

Electron correlation, d -band formation, and magnetism in V_5S_8 : Photoemission-spectroscopy study

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We have studied the electronic structure of a metallic antiferromagnet V_5S_8 above the Néel temperature by photoemission spectroscopy. The V $3s$ core-level peak shows a splitting dominated by the exchange splitting resulting from the high-spin $d^2(V^{3+})$ configuration in the ground state. On the contrary, the valence-band photoemission spectra are in good agreement with band-structure calculations that show a high density of states at the Fermi level. In order to reconcile these apparently contradictory results, we propose that the on-site d - d Coulomb energy is effectively reduced from the average Coulomb energy through Hund's-rule coupling and that this leads to the metallic state even though the average Coulomb energy may be comparable to or exceed the one-electron V $3d$ - t_{2g} band width. While the local-moment picture is sufficient to explain the paramagnetic state, itinerant character also has to be taken into account to consider the antiferromagnetic state.

I. INTRODUCTION

Electron correlation in narrow-band metals has been the subject of extensive research in solid-state physics. In the metallic V-S system, the degree of d -electron localization can be varied through changing the composition between VS and V_5S_8 : VS and V_3S_4 show weak temperature-independent paramagnetism,¹ whereas V_5S_8 shows Curie-Weiss behavior above the Néel temperature.¹⁻³ V_3S_4 and V_5S_8 order antiferromagnetically below $T_N = 8$ (Ref. 4) and 32 K,¹⁻³ respectively. Since the V $3d$ electrons are thought to be responsible for both metallic conductivity⁵ and magnetism, it has been controversial whether the magnetism is of the itinerant-electron type or local-moment type.^{1-4,6,7}

In the present work, we have investigated the electronic structure of V_5S_8 by photoemission spectroscopy in order to get insight into the nature of electron correlation and magnetism. V_5S_8 has a monoclinic structure derived from the metal-deficient NiAs-type structure⁸ as shown in Fig. 1: V vacancies occur in every second metal layer; the V atoms in the vacancy layers are ordered, resulting in three types of V sites (V^I , V^{II} , and V^{III}). This structure can also be viewed as a layered compound VS_2 intercalated with V^I atoms, i.e., $V_{0.25}VS_2$. Nuclear-magnetic-resonance (NMR) studies have shown that only V atoms in the vacancy layers V^I have magnetic moments.⁷ From their NMR experiments, Kitaoka and Yasuoka¹ have deduced an ordered moment of $0.22\mu_B$ at the V^I site. As this value is much smaller than the effective moment of the paramagnetic state, $\sim 2.3\mu_B$, these authors have proposed that the antiferromagnetism is of itinerant-electron type. A neutron-diffraction study by Funahashi *et al.*,⁶ on the other hand, has yielded a larger ordered moment

$[(0.7-1.5)\mu_B]$ at the V^I site, favoring a local-moment picture.

Our spectra have shown both local-moment-like and bandlike features for V $3d$ electrons depending on the energy level studied. In order to reconcile these apparently contradictory results, we propose that the effective reduction of the on-site d - d Coulomb energy through the intra-atomic exchange interaction (Hund's-rule coupling) serves to stabilize the metallic d -band formation. We have discussed the implications of the previous and present results for the anomalous magnetic properties of

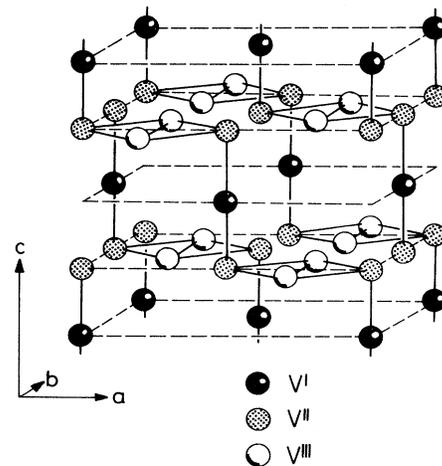


FIG. 1. Arrangement of V atoms in V_5S_8 . The structure is distorted from the ideal metal-deficient NiAs structure. V-V bonds shorter than 3.1 Å are indicated by solid lines (Ref. 8).

