

## Control of the hole concentration in the $\text{YBa}_2\text{Cu}_3\text{O}_{6+z}$ -type superconductors $(\text{Yb,Ca})(\text{Ba,Sr})_2\text{Cu}_3\text{O}_{6+z}$ with low and high Ca contents

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$(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  ( $0 \leq x \leq 0.4$ ) solid solutions of the  $\text{YBa}_2\text{Cu}_3\text{O}_{6+z}$  ("1:2:3")-type structure were successfully synthesized. The solid-solution samples were characterized with respect to the oxygen content, crystal structure, and superconducting properties. The "fully oxygenated" samples with  $z \sim 0.8$  were prepared employing postannealing at high oxygen partial pressure atmosphere [ $P(\text{O}_2) = 400$  atm]. The samples had orthorhombic unit cells and showed bulk superconductivity. The superconducting transition temperatures ( $T_c$ 's) ranged from 80 to 32 K, depending on the Ca content. Samples with  $x = 0.1$  and 0.3, and various oxygen contents ( $0.36 \leq z \leq 0.89$  for  $x = 0.1$  and  $0.10 \leq z \leq 0.78$  for  $x = 0.3$ ) were prepared by employing quenching and annealing techniques. For  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$ , as the oxygen content  $z$  decreased,  $T_c$  increased from 40 K first, then peaked at 82 K at  $z = 0.56$ , and decreased down to 48 K at  $z = 0.10$ . The relationship between  $T_c$  and the hole concentration in the  $\text{CuO}_2$  sheet,  $p_{\text{sheet}}$ , was obtained.  $T_c$  was maximum at  $p_{\text{sheet}} = 0.18$  for both samples with  $x = 0.1$  and 0.3.

### I. INTRODUCTION

The importance of the hole concentration in copper-oxide superconductors is widely recognized.<sup>1</sup> A number of studies concerning the relationship between the hole concentration ( $p$ ) and the superconducting transition temperature ( $T_c$ ) have been reported.<sup>2</sup> In the  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  system, as the Sr content  $x$ , and therefore  $p$ , increases,  $T_c$  increases first to have a maximum and then becomes zero for  $x \geq 0.26$ .<sup>3</sup>

In  $\text{YBa}_2\text{Cu}_3\text{O}_{6+z}$  (1:2:3), a tetragonal-orthorhombic structural phase transition and a stepwise increase in  $T_c$  are observed as the oxygen content increases, i.e.,  $6+z$ .<sup>4</sup>  $\text{YBa}_2\text{Cu}_3\text{O}_{6+z}$  consists of two kinds of oxygen-deficient perovskite blocks, i.e., the Y-CuO<sub>2</sub>-BaO block with a fixed oxygen content and the BaO-CuO<sub>2</sub>-BaO block with variable oxygen content.<sup>5</sup> The structural phase transition can be explained by a preferential ordering of oxygen in the CuO<sub>2</sub> plane.<sup>6</sup>  $T_c$  for the  $\text{YBa}_2\text{Cu}_3\text{O}_{6+z}$  system reaches a maximum plateau around  $z \sim 1.0$ .<sup>2</sup> Some attempts to demonstrate the decrease in  $T_c$  with increasing hole concentration was made for the  $(\text{Y}_{1-x}\text{Ca}_x)\text{Ba}_2\text{Cu}_3\text{O}_{6+z}$  system.<sup>7,8</sup> However, the minimum  $T_c$  obtained was as high as 80 K because the solubility of Ca for the Y site in this system is low, being limited to  $x = 0.2$ .<sup>8</sup>

A preliminary investigation was carried out to obtain the optimum composition in  $(\text{R}_{1-x}\text{Ca}_x)(\text{Ba}_{1-y}\text{Sr}_y)_2\text{Cu}_3\text{O}_{6+z}$  ( $R$  being a rare-earth element) system with the high Ca content  $x$ . It was concluded that the highest Ca content,  $x = 0.4$ , was obtained at  $y = 0.2$  when  $R = \text{Yb}$ . Therefore, the  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  system was chosen for studying the 1:2:3 superconductors with high

hole concentrations. As was found in  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$ , the superconducting transition temperatures linearly decreased with increasing Ca content when post annealed at  $P(\text{O}_2) = 400$  atm. The minimum  $T_c$  of 32 K was obtained for  $(\text{Yb}_{0.6}\text{Ca}_{0.4})(\text{Ba,Sr})_2\text{Cu}_3\text{O}_{6.71}$ .

