Magnetic properties of stage-2 Ni_c Mn_{1-c} Cl₂-graphite intercalation compounds

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Stage-2 Ni_cMn_{1-c}Cl₂-graphite intercalation compounds (with $0 \le c \le 1$) are two-dimensional randomspin systems with competing ferromagnetic and antiferromagnetic exchange interactions. The magnetic properties of these compounds have been studied by dc and ac magnetic susceptibilities. The Curie-Weiss temperature increases monotonically with increasing Ni concentration, suggesting that both Ni and Mn ions are randomly distributed on the triangular-lattice sites of the Ni_cMn_{1-c}Cl₂-intercalate layers. Its sign changes from negative to positive around $c \approx 0.22$. The exchange interaction between Ni-Mn spin pairs is ferromagnetic and is described by $J(Ni-Mn)=1.09[|J(Ni-Ni)J(Mn-Mn)|]^{1/2}=1.44$ K. The critical temperature T_c decreases rapidly with a dilution of Mn. In spite of ferromagnetic J(Ni-Mn), the ferromagnetic long-range order of Ni²⁺ disappears below $c \approx 0.6$. The large initial slope of $[d \ln T_c/dc]_{c=1}=2.38$ is ascribed to the two-dimensional Heisenberg-like character of stage-2 NiCl₂graphite intercalation compound. The critical behavior of these compounds shows a two-dimensional XY character. The critical exponent γ appears to be independent of c for $c \ge 0.7$: It is determined that $\gamma=2.27\pm0.02$ at c=0.9.

I. INTRODUCTION

Recently, the magnetic properties of random-mixture graphite intercalation compounds (RMGIC's) have received considerable interest.¹⁻⁵ The magnetic RMGIC's provide a variety of opportunities to study magnetic phase transitions of two-dimensional (2D) random-spin systems. There have been several studies of the magnetic properties of magnetic RMGIC's: stage-2 $Co_c Ni_{1-c}Cl_2$ GIC's,^{1,2} stage-1 Co_cMg_{1-c}Cl₂ GIC's,³ and stage-2 Co_cMn_{1-c}Cl₂ GIC's,^{4,5} where c is the Co concentration $(0 \le c \le 1)$. Yeh et al.^{1,2} succeeded in synthesizing stage-2 $Co_c Ni_{1-c} Cl_2$ GIC samples and reported the results of the dc magnetic susceptibility. These compounds have ferromagnetic intraplanar exchange interactions between Co-Co spin pairs and between Ni-Ni spin pairs. Nicholls and Dresselhaus³ have studied the magnetic phase transition of stage-1 $Co_c Mg_{1-c} Cl_2$ GIC's from the temperature and field dependences of the ac magnetic susceptibility. In these compounds a part of the Co^{2+} ions on the triangular-lattice sites is replaced by nonmagnetic Mg^{2+} ions. Suzuki et al.^{4,5} have studied the magnetic properties of stage-2 $Co_c Mn_{1-c} Cl_2$ GIC's, where the intraplanar exchange interaction between Co-Co spin pairs is ferromagnetic, but the intraplanar exchange interaction between Mn-Mn spin pairs is antiferromagnetic.

The magnetic behavior of stage-2 $Ni_c Mn_{1-c} Cl_2 GIC$'s seems to be similar to that of stage-2 $Co_c Mn_{1-c} Cl_2$ GIC's. The spin-frustration effect is expected to occur because of the competition between ferromagnetic intraplanar interactions between Ni-Ni spin pairs and antiferromagnetic intraplanar interactions between Mn-Mn spin pairs. In this paper we study the magnetic properties and magnetic phase transitions of stage-2 $Ni_c Mn_{1-c} Cl_2$ GIC's by using dc and ac magnetic susceptibility. The Curie-Weiss temperature, effective magnetic moment, and critical temperature will be determined as a function of Ni concentration. The magnetic phase diagram of these compounds will be discussed in comparison with that of stage-2 $Co_c Mn_{1-c} Cl_2$ GIC's.⁵

