

## Magnetic-ordering, hyperfine, and linear contributions to the low-temperature specific heat of $(Y_{1-x}Pr_x)Ba_2Cu_3O_{7-\delta}$

N. E. Phillips, R. A. Fisher, R. Caspary,\* and A. Amato†

*Materials and Chemical Sciences Division, Lawrence Berkeley Laboratory,  
University of California, Berkeley, Berkeley, California 94720*

H. B. Radousky

*Lawrence Livermore National Laboratory, Livermore, California 94550*

J. L. Peng,‡ L. Zhang, and R. N. Shelton

*Department of Physics, University of California, Davis, Davis, California 95616*

(Received 24 September 1990; revised manuscript received 10 December 1990)

Specific-heat measurements on  $(Y_{1-x}Pr_x)Ba_2Cu_3O_{7-\delta}$ , for  $x=0, 0.1, 0.2, 0.3$ , and 1, with  $0.3 \leq T \leq 65$  K, which include measurements in magnetic fields to 7 T, are reported. The combination of low-temperature and in-field data allows the separation of hyperfine and magnetic-ordering contributions from the low-temperature linear term,  $\gamma_0 T$ . The value of  $\gamma_0$ , 200 mJ/molPrK<sup>2</sup> for  $x=0.1, 0.2$ , and 0.3, is substantially lower than that deduced from earlier measurements, but the determination of a cutoff temperature of  $\sim 50$  K for this contribution adds to the appearance of heavy-fermion-like behavior.

Among the compounds prepared by substitution of a rare earth ( $R$ ) for  $Y$  in  $YBa_2Cu_3O_{7-\delta}$  ( $Y$ - $Ba$ - $Cu$ - $O$ ) with the retention of the superconducting orthorhombic phase, the  $Pr$ -substituted materials exhibit unique properties. For the others ( $Nd, Sm, Eu, Gd, Dy, Ho, Er, Tm, Yb$ , and  $Lu$  substituted),  $T_c$  is essentially unaffected by the substitution,<sup>1-4</sup> and, although the magnetic  $R^{3+}$  ions order at temperatures of a few degrees Kelvin, there is no evidence of ordering of  $Cu$  moments. For the  $Pr$ -substituted materials, the corresponding properties are substantially different. For  $(Y_{1-x}Pr_x)Ba_2Cu_3O_{7-\delta}$  ( $Y$ - $Pr$ - $Ba$ - $Cu$ - $O$ ),  $T_c$  decreases nearly linearly with increasing  $x$  and superconductivity disappears for  $x \geq 0.55$ .<sup>5-7</sup> For  $x > 0.55$ , the materials are magnetic insulators with the  $Cu$  moments in the  $CuO_2$  planes antiferromagnetically ordered.<sup>8,9</sup> For  $x=1$ , that ordering occurs at  $T_{N1}=270$  K, and a second magnetic ordering,<sup>8-10</sup> for which the associated entropy change<sup>10</sup> is  $\sim \mathcal{R} \ln 2$ , occurs at  $T_{N2}=17$  K. Neutron-diffraction line shapes and intensities<sup>8</sup> indicate that the second ordering is of  $Pr$  moments, but ordering of  $Cu$  moments on the  $CuO$  chains<sup>9</sup> is not completely ruled out. If it is  $Pr$  that orders,  $T_{N2}$  is a factor of 10 higher than expected<sup>10</sup> on the basis of scaling the  $T_N$  values for other  $R$ - $Ba$ - $Cu$ - $O$ 's.

The explanations for the anomalous  $x$  dependence of  $T_c$  in  $Y$ - $Pr$ - $Ba$ - $Cu$ - $O$  can be summarized by two models. In one,<sup>6,10-12</sup>  $Pr$  is primarily in the +4 state and one electron that is removed from the  $Pr$  fills holes in the conducting  $CuO_2$  planes. In the other,<sup>13-17</sup>  $Pr$  is primarily in the +3 state and the hybridization of the  $Pr$  4*f* and  $O$  2*p* orbitals (which is critically dependent on the 4*f* energy and occurs to a significant degree only for  $Pr$ ) produces the effect on  $T_c$  by a pair-breaking mechanism. The second model would also account for the relatively strong  $Pr$ - $Pr$  interactions implied by the high value of  $T_{N2}$ —if indeed it is  $Pr$  moments that order at  $T_{N2}$ .

