits to the data.

ductors is the short coherence lengths of the HTS. Since the coherence length in the *a-b* plane,  $\xi_{ab}$ , of the 1:2:3 system is so small (~10-15 Å), supercurrents are easily perturbed by microscopic inhomogeneities.<sup>13,14</sup> Whereas isolated defect regions with dimensions of the order of  $\xi_{ab}$  should be ideal pinning centers, extended regions with a thickness of that size (or smaller) will impede the supercurrent flow when the current density exceeds the local  $J_c(H,T)$ .

Contamination from the alumina, gold, or MgO crucibles used in the crystal growth undoubtedly contributed to the inhomogeneity of crystals in some of the earlier work. As stated above, the contamination due to the zirconia crucibles used in the synthesis of the crystals used in this study is below observable levels. We therefore assume that the observed magnetization behavior is due principally to oxygen defects.

The perturbing inhomogeneity boundaries can form at rather low oxygen-defect densities. We can estimate the value of  $\delta$  for which supercurrents become sensitive to defects by assuming a uniform defect density and currents that flow in independent layers. The last assumption is reasonable considering the anisotropy of the system. Since superconductivity is a reflection of the properties of a material averaged over a coherence volume, we also assume that the coherence length in the *a-b* plane is approximately independent of  $\delta$ .

The average distance between defects in the *a*-*b* plane<sup>4</sup> is  $\sim a/\sqrt{\delta}$ . Using  $a \sim 3.8$  Å and  $\xi_{ab} \sim 15$  Å, we estimate that, for currents circulating in the *a*-*b* planes of a crystal, defects are separated by one coherence length when  $\delta \sim 0.06$ . Such a crystal should not exhibit granular effects since it is uniform. (Several groups<sup>15-17</sup> have reported conditions which produce samples with ordered defects and exhibit depressed  $T_c$ 's.) As the crystals deviate from uniformity, extended defect-free regions surrounded by higher- $\delta$  "boundaries" are formed.

The pervasive presence of the oxygen-sensitive magnetization anomalies, along with the difficulty in preparing samples with ordered defects, leads us to conclude that a realistic analysis of samples synthesized with conventional oxygenation regimens (i.e., slow cools and/or long soaks) must include the effects of defect density fluctuations. A percolation model, in which oxygen defects randomly populate the chains, is the natural choice for describing how these defect fluctuations create oxygenpoor "grain boundaries." Since the superconductive properties of "1:2:3" are a function of  $\delta$ , these local fluctuations in the oxygen content (local being defined as a square of  $\xi_{ab}$ , or about four units cells, on each side) then modify the local properties of the sample creating regions with differing resistivities, critical current densities, transition temperatures, and critical fields. The result will be a distribution of current paths as currents flow through regions of least resistance at a given temperature and field. Since regions of lower and higher  $T_c$  are then in intimate contact, there should be a contribution from proximity effects to the  $J_c$  and  $H_c$  of the boundaries.

Assuming a random distribution of oxygen defects,  $p=1-\delta$  is the occupation probability of oxygen in a unit cell. There exists a critical oxygen deficiency,  $\delta_c$ , above

which there are no continuous current paths. The scaling theory of percolation clusters predicts<sup>18</sup> that, for electrical conductivity,  $\sigma \sim (p - p_c)^{\mu}$  or  $(\delta_c - \delta)^{\mu}$  near  $\delta_c$ . The critical exponent,  $\mu$ , has been found to be 1.7 in three dimensions and 1.2 in two.<sup>18</sup>

Adopting this percolation framework, Kubo *et al.*<sup>19</sup> have employed Monte Carlo simulations for a twodimensional square lattice and found  $\delta_c \sim 0.26$ . For  $\delta$ greater than 0.26, oxygen-rich, superconducting "grains" are separated by oxygen-poor, insulating boundaries so that there is no superconducting path through a sample. For  $\delta$  less than 0.26, a complete current path spans the sample and resistance measurements show metallic behavior with a superconducting transition.

