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## Flux-pinning potential and its measurement from magnetization decay

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We present calculations of the magnetization decay for a zero-field-cooled sample subject to a field H. The calculations are within the framework of the critical-state model and assume that the current density decays exponentially with the field. The results provide a possible explanation for the reported anomalous increase of the pinning potential with field and temperature.

Measurements of the time decay of magnetization are being extensively used to infer<sup>1-8</sup> the pinning potential  $U_0$  for high-temperature superconductors (HTSC). The well-established explanation of this magnetization decay is provided by Anderson's idea<sup>9</sup> of the thermal excitation of flux bundles, over an effective pinning potential, in the direction of the flux gradient. If one assumes that the effective potential is  $U_e = U_0 - \alpha JB$ , then one obtains (see Xu *et al.*,<sup>4</sup> and references therein)

$$M(t) = M_0 [1 - (kT/U_0) \ln(1 + t/\tau)], \qquad (1)$$

where  $\tau(\sim 10^{-6} - 10^{-12} \text{ s})$  is the characteristic relaxation time of a flux bundle. For  $t \gg \tau$ , one then obtains

$$U_0 = -(kTM_0)/(dM/d\ln t), \qquad (2)$$

and Eq. (2) has been used to extract  $U_0$ .

Magnetization-decay measurements at various temperatures (T) and applied fields (H) have, however, yielded<sup>3,4,7</sup> the unphysical results that  $U_0$  rises as T rises, and also as H rises. Hagen and Griessen<sup>3</sup> first emphasized that the inferred  $U_0$  rises with T in HTSC, and that this manifests itself in the experimental data as a peak in  $(1/M)(dM/d \ln t)$ ]. They have explained this T dependence by requiring that there be a distribution of  $U_0$  in any sample; others<sup>4,6,8</sup> have invoked the idea of Beasley, Labusch, and Webb<sup>10</sup> that  $U_e$  is actually a nonlinear function of J. In this paper we shall pursue our earlier suggestion<sup>11</sup> that Eq. (1) is not valid in most experimental situations; that the critical-state model must be invoked, and that the field dependence of  $J_c$  can explain why  $-(kTM_0)/(dM/d \ln t)$  rises with increasing T and H.

Magnetization-decay measurements have been reported, in both conventional superconductors and in HTSC, for samples cooled in zero field (ZFC) to a temperature T, subjected to a field H, and then H is either (i) maintained at constant value along with the temperature;<sup>2,4-7,12-15</sup> (ii) increased after a time t;<sup>16-18</sup> (iii) reduced to zero and only then measurements begin;<sup>12,13,19</sup> or (iv) held fixed and the decay is studied after cooling the sample to a lower temperature.<sup>8,20</sup> In addition, the magnetization decay has been studied in field-cooled samples, held at constant T, after the field is switched off.<sup>21</sup> It has generally been found that the magnetization decays logarithmically with time in all these cases, though careful measurements do show some deviations from this behavior.<sup>6,15</sup>

In all the experimental situations mentioned in the pre-

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vious paragraph, the sample is subjected to an isothermal field variation, and shielding currents are set up in accordance with the critical-state model. The large values of  $J_c$  imply that  $B(\mathbf{r})$  varies sharply within the sample, and this flux profile will also vary as the shielding currents decay. The critical-state model was first invoked, to explain the details of magnetization decay in HTSC, by Yeshrun *et al.*<sup>2</sup> They basically assumed constant-*B* shells in the sample, where the shielding current at each shell decays because of flux creep as

$$J_{c}(t) = J_{c0}[1 - (kT/U_{0})\ln(t/\tau)].$$
(3)

This results, to first order in  $kT/U_0$ , in the magnetization decaying as

$$M(t) = M_0 [1 - (kT/U_0)A(H)\ln(t/\tau)].$$
(4)