The first specific-heat ( $C$ ) measurements<sup>10</sup> on  $Y$ - $Pr$ - $Ba$ - $Cu$ - $O$  showed very large low-temperature contributions that were approximately proportional to  $T$ . They were interpreted as large values of the 0-K Sommerfeld constant,  $\gamma_0 \sim 400$  mJ/molPrK<sup>2</sup>, and evidence of heavy-fermion behavior, although the possibility of a magnetic ordering contribution to  $C$  was also recognized. This paper is a preliminary report on measurements of  $C$  for  $x=0, 0.1, 0.2, 0.3$ , and 1 that extend to lower temperatures and include measurements in magnetic fields ( $H$ ) up to 7 T. The emphasis is on the low-temperature, in-field, small- $x$  data that clearly reveal a hyperfine contribution that is important for  $T < 1$  K, and an  $H$ -dependent magnetic-ordering contribution with a maximum at temperatures ranging from  $\sim 0.4$  K for  $x=0.1$  to  $T \sim 2$  K for  $x=0.3$ . When these contributions to  $C$  are taken into account, there remains a large,  $H$ -independent  $\gamma_0 T$  term,  $\gamma_0 \sim 200$  mJ/molPrK<sup>2</sup>, that extends to approximately 50 K. The coefficient  $\gamma_0$  is substantially smaller than that deduced from the earlier measurements, and not as large as for many heavy-fermion compounds; it is still much larger, however, than the usual values for metals, and certainly suggestive of heavy-fermion behavior. Furthermore, this determination of the 50-K cutoff temperature constitutes a significant additional contribution to the appearance of heavy-fermion-like behavior. (In the low-temperature limit, known heavy-fermion behavior includes temperature-dependent values of  $\gamma_0$ , both increasing and decreasing with decreasing temperature, as well as constant values as observed in the present case.)

The samples studied were essentially single-phase, polycrystalline material. They were characterized by field-cooled magnetization, x-ray diffraction, Raman spectroscopy, and resistivity measurements. The magnetization measurements showed a superconducting transition width, 10%-90%, of 10 K or less with no evidence of multiple

transitions, suggesting reasonable homogeneity of the Pr substitution. Thermal gravimetric analysis showed the materials to be nearly fully oxygenated ( $\delta = 0.05 \pm 0.02$ ). Details of their preparation and characterization have been published previously.<sup>13,18</sup> Specific heats of  $\sim 20$ -g samples were measured using a semiadiabatic heat-pulse technique for  $T < 30$  K and a continuous-heating technique for  $T > 30$  K. The precision of the data is  $\sim 0.2\%$ .

Representative specific-heat data are shown in Figs. 1–4. Results for  $x = 0.3$  are emphasized because the different contributions are most clearly delineated for that sample. Data for  $x = 0$  are included because they are taken as a “background” contribution in evaluating the magnetic ordering and  $\gamma_0 T$  contributions, on the assumption that the lattice and impurity (e.g.,  $\text{BaCuO}_2$ ) contributions are approximately the same in all samples. Figure 1 gives an overview of the data for  $x = 0.3$ ,  $H = 0$ , and 7 T. The magnetic ordering is indicated by the broad maxima in  $C/T$  near 1 and 5 K, for  $H = 0$  and 7 T, respectively. The upturns in  $C/T$  for  $T < 0.5$  K correspond to a strongly  $H$ -dependent hyperfine field. In Fig. 2, data are shown for the  $x = 0.1$  sample, the only one (except the  $x = 0$  sample) for which the superconducting transition is clearly evident in  $C$ . The entropy-conserving construction in the lower inset gives  $\Delta C(T_c)/T_c \sim 8 \text{ mJ/mol K}^2$ , about 10% of the value expected for a fully superconducting sample of Y-Ba-Cu-O, and could indicate, e.g., a substantially lower value of the electronic density of states or gapless superconductivity. [The magnetization data suggest that the transition width would not have led to a serious underestimate of  $\Delta C(T_c)$ .] Furthermore, a small volume fraction of superconductivity seems to be ruled out by the 40% Meissner effect.] For this sample, the magnetic ordering and hyperfine contributions are superimposed for  $H = 0$ , but clearly separated for  $H = 7$  T. Analyses of the 7-T, low-temperature data into  $\gamma_0 T$ - and  $T^{-2}$ -proportional hyperfine terms are shown in Fig. 3 for  $x = 0, 0.1, 0.2$ , and 0.3. The  $x$  dependence of the  $\gamma_0$  values is well represented