There have been several studies on the magnetic properties of the stage-2 NiCl₂ GIC (Refs. 6–8) and stage-2 MnCl₂ GIC.^{9–11} The stage-2 NiCl₂ GIC magnetically behaves like a 2D Heisenberg ferromagnet with small XY anisotropy on the triangular-lattice sites. The spin Hamiltonian of Ni²⁺ ions is described by

$$\mathcal{H} = -2J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + D \sum_i (S_i^z)^2 + 2J' \sum_{\langle i,m \rangle} \mathbf{S}_i \cdot \mathbf{S}_m , \qquad (1)$$

where z axis coincides with the c axis, $\langle i, j \rangle$ denotes nearest-neighbor pairs on the same intercalate layer, $\langle i, m \rangle$ denotes nearest-neighbor pairs on the adjacent intercalate layer, S is the spin of Ni^{2+} [S(Ni)=1], J is the intraplanar exchange interaction [J(Ni-Ni)=8.75 K], D is a single-ion anisotropy parameter [D(Ni)=0.80 K], and J' is the antiferromagnetic interplanar exchange interaction $(|J'|/J \approx 10^{-3})$. The magnetic and structural data of this compound are listed in Table I. This compound shows two magnetic phase transitions at $T_{cu} = 22.0$ K and $T_{cl} = 17.5$ K. Above T_{cu} the system is in the paramagnetic phase. In the intermediate phase between T_{cl} and T_{cu} , the system has 2D spin ordering. There is no spin correlation between adjacent NiCl₂ layers. Below T_{cl} there occurs the 3D antiferromagnetic phase where 2D ferromagnetic layers are antiferromagnetically stacked along the c axis. The stage-2 MnCl₂ GIC magnetically behaves like a 2D XY-like antiferromagnet on the triangular-lattice sites. The spin Hamiltonian of Mn^{2+} ions is expressed by the same form as Eq. (1) with spin $S(Mn) = \frac{5}{2}$, antiferromagnetic intraplanar exchange

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TABLE I. Structural and magnetic properties of the stage-2 NiCl₂ GIC and MnCl₂ GIC, where g is the g factor along the c plane, a is the in-plane lattice constant, and d is the c-axis repeat distance.

Stage-2 NiCl ₂ GIC		Stage-2 MnCl ₂ GIC		
S	1	S	5/2	
J (K)	8.75	J (K)	-0.20	
D (K)	0.80	D (K)	0.97	
T_{cl} (K)	17.5	T_N (K)	1.1	
T_{cu} (K)	22.0			
Θ (K)	69.28	Θ (K)	-10.19	
$P(\mu_B)$	3.19	$P(\mu_B)$	6.04	
g	2.26	g	2.04	
d (Å)	12.70	d (Å)	12.89	
a (Å)	3.46	a (Å)	3.67	

interaction J(Mn-Mn) = -0.20 K, and single-ion anisotropy D(Mn) = 0.97 K. The magnetic and structural data of this compound are shown in Table I. This compound shows a magnetic phase transition at $T_N = 1.1$ K. Above T_N it is in the paramagnetic phase. Below T_N it is in the antiferromagnetic phase where all spins lie in the MnCl₂ layers.⁹⁻¹¹

II. EXPERIMENT

Single crystals of $Ni_c Mn_{1-c} Cl_2$ were prepared by heating a mixture of c-NiCl₂ and (1-c)-MnCl₂ sealed in vacuum at a reaction temperature 990 °C. Stage-2 $Ni_c Mn_{1-c} Cl_2$ GIC's were synthesized by heating singlecrystal Kish graphites and single-crystal $Ni_c Mn_{1-c} Cl_2$ in a chlorine-gas atmosphere at a pressure of 740 Torr. The reaction was continued at 560 °C for 20 days. The stoichiometry of the GIC samples listed in Table II was determined from a weight uptake measurement. The dc magnetic susceptibility of stage-2 $Ni_c Mn_{1-c} Cl_2$ GIC's was measured by the Faraday balance method in the tem-

III. RESULTS

the c plane of the samples.

