

## Molecular motion in solid H<sub>2</sub> at high pressures

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Solid molecular hydrogen has been studied with proton nuclear magnetic resonance in a diamond anvil cell. Pressures from 18 to 68 kbar were used, resulting in melting temperatures from 160 to 350 K and relative densities  $\rho/\rho_0$  as high as 3. At temperatures above  $0.7T_{\text{melt}}$ , translational self-diffusion narrows the resonance line. The pressure variation of the activation enthalpy  $\Delta H$  yields an activation volume of  $5.7 \pm 0.6 \text{ cm}^3/\text{mol}$  or 63% of the molar volume, a reasonable value for a vacancy diffusion mechanism. The smooth variation of  $\Delta H/kT_{\text{melt}}$  with density also suggests that the diffusion mechanism remains the same for  $\rho/\rho_0$  between 1 and 3. The spin-lattice relaxation is controlled primarily by molecular reorientation. The observed density dependence  $T_1 \propto \rho^{5/3}$  indicates that molecular electric quadrupole-quadrupole interactions cause reorientation, even at the high temperatures and densities of this work.

### I. INTRODUCTION

In recent years there has been substantial interest in the behavior of molecular solids at high pressures and densities. Much work on structural phase transitions using x-ray diffraction<sup>1-3</sup> and Raman spectroscopy<sup>4-7</sup> has been reported. Optical techniques<sup>8,9</sup> and dc resistance measurements<sup>9</sup> have been used to study insulator-metal transitions. Recently, we reported the feasibility of nuclear magnetic resonance (NMR) experiments in a diamond anvil cell (DAC).<sup>10</sup> Using the sensitivity of NMR to molecular motions, we have studied and report here the effects of high pressure on self-diffusion and molecular reorientation in solid H<sub>2</sub>.

The effects of pressures up to 68 kbar upon solid H<sub>2</sub> are profound. The melting temperature (see Fig. 1) varies from 14 K at essentially zero pressure (the lowest triple temperature of any substance) to 350 K at 68 kbar,<sup>11</sup> a factor of 25 increase. Over this pressure range the density<sup>12,13</sup> increases by a factor of 3. The large compressibility of solid H<sub>2</sub> arises in part from the small number of electrons and the correspondingly small repulsion term. Also, at low pressures the volume of condensed H<sub>2</sub> is expanded by zero-point motion, which is large because of the small mass. The large changes in  $T_{\text{melt}}$  and density in H<sub>2</sub> may be contrasted with the smaller effects of 70 kbar upon solid N<sub>2</sub>: a factor of 8 increase in  $T_{\text{melt}}$  and 1.7 increase in density.<sup>3</sup>

Self-diffusion in most solids at normal densities occurs through the monovacancy mechanism.<sup>14</sup> This mechanism naturally has a large activation volume  $\Delta V$ , which increases the activation enthalpy  $\Delta H = \Delta E + P\Delta V$  at high pressures. One may expect at sufficiently high pressures that some other mechanism with a smaller  $\Delta V$  will become the dominant diffusion mechanism. For example, ring exchange (interchange) occurs via quantum tunneling<sup>15</sup> in solid He<sup>3</sup>. Ring exchange has also been discussed as a possible classical diffusion mechanism of silicon<sup>16-18</sup> and graphite.<sup>17</sup> We have examined our H<sub>2</sub> diffusion data

for a change in mechanism; we find no such evidence.

In molecular solids, it has been observed that the diffusion rate in the solid at the melting point is a constant, independent of pressure.<sup>19</sup> Because only small changes in the diffusion prefactor occur, this implies that the ratio of the activation enthalpy to the melting temperature stays constant. This has been studied previously

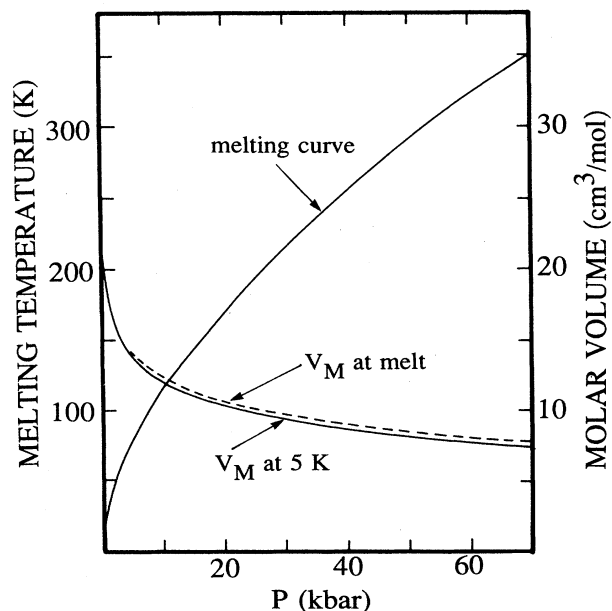


FIG. 1. The pressure variation of the melting temperature and the molar volume of H<sub>2</sub>. The solid curve is for 5-K molar volume and the dashed curve refers to the solid at the melting point. The values are taken from Refs. 11-13 with some small extrapolations for melting point volumes and the melting temperatures.

with modest pressures producing only 30% changes in  $T_{\text{melt}}$ . The H<sub>2</sub> data reported here test this empirical relation over a much wider range of conditions.