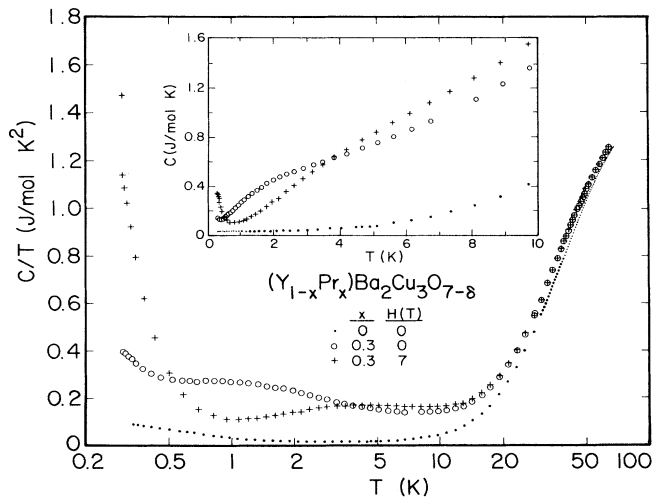


FIG. 1.  $H = 0$  and 7-T data for  $(\text{Y}_{0.7}\text{Pr}_{0.3})\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}$ .  $H = 0$  data for  $x = 0$  are shown for comparison. (For  $x = 0$ , the weak  $H$  dependence would not be apparent.)

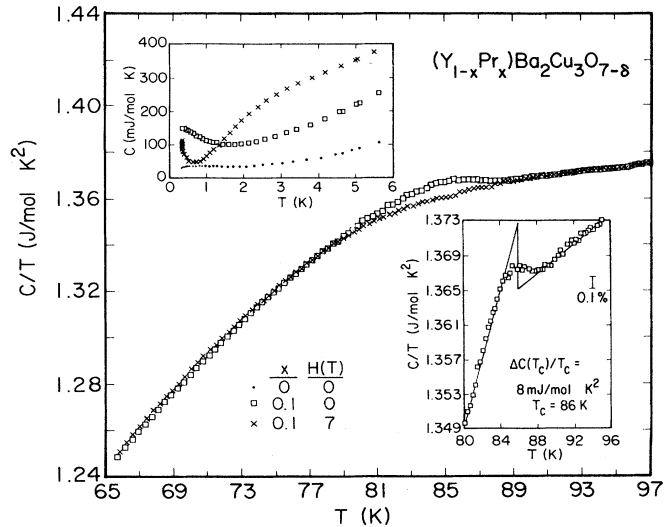


FIG. 2. Data for  $(\text{Y}_{0.9}\text{Pr}_{0.1})\text{Ba}_2\text{Cu}_3\text{O}_{7-\delta}$  in the vicinity of  $T_c$  and, in the upper inset, for  $T \leq 6$  K.

by the sum of an  $x = 0$  value,  $7.6 \text{ mJ/mol K}^2$ , which is typical of Y-Ba-Cu-O samples, and an  $x$ -proportional term corresponding to  $\gamma_0 = 200 \text{ mJ/mol Pr K}^2$ .