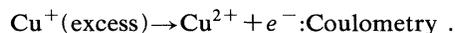
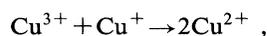
### II. EXPERIMENT

The  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  samples with  $x = 0.0, 0.1, 0.2, 0.3$ , and 0.4 were prepared by a solid-state reaction method. High-purity powders of  $\text{Yb}_2\text{O}_3$ ,  $\text{CaCO}_3$ ,  $\text{BaCO}_3$ ,  $\text{SrCO}_3$ , and  $\text{CuO}$  were used as starting materials. Appropriate amounts of powders were mixed, calcined, and compacted. The bars were sintered at 850°C for 20 h in a mixed gas of 99%  $\text{N}_2$  and 1%  $\text{O}_2$ . The "fully oxygenated" samples 1–5 were obtained by post annealing at  $P(\text{O}_2) = 400$  atm and at 600°C for 3 h and then at 400°C for 3 h. The post annealing was made by using a hot isostatic pressing (HIP) technique.<sup>9</sup>

The  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  samples with lower oxygen contents (samples 6–10 for  $x = 0.1$  and samples 11–14 for  $x = 0.3$ ) were prepared employing quenching and annealing techniques. Some of the samples were re-heat-treated at 300°C or 500°C for 3 h in air and then quickly cooled into liquid nitrogen. The quenched sample was post annealed at about 450°C for 100 h in an evacuated silica tube to obtain a homogeneous distribution of oxygen throughout the sample. Other quenched samples were reduced further using  $\text{Ti}_2\text{O}_3$  as the reducing agent at about 500°C for 100 h.

The lattice constants were determined by powder x-ray diffraction using  $\text{CuK}\alpha$  radiation. The average valence of copper was determined by a Coulometric titration tech-

nique.<sup>10</sup> A hydrochloric acid solution (1 N HCl) was used for the solvent. The 1 N HCl solution was free from dissolved oxygen and titrations were carried out in oxygen-free N<sub>2</sub> gas flow. In this technique, the concentration of a Cu<sup>+</sup> ion in the CuCl solution was previously determined by a blank titration. Then Cu<sup>3+</sup> ions in the sample solutions reacted with Cu<sup>+</sup> ions (CuCl) and the excess of Cu<sup>+</sup> ions was titrated by an anodic oxidation as follows:



The oxygen content was calculated from the determined average Cu valence: the valences of the ions such as Yb, Ca, Ba, and Sr were considered to be constants, i.e., Yb<sup>3+</sup>, Ca<sup>2+</sup>, Ba<sup>2+</sup>, and Sr<sup>2+</sup>, respectively. This Coulometric titration technique allowed the determination of oxygen content to an accuracy of 0.02 per formula unit.<sup>10</sup>

Electrical resistivity measurements were carried out using a conventional dc four-probe method and the dc magnetic susceptibility measurements using a SQUID magnetometer (quantum design, model MPMS). The measurements were performed by decreasing temperature with a constant magnetic field of 10 Oe. Superconducting transition temperatures ( $T_c^{\text{mag}}$ 's) were determined from the temperature dependences of the dc magnetic susceptibility.  $T_c^{\text{mag}}$  was the highest temperature at which the sample showed a negative magnetic susceptibility.

### III. RESULTS

#### A. (Yb,Ca)(Ba,Sr)<sub>2</sub>Cu<sub>3</sub>O<sub>6+z</sub> with $z \sim 0.8$

Figure 1 shows the x-ray powder diffraction patterns for the (Yb<sub>1-x</sub>Ca<sub>x</sub>)(Ba<sub>0.8</sub>Sr<sub>0.2</sub>)<sub>2</sub>Cu<sub>3</sub>O<sub>6+z</sub> samples which were post annealed at  $P(\text{O}_2)=400$  atm (samples 1–5). The peaks in the pattern are indexed for an orthorhombic unit cell with the lattice constants  $a=3.79$  Å,  $b=3.86$  Å, and  $c=11.6$  Å. The crystal structures of these samples were of the orthorhombic YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6+z</sub> type. The determined lattice constants for samples 1–5 are summarized in Table I. The lengths of the  $a$  and  $c$  axes slightly increased and that of the  $b$  axis decreased with increasing Ca content. The figure shows that the sample with  $x=0.1, 0.2, 0.3,$  and  $0.4$  (samples 2–5) were single phases and the samples with  $x=0.0$  (sample 1) contained Yb<sub>2</sub>BaCuO<sub>5</sub> as a minor impurity phase but the amount was estimated to be less than 5%. Therefore, we determined the oxygen content in the sample, disregarding the impurity phase.