In Fig. 6(b) we plot  $H_{\min}$  as a function of  $\delta$  for three different temperatures. A remarkable feature of these curves is that  $H_{\min}(T)$  extrapolates to zero near  $\delta \sim 0.20$ . Since  $H_{\min}$  signals the onset of granularity, a sample with  $H_{\min} = 0$  implies that the crystal has so many oxygen defects that it never exhibits single-grain behavior. The convergence of the three temperature curves at a  $\delta$  near the 0.26 predicted by Kubo *et al.*<sup>19</sup> suggests that the two-dimensional percolation picture is appropriate. The temperature independence of that critical point indicates that the coupling of the isolated grains is virtually temperature independent at these temperatures.

Encouraged by these observations, we present the following argument, which makes the connection between  $H_{\rm min}$  and  $\delta$ . Just as a dc critical current measurement of an inhomogeneous material reflects a distribution of weak link regions, so should  $H_{\rm min}$  reflect this granularity in a magnetization measurement. As percolation theory predicts and experiments have confirmed, <sup>12,20,21</sup>  $J_c \sim (p - p_c)^{(d-1)\nu}$  or  $(\delta_c - \delta)^{(d-1)\nu}$  with  $\nu = 1.35$  and 0.9 for two and three dimensions, respectively, exponents similar to those for conductivity.  $H_{\rm min}$ , being sensitive to these weak links, should scale in a similar manner and provide a sensitive probe of the onset of percolation. We can then correlate the shape of the boundary in the  $H_{\rm min}$ - $\delta$  phase diagram with the scaling law for critical current density in the inhomogeneous system.

As Kubo and Igarashi<sup>19</sup> pointed out, it is difficult to incorporate effects of local ordering into such a model. Fortunately, it is not necessary to know the details of the complex relationships between the superconducting parameters and  $\delta$  to understand the general behavior of the magnetization dip, only that the currents will seek the paths of least resistance and that these paths are uncorrelated.<sup>12</sup> Since  $J_c$  is a function of temperature and oxygen content, a scaling relation of the form  $H_{\min} \sim C(T) |\delta_c - \delta|^m$  should describe the shape of the boundary curve. A least-squares fit of the rather scattered 60-K data to that power law (Fig. 7) gives  $\delta_c = 0.22 \pm 0.03$  and  $m = 1.4 \pm 0.5$ . The results are consistent with both the Kubo and Igarashi<sup>19</sup> value for  $\delta_c$ and the above power law for two- or three-dimensional percolation.

It is likely that the subgranularity will be manifested in other electrical measurements. Resistivity measurements



FIG. 7. The 60 K data of Fig. 6(b). The line is a least-squares fit of the data to the function  $H_{\min} = C(T) |\delta_c - \delta|^m$ .

in the presence of an applied magnetic field show a broadening of the transition particularly for  $H \perp J$ . This broadening has been qualitatively fitted to a Bardeen-Stephen flux-flow model.<sup>22</sup> Measurements of the angular dependence of the resistivity in the transition also fit well within a flux-flow model.<sup>23</sup> However, an angleindependent background resistance is not accounted for in these simple flux-motion models, most likely because such models neglect the effects of granularity. These models assume a homogeneous superconductor in which the dissipation is due to the viscous flow of Lorentzforce-driven vortices. However, with the granularity and/or weak-link nature of these materials, one would expect a broadening of the transition even in the forcefree configuration  $(\mathbf{H} \| \mathbf{J})$  due to the percolative nature of the system.

### CONCLUSIONS

We have used magnetization as a sensitive tool to validate the "quality" of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7- $\delta}$  crystals. The observed dip in the magnetization signals the onset of granularity due to locally oxygen-depleted regions and correlates with average oxygen content via the *c*-lattice parameter. We construct an  $H_{\min}$ -T pseudo-phasediagram with boundaries that separate the phase space into single-grain and multigrain regimes for each  $\delta$ . By plotting the same data in an  $H_{\min}$ - $\delta$  diagram, the percolative nature of the problem becomes apparent. The data at 60 K follow an  $H_{\min} \sim C(\delta_c - \delta)^{\mu}$  scaling law with  $\delta_c$ close to a predicted value of 0.26 and  $\mu$  of 1.4, which is consistent with the scaling law for critical currents in two or three dimensions.</sub>

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