The separation of the various low-temperature contributions to  $C$  is shown in Fig. 4 for  $x = 0.3$ , as  $\Delta C/T$  vs  $T$ , where  $\Delta C$  is the excess of  $C$  over the hyperfine and “background” ( $x = 0$ ) contributions. The  $H = 0$  value of  $\gamma_0$  is not well determined at low temperatures because it is small compared with the hyperfine and/or magnetic-ordering contributions, but the 7-T value of  $\gamma_0$ , which is well determined by the construction in Fig. 3, is represented by the horizontal line at  $\Delta C/T = 63 \text{ mJ/mol K}^2 = 210 \text{ mJ/mol Pr K}^2$ . (The fact that the lowest-temperature 7-T datum point falls below that line is misleading—the discrepancy is a small part of the total  $C$ , and within the precision of the data.) For both  $H = 0$  and  $H = 7$  T,  $\Delta C/T$  is close to the 7-T value of  $\gamma_0$  in the region 20–40 K, and drops below that value at higher temperatures. Thus, taken together, the zero-field and 7-T data suggest a  $\gamma_0 T$  contribution that is only weakly  $H$  dependent and extends to a

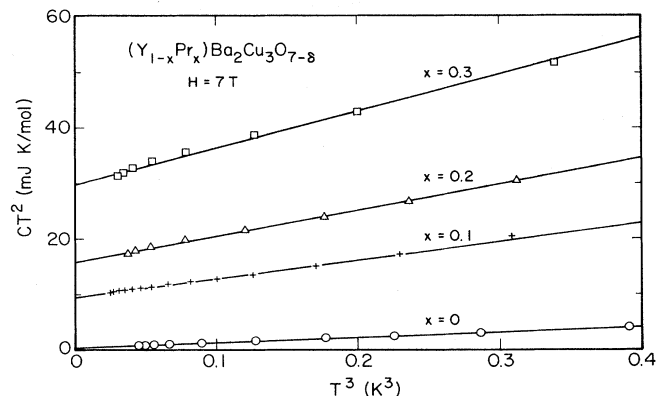


FIG. 3. Analysis of the low-temperature  $H = 7$ -T data into  $T$  and  $T^{-2}$  terms.

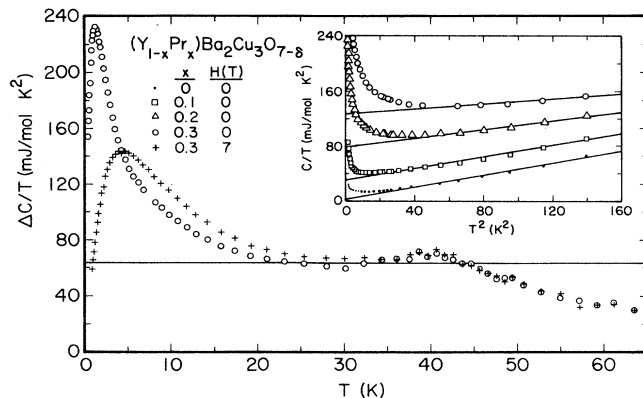


FIG. 4.  $\Delta C/T$  vs  $T$ , where  $\Delta C$  is the magnetic ordering plus “heavy-fermion-like,”  $\gamma_0 T$ , contributions to  $C$ . The inset shows  $C/T$  vs  $T^2$  for  $T < 13$  K.