In this scheme A(H) does not depend on the absolute value of H but on the ratio  $H/H^*$ , where  $H^* = J_c(T)D/2$ is Bean's parametric field for a sample of transverse dimension D. Bean had assumed that  $J_c$  is independent of field, and it is then easily shown<sup>2,5,22</sup> that A(H) increases with H for  $H \leq H^*$ , and is constant for  $H \geq H^*$ . In actual practice  $J_c$  for HTSC decreases sharply with increasing field, and magnetization measurements indicate that this decrease is exponential.<sup>23,24</sup> The decay rate can be characterized by another parametric field  $H_0$ . M(t) is then obtained<sup>2,22</sup> in the form of Eq. (4) where  $A(H) = A[H, H^*(T), H_0(T)]$  has an implicit temperature dependence through  $J_c(T)$  and  $H_0(T)$ . It has been our contention<sup>11</sup> that the T and H dependences attributed by the use of Eq. (2) to  $U_0$ , actually may have a major contribution from  $A[H, H^*(T), H_0(T)]$ . Equation (2) should thus be replaced by

$$U_0 = kTA[H, H^*(T), H_0(T)][-M_0/(dM/d\ln t)].$$
(5)

If the actual  $U_0$  is independent of T and H, and we use Eq. (2) to infer the pinning potential (which is denoted by  $U^*$ ), then since

$$U^* = U_0 / A[H, H^*(T), H_0(T)],$$

the inferred T and H dependences of  $U^*$  are actually the T and H dependences of A. Similarly, the peak<sup>3</sup> in  $[(-1/M_0)dM/d\ln t]$  is then attributed<sup>11</sup> to a peak in kTA. In this paper we present calculations to substantiate this contention.

Before presenting our calculation we must stress that

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Eq. (5) has been successfully used, with a constant value for  $U_0$ , to explain <sup>2,5,22</sup> the field dependence of  $dM/d \ln t$  at small H for ZFC samples in the field-on case, the samplesize dependence of the decay rate in this case, and also<sup>22</sup> the smaller decay rate (by a factor of 3-4) observed<sup>12</sup> for ZFC samples in the field-off case. Kunchur, Poon, and Subramanian<sup>18</sup> have used this equation to explain the memory effect<sup>16-18</sup> seen in magnetization decay.

We have earlier<sup>22</sup> calculated  $A(H,H^*,H_0)$  for a sample in the shape of an infinite slab, with the assumption that  $J_c$  decays exponentially with H as

$$J_{c}(T,H) = J_{c}(T,0) \exp[-|H|/H_{0}(T)].$$
(6)

For a ZFC sample exposed to a field  $H < H_I$ , where  $H_I = H_0 \ln(1 + H^*/H_0)$  is the minimum field for full penetration, we have

$$A(H,H^*,H_0) = \left(\frac{(H^*H/H_0^2)\exp(-H/H_0)}{(H/H_0) - 1 + \exp(-H/H_0)} - 1\right)^{-1}.$$
(7)

For  $H > H_I$ , we have



FIG. 1. We plot the temperature dependence of  $kTA(H,H^*,H_0)$  for different values of H (indicated in tesla).  $H^*(T)$  and  $H_0(T)$  follow Ref. 25. For a constant  $U_0$ , this is the calculated T dependence of  $(-1/M_0)dM/d \ln t$ . The sample is assumed to have D=0.5 mm, and the arrows indicate the temperature at which the applied  $H=H_1(T)$ .

$$A(H,H^*,H_0) = \left(\frac{(H^*/H_0)\ln[1-(H^*/H_0)\exp(-H/H_0)]}{(H^*/H_0)+\exp(H/H_0)\ln[1-(H^*/H_0)\exp(-H/H_0)]} - 1\right)^{-1}.$$
(8)