The dc magnetic susceptibility of stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c = 0, 0.1, 0.15, 0.25, 0.3, 0.35, 0.4, 0.5, 0.65, 0.7, 0.8, 0.85, 0.9, and 1 was measured at <math>H = 4 kOe in the temperature range $20 \le T \le 300$ K. A least-squares fit of the dc magnetic-susceptibility data for $150 \le T \le 300$ K to the Curie-Weiss law

$$\chi = \frac{C}{T - \Theta} + \chi_0 \tag{2}$$

yields values of the Curie-Weiss constant C (emu K/av. mol), the Curie-Weiss temperature Θ (K), and the temperature-independent susceptibility χ_0 (emu/av. mol). The values of C, Θ , and χ_0 are listed in Table II. Figure 1 shows the reciprocal susceptibility $(\chi - \chi_0)^{-1}$ for c = 0, 0.3, 0.65, and 0.9 as a function of temperature. The dc magnetic susceptibility is found to obey the Curie-Weiss law above 150 K. The deviation of the reciprocal susceptibility from a straight line below 150 K may indicate the appearance of spin short-range order. The Curie-Weiss temperature Θ vs Ni concentration is shown in Fig. 2. The value of Θ monotonically increases as the Ni concentration increases and changes its sign from negative to positive around $c \approx 0.22$. This implies that the average intraplanar exchange interaction changes from antiferromagnetic to ferromagnetic. According to the molecularfield theory developed by Hashimoto¹² and subsequently modified by Yeh, Suzuki, and Burr,¹ the Curie-Weiss temperature Θ is expressed by

$$\Theta = \frac{c^2 P^2(\mathrm{Ni})\Theta(\mathrm{Ni}) + (1-c)^2 P^2(\mathrm{Mn})\Theta(\mathrm{Mn}) + 2pc(1-c)\sqrt{|\Theta(\mathrm{Ni})\Theta(\mathrm{Mn})|}P(\mathrm{Ni})P(\mathrm{Mn})}{cP^2(\mathrm{Ni}) + (1-c)P^2(\mathrm{Mn})} , \qquad (3)$$

where P(Ni) and P(Mn) are the effective magnetic moments of the stage-2 NiCl₂ GIC and MnCl₂ GIC, respectively, and $\Theta(Ni)$ and $\Theta(Mn)$ are the Curie-Weiss temperature of the stage-2 NiCl₂ GIC and MnCl₂ GIC, respectively (Table I). Here p is a parameter defined by $p=J(Ni-Mn)/[|J(Ni-Ni)J(Mn-Mn)|]^{1/2}$, where J(Ni-Mn) is the intraplanar exchange interaction between Ni-Mn) is the intraplanar exchange interaction between Ni-Mn pairs in the Ni_cMn_{1-c}Cl₂ intercalate layer. The data of Θ in Fig. 2 can be fit well by Eq. (3) with p=1.09, indicating that J(Ni-Mn) is ferromagnetic and is estimated as 1.44 K. Note that

$$p = J(\text{Co-Mn}) / [|J(\text{Co-Co})J(\text{Mn-Mn})|]^{1/2} = 1.20$$

for stage-2 $Co_c Mn_{1-c} Cl_2 GIC's.^5$ We find that J(Ni-Mn)(=1.44 K) of stage-2 $Ni_c Mn_{1-c} Cl_g GIC's$ is almost the same as J(Co-Mn) (=1.49 K) of stage-2 Co₂Mn_{1-c}Cl₂ GIC's. Figure 3 shows the average effective magnetic moment P_{eff} of these compounds as a function of Ni concentration. The magnetic moment P_{eff} monotonically decreases with increasing Ni concentration. According to the molecular-field theory, ${}^{1}P_{\text{eff}}$ is given by

$$P_{\rm eff}(c) = [cP^2(Ni) + (1-c)P^2(Mn)]^{1/2}.$$
(4)

The solid line in Fig. 3 denotes the value of $P_{\rm eff}$ described by Eq. (4) with $P(Ni)=3.19\mu_B/mol$ and P(Mn)= $6.04\mu_B/mol$. Our data are fit well to the solid line, indicating that (i) the Ni concentration of GIC samples coincides with that of intercalant samples and (ii) Ni and Mn exist as divalent ions in the intercalate layer.