At low temperatures and pressures, ortho-H<sub>2</sub> molecules are in the  $J=1$  state and are the only species with nonzero nuclear spin.<sup>20</sup> The ortho-H<sub>2</sub> may be regarded as a system of molecular spins-one coupled by their electrical quadrupole-quadrupole (EQQ) interactions. This model is very successful in explaining molecular reorientation and the resulting nuclear spin relaxation<sup>21</sup> in solid H<sub>2</sub>. By contrast, our study involves temperatures as high as 330 K, so higher  $J$  states will be present. Further, coupling between phonons and molecular orientations may be important at the high temperatures. Finally, at high density one expects that shorter-range anisotropic molecular repulsion and attraction terms may couple the molecular orientations, in addition to the EQQ coupling. These effects are examined in the nuclear spin relaxation data of H<sub>2</sub> at high pressures, as reported here.

## II. EXPERIMENTAL METHODS

Some techniques for NMR in a diamond anvil cell have been described previously.<sup>10</sup> The essential feature is to apply a rf field  $H_1$  parallel to the metallic gasket so that  $H_1$  penetrates into the gasket hole. Here we use a copper ribbon resonator, a one-turn coil resonating with a small chip capacitor. The current path is physically small to improve the filling factor, which nevertheless is only about  $10^{-2}$ . Adjustable tuning and coupling capacitors are located nearby and transform the impedance to 50  $\Omega$ . The capacitors are adjusted from the room via long extension shafts. For high sensitivity the experiments are performed at 340 MHz in an 8-T superconducting solenoid. An important feature of the ribbon resonator is that it can be cleaned in acetone with ultrasound to remove finger grease, etc. (the H<sub>2</sub> samples are  $\sim 4 \mu\text{g}$  and stray proton signals must be avoided).

The NMR spectrometer is of conventional design. The  $\sim 25$ -W output power results in a  $\pi/2$  pulse length of 7  $\mu\text{s}$ . The signal-to-noise ratio of single transients is  $\sim 2$ , depending on bandwidth, and is adequate for tuneup. Signal averaging of  $\sim 200$  transients is generally used for quantitative data.

The DAC (Refs. 22 and 23) is constructed of titanium alloy (6% Al, 4% V) (Ref. 24) and uses a piston and cylinder as a guide for stable alignment. The force required to clamp the gasket and trap a H<sub>2</sub> sample is generated by a single 8-32 screw. For pressures above 30 kbar a lever system is used that fits into the narrow 54-mm magnet bore. The diamonds are  $\frac{1}{4}$  carat each, with 1-mm culets. The 0.25-mm-thick gasket is used without preindentation; the gasket hole is 0.5 mm diameter. Hardened Be-Cu is used below 35 kbar and rhenium is used for higher pressures.<sup>25,26</sup> Temperatures are controlled by thermostatted, flowing N<sub>2</sub> gas. The temperature is measured with a thermocouple. We intend to publish more details of the NMR DAC separately.

The fluorescence of a ruby chip is used to measure the pressure.<sup>27</sup> An argon ion laser and monochromator are coupled to the DAC by a single 0.1-mm-diam graded in-

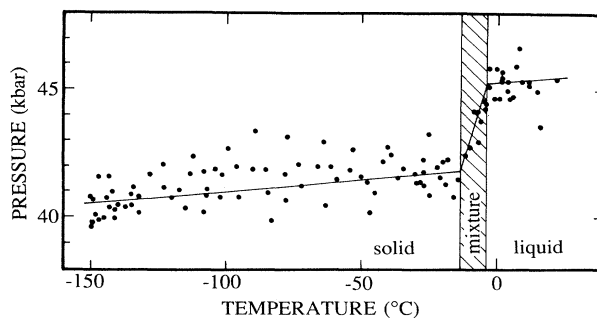


FIG. 2. Typical variation of pressure with temperature, as determined from ruby fluorescence. The temperature interval of H<sub>2</sub> melting is indicated.

dex optical fiber with coupling lenses. Our intention was to measure the pressure *in situ*, but the 8-T field broadens the ruby spectrum. We resorted to measuring the pressure outside the magnet in a separate temperature controlling apparatus. Correction for the temperature shift of the ruby spectrum is performed.<sup>28</sup> A typical variation of pressure with temperature appears in Fig. 2. The pressure is nearly constant in the solid, but increases upon melting. This pressure rise is due to the approximately constant volume conditions. The observation of sharp ruby fluorescence lines implies that the pressure is nearly hydrostatic.