The oxygen contents,  $6+z$ , of the samples are also summarized in Table I and they are plotted against the Ca content,  $x$ , in Fig. 2. This figure shows that the oxygen content monotonically decreases from 6.88 for the sample with  $x=0.0$  to 6.71 for the sample with  $x=0.4$ , as  $x$  increases. It was not straightforward to obtain samples with high Ca contents and high oxygen contents.

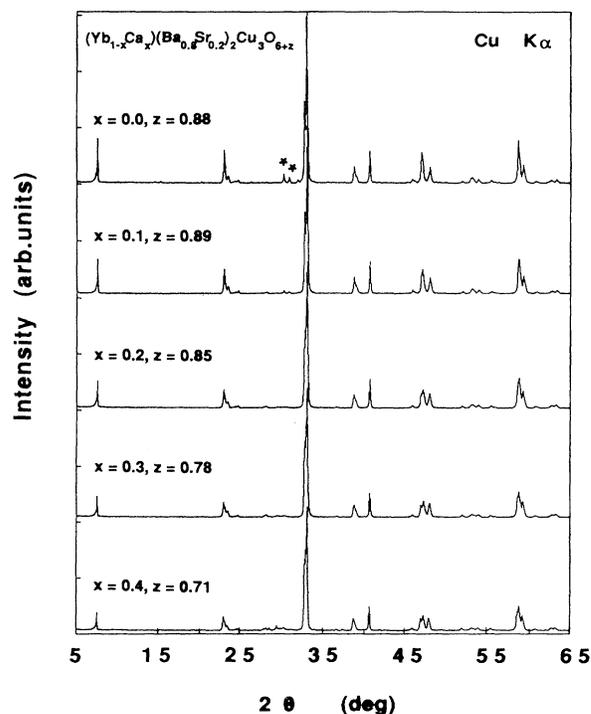


FIG. 1. X-ray powder diffraction patterns for (Yb<sub>1-x</sub>Ca<sub>x</sub>)(Ba<sub>0.8</sub>Sr<sub>0.2</sub>)<sub>2</sub>Cu<sub>3</sub>O<sub>6+z</sub> samples which were prepared by postannealing at  $P(\text{O}_2)=400$  atm.

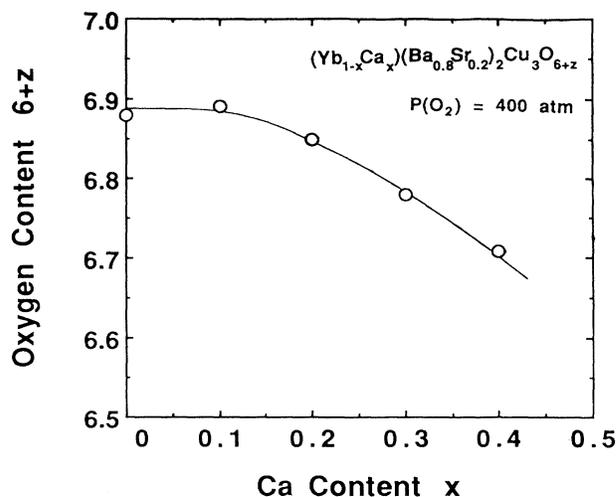


FIG. 2. The relation of oxygen contents,  $6+z$ , and the Ca content,  $x$ , for (Yb<sub>1-x</sub>Ca<sub>x</sub>)(Ba<sub>0.8</sub>Sr<sub>0.2</sub>)<sub>2</sub>Cu<sub>3</sub>O<sub>6+z</sub> samples which were prepared by postannealing at  $P(\text{O}_2)=400$  atm.

TABLE I. Compositions, lattice constants, and superconducting properties of  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$ . (Numbers in parentheses indicate standard deviations.)