The dc magnetic susceptibility of stage-2 $Ni_c Mn_{1-c} Cl_2$

TABLE II. Curie-Weiss temperature Θ and average effective magnetic moment P_{eff} for stage-2 Ni_cMn_{1-c}Cl₂ GIC's with the stoichiometry C_nNi_cMn_{1-c}Cl₂.

с	n	Θ (K)	$P_{\rm eff}$ (μ_B /av. mol)
0.0	11.03	-10.19 ± 0.77	6.04
0.1	9.50	-6.68 ± 0.26	5.73
0.15	10.99	$-4.95{\pm}0.43$	5.45
0.25	13.57	$0.44{\pm}0.55$	5.35
0.3	13.08	0.04±0.54	5.24
0.35	14.62	7.71±0.46	5.21
0.4	16.83	9.04±0.95	4.85
0.5	12.18	$18.07 {\pm} 0.50$	4.77
0.65	14.98	24.94±0.28	4.27
0.7	11.95	31.90±0.73	4.23
0.8	14.33	38.49±1.04	4.08
0.85	13.76	42.95±0.58	3.94
0.9	12.03	58.45±0.25	3.48
1	15.37	69.28±0.36	3.19

GIC's with c=0, 0.1, 0.15, 0.25, 0.3, 0.35, 0.4, 0.5, 0.65, 0.7, 0.8, 0.85, 0.9, and 1 was measured in the temperature range $1.5 \le T \le 25$ K, where an external field H (=100 and 840 0e) is applied along the direction perpendicular to the c axis. Figure 4(a) shows the temperature dependence of M/H at H=100 Oe for stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c=0.65, 0.7, 0.8, 0.9, and 1, where M is the magnetization measured in units of emu/av. mol. The magnetization rapidly decreases with increasing tempera-



FIG. 1. Reciprocal susceptibility $(\chi - \chi_0)^{-1}$ vs *T* for stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c=0 (\blacktriangle), 0.30 (\triangle), 0.65 (\bigcirc), and 0.90 (\bigcirc), where χ_0 is a temperature-independent susceptibility. The solid line is described by Eq. (2) with *C*, Θ , and χ_0 listed in Table II.

FIG. 2. Curie-Weiss temperature Θ vs c for stage-2 Ni_cMn_{1-c}Cl₂ GIC's. The solid line is described by Eq. (3) with p = 1.09.

ture. It does not reduce to zero at a critical temperature T_c , but shows a tail around T_c . This tail is due to the smearing of T_c , which arises from a macroscopic gradient of the Ni concentration over the sample and from the



FIG. 3. Average effective magnetic moment P_{eff} (μ_B/av mol) vs c for stage-2 Ni_cMn_{1-c}Cl₂ GIC's. The solid line is described by Eq. (4).

finite-size effect of islands.² When the distribution of the critical temperature is assumed to be Gaussian with average critical temperature $\langle T_c \rangle$ and width σ , the magnetization can be expressed by a power law, with critical exponent β ,



FIG. 4. (a) M/H vs T for stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c=0.65, 0.7, 0.8, 0.9, and 1, where H=100 Oe and Hic. (b) M/H vs T for stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c=0.2, 0.3, and 0.4, where H=840 Oe and Hic.



FIG. 5. Real part of ac magnetic susceptibility (χ') vs T for stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c=0.8, 0.9, and 1.0. An ac magnetic field of $\nu=330$ Hz and h=300 mOe is applied along the c plane.

$$M(T) = A \int_{T}^{\infty} \left[1 - \frac{T}{T_c} \right]^{\beta} f(T_c) dT_c , \qquad (5)$$

with

$$f(T_c) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left[-\frac{1}{2} \left[\frac{T_c - \langle T_c \rangle}{\sigma}\right]^2\right], \quad (6)$$

where A is a constant. The least-squares fit of M/H vs T of Fig. 4(a) to Eq. (5) yields the values of $\langle T_c \rangle$, σ , and β listed in Table III. The value of β seems to be independent of Ni concentration at least for $0.7 \le c \le 1$: $\beta \approx 0.25$. Figure 4(b) shows the temperature dependence of M/H at H=840 Oe for stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c=0.2, 0.3, and 0.4. The magnetization monotonically decreases with decreasing temperature, indicating no magnetic phase transition, at least above 1.5 K.