cutoff temperature of  $\sim 50$  K, and an  $H$ -dependent magnetic ordering contribution that produces the maxima in  $\Delta C/T$  near 1 and 5 K. The weak  $H$  dependence of  $\gamma_0$  is understandable even if the  $\gamma_0 T$  contribution is magnetic in origin if the cutoff temperature is a measure of the strength of interaction underlying the contribution. The associated entropy, the area below the line at  $\Delta C/T = 210$  mJ/molPrK<sup>2</sup> and below  $T = 50$  K, is  $\sim \mathcal{R} \ln 4$  (per mol Pr). The  $x = 0.1$  and  $0.2$  data are consistent with these results with respect to both entropy and cutoff temperature. The entropy of the magnetic ordering anomaly, the area between the line and the data is  $\sim \frac{1}{2} \mathcal{R} \ln 2$  (per mol Pr) for both  $H = 0$  and  $H = 7$  T, about half that observed for  $x = 1$ . Within the experimental uncertainty it has the same value in 7 T for  $x = 0.1$  and  $0.2$ . (For  $H = 0$  and  $x = 0.1$  and  $0.2$ , the data do not determine the magnetic ordering contribution.) The small “bump” in  $\Delta C/T$  near 40 K occurs in the vicinity of the superconducting transition, but its field independence suggests another origin. In fact, it corresponds to only  $\sim 1\%$  of the total  $C$ , and could be just an artifact associated with the assumption that the background  $C$  is the same for  $x = 0$  and  $0.3$ . Furthermore, it is not observed for  $x = 0.1$  and  $0.2$ . The failure to observe an anomaly in  $C$  associated with the superconducting transition (there is a 35% Meissner effect in the  $x = 0.3$  sample) is consistent with the trend established by typical  $x = 0$  samples and the  $x = 0.1$  sample, and with the possible explanations cited in connection with the  $x = 0.1$  sample. The values of  $\gamma_0$  reported here are lower than those derived from earlier measurements<sup>10,19</sup> because they are based on an analysis that took into account the magnetic contributions to  $C$  identified by the combination of lower-temperature and in-field data, not because there is any great discrepancy in the data. The origin of the differences in the values of  $\gamma_0$  can be seen in Fig. 1; in the interval  $5 \leq T \leq 12$  K,  $C/T$  is relatively constant, and fits with a sum of  $T$  and  $T^3$  terms (illustrated in the inset to Fig. 4) lead to the higher values of  $\gamma_0$  reported earlier.

At low temperatures the behavior of the  $x = 1$  sample is qualitatively different from that of the  $x = 0.1, 0.2$ , and  $0.3$  samples. For Pr-Ba-Cu-O in  $H = 0$  at  $T \leq 1.5$  K,  $C = D/T^2 + \gamma_0 T + AT^3$  with  $D = 61$  mJ K/mol,  $\gamma_0 = 102$

mJ/molK<sup>2</sup>, and  $A = 6.99$  mJ/molK<sup>4</sup>. The parameters  $D$ ,  $\gamma_0$ , and  $A$  are all strongly  $H$  dependent. The  $H$  dependence of the Pr hyperfine field (calculated on the assumption that contributions from the Cu nuclei are negligible and from a  $CT^2$ -vs- $T^3$  analysis as shown in Fig. 3 for  $H = 7$  T) is shown for the  $x = 0.3$  and  $1$  samples in Fig. 5. For all Pr-containing samples, the hyperfine field is  $\sim 100$  T at  $H = 7$  T. However, for Pr-Ba-Cu-O, the hyperfine field is substantially higher than that for  $x = 0.3$  at  $H = 0$ , and the field dependence is weaker and qualitatively different. For  $x = 0.1$  and  $0.2$ , the hyperfine contribution cannot be separated from the magnetic-ordering contribution at  $H = 0$ , and no measurements were made for  $0 < H < 7$  T.

In summary, the Pr-related contributions to  $C$  are as follows: (1)  $H$ - and  $x$ -dependent hyperfine contributions; (2)  $H$ - and  $x$ -dependent, magnetic-ordering contributions, exemplified by the broad maxima in  $C/T$  in Fig. 1 and the maxima in  $\Delta C/T$  in Fig. 4; (3) for  $x \leq 0.3$ , a heavy-fermion-like  $\gamma_0 T$  contribution that extends to a cutoff temperature of  $\sim 50$  K [clearly these excitations do not take part in the condensation to the superconducting state—the density of states is more than an order of magnitude too high in comparison with the observed  $\Delta C(T_c)$ ]; and (4) for  $x = 1$ , at temperatures below  $T_{N2}$ , large  $T$  and  $T^3$  terms presumably associated with low-energy magnetic excitations in the ordered state.

The hyperfine fields are, in principle, dependent on the crystal-field levels and therefore the valency of the ion. In the absence of detailed calculations, however, it is not possible to distinguish between a  $\text{Pr}^{4+}$ ,  $J_z = \pm \frac{1}{2}$  ground state and low-lying states of higher  $J_z$ , or a  $\text{Pr}^{3+}$  singlet ground state with exchange-induced mixing of higher states.