Sample number	Composition		Lattice constants			$T_c^{\text{mag}}$ (K)	$\chi$ at 10 K ( $10^{-3}$ emu/gOe)
	$x$	$z$	$a$ (Å)	$b$ (Å)	$c$ (Å)		
1	0.0	0.88	3.789(1)	3.866(1)	11.598(1)	80	4.7
2	0.1	0.89	3.789(1)	3.859(1)	11.600(1)	68	6.9
3	0.2	0.85	3.794(1)	3.854(1)	11.607(1)	48	5.8
4	0.3	0.78	3.794(1)	3.851(1)	11.622(1)	40	2.2
5	0.4	0.71	3.797(1)	3.851(1)	11.624(1)	32	2.4
6	0.1	0.86	3.790(1)	3.859(1)	11.603(1)	72	4.6
7	0.1	0.84	3.791(1)	3.859(1)	11.600(1)	76	6.4
8	0.1	0.69	3.800(1)	3.858(1)	11.611(1)	77	3.7
9	0.1	0.61	3.822(1)		11.686(1)	76	3.7
10	0.1	0.36	3.821(1)		11.745(1)	48	2.3
11	0.3	0.73	3.797(1)	3.856(1)	11.593(1)	68	4.3
12	0.3	0.56	3.830(1)		11.677(1)	82	4.3
13	0.3	0.43	3.822(1)		11.708(1)	64	3.3
14	0.3	0.10	3.817(1)		11.750(1)	48	1.4

The maximum average valence of the Cu ion obtained was 2.30 (for the sample with  $x = 0.2$  and  $z = 0.85$ ).

All of the samples 1–5 showed a metallic temperature dependence of resistivity and exhibited bulk superconductivity with sharp superconducting transitions. Figure 3 shows the temperature dependences of the dc magnetic susceptibility. The magnetically determined superconducting transition temperatures ( $T_c^{\text{mag}}$ 's) were 80 K for  $x = 0.0$ , 68 K for  $x = 0.1$ , 48 K for  $x = 0.3$ , and 32 K for  $x = 0.4$ . These values for  $T_c^{\text{mag}}$  were in good agreement with  $T_c$ 's electrically determined. Thus, for the first time, we demonstrated a decrease in  $T_c$  for the  $\text{YBa}_2\text{Cu}_3\text{O}_{6+z}$  superconductors as the hole concentration increased.

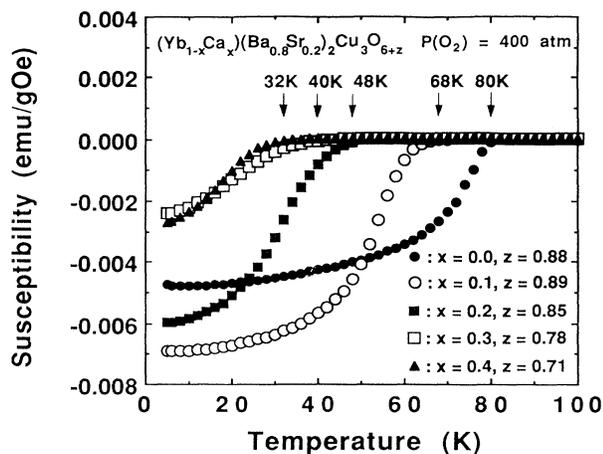


FIG. 3. Temperature dependence of the dc magnetic susceptibility for  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  samples which were prepared by postannealing at  $P(\text{O}_2) = 400$  atm.

#### B. Control of oxygen content in $(\text{Yb,Ca})(\text{Ba,Sr})_2\text{Cu}_3\text{O}_{6+z}$

Figure 4 shows the x-ray powder diffraction patterns for the  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  samples with  $0.10 \leq z \leq 0.79$  (samples 4 and 11–14). The patterns for the samples with  $z = 0.78$  and  $0.73$  are in-

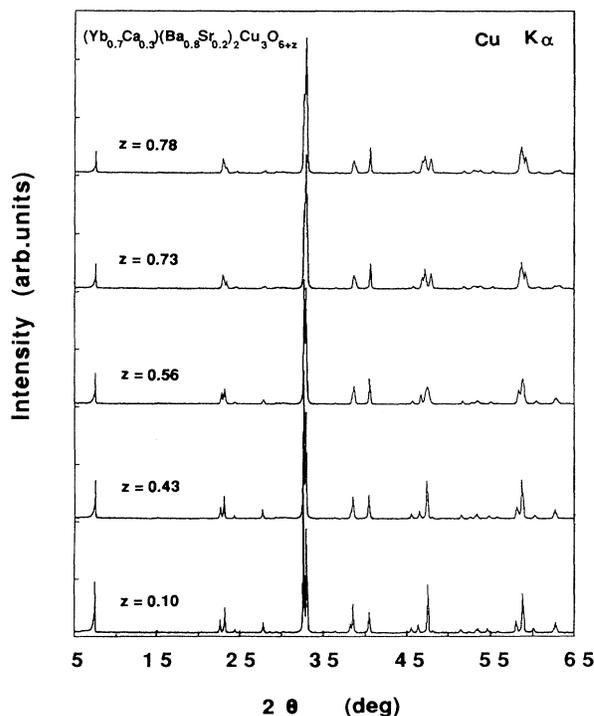


FIG. 4. X-ray powder diffraction patterns for  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  samples with various oxygen contents.