Hydrogen is loaded by placing the DAC without its lever system into a conventional pressure vessel.<sup>29</sup> H<sub>2</sub> gas at 400 bars directly from a commercially available cylinder is introduced into the pressure vessel at 77 K. The density of H<sub>2</sub> under these conditions is approximately equal to that of normal liquid H<sub>2</sub>. The DAC is closed using an O-ring sealed screwdriver.

## III. RESULTS AND DISCUSSION

The spin-spin relaxation time  $T_2$  was determined from free induction decays (FID's) for  $T_2 \lesssim 75 \mu\text{s}$ . The pulse sequence of Carr, Purcell, Meiboom, and Gill (CPMG) was used for longer  $T_2$ .<sup>30</sup> The presence of liquid H<sub>2</sub> was indicated by a substantial increase in  $T_2$ . Also, in the liquid phase only, the apparent  $T_2$  from the CPMG experiment increased as the pulse separation was decreased. This behavior indicates rapid diffusion through the magnetic field gradient.<sup>30</sup> For liquid H<sub>2</sub>, the FID had a decay time  $T_2^*$  of  $\sim 900 \mu\text{s}$  with Be-Cu gasket, presumably arising from the magnetic susceptibilities of the gasket, diamonds, and ruby chip. Rhenium gaskets gave a considerably shorter value,  $T_2^* \approx 100 \mu\text{s}$ .

The  $T_2$  measurements for solid H<sub>2</sub> at several pressures are plotted in Fig. 3 as a function of reciprocal temperature. As temperature increases, the line is narrowed and  $T_2$  is increased by motional narrowing from self-diffusion. For some samples the rigid lattice limit was studied. Other samples suffered from proton-bearing contamination (e.g., finger grease); for these samples the H<sub>2</sub> signal could be distinguished only when the H<sub>2</sub> was motionally narrowed. During the course of the research,

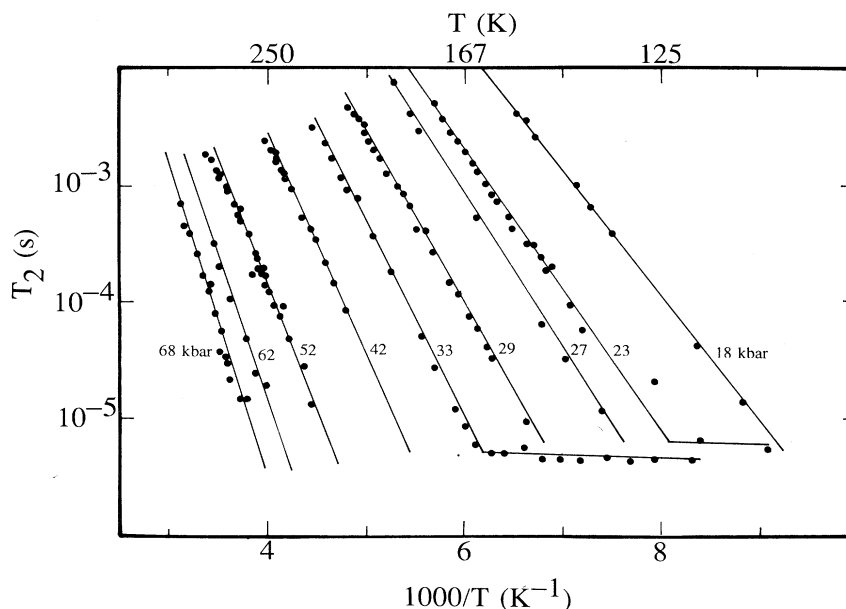


FIG. 3. Transverse relaxation time  $T_2$  of solid  $H_2$  as a function of reciprocal temperature. The numbers on each line label the pressure in kilobars. Self-diffusion motionally narrows the line and increases  $T_2$  as temperature increases. The activation enthalpy derived from the slope increases with pressure (see Figs. 4 and 5 and Table I).

we became more successful in cleaning away contaminants.