The temperatures of the magnetic-ordering contributions for  $x = 0.1, 0.2$ , and  $0.3$  are qualitatively consistent with the expected effect of dilution on the 17-K ordering anomaly for  $x = 1$ , and with the recent phase diagram determined by Cooke *et al.*,<sup>9</sup> who used muon spin rotation to follow the Pr antiferromagnetic ordering to  $x = 0.4$ , where it was observed near 2 K. The strong field dependence of the heat-capacity anomaly at 1 K in the  $x = 0.3$  sample is consistent with antiferromagnetic ordering.

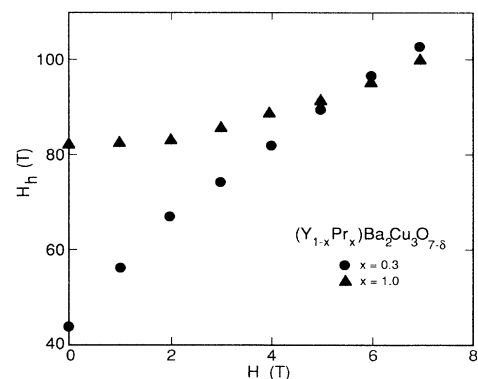


FIG. 5.  $H$  dependence of the Pr hyperfine field for  $x = 0.3$  and  $1$ .

Although smaller than deduced from earlier measurements,<sup>10,19</sup> the value of  $\gamma_0$  is still large compared with those typical of ordinary metallic systems, and may be associated with hybridization of the Pr 4*f* and O 2*p* electrons. Many authors<sup>15-26</sup> have pointed out that some hybridization is necessary in order to explain several of the anomalous features in these materials. In addition to the anomalous thermopower and the strong dependence of  $T_c$  on pressure,<sup>25</sup> there is other evidence of strong coupling between the Pr local moments. This coupling is evident both in the temperature at which the magnetic ordering is observed<sup>10</sup> (17 K for  $x=1$ ), which is too high with respect to the other rare earths, as well as the pair-breaking behavior implied by the critical-field results.<sup>13,14</sup> This pair breaking is distinct from that proposed by Kebede *et al.*,<sup>10</sup> which is of the Abrikosov-Gorkov type,<sup>27</sup> and does not require the magnetic ions to be coupled. In the absence of conduction electrons to mediate the Ruderman-Kittel-Kasuya-Yosida interaction, some form of hybridization is required to provide a superexchange interaction between the Pr ions. Hybridization of the Pr 4*f* electrons with those of copper and oxygen has also been proposed by Torrance and Metzger<sup>26</sup> as a mechanism which causes a localization of the conducting holes in the copper-oxygen planes. This would be consistent with the insulating behavior found at high  $x$ .<sup>10,14</sup> As  $x$  increases, percolative paths vanish and the material ceases to conduct. In the low- $x$  region, however, the material would not be substantially affected, and this mechanism alone would not explain the absence of superconductivity when the material is still metallic. It has sometimes been argued that the presence of hybridization is consistent only with a +4 or mixed-valence state. In fact, the Pr ion can hybridize out

of either the +4 or +3 states, but is much more likely to do so from the +3 state, since one of the two remaining 4*f* electrons is loosely bound. In the +4 state, which would correspond to one of these electrons being placed in a different location, presumably in the CuO<sub>2</sub> planes, the remaining 4*f* electron is more strongly bound, and would not tend to hybridize. The possibility of the Pr ion hybridizing out of the +3 valence state may be what distinguishes Pr from the other rare earths for which the *f* electrons are bound more securely in the +3 state.

Recent measurements on an  $x=0.3$  sample by Ghamaaty *et al.*<sup>24</sup> show some of the features reported here. A value of  $\gamma_0=235$  mJ/molPrK<sup>2</sup> was obtained, compared with the value 200 mJ/molPrK<sup>2</sup> obtained in this work, but the measurements did not extend to temperatures high enough to determine the cutoff temperature. A magnetic-ordering anomaly similar in magnitude to that reported here was found, but it was represented there by a Kondo anomaly, which has a very different temperature dependence from that deduced in this work (although the low-temperature deviations of their data from the fitting expression are not inconsistent with this work).