indexed for orthorhombic unit cells and those for the samples with  $z=0.56$ ,  $0.43$ , and  $0.10$  are indexed for tetragonal unit cells. The lattice constants of  $(\text{Yb}_{0.9}\text{Ca}_{0.1})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  and  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  are summarized in Table I. The relationship between the lattice constants ( $a$ ,  $b$ , and  $c/3$ , for the orthorhombic phase or  $a$  and  $c/3$  for the tetragonal phase) and oxygen contents,  $6+z$ , are given in Fig. 5 for the two systems. The  $c$  axes linearly increase with decreasing oxygen content. It is seen in the figure that orthorhombic-tetragonal phase transitions occur around  $(6+z)=6.6$  for both systems. This indicates that the orthorhombic-tetragonal structural phase transition in the 1:2:3 compound is mostly dependent on the oxygen content of the sample.

The temperature dependences of electrical resistivity for  $(\text{Yb}_{0.9}\text{Ca}_{0.1})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  and  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  are shown in Figs. 6(a) and 6(b). Samples with high oxygen contents are metallic and exhibit fairly sharp superconducting transitions with  $\Delta T_c (=T_c^{\text{on}} - T_c^{R=0}) \sim 5$  K. Those with low oxygen contents such as  $(\text{Yb}_{0.9}\text{Ca}_{0.1})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6.36}$  and  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6.10}$  are metallic only at high temperatures above 125 K and semiconductive at low temperatures, and they exhibited rather broad superconducting transitions with  $\Delta T_c > 10$  K. The resistivities at 200 K for the  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  samples with  $z=0.78$ ,  $0.73$ ,  $0.56$ ,  $0.43$ , and  $0.10$  were  $1.16 \times 10^{-3}$ ,  $1.36 \times 10^{-3}$ ,  $2.14 \times 10^{-3}$ ,  $4.02 \times 10^{-3}$  and  $5.73 \times 10^{-3}$   $\Omega$  cm, respectively. Thus, the resistivity in the normal state, i.e., at 200 K, increases with decreasing oxygen content. The zero-resistance temperatures ( $T_c^{R=0}$ ) of the  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  samples were 40 K for  $z=0.78$ , 57 K for  $z=0.73$ , 80 K for  $z=0.56$ , 58 K for  $z=0.43$ , and 36 K for  $z=0.10$ . Thus, as the oxygen content decreases,  $T_c^{R=0}$  exhibits maximum.

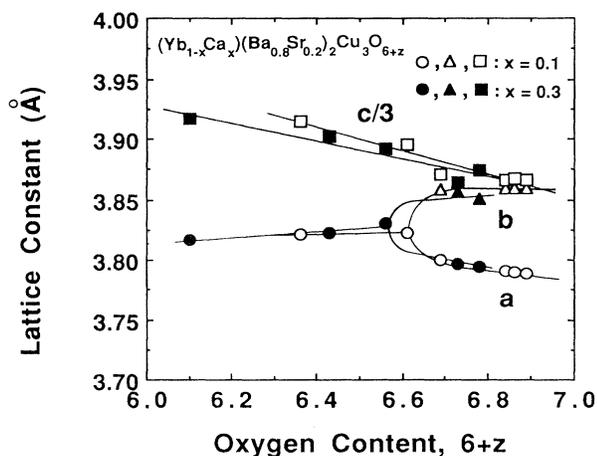


FIG. 5. Relationship between the lattice constants and the oxygen content in  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  with  $x=0.1$  and  $0.3$ .

The temperature dependences of the dc magnetic susceptibility for  $(\text{Yb}_{0.9}\text{Ca}_{0.1})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  and  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  are shown in Fig. 7. Both samples exhibited bulk superconductivity. The magnetic superconducting transition temperatures ( $T_c^{\text{mag}}$ ) are summarized in Table I. The relationship between ( $T_c^{\text{mag}}$ ) and the oxygen content is shown in Fig. 8. The  $T_c^{\text{mag}}$ 's are in good agreement with  $T_c$ 's electrically determined. For the system with  $x=0.1$ , as the oxygen content  $6+z$  is decreased,  $T_c$  shows a maximum around  $(6+z)=6.69$  and decreases down to 48 K at  $(6+z)=6.36$ . For the system with  $x=0.3$ ,  $T_c$  also exhibits a maximum around  $(6+z)=6.56$  and decreases down to 40 K at  $(6+z)=6.10$ . In the