For incorporating the T dependence, we provide as an experimental input the data of Hampshire, Chan, and Larbalestier.<sup>25</sup> For epitaxial thin films of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub>, they found that for fields along the c axis and transport currents in the ab plane, an exponential law holds over large ranges of H and T. For 20 K < T < 70 K, they fit their data to Eq. (6) with  $J_c(T,0) = 5.2 \times 10^5 [1 - (T/75)^2]$  amp/cm<sup>2</sup> and  $\mu_0 H_0(T) = 1250/T^2$  tesla. Using these experimental temperature dependences, we have calculated  $A[H,H^*(T),H_0(T)]$  for various sample dimensions. In Fig. 1 we show typical results for  $kTA(H,H^*,H_0)$ , which would be the observed  $\left[-(1/M_0)dM/d\ln t\right]$  for a constant  $U_0$ . Our calculations show a peak in  $A(H,H^*,H_0)$  at  $H=H_I$ , and the plots of kTA in Fig. 1 mimic some of the temperature dependences reported for  $|(1/M_0)dM/d\ln t|$  (see Fig. 1 of Ref. 3). We note that the peak shifts to lower temperature as *H* is increased. In Figs. 2 and 3 we note that  $U^* = U_0/A(H, H^*, H_0)$  increases with increasing *H*, and



While we have chosen the transport measurements of Hampshire, Chan, and Larbalestier<sup>25</sup> for our analysis, we note that the details of  $J_c(T,H)$  may vary from sample to sample because of weak links, twinning, microstructure, etc. We wish to point out that a different T dependence of  $H^*$  (Fig. 4), or a different set of values for  $H_0$  (Fig. 5), do reproduce (and, in fact, enhance) the peak in kTA [and thus in  $(-1/M_0)dM/d\ln t$ ] as a function of temperature. Calculations of  $A(H,H^*,H_0)$  are available for samples in the shape of a cylinder,<sup>26</sup> and the peak in kTA would still



FIG. 2. Following the calculations shown in Fig. 1, we plot  $U^*(H)$  at two temperatures.  $H > H_1$  throughout, and  $U_0$  is assumed to be constant.



FIG. 3. For a constant  $U_0$ , we plot  $U^*(T)$  at two fields (indicated in tesla).  $H > H_1$  throughout, and A is calculated as in Fig. 1.



FIG. 4. Same as Fig. 1 except that  $H^*(T)$  is assumed to vary as 1/T. We assume that  $H^*(20 \text{ K}) = 31.5$  tesla.

be seen at the temperature  $T_0$  where  $H_I(T_0) = H$ . Similarly, the fact that A decreases with increasing H for  $H > H_I$  is common to the three forms<sup>27</sup> of  $J_c(H)$  in current usage.

The pinning potential  $U_0$  is, in general, a function of both T and H; its estimation from an experimentally measured  $(d \ln M/d \ln t)$  requires the use of Eq. (5), with  $A[H,H^*(T),H_0(T)]$  determined using Eqs. (7) or (8). The full penetration field  $H_I(T) = H_0(T) \ln[1 + H^*(T)/H_0(T)]$  is easily determined experimentally from the isothermal-magnetization data (at T) as the field at which the ZFC virgin magnetization and the forward hysteresis curves merge.<sup>28</sup>  $H_I(T)$  is also the field at which  $dM/d \ln t$ shows a peak [provided  $U_0(T,H)$  is a smooth function of

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FIG. 5. Same as Fig. 1 except that  $H_0(T)$  is smaller throughout by a factor of 10.

*H*]. The hysteresis curve can also yield  $H_0$  and thus  $H^*$ , with the provision that one uses the curve in the region  $H > H_I(T)$ .<sup>28</sup>  $H^*$  and  $H_0$  can also be determined directly by transport measurements of  $J_c(T,H)$ —except that these are not possible for the grain-aligned powders used in some studies.<sup>4,7</sup>

To conclude, we have argued that the critical-state model must be incorporated when determining  $U_0$  from the magnetization decay measured on samples subjected to isothermal-field variations. Most of the anomalous T and H dependences<sup>4,7</sup> predicted for  $U_0$  may be attributable to the use of Eq. (2) instead of the more appropriate Eq. (5).

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