V_5S_8 , and concluded that itinerant character of d electrons becomes important for the V^I site in going from the paramagnetic to the antiferromagnetic states.

II. EXPERIMENTAL

A single crystal of V_5S_8 was grown by the chemical transport method.⁹ The composition was determined to be $VS_{1.64}$, which is in the homogeneity range of the V_5S_8 phase, namely, between $VS_{1.57}$ and $VS_{1.64}$.

Photoemission experiments were carried out using a spectrometer equipped with a Mg x-ray source (Mg $K\alpha$: $h\nu=1253.6$ eV) for x-ray photoemission spectroscopy (XPS) and a He discharge lamp (He I: $h\nu=21.2$ eV and He II: 40.8 eV) for ultraviolet photoemission spectroscopy (UPS). In order to obtain clean surfaces, the sample was scraped *in situ* with a diamond file. No oxygen 1s core-level peak (at binding energy $E_B \sim 530$ eV) and carbon 1s core-level peak was detected by XPS, and no oxygen 2p emission in the valence band UPS. Measurements were performed at room temperature, well above T_N . Auger-electron spectra were recorded using the Mg $K\alpha$ line as an excitation source.

The energy resolution was ~ 1 and ~ 0.2 eV for XPS and UPS, respectively. For XPS, the natural width of the Mg $K\alpha$ line is $2\gamma=0.36$ eV at full width at half maximum (FWHM).¹⁰ The resolution of the analyzer (operated with a pass energy of 25 eV) plus unresolved Mg $K\alpha_1$ and $K\alpha_2$ lines can be represented by a Gaussian FWHM of $2G=0.8$ eV, which will be taken into account in the following line-shape analyses.

III. RESULTS

A. Core levels

Sulfur core-level photoemission spectra of V_5S_8 are found to have simple line shapes. Figure 2 shows that the

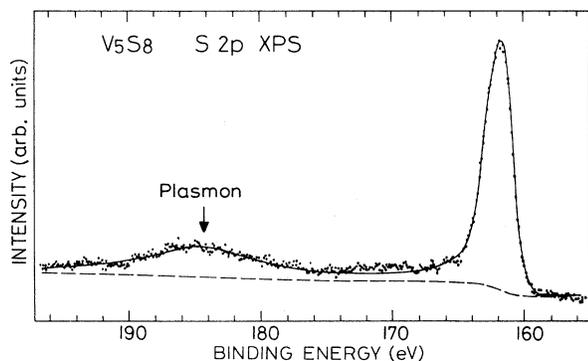


FIG. 2. S 2p core-level photoemission spectrum of V_5S_8 . The measured spectrum (dots) is fitted to the theoretical line shape (solid curve) of a spin-orbit doublet ($\Delta E_{s.o.}=1.15$ eV, $2\gamma=0.54$ eV, $2G=1.2$ eV, asymmetry parameter $\alpha=0.18$) and a plasmon satellite.

S 2p core-level spectrum can be fitted using a single spin-orbit doublet accompanied by a plasmon satellite.

Vanadium core-level spectra, on the other hand, exhibit complex line shapes. The V 3s core-level peak (Fig. 3) is not sharp and appears to consist of overlapping two peaks separated by about 2–3 eV. It is well known that the s core-level photoemission peak of the 3d transition-metal ion with an incomplete 3d shell is split into two peaks due to the exchange interaction between the core hole and the 3d electrons.¹¹ Since the V 3s core levels of high-spin V^{3+} compounds show an exchange splitting of about 2.5 eV (Refs. 11 and 12) and the mean valence of V in V_5S_8 is 3.2+ (assuming the S ions to be 2-), the splitting of the V 3s peak would be attributed to the exchange splitting of the high-spin V^{3+} state. Thus, we fitted the V 3s spectrum using a 1:4 superposition of the spectra of high-spin V^{4+} and V^{3+} states (corresponding to the mean valence of 3.2+) as shown in Fig. 3(a). Here, the exchange splitting for each configuration is given by

$$\Delta E_{ex} \sim [(2S+1)/5]G^2(3s, 3d)$$

and the intensity ratio of the two peaks is given by $S/(S+1)$, where S is the spin of the d^n configuration ($S=1$ for V^{3+}) and $G^2(3s, 3d)$ is a Slater integral which