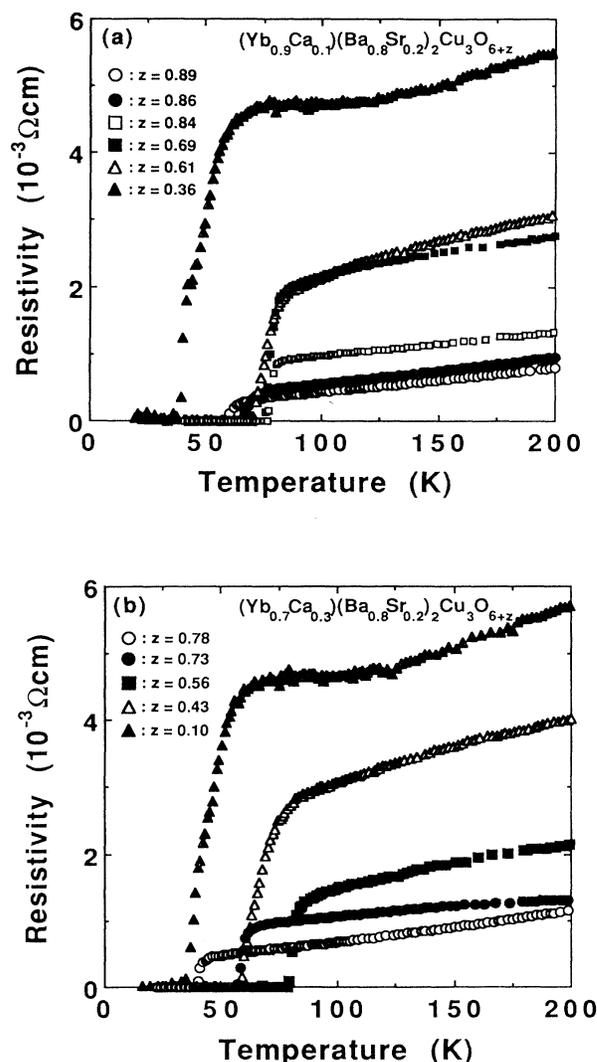


FIG. 6. Temperature dependence of electrical resistivity for  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  with  $x=0.1$  and  $0.3$ .

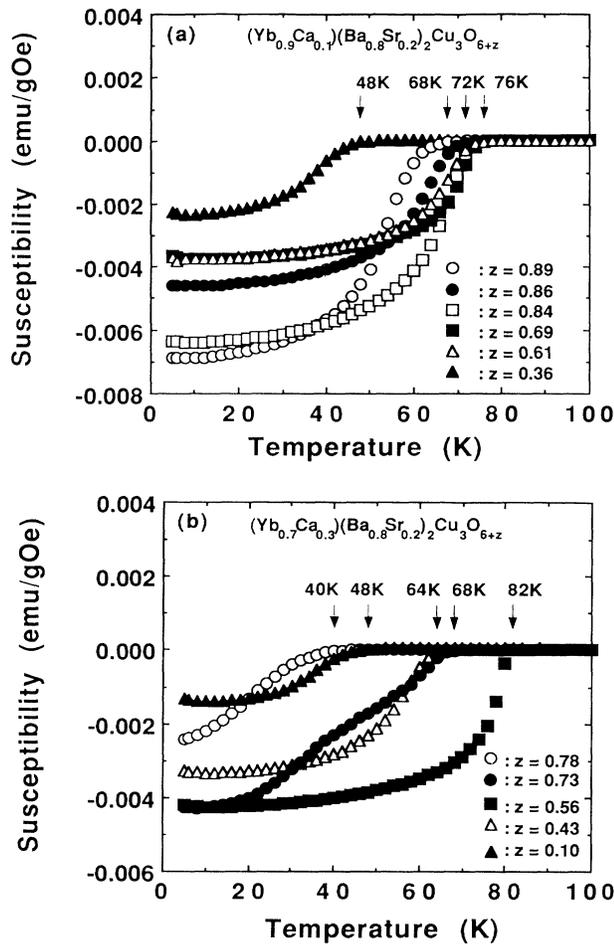


FIG. 7. Temperature dependence of dc magnetic susceptibility for  $(Yb_{1-x}Ca_x)(Ba_{0.8}Sr_{0.2})_2Cu_3O_{6+z}$  with  $x=0.1$  and  $0.3$ .