The magnetic phase transition of stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c = 0.7, 0.8, 0.9, and 1 was investigated by ac magnetic-susceptibility measurement in the temperature range $2.6 \le T \le 25$ K. Figure 5 shows the temperature dependence of the real part of the ac magnetic susceptibility χ' of stage-2 Ni_cMn_{1-c}Cl₂ GIC's with c = 0.8, 0.9, and 1. The real part χ' shows a broad peak at the critical

TABLE III. Critical exponent β , distribution width of critical temperature, σ , average critical temperature $\langle T_c \rangle$, and critical temperature T_c for stage-2 Ni_cMn_{1-c}Cl₂ GIC's.

с	β	σ (K)	$\langle T_c \rangle$ (K)	T_c (K)
0.7	0.275	1.218	6.954	5.31
0.8	0.262	1.154	11.570	9.58
0.9	0.290	1.669	16.020	14.34
1	0.241	1.869	21.051	18.38



FIG. 6. Log-log plot χ' vs $t (=T/T_c-1)$ for the stage-2 Ni_cMn_{1-c}Cl₂ GIC with c=0.90. The solid line denotes a least-squares fit to a power law with $\gamma = 2.27$.



FIG. 7. Critical temperature T_c vs c for stage-2 Ni_cMn_{1-c}Cl₂ GIC's which are determined from the ac magnetic-susceptibility (•) and magnetization measurements (\odot). The solid line is a straight line with slope $d[\ln T_c(c)]/dc = 2.38$.

temperature T_c listed in Table III. The critical temperature T_c shifts to the lower-temperature side with decreasing Ni concentration. The peak value of χ' rapidly decreases as the Ni concentration decreases and tends to reduce to zero for samples with $c \leq 0.7$. Figure 6 shows the log-log plot of χ' versus reduced temperature t $(=T/T_c-1)$ for c=0.9. In the temperature range $0.19 \le t \le 0.35$, the least squares fit of the data to the power law yields the critical exponent $\gamma = 2.27 \pm 0.02$. For t < 0.19 the slope of the curve $\log_{10}\chi'$ vs $\log_{10}t$ decreases with decreasing t, probably because of intrinsic behavior such as a crossover effect or a smearing of the critical temperature. The value of γ for c=0.8 is obtained as $\gamma = 2.25 \pm 0.02$ in the temperature range $0.16 \le t \le 0.27$. These values of γ are likely to be close to that of the stage-2 NiCl₂ GIC: $\gamma = 1.99 \pm 0.02$. Rogiers, Grundke, and Betts¹³ have shown from a hightemperature series expansion of the 2D XY model that the susceptibility has a conventional power-law divergence with $\gamma = 2.51 \pm 0.25$ rather than an exponential singularity. The value of γ in the stage-2 Ni_cMn_{1-c}Cl₂ GIC's, which is a little smaller than this theoretical value of γ , is indicative of the 2D XY character in the critical behavior of these compounds.

Figure 7 shows the critical temperature T_c vs Ni concentration for stage-2 $Ni_c Mn_{1-c} Cl_2$ GIC's, where the critical temperatures denoted by solid and open circles are determined from ac susceptibility measurements at $H \approx 0$ and dc magnetic-susceptibility measurements at H = 100 Oe, respectively. The values of T_c at H = 100 Oe are larger than those at $H \approx 0$. This is consistent with a well-known result that the critical temperature of a 2D XY ferromagnet apparently shifts to higher temperatures when an external field H is applied along the direction of the easy axis.¹⁴ For c=0, the stage-2 MnCl₂ GIC undergoes a phase transition at the Néel temperature $T_N = 1.1$ K.^{10,11} The critical temperature rapidly decreases with decreasing Ni concentration. The initial slope $\zeta = [d \ln T_c(c)/dc]$ at c = 1 is obtained as $\zeta = 2.38$.