We are grateful to V. Kresin for valuable discussions. The work at Berkeley was supported by the Director, Office of Energy Research, Office of Basic Energy Sciences, Materials Sciences Division of the U.S. Department of Energy under Contract No. DE-AC03-76SF00098. The work at Lawrence Livermore National Laboratory and University of California-Davis was performed under the auspices of the U.S. Department of Energy under Contract No. W-7405-ENG-48.

\*Present address: Institut für Festkörperphysik, Technische Hochschule Darmstadt, Darmstadt, Federal Republic of Germany.

†Present address: Laboratorium für Festkörperphysik, Eidgenössische Technische Hochschule Hönggerberg, Zürich, Switzerland.

‡Present address: Department of Physics, University of Maryland, College Park, MD 20742.

<sup>1</sup>K. N. Yang *et al.*, Solid State Commun. **63**, 515 (1987).

<sup>2</sup>Z. Fisk *et al.*, Solid State Commun. **62**, 743 (1987).

<sup>3</sup>P. H. Hor *et al.*, Phys. Rev. Lett. **58**, 1891 (1987).

<sup>4</sup>D. W. Murphy *et al.*, Phys. Rev. Lett. **58**, 1888 (1987).

<sup>5</sup>L. Soderholm *et al.*, Nature (London) **328**, 604 (1987).

<sup>6</sup>Y. Dalichaouch *et al.*, Solid State Commun. **65**, 1001 (1987).

<sup>7</sup>K. K. Liang *et al.*, Z. Phys. B **69**, 137 (1987).

<sup>8</sup>W. H. Li *et al.*, Phys. Rev. B **40**, 5300 (1989).

<sup>9</sup>D. W. Cooke *et al.*, Phys. Rev. B **41**, 480 (1990).

<sup>10</sup>A. Kebede *et al.*, Phys. Rev. B **40**, 4453 (1989).

<sup>11</sup>A. Matsuda *et al.*, Phys. Rev. B **38**, 2910 (1988).

<sup>12</sup>J. J. Neumeier *et al.*, Phys. Rev. Lett. **63**, 2516 (1989).

<sup>13</sup>J. L. Peng *et al.*, Phys. Rev. B **40**, 4517 (1989).

<sup>14</sup>H. B. Radousky *et al.*, Physica C **162-164**, 1363 (1989).

<sup>15</sup>L. Soderholm and G. L. Goodman, J. Solid State Chem. **81**, 121 (1989).

<sup>16</sup>G. Y. Guo and W. M. Temmerman, Phys. Rev. B **41**, 6372 (1990).

<sup>17</sup>M. E. Lopez-Morales *et al.*, Phys. Rev. B **41**, 6655 (1990).

<sup>18</sup>H. B. Radousky *et al.*, Phys. Rev. B **39**, 12383 (1989).

<sup>19</sup>M. B. Maple *et al.*, J. Less-Common Met. **149**, 405 (1989).

<sup>20</sup>J. S. Kang *et al.*, J. Less-Common Met. **148**, 121 (1989).

<sup>21</sup>A. P. Goncalves *et al.*, Phys. Rev. B **37**, 7476 (1988).

<sup>22</sup>X. X. Tang *et al.*, Physica C **161**, 574 (1989).

<sup>23</sup>L. Soderholm, C.-K. Loong, G. L. Goodman, and B. D. Dabrowski, Phys. Rev. B **43**, 7923 (1991).

<sup>24</sup>S. Ghamaaty, B. W. Lee, J. J. Neumeier, G. Nieva, and M. B. Maple, Phys. Rev. B **43**, 5430 (1991).

<sup>25</sup>J. J. Neumeier *et al.*, Physica C **156**, 574 (1988).

<sup>26</sup>J. B. Torrance and R. M. Metzger, Phys. Rev. Lett. **63**, 1515 (1989).

<sup>27</sup>A. A. Abrikosov and L. P. Gorkov, Zh. Eksp. Teor. Fiz. **39**, 1781 (1960) [Sov. Phys. JETP **12**, 1243 (1961)].