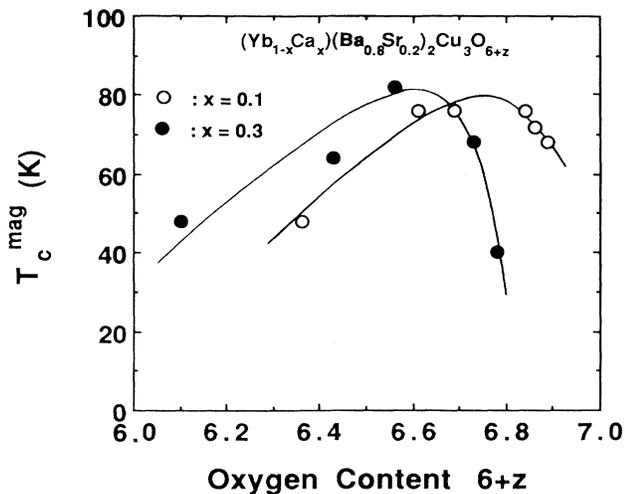


FIG. 8. Relationship between the oxygen content and the magnetic  $T_c$  for  $(Yb_{1-x}Ca_x)(Ba_{0.8}Sr_{0.2})_2Cu_3O_{6+z}$  with  $x=0.1$  and  $0.3$ .

$(Yb_{0.9}Ca_{0.1})(Ba_{0.8}Sr_{0.2})_2Cu_3O_{6+z}$  system, the maximum  $T_c$  was obtained for an orthorhombic compound with  $(6+z)=6.69$ . In the  $(Yb_{0.7}Ca_{0.3})(Ba_{0.8}Sr_{0.2})_2Cu_3O_{6+z}$  system, the maximum  $T_c$  was recorded for a tetragonal compound with  $(6+z)=6.56$ . Thus,  $T_c$  maxima of the system with different Ca contents were found at different oxygen contents.

#### IV. DISCUSSION

The Ca content ( $x$ ), oxygen content ( $6+z$ ), average copper valence [ $V(Cu)$ ], and magnetic superconducting transition temperature ( $T_c^{mag}$ ) are summarized in Table II.  $T_c$  apparently depends on both the Ca content and the oxygen content. For samples 1–5, post annealed at  $P(O_2)=400$  atm, as the Ca content increases,  $T_c$  linearly decreases, while the average copper valence  $V(Cu)$  has a maximum peak at  $x=0.2$ . Therefore,  $T_c$  of the present 1:2:3 superconducting compounds is not simply proportional to the average valence of Cu.

Tokura *et al.*<sup>11</sup> proposed a model that  $T_c$  of the 1:2:3 superconductor depends on the concentration of mobile holes in the  $CuO_2$  sheet contained in the Y-CuO<sub>2</sub>-BaO block. The mobile hole concentration in the  $CuO_2$  sheet,  $p_{sheet}$ , is calculated as follows. First, the average hole concentration per Cu,  $p$ , is calculated from the average Cu valence

$$p = V(Cu) - 2,$$

and the critical hole concentration per Cu,  $p_c$ , is estimated from the empirical relation

$$p_c = -2.21 + 0.34(6+z).$$

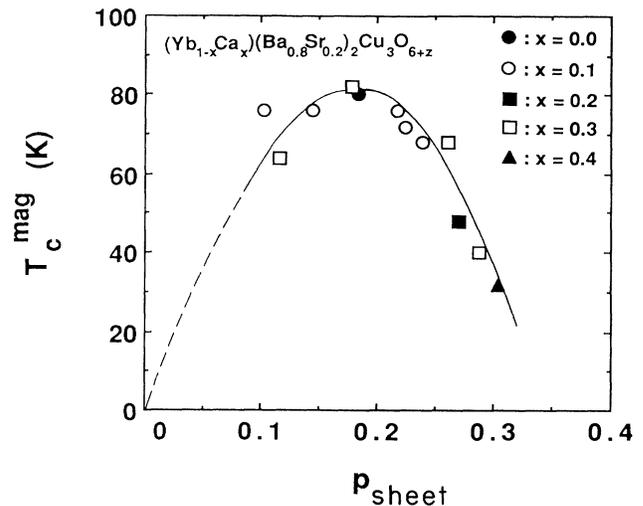


FIG. 9. Relationship between  $T_c$  and mobile hole concentration in the  $CuO_2$  sheet,  $p_{sheet}$  for the  $(Yb_{1-x}Ca_x)(Ba_{0.8}Sr_{0.2})_2Cu_3O_{6+z}$  systems with  $x=0.1$  and  $0.3$ .