The slopes of the lines fit to the motionally narrowed data in Fig. 3 directly yield the activation enthalpies  $\Delta H$  in Table I. That is, we can write

$$T_2 = T_2^\infty \exp(-\Delta H/kT), \quad (1)$$

because the observed  $T_2$  is proportional to the rate  $\omega_j$  of molecular diffusion jumps.<sup>19,30</sup> The values of  $T_2$  extrapolated to infinite temperature are  $T_2^\infty$  and depend only weakly upon pressure (Table I).

In the theory of thermally activated processes,<sup>14</sup> the activation enthalpy  $\Delta H$  is expressed as  $\Delta H = \Delta E + P\Delta V$ , with  $\Delta E$  and  $\Delta V$  constant over a range of temperature and pressure. The pressure variation of  $\Delta H$  is presented in Fig. 4. The dashed curve schematically connects the high-pressure data of this work to the low-pressure results of Ref. 31. The slope of the straight line fit to the

high-pressure data yields  $\Delta V = 5.7 \pm 0.6 \text{ cm}^3/\text{mol}$ . This  $\Delta V$  is about  $63\% \pm 7$  of the molar volume  $V_M$  of the 40-kbar solid at the melt,<sup>12,13</sup> chosen as the middle of the pressure range studied. We note that the molar volume changes by  $\sim 30\%$  from 20 to 70 kbar, so only a slight curvature is expected in Fig. 4, assuming  $\Delta V$  to be a fixed fraction of  $V_M$ .

In pure metals, the diffusion mechanism is certainly monovacancy.<sup>14</sup> Activation volumes, expressed as a fraction of the molar volume, range from 0.33 for tin<sup>32</sup> to 1.35 for aluminum.<sup>14</sup> The alkali metals have values near 0.5 and gold, silver, and lead have values near 0.8.<sup>14</sup> In the case of gold, the activation volume for vacancy migration was found to be much smaller than the diffusion activation volume. Thus most of the diffusion activation volume is associated with vacancy formation. In most molecular (organic) solids, diffusion is also believed to be a monovacancy process.<sup>33</sup> The ratio of diffusion activation volume to molar volume ranges from 0.57 to

TABLE I. Measured and derived parameters of  $H_2$  self-diffusion.

Pressure (kbar)	0	18	23	27	29	33	42	52	62	68
Density, $\rho/\rho_0$	1	2.15	2.23	2.40	2.45	2.55	2.73	2.86	2.93	2.95
$T_{\text{melt}}$ (K)	14	159	183	202	210	227	261	296	328	350
$\Delta H$ (K)	190 <sup>a</sup>	2480	2770	3040	3400	3790	4320	5030	5650	6140
$\Delta H/T_{\text{melt}}$	13.6	15.6	15.1	15.0	16.2	16.7	16.6	17.0	17.2	17.5
Theoretical $M_2$ ( $10^{10} \text{ s}^{-2}$ )	0.24	1.11	1.19	1.38	1.44	1.56	1.79	1.96	2.06	2.09
$T_2^\infty$ ( $10^4 \text{ s}$ )	0.31 <sup>a</sup>	4.7	3.3	7.1	6.9	8.5	8.7	6.8	9.8	15.0
$\omega_j^\infty$ ( $10^{14} \text{ s}^{-1}$ )	0.07	4.8	3.6	9.0	9.2	12.2	14.4	12.3	18.6	28.9
$T_2^{\text{melt}}$ (ms)	4.0 <sup>a</sup>	7.9	8.8	20.7	6.4	4.8	5.6	2.8	3.2	3.6
$\omega_j^{\text{melt}}$ ( $10^7 \text{ s}^{-1}$ )	0.89	8.1	9.7	26.3	8.5	6.9	9.2	5.1	6.1	6.9

<sup>a</sup>Reference 51.

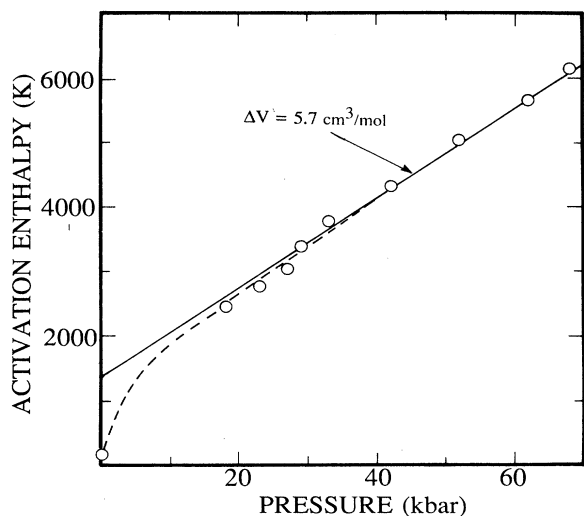


FIG. 4. Activation enthalpy of self-diffusion  $\Delta H$  in solid H<sub>2</sub> as a function of pressure. The slope of the line through the data yields an activation volume  $\Delta V$  of  $5.7 \pm 0.6$  cm<sup>3</sup>/mol. The dashed curve schematically connects the high-pressure data of this work with a low-pressure datum from Ref. 31.

1.2.<sup>19,34-37</sup> The value reported here for H<sub>2</sub> at high pressures,  $0.63 \pm 0.07$ , is at the low end of the range of previous values. A much smaller value would be expected for interstitial mechanisms<sup>32</sup> or the direct exchange mecha-

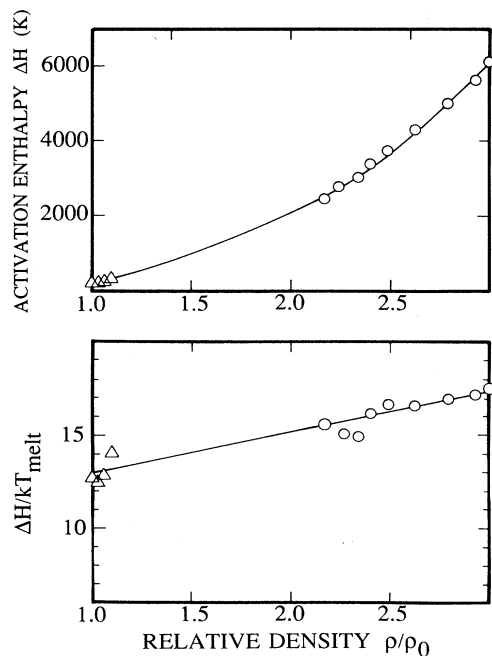


FIG. 5. Activation enthalpy of self-diffusion  $\Delta H$  as a function of relative density. The density  $\rho_0$  refers to H<sub>2</sub> at 4.2 K and 1 bar. The high-density data (circles) are from this work and the low-density data (triangles) are from Ref. 31. The ratio  $\Delta H/kT_{\text{melt}}$  also is displayed.

nism. The measured value indicates that diffusion in high-pressure H<sub>2</sub> occurs through vacancies.

The density dependence of the activation enthalpy  $\Delta H$  appears in Fig. 5. The high-density data of this work and previous low-density data<sup>31</sup> are shown. The relative densities  $\rho/\rho_0$  were obtained from Refs. 12 and 13, where  $\rho_0$  is the 1/23.2 mol/cm<sup>3</sup> density of solid H<sub>2</sub> at 4.2 K and 1 bar. A single smooth curve fits through all of the data.

The dimensionless ratio  $\Delta H/kT_{\text{melt}}$  varies between 10 and 35 for a wide variety of solids.<sup>17</sup> For similar solids (e.g., molecular solids with orientation disorder), the range is narrower. In fact,  $\Delta H/kT_{\text{melt}}$  has been found to be independent of pressure for molecular solids such as hexamethylethane and cyclohexane.<sup>19</sup> However, the reported 2.8-kbar pressure range causes only a  $\sim 30\%$  change in  $T_{\text{melt}}$ . In Fig. 5, we present  $\Delta H/kT_{\text{melt}}$  for solid H<sub>2</sub>, covering a density range of 3 and a melting temperature range of 25. The low-density data<sup>31</sup> have  $\pm 10\%$  error bars. The value of  $\Delta H/kT_{\text{melt}}$  increases slowly and smoothly with pressure. The absence of a larger or sharper variation suggests that the same diffusion mechanism is present over a remarkably wide range of conditions.

The molecular jump rate  $\omega_j$  may be computed from the motionally narrowed  $T_2$  values using<sup>19</sup>

$$T_2^{-1} = 0.9M_2/\omega_j. \quad (2)$$

This refers to the adiabatic limit  $\omega_j \ll \omega_0$  which applies here ( $\omega_0$  is the spin precession frequency). The second moment  $M_2$  refers only to intermolecular interactions. We make the standard assumptions that the molecules rotate spherically and without correlation between neighbors. It has been shown in this case that the correct intermolecular second moment  $M_2$  is obtained by locating all the spins at the centers of the molecules.<sup>38</sup> Thus, for H<sub>2</sub> with 75% ortho-H<sub>2</sub> molecules with nuclear spin  $I=1$ , the powder average  $M_2$  is<sup>19,39</sup>

$$M_2 = \frac{3}{5}\gamma^4\hbar^2 I(I+1) \frac{3}{4} \sum_k (1/r_{jk}^6). \quad (3)$$

For hcp H<sub>2</sub> at the density corresponding to 33 kbar at the melt, Eq. (3) yields  $M_2 = 1.56 \times 10^{10} \text{ s}^{-2}$ . Using this value of  $M_2$  and the  $T_2$  value from Fig. 3 extrapolated to infinite temperature (Table I),  $T_2^\infty = 8.5 \times 10^4 \text{ s}$ , the value of molecular jump rate extrapolated to infinite temperature is  $\omega_j^\infty = 1.2 \times 10^{15} \text{ s}^{-1}$ . This is an acceptable value of the attempt frequency  $\omega_j^\infty$  and indicates that our analysis is reasonable. Values of  $\omega_j^\infty$  for other pressures are listed in Table I.

The values of  $T_2$  in Fig. 3 have also been extrapolated to give values at the melting temperatures. Using Eq. (2) and second moments from Eq. (3) with densities from Refs. 12 and 13, molecular jump rates  $\omega_j$  at the melt are determined. The jump rates at the melt are plotted in Fig. 6 and listed in Table I as a function of pressure, along with a zero-pressure datum.<sup>31</sup> The rate of jumps at the melt varies relatively little (after removing scatter) while the melting temperature varies by about 25. It has been proposed<sup>40</sup> that the rate of diffusion is a function only of the reduced temperature  $T/T_{\text{melt}}$ . The H<sub>2</sub> data of

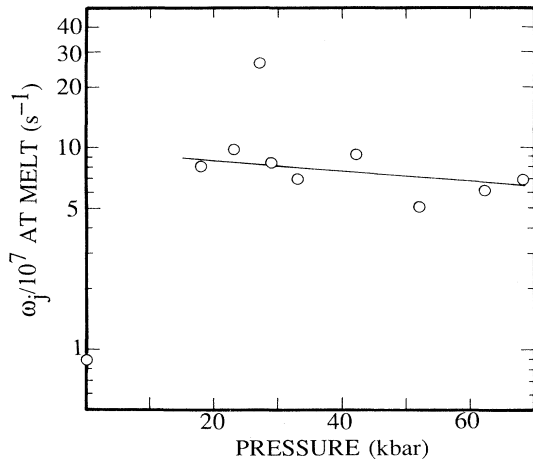


FIG. 6. Rate of molecular diffusion jumps  $\omega_j$  at the melting temperature as a function of pressure. The high-pressure data are from this work; the zero-pressure datum is from Ref. 51. The line is an eye guide.

Fig. 6 provide remarkable support for this view, because of the wide range of melting temperature included.

The measured and derived values relating to self-diffusion in  $H_2$  are summarized in Table I.

The spin-lattice relaxation time  $T_1$  is presented in Fig. 7 as a function of temperature for two pressures. The regions of two-phase coexistence are shown by cross-hatching. In the solid near the melt,  $T_1$  decreases because of the rapid diffusion modulation of the intermolecular dipole interactions. This behavior is identical to that observed in several molecular solids<sup>19</sup> and, in particular, solid  $H_2$  at low pressure.<sup>21</sup> Well below the melting temperature,  $T_1$  appears to be temperature independent and presumably reflects only molecular reorientations.

The observed relaxation rate  $T_1^{-1}$  can be expressed as a sum of two terms,

$$T_1^{-1} = T_{1\text{rot}}^{-1} + T_{1\text{diff}}^{-1} . \quad (4)$$

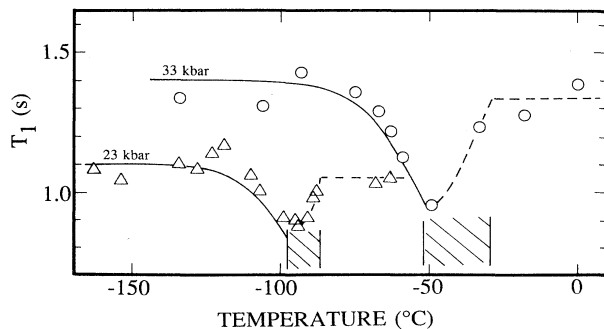


FIG. 7. Spin-lattice relaxation time  $T_1$  as a function of temperature at two pressures. The melting regions are shown by cross-hatching. Just below the melting temperature, relaxation from diffusion decreases  $T_1$ . At lower temperatures the relaxation is from molecular reorientation only. The dashed lines are eye guides and the solid curves are from Eqs. (4) and (6).

The rate from translational diffusion may be written in the slow jump limit ( $\omega_j \ll \omega_0$ ),<sup>19</sup>

$$T_{1\text{diff}}^{-1} = 2.3M_2\omega_j/\omega_0^2 . \quad (5)$$

Combining Eq. (5) with Eq. (2), one obtains

$$T_{1\text{diff}}^{-1} = 2.1M_2^2T_2/\omega_0^2 . \quad (6)$$

Using the  $1.56 \times 10^{10} \text{ s}^{-2}$  value of  $M_2$  for 33 kbar,  $T_{1\text{diff}}^{-1}$  was calculated from the measured  $T_2$ . Assuming a constant value of  $T_{1\text{rot}} = 1.4 \text{ s}$  as measured and using Eq. (4) to add the relaxation rates, we obtain the solid curve in Fig. 7. A similar curve appears for 23 kbar. The good agreement with the data demonstrates that the decrease in  $T_1$  below the melt indeed arises from diffusion.

The density dependence of the relaxation time  $T_{1\text{rot}}$  is displayed in Fig. 8. The low-density datum<sup>21</sup> is for 75% ortho- $H_2$  at 1 bar and 10 K. We believe our samples remained at 75% ortho- $H_2$  fraction because the conversion rate is expected to be low at high densities.<sup>41</sup> Also, our temperature range of 120–330 K is high enough that the equilibrium concentration varies only from 65 to 75%.<sup>20</sup> The straight line fit to the data corresponds to  $T_1 \propto \rho^{5/3}$ . Since the molecular reorientation rate  $\omega_{\text{rot}}$  certainly exceeds the nuclear spin resonance frequency  $\omega_0$ , we have  $T_1 \propto \omega_{\text{rot}}$  and thus  $\omega_{\text{rot}} \propto \rho^{5/3}$ . The electrostatic interaction between the molecular quadrupoles (EQQ) varies as  $r^{-5}$  and, therefore,  $\rho^{5/3}$ . Thus it appears that EQQ interactions cause molecular reorientations at the elevated densities and temperatures of this work as well

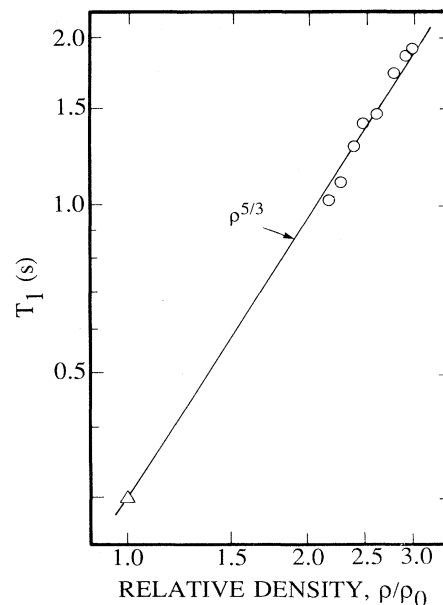


FIG. 8. The spin-lattice relaxation time  $T_1$  due to reorientation as a function of relative density. The  $T_1$  values are from the temperature-independent region well below the melt (see Fig. 7). The low-density datum is from Ref. 21 and refers to  $H_2$  at 10 K, 1 bar, and 75% ortho- $H_2$  concentration. The straight line corresponds to  $T_1 \propto \rho^{5/3}$ .

as at low density and temperature. The large density range makes zero-point motion corrections to EQQ unimportant.

We note that in a previous study<sup>42</sup> of H<sub>2</sub> at pressures up to 7 kbar at 4.2 K,  $T_1$  increased only as  $\rho^{1.25}$ . The sample had an ortho-H<sub>2</sub> fraction of 18%. At such relatively low densities (1.0–1.6) one expects the EQQ interactions to be dominant, as shown by the Raman work of Durana and McTague.<sup>43</sup> This should result in  $T_1 \propto \rho^{5/3}$ ; we do not understand the density dependence observed by the Duke group.

At 300 K, 12% of the ortho-H<sub>2</sub> molecules are in the  $J=3$  level. Fedders has calculated<sup>44</sup> the effect of the  $J=3$  fraction upon  $T_1$  for the case of phonon-induced reorientation (i.e., dilute ortho-H<sub>2</sub>). However, there are no calculations relevant to the present situation of EQQ-induced reorientations. Our only estimate of the effect is from Fedders;<sup>45</sup> the fractional effect upon  $T_1$  should be no longer than the fractional concentration of  $J=3$ .

A second effect of the high temperatures used in this work is that the para-H<sub>2</sub> molecules are not all in the  $J=0$  state. Being spherically symmetric, the  $J=0$  molecules serve as an inert diluent for the ortho-H<sub>2</sub> molecular spins. At 250 K, 39% of the para-H<sub>2</sub> are in the  $J=2$  state. These  $J=2$  molecules can couple to the  $J=1$  molecules and induce mutual  $\Delta m_J$  transitions. One expects that the net effect of the  $J=2$  population will be to increase the effective concentration of  $J \neq 0$  molecules, increasing the reorientation rate  $\omega_{\text{rot}}$  and  $T_1$ . The magnitude of this change will depend upon the  $J=2$  lifetime compared to the characteristic time for  $\Delta m_J$  transitions. For example if the  $J=2$  lifetime is short, mutual  $\Delta m_J$  transitions between a  $J=2$  and a  $J=1$  will be interrupted. In the limit of very short  $J=2$  lifetimes, the  $J=2$  population will have no effect upon the dynamics of the  $J=1$  molecules. Since no calculations of these effects are available, we can only alert the reader to the uncertainties in the above analysis leading to  $T_1 \propto \rho^{5/3}$ . On the other hand, at 150 K only 14% of the para-H<sub>2</sub> are  $J=2$ , so the effect upon  $T_1$  should be small. The good fit in Fig. 8 to the  $\rho^{5/3}$  dependence is an indication that the total influence of higher  $J$  states is not substantial.

At sufficiently high densities, the anisotropic parts of molecular attraction and repulsion should become important. Only at large separations is the EQQ with its  $r^{-5}$  dependence the dominant anisotropic interaction. The  $\rho^{5/3}$  dependence of the rotational  $T_1$  indicates that EQQ dominates even at  $\rho/\rho_0=3$ . We note previous work indicated that EQQ is the main anisotropic interaction in H<sub>2</sub> up to relative densities of 1.56 (Ref. 43) and 1.7.<sup>46</sup> A phase transition was observed at 77 K and 1450 kbar;<sup>47</sup> it was interpreted as the hcp-Pa3 orientational ordering transition at relative density 8. The transition temperature scaled as  $\rho^{5/3}$  from low-density data, suggesting that EQQ interactions dominate even at this very high density. Recently the temperature and ortho-concentration dependences of the transition pressure have been mea-

sured<sup>38</sup> and are in disagreement with the interpretation of the transition as orientational ordering.

At low concentrations of ortho-H<sub>2</sub>, a phonon-rotation coupling was observed for H<sub>2</sub> in Ne, Ar, and Kr as well as in para-H<sub>2</sub> host.<sup>49</sup> This coupling causes a phonon-induced reorientation rate  $\Gamma_{\text{ph}}$ . The temperature dependence of  $\Gamma_{\text{ph}}$  ( $T^2$  at high temperatures and  $T^7$  at low temperatures) indicates a two-phonon Raman process. A  $T^2$  extrapolation of the H<sub>2</sub> in argon data yields an expected  $\Gamma_{\text{ph}}=1.8 \times 10^{11} \text{ s}^{-1}$  at 300 K. (The H<sub>2</sub> in argon data are more complete than the H<sub>2</sub> in para-H<sub>2</sub> data, but are approximately equal where they overlap. Of course, the H<sub>2</sub> host in the present work has been stiffened by pressure, so the value of  $\Gamma_{\text{ph}}$  is only an estimate.) The observed  $T_{1\text{rot}}$  at 62 kbar of 1.8 s can be used to estimate the total (from all sources) rate  $\omega_{\text{rot}}$  of molecular reorientation. Using Fedders' language,  $\omega_{\text{rot}}$  equals  $\Gamma_2$ ; assuming the cubic symmetry case, we have<sup>50</sup>

$$T_1^{-1} = 18.1 \omega_d^2 / \omega_{\text{rot}} \quad (7)$$

Using Fedders' numerical values,  $\Gamma_2$  is given by

$$\omega_{\text{rot}} = 2.37 T_1 \times 10^{12} \text{ s}^{-1}, \quad (8)$$

where  $T_1$  is in seconds. Thus at 62 kbar the reorientation rate  $\omega_{\text{rot}}=4.3 \times 10^{12} \text{ s}^{-1}$ . This is considerably larger than the estimated phonon contribution. Thus the observed independence of  $T_{1\text{rot}}$  upon temperature is explained.

#### IV. CONCLUSIONS

We have presented proton NMR data on molecular self-diffusion and reorientation in solid H<sub>2</sub> at diamond anvil cell pressures. The activation enthalpy  $\Delta H$  of diffusion increases with pressure, yielding an activation volume of  $5.7 \pm 0.6 \text{ cm}^3/\text{mol}$ . This volume is 63% of the molar volume, a reasonable value for the monovacancy diffusion mechanism. The variation of  $\Delta H/kT_{\text{melt}}$  with density is slow and smooth, suggesting that a single mechanism controls diffusion over the range  $\rho/\rho_0=1$  to 3. The spin-lattice relaxation time  $T_1$  arising from molecular reorientation is independent of temperature and varies as  $\rho^{5/3}$ . This indicates that the EQQ interaction dominates molecular reorientation ( $\Delta m_J$  transitions) over the range