IV. DISCUSSION

First, we discuss the magnetic phase diagram of stage-2 $Ni_c Mn_{1-c} Cl_2$ GIC's. In Fig. 7 the critical temperature T_c rapidly decreases with an increase of Mn concentration and tends to reduce to zero around $c \approx 0.6$. Since the ferromagnetic interaction J(Ni-Ni) is much stronger than J(Ni-Mn), the role of Mn^{2+} ions may not be different from that of the diamagnetic ions in the Ni-rich concentration region. A continuous replacement of Ni²⁺ ions by Mn²⁺ ions results in a weakening of the ferromagnetic long-range order in the intercalate layer. The disappearance of ferromagnetic long-range order of Ni²⁺ spins below $c \approx 0.6$ can be confirmed from the Niconcentration dependence of spontaneous magnetization. It is predicted from the percolation theory¹⁵ that the Ni²⁺ ions belong either to 2D infinite networks or to finite clusters in the $Ni_c Mn_{1-c} Cl_2$ intercalate layers with $c > c_p$, where c_p is a percolation threshold and is predicted as $c_p = 0.5$ for the triangular lattice. Only the Ni²⁺ ions belonging to 2D infinite networks contribute to the magnetization per Ni mol, M_{Ni} . The fraction of the magnetization $M_{\rm Ni}$ to the saturation magnetization M_S , F, may be described by

$$F = \frac{M_{\rm Ni}}{M_{\rm s}} = \frac{N_0}{N} , \qquad (7)$$

where N_0 is the number of Ni²⁺ ions belonging to 2D infinite networks, N is the total number of Ni²⁺ ions, and

$$M_s = N_A \mu_B g(\text{Ni}) S(\text{Ni})$$

= 1.262 × 10⁴ emu/Ni mol.

Figure 8 shows the fraction F vs Ni concentration at T=4 K and H=100 Oe for stage-2 Ni_cMn_{1-c}Cl₂ GIC's, where $M_{\rm Ni}$ is defined by M/c and the value of M is obtained from Fig. 4(a). The smaller value of F at c=1 than unity indicates that the magnetization does not saturate sufficiently at T=4 K and H=100 Oe. The value of F rapidly decreases with decreasing Ni concentration and is extrapolated to zero around $c \approx 0.6$. This result indicates that the ferromagnetic long-range order may disappear below $c \approx 0.6$. In Fig. 8, for comparison, we also show the fraction $F(=M_{\rm Co}/M_s)$ vs Co concentration at T=2 K and H=100 Oe for stage-2 Co_cMn_{1-c}Cl₂ GIC's,⁵ where

$$M_s = N_A \mu_B g(\text{Co}) S(\text{Co}) = 1.787 \times 10^4 \text{ emu/Co mol}$$
,

with g(Co)=6.4 and $S(\text{Co})=\frac{1}{2}$. The fraction F gradually decreases with increasing Mn concentration and exhibits a noticeable tail even below $c_p = 0.5$, indicating that the ferromagnetic long-range order of Co^{2+} spins does not vanish even below $c_p = 0.5$. In Fig. 9 we show the data of



FIG. 8. Concentration dependence of fraction $F = M_{\text{Ni}}/M_s$ at T=4 K and H=100 Oe in stage-2 Ni_cMn_{1-c}Cl₂ GIC's (\bigcirc) and $F=M_{\text{Co}}/M_s$ at T=2 K and H=100 Oe in stage-2 Co_cMn_{1-c}Cl₂ GIC's [Suzuki *et al.* (Ref. 5)] (\bigcirc). The solid line is a guide to the eye.



FIG. 9. $T_c(c)T_c(1)$ vs c for stage-2 Ni_cMn_{1-c}Cl₂ GIC's (\bigcirc) (present work), stage-2 Co_cMn_{1-c}Cl₂ GIC's (\triangle) [Suzuki *et al.* (Ref. 5)], and K₂Cu_cZn_{1-c}F₄(\bigcirc) [Okuda *et al.* (Ref. 17)].