TABLE II. Composition, average copper valence, hole concentrations and magnetic superconducting transition temperature of  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$ .

Sample number	Composition		$V(\text{Cu})^a$	Hole concentration		$T_c^{\text{mag}}$ (K)
	$x$	$(6+z)$		$p_c^b$	$p_{\text{sheet}}^c$	
1	0.0	6.875	2.250	0.128	0.184	80
2	0.1	6.885	2.290	0.131	0.239	68
3	0.2	6.845	2.297	0.117	0.270	48
4	0.3	6.780	2.287	0.095	0.288	40
5	0.4	6.712	2.275	0.072	0.304	32
6	0.1	6.858	2.272	0.122	0.225	72
7	0.1	6.843	2.262	0.117	0.218	76
8	0.1	6.692	2.161	0.065	0.144	76
9	0.1	6.609	2.106	0.037	0.103	76
10	0.1	6.364	1.943	-0.046	-0.017	48
11	0.3	6.727	2.251	0.077	0.261	68
12	0.3	6.558	2.139	0.020	0.179	82
13	0.3	6.431	2.054	-0.024	0.116	64
14	0.3	6.100	1.833	-0.136	-0.047	48

<sup>a</sup> $V(\text{Cu})$  average copper valence  $V(\text{Cu}) = [\{x - 7 + 2(6+z)\} / 3]$ .

<sup>b</sup> $p_c$ , critical hole concentration per Cu [ $p_c = -2.21 + 0.34(6+z)$ ] (Ref. 11).

<sup>c</sup> $p_{\text{sheet}}$ , hole concentration per Cu at the sheet site [ $p_{\text{sheet}} = 3(p - p_c) / 2$ ].

The average hole concentration  $p$  relates to the hole concentration in the  $\text{CuO}_2$  chain (plane),  $p_{\text{chain}}$ , and the hole concentration in the  $\text{CuO}_2$  sheet,  $p_{\text{sheet}}$ :

$$p = (p_{\text{chain}} + 2p_{\text{sheet}}) / 3.$$

When  $p = p_c$ ,  $p_{\text{sheet}}$  is zero. Thus,  $p_{\text{chain}}$  is calculated

$$p_{\text{chain}} = 3p_c.$$

Consequently,  $p_{\text{sheet}}$  is obtained:

$$p_{\text{sheet}} = 3(p - p_c) / 2.$$

The calculated values for  $p_c$  and  $p_{\text{sheet}}$  are summarized in Table II.  $T_c^{\text{mag}}$ 's are plotted against  $p_{\text{sheet}}$  in Fig. 9. As the  $p_{\text{sheet}}$  increases,  $T_c$  shows a maximum peak at  $p_{\text{sheet}} = 0.18$  and decreases down to 32 K at  $p_{\text{sheet}} = 0.304$ . The shape of this  $T_c^{\text{mag}}$  versus  $p_{\text{sheet}}$  curve is similar to that of the one obtained for the  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  system.

The average valence of Cu for the samples with low oxygen contents, such as  $(\text{Yb}_{0.9}\text{Ca}_{0.1})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6.36}$  and  $(\text{Yb}_{0.7}\text{Ca}_{0.3})(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6.10}$ , is lower than 2, and the calculated hole concentration in the  $\text{CuO}_2$  sheet is also minus. Nevertheless, these samples are superconducting. Therefore, we concluded that the present estimation<sup>11</sup> of the mobile hole concentration in the  $\text{CuO}_2$

sheet was not adequate for the system with low oxygen content. This may be due to the ordering of oxygen on the  $\text{CuO}_2$  chain site.<sup>12,13</sup>

## V. SUMMARY

The  $(\text{Yb}_{1-x}\text{Ca}_x)(\text{Ba}_{0.8}\text{Sr}_{0.2})_2\text{Cu}_3\text{O}_{6+z}$  ( $0 \leq x \leq 0.4$ ) solid solutions were synthesized. The superconducting transition temperatures ( $T_c$ 's) of the samples post annealed at  $P(\text{O}_2) = 400$  atm ranged from 80 to 32 K depending on the Ca content. As the oxygen content,  $6+z$ , of  $(\text{Yb,Ca})(\text{Ba,Sr})_2\text{Cu}_3\text{O}_{6+z}$  decreased,  $T_c$  showed a maximum peak at  $p_{\text{sheet}} = 0.18$ . The curve of  $T_c$  versus the concentration of mobile holes in the  $\text{CuO}_2$  sheet exhibited a similar shape as the one reported for the  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  system.

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