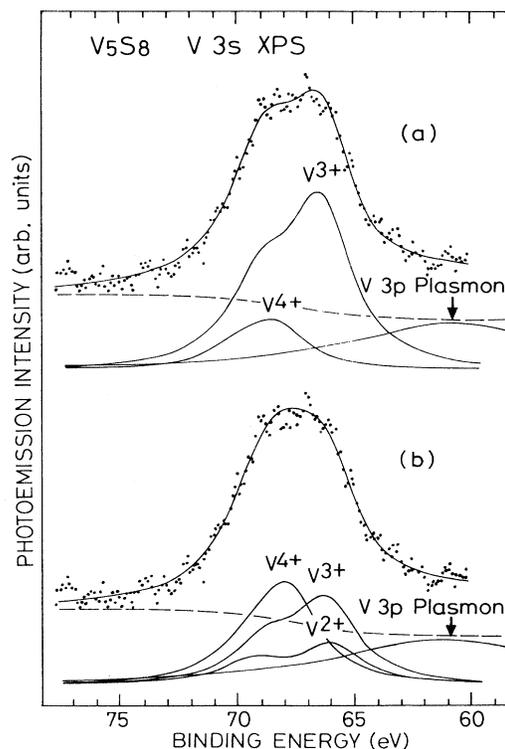


FIG. 3. V 3s core-level photoemission spectrum of V_5S_8 (dots). (a) Line-shape analysis assuming $V^{3+}:V^{4+}=4:1$ ($2\gamma=2.9$ eV, $2G=0.8$ eV, $\alpha=0.0$); (b) line-shape analysis assuming $V^{2+}:V^{3+}:V^{4+}=1:2:2$ ($2\gamma=2.8$ eV, $2G=0.8$ eV, $\alpha=0.0$). The broad feature centered at $E_B \sim 60$ eV is a plasmon satellite accompanying the V 3p core level.

we set to be 4.2 eV.¹¹ The presence of the overlapping V^{4+} component explains the observed intensity ratio of the two peaks larger than $S/(S+1)=\frac{1}{2}$. Another fit corresponding to the mean valence of $V^{3.2+}$ was also attempted using a 2:2:1 superposition of the V^{4+} , V^{3+} , and V^{2+} spectra as shown in Fig. 3(b). In the latter fit, the center of gravity of the V^{2+} component is slightly shifted toward higher binding energy than that of V^{3+} , contrary to what would be expected for core-level chemical shifts.

The $V\ 2p$ core-level spectrum exhibits highly asymmetric $j = \frac{3}{2}$ and $\frac{1}{2}$ peaks as shown in Fig. 4. All attempts to fit the spectrum using a superposition of different valences as has been applied to mixed-valence V oxides^{12,13} were not successful. Therefore, we assumed that the spectrum was dominated by an asymmetric broadening resulting from the screening of the core hole by conduction electrons,¹⁴ but the asymmetry was found to be too strong to be fitted using a single peak having a standard asymmetric line shape.¹⁵ According to Kotani and Toyozawa,¹⁶ core-level photoemission from a narrow-band metal exhibits a two-peak structure as a result of two types of final states, namely, well-screened and poorly screened core-hole states depending on whether a local screening orbital ($V\ 3d$, in this case) is occupied in the final state or not. Figure 4 shows such a tentative fit using two overlapping spin-orbit doublets. The poorly screened component (at higher binding energy) is broader than the well-screened one (at lower binding energy) because the former states decay into the latter states via an Auger-type process.

The absence of well-screened and poorly screened peaks in the $V\ 3s$ spectrum would be due to the large spatial extent of the $V\ 3s$ orbital compared to $V\ 2p$. Because of the different sizes of the core orbitals, the attractive Coulomb energy between the $V\ 3s$ hole and the $V\ 3d$ elec-

tron would be much smaller than that between the $V\ 2p$ hole and the $V\ 3d$ electron and would not be strong enough to split a local screening orbital off the $V\ 3d$ band. The weak $V\ 3s$ core-hole potential is consistent with the vanishingly small asymmetry parameter (see caption for Fig. 3).

B. Valence band

Figure 5 shows the valence-band XPS and UPS spectra. Each spectrum shows the narrow occupied part of the $V\ 3d-t_{2g}$ conduction band with a resolution-limited Fermi cutoff and a broad $S\ 3p$ band 1–8 eV below the Fermi energy (E_F). The observation of the sharp Fermi edge with a high density of states (DOS) indicates the presence of a sufficient amount of metallic electrons in this system. The separation between the $V\ 3d$ and the $S\ 3p$ bands is smaller than that between the $V\ 3d$ and the $O\ 2p$ bands in V oxides by 1.5–2.5 eV (see Fig. 6). This should lead to a stronger $p-d$ hybridization in the sulfide than in the V oxides.

So far no band-structure calculation has been reported for V_5S_8 . Therefore, we have simulated the DOS of paramagnetic V_5S_8 using that of VS (Refs. 17 and 18) or VS_2 (Ref. 19) by changing the relative weight of the DOS in the $V\ 3d$ - and $S\ 3p$ -band regions to represent the atomic ratio $V/S=5/8$ and by shifting E_F to accommodate the correct number of electrons. Considering the photoionization cross sections of the $V\ 3d$ and $S\ 3p$ atomic orbitals,²⁰ one can compare the He I spectrum with the total DOS. The intensity of the $S\ 3p$ band is suppressed in the $h\nu=40.8$ -eV spectrum due to a Cooper minimum in the $S\ 3p$ atomic orbital cross section around this photon ener-

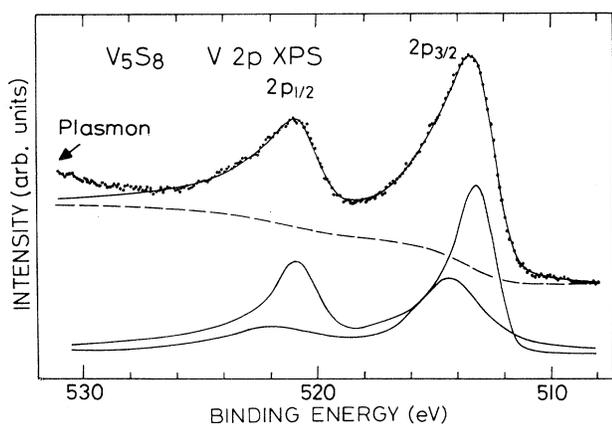


FIG. 4. $V\ 2p$ core-level photoemission spectrum of V_5S_8 . The measured spectrum (dots) is fitted using overlapping two spin-orbit doublets (solid curves). Line-shape parameters of the well-screened $2p_{3/2}$ peak are $2G = 1.5$ eV, $2\gamma = 0.24$ eV, $\alpha = 0.4$, and those for the poorly screened $2p_{3/2}$ peak are $2G = 1.5$ eV, $2\gamma = 2.5$ eV, $\alpha = 0$.

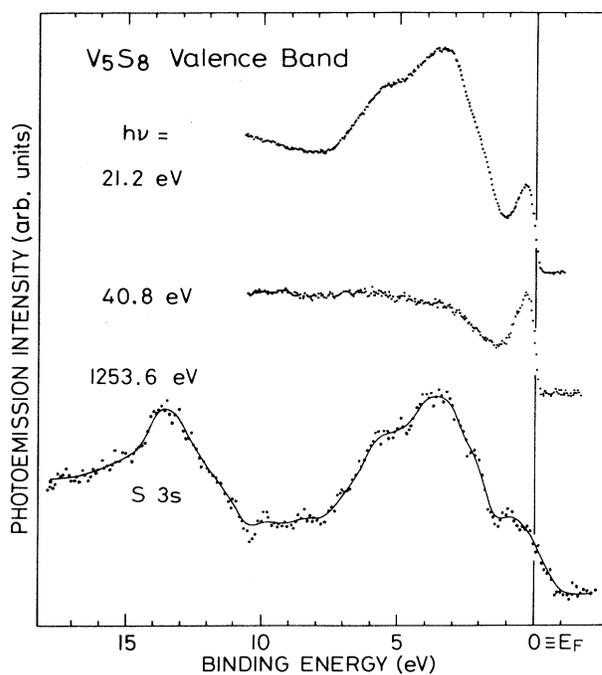


FIG. 5. Valence-band photoemission spectra of V_5S_8 .

gy.²⁰ (This observation confirms the absence of O 2*p* emission due to contamination since the O 2*p* cross section monotonically increases with decreasing photon energy.) The He II spectrum can therefore be compared with the V 3*d* partial DOS. As shown in Fig. 6, we find good agreement between the experiment and band theory with respect to the width and the line shape of the V 3*d* conduction band as well as those of the S 3*p* band, suggesting that electron correlation is unimportant in V₅S₈. We note that good agreement between band theory and photoemission experiment has been reported for VS.²¹ This is sharply contrasted with the spectrum of VO₂ in the metallic phase²² shown in the same figure, where the measured V 3*d* conduction band is considerably broadened as compared to the calculated DOS (Ref. 23) due to significant electron correlation within the V 3*d* band.²⁴

C. Auger-electron spectra

Core-valence-valence (*CVV*) Auger-electron spectra can be used to study the interactions between two holes

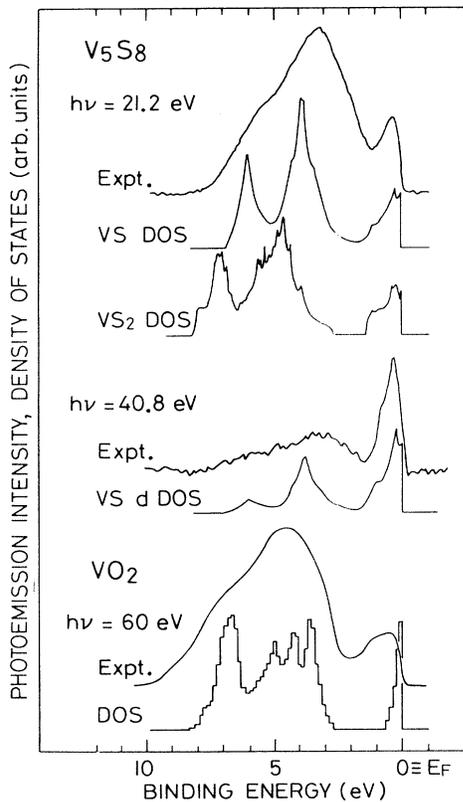


FIG. 6. Valence-band photoemission spectra of V₅S₈ compared with DOS given by band-structure calculations. The DOS of V₅S₈ have been synthesized from those of VS [Motizuki *et al.* (Ref. 18)] and that of VS₂ [Myron (Ref. 19)] as described in the text. Also shown is the valence-band UPS spectrum of VO₂ in the metallic phase [Shin *et al.* (Ref. 22)] and its calculated DOS [Gupta *et al.* (Ref. 23)]. Integral backgrounds have been subtracted from the experimental data.

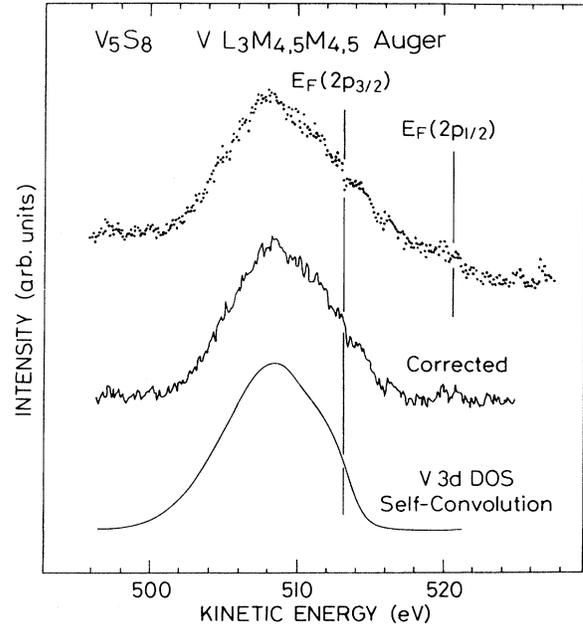


FIG. 7. V $L_3M_{4,5}M_{4,5}$ Auger-electron spectrum of V₅S₈ compared with the self-convolution of the He II UPS spectrum (broadened with a Gaussian function with $2G \sim 2.5$ eV in order to simulate the width of the initial core-hole state). The secondary-electron background and the L_2 component have been subtracted from the raw data (top) to yield the corrected curve (middle). $E_F(2p_{3/2})$ marks E_F for the $2p_{3/2}$ core-hole initial state, etc.

in the valence band or in the conduction band. In the absence of electron correlation, a *CVV* Auger spectrum involving a V core level is the self-convolution of the V 3*d* DOS, and electron correlation, if exists, distorts its line shape.²⁵ In Fig. 7, we compare the V $L_3M_{4,5}M_{4,5}$ ($2p_{3/2}$ - $3d$ - $3d$) Auger spectrum of V₅S₈ with the self-convolution of the He II UPS spectrum representing the V 3*d* partial DOS. One can see good agreement between the self-convolution and experiment without any sign of distortion, again implying that the electron correlation is not important.

IV. DISCUSSION

A. Electron correlation within the V 3*d* band

The valence-band photoemission and Auger-electron spectra suggest that *d* electrons in V₅S₈ are essentially itinerant and electron correlation is not important. The exchange splitting of the V 3*s* core-level spectrum, on the other hand, reveals atomic Hund's-rule coupling between 3*d* electrons in the ground state. These apparently contradicting results can be rationalized if one notices that, for high-spin configurations except for the half-filling (d^5), the effective *d-d* Coulomb energy U_{eff} , the lowest energy required for the charge fluctuation $d^n + d^n$

$\rightarrow d^{n+1}d^{n-1}$, is smaller than the average Coulomb energy U by the d - d exchange energy J , which is of the order of 1 eV, i.e., $U_{\text{eff}} = U - J$.²⁶ The photoemission results can be understood if $U_{\text{eff}} \ll W$ and $U \gtrsim W$: Under these conditions, a metallic d band is formed as a result of Hund's-rule coupling and therefore the coupling survives in the metallic state. The width of the V $3d$ - t_{2g} band in V_5S_8 is estimated to be $W \sim 2$ eV from the band-structure calculations¹⁷⁻¹⁹ (Sec. III B), and therefore we may infer that $U \sim 2$ eV and $U_{\text{eff}} = U - J \sim 1$ eV, which are similar to other estimates.^{22,27,28}

Here, it should be noted that the on-site Coulomb energies in V_5S_8 are defined for electrons in antibonding states formed between the V $3d$ - t_{2g} and the S $3p$ states and not for bare $3d$ electrons as in the case of (charge-transfer-type) late $3d$ transition-metal compounds.²⁹ This is one reason why the Coulomb energies in the V compounds ($U \sim 1$ – 2 eV) are much smaller than those in the late $3d$ transition-metal compounds ($U \sim 5$ – 8 eV).^{29,30}

B. Implications for the magnetic properties

It has been controversial whether the magnetic properties of V_5S_8 are of the local-moment type or itinerant-electron type. According to the NMR studies,⁷ only the V^I site has a local moment and the V^{II} and V^{III} sites (constituting 80% of the total V atoms) are believed to be nonmagnetic. The exchange splitting of the V $3s$ core-level peak indicates that the nonmagnetic behavior of the V^{II} and V^{III} sites is not due to an atomic low-spin configuration but due to an intersite coupling between the V local moments. (The dynamical fluctuation of the V^{II} - and V^{III} -site moments should be slow compared to the time scale of photoemission for the exchange splitting to be observed.) Magnetotorque measurements below T_N have indicated that the c axis is the easy magnetization axis but that the magnetic anisotropy energy is very small, ~ 0.24 cm⁻¹.³

As for the possible valences of the V^I ion, we shall consider V^{2+} , V^{3+} , and V^{4+} . In Table I, we list their effective moments to compare with that of the paramagnetic state. Such ionic models may not be fully justified because of the strong V $3d$ -S $3p$ hybridization and possible itinerancy of d electrons, but in the following we shall take these models as a well-defined starting point and

TABLE I. Effective moments and the ordered spin moments of V (in μ_B).

| | Effective Bohr magneton | | Ordered magnetic moment |
|------------------|----------------------------|--------------------------|-------------------------------|
| | Spin only (ion in crystal) | Spin+orbital (free atom) | |
| V^{2+} | 3.87 | 0.77 | 3.0 |
| V^{3+} | 2.83 | 1.63 | 2.0 |
| V^{4+} | 1.73 | 1.55 | 1.0 |
| V_5S_8 (expt.) | | $\sim 2.3^a$ | 0.22^b 0.7–1.5 ^c |

^aReference 3.

^bNMR (Ref. 4).

^cNeutron diffraction (Ref. 6).

consider the deviations from it when they become necessary.

In order to discuss the magnetic anisotropy in the antiferromagnetic state, we consider the splitting of the V $3d$ - t_{2g} level under the trigonal crystal field as shown in Fig. 8. The VS_6 unit is elongated along the c axis,⁸ which will lower the $3z^2$ - r^2 level relative to the doubly degenerate xy , x^2 - y^2 level through the anisotropic V $3d$ -S $3p$ hybridization. Furthermore, positive V^{II} ions are located above and below the V^I ion, which will also lower the $3z^2$ - r^2 level relative to the others.

If the V^I ion is in the high-spin V^{2+} state, it is magnetically isotropic in agreement with experiment [Figs. 8(c) and 8(f)]. For the high-spin V^{2+} state, $U_{\text{eff}} = U - J + 10Dq$ ($10Dq$: cubic crystal-field splitting), which is much larger than those for V^{3+} and V^{4+} ($U_{\text{eff}} = U - J$) and would explain why V $3d$ electrons are localized only at the V^I site. The effective moment of V^{2+} , however, is too large compared to the experimental value (Table I).

The effective moment of the V^{3+} ion is close to the experimental value. The small discrepancy could be due to an incomplete quenching of the angular momentum (see Table I). In this case, d electrons are localized at the V^I site probably because of the relatively isolated structural environment and hence the effectively reduced d -band width at this site. However, the magnetic anisotropy energy of the V^{3+} ion in the trigonal crystal field is too large to explain the observed small anisotropy unless the trigonal crystal-field splitting Δ is unreasonably large (of the order of ~ 5 eV).³ [The V^{3+} ion remains anisotropic even if the sign of Δ were negative as shown in Fig. 8(b).]

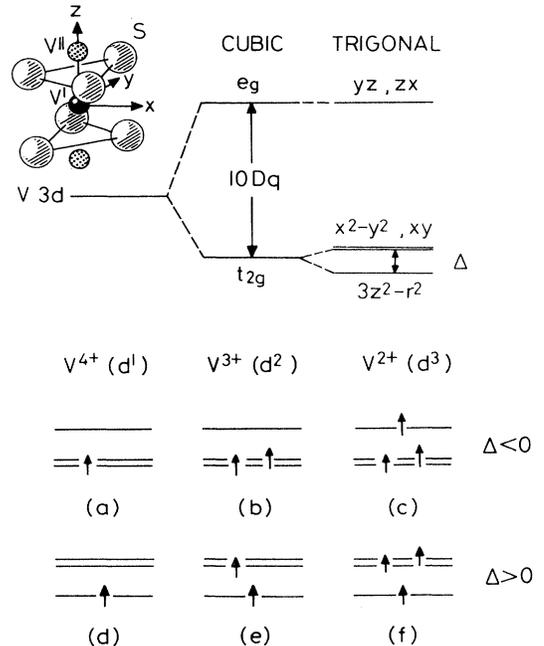


FIG. 8. Schematic energy-level diagrams for the V^I ion in V_5S_8 . The trigonal crystal-field splitting Δ is probably positive.

The ground state of the V^{4+} ion is magnetically isotropic for the present trigonal crystal field [Fig. 8(d)].³ However, the effective moment of the V^{4+} ion is too small to account for the paramagnetic susceptibility (Table I).

From the crystal structural point of view, we note that the three V sites have nearly the same average V-S distances (V^I : 2.399 Å, V^{II} : 2.384 Å, V^{III} : 2.390 Å).⁸ If the V^I ion is V^{3+} , the average valence of the V^{II} and V^{III} ions becomes 3.25+. This rather uniform valence distribution is consistent with the structural data. If V^I is 4+, the average valence of V^{II} and V^{III} is 3+; if V^I is 2+, it is 3.5+. In the latter two cases, the V-S distance should be quite different for the different V sites in the ionic model, since the ionic radius significantly differs for the different valences (V^{2+} : 0.79 Å, V^{3+} : 0.64 Å, and V^{4+} : 0.59 Å).³¹

Thus, the crystal structure and the paramagnetic behavior favor the V^I site being V^{3+} , whereas none of the ionic models can account for the antiferromagnetic states in a way consistent with the paramagnetic state. This suggests that the local-moment picture is insufficient to describe the antiferromagnetic state in V_5S_8 . In the antiferromagnetic state, partial delocalization of the V^I -state local moment possibly occurs, which might be related to the small magnetic anisotropy. Such a delocalization may be the origin of the small V^I -site ordered moment as determined by NMR ($0.22\mu_B$) (Ref. 4) compared to that estimated by neutron diffraction [$(0.7-1.5)\mu_B$].⁶ The former value has been obtained from the hyperfine coupling constant above T_N and the hyperfine field at the V^I site below T_N under the assumption that the coupling constant does not change across T_N . Therefore, the small ordered moment deduced from NMR is most probably due to a change in the hyperfine coupling constant across T_N , and such a change would result from a change in the character of d electrons in going from the paramagnetic state to the antiferromagnetic state. This "weakly itinerant" antiferromagnetism is considered to be inter-

mediate between the weak antiferromagnetism as described by the self-consistent-renormalization spin-fluctuation theory³² in the weak-correlation limit and the local-moment antiferromagnetism in the strong-correlation limit.

V. CONCLUSION

We have studied the electronic structure of an antiferromagnetic metal V_5S_8 above the Néel temperature by photoemission and Auger-electron spectroscopy. The exchange splitting of the V 3s core-level spectrum is interpreted as due to a mixture of high-spin d^1 , d^2 , and possibly d^3 configurations in the ground state, whereas the valence-band photoemission spectra show a sharp Fermi edge and are in good agreement with the DOS given by the band-structure calculations. In order to explain these observations in a consistent way, we have proposed that the effective on-site Coulomb energy for the Hund's-rule ground states of the V^{4+} (d^1) and V^{3+} (d^2) configurations $U_{\text{eff}} = U - J$ is smaller than the one-electron t_{2g} bandwidth even if the average Coulomb energy U may be comparable to or exceed the bandwidth.

The d electrons at the V^I site appear to behave as a localized high-spin V^{3+} (d^2) configuration at least in the paramagnetic state, whereas partial delocalization or weak itinerancy of the same d electrons would have to be taken into account in order to understand the antiferromagnetic state.

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