 $T_c(c)/T_c(1)$ versus concentration c for stage-2 Ni_cMn_{1-c}Cl₂ GIC's, stage-2 Co_cMn_{1-c}Cl₂ GIC's,¹⁶ and K₂Cu_cZn_{1-c}F₄.¹⁷ The value of $T_c(c)/T_c(1)$ for the stage-2 Co_cMn_{1-c}Cl₂ GIC's is larger than that for the stage-2 Ni_cMn_{1-c}Cl₂ GIC's for $c \ge 0.7$, which is consistent with the above result that the critical concentration, below which the ferromagnetic long-range order of Co²⁺ in stage-2 Co_cMn_{1-c}Cl₂ GIC's disappears, is lower than that of Ni²⁺ in stage-2 Ni_cMn_{1-c}Cl₂ GIC's ($c \approx 0.6$).

Here we note that the interaction J(Co-Mn) in stage-2 $\text{Co}_c \text{Mn}_{1-c} \text{Cl}_2$ GIC's is almost the same as J(Ni-Mn) in stage-2 Ni_cMn_{1-c}Cl₂ GIC's. The different concentration dependence of F around c=0.5-0.6 in stage-2 Ni_cMn_{1-c}Cl₂ GIC's and Co_cMn_{1-c}Cl₂ GIC's may be ascribed to the difference of the spin symmetry in the stage-2 NiCl₂ GIC and CoCl₂ GIC. In the stage-2 NiCl₂ GIC, the Ni-Ni interactions are predominantly of Heisenberg character, while in the stage-2 CoCl₂ GIC the Co-Co interactions are of largely XY character. In fact, the inplane spin Hamiltonian of the stage-2 CoCl₂ GIC is described by

$$H = -2J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + 2J_A \sum_{\langle i,j \rangle} S_i^z S_j^z , \qquad (8)$$

where J(Co-Co) (=7.75 K) is the ferromagnetic intraplanar exchange interaction and $J_A(\text{Co-Co}) (=3.72 \text{ K})$ is the anisotropic exchange interaction. The XY anisotropy parameter of the stage-2 CoCl₂ GIC, $\eta(\text{Co-Co})$, is much larger than that of the stage-2 NiCl₂ GIC, $\eta(\text{Ni-Ni})$:

$$\eta(\text{Co-Co}) = J_A(\text{Co-Co})/J(\text{Co-Co}) = 0.48$$

and

η (Ni-Ni)=D(Ni)/2zJ(Ni-Ni)=7.62×10⁻³.

It is qualitatively understood from the following simple model¹⁸ that the value of $T_c(c)/T_c(1)$ decreases more rapidly with dilution for the Heisenber-like system than for the XY-like system. For $c \approx c_n$ the infinite cluster is represented in terms of weakly coupled 1D chains with intrachain interaction J_0 and interchain interaction J_1 . The critical temperature T_c is determined by equating the thermal energy $k_B T$ to the interaction energy between adjacent nearest-neighbor in spins chains, $k_B T = \xi_{1D}(T_c) |J_1| S(S+1),$ where the intrachain correlation length $\xi_{1D}(T)$ is given by $\xi_{1D}(T)=2|J_0|S(S+1)/k_BT$ for Heisenberg symmetry and $\xi_{1D}(T) = 4|J_0|S(S+1)/k_BT$ for XY symmetry. Then it follows that the critical temperature T_c^{XY} for the system with XY symmetry is lower than T_c^H for the system with Heisenberg symmetry: $T_c^{XY}/T_c^H = \sqrt{2}$.

From the above discussion we can conclude that the T_c -vs c curve of stage-2 Ni $_c$ Mn $_{1-c}$ Cl₂ GIC's agrees well with the phase boundaries of diamagnetically diluted systems. It is well known that the initial slope of $T_c(c)/T_c(1)$ vs c, ζ , strongly depends on the dimensionality and spin symmetry of system. In Fig. 9 the initial slope of stage-2 Ni $_c$ Mn $_{1-c}$ Cl₂ GIC's (ζ =2.38) is a little smaller than that of K₂Cu $_c$ Zn $_{1-c}$ F₄ (ζ ≈3).¹⁷ Note that the in-plane spin Hamiltonian of K₂CuF₄ is also described by Eq. (8) with J(Cu-Cu) (=11.93 K) and J_A (Cu-Cu) (=0.09 K).¹⁹ The XY spin anisotropy parameter of K₂CuF₄ is almost the same as that of stage-2 NiCl₂ GIC's:

$$\eta$$
(Cu-Cu)= J_A (Cu-Cu)/ J (Cu-Cu)=7.54×10⁻³

The large initial slopes observed in stage-2 Ni_cMn_{1-c}Cl₂ GIC's and K₂Cu_cZn_{1-c}F₄ may be closely related to the fact that these systems magnetically behave like a 2D Heisenberg ferromagnet with very small XY anisotropy. Stinchcombe²⁰ has shown from a position-space renormalization-group method that the dependence of T_c on Ising anisotropy δ and concentration c is described by

$$\frac{T_c(c,\delta)}{J} \sim \frac{2c-1}{\mu \ln(1/\delta)} \quad \text{as } (\delta \to 0) , \qquad (9)$$

with $\mu = 0.21$, where the spin Hamiltonian of the pure system is given by

$$\mathcal{H} = -2J \sum_{\langle i,j \rangle} \left[(1 - \delta) (S_i^x S_j^x + S_i^y S_j^y) + S_i^z S_j^z \right] \,. \tag{10}$$

From Eq. (9) the initial slope of this system is estimated as $\zeta = 2$ and is independent of the Ising spin anisotropy δ in the limit of $\delta \approx 0$. With increasing Ising anisotropy δ , the initial slope ζ is predicted to decrease rapidly from $\zeta = 2$, approaching that for the 2D Ising model. McGurn²¹ has predicted from a random-phase approximation that the initial slope for the system with the spin Hamiltonian of Eq. (10) takes the value of $\zeta = 3.14$ for the isotropic limit of $\delta \approx 0$, which is much larger than the value predicted by Stinchcombe.²⁰ In spite of different values in ζ between these two theories, it may be understood that the large value of ζ is characteristic of the 2D Heisenberg system with small Ising anisotropy. As far as we know, there has been no theory for the initial slope in a 2D Heisenberg ferromagnet with XY anisotropy. However, the initial slope for the 2D Heisenberg ferromagnet with small *XY* anisotropy is expected to be a little smaller than that for a 2D Heisenberg ferromagnet with small Ising anisotropy because of the monotonic decrease of initial slope with the lowering of spin symmetry.

In contrast to the phase diagram for the Ni-rich concentration, the magnetic phase diagram in the Mn-rich concentration is not established at all because of lack of experimental data. In this concentration region there may occur a competition between the antiferromagnetic interaction J(Mn-Mn) and ferromagnetic interaction J(Ni-Mn), which gives rise to a spin-frustration effect. A continuous replacement of Mn^{2+} ions by Ni^{2+} ions results in a weakening of the antiferromagnetic long-range order in the intercalate layer. This antiferromagnetic long-range order may disappear around $c \approx 0.22$, where the Curie-Weiss temperature becomes zero.

V. CONCLUSION

The magnetic phase transition of stage-2 Ni_c $Mn_{1-c}Cl_2$ GIC's has been studied by dc and ac magneticsusceptibility measurements. The magnetic phase diagram has been determined for $c \ge 0.6$ and c = 0. It becomes clear that a Ni-rich ferromagnetic phase is built up by the Ni²⁺ ions, whereas the Mn-rich antiferromagnetic phase may be formed by Mn^{2+} ions at least at $c \approx 0$. The ferromagnetic and antiferromagnetic phases are separated by a paramagnetic phase. The Ni^{2+} and Mn^{2+} spins do not take part in the magnetic long-range order of the Ni^{2+} and Mn^{2+} networks, respectively. Thus the magnetic behavior of this system can be explained by percolation effects. In the present work, no spin-glass phase is observed at temperatures above 2.6 K. However, there may be still a possibility of a spin-glass phase at low temperature around $c \approx 0.22$, because of the competition between ferromagnetic J(Ni-Mn) and antiferromagnetic interactions J(Mn-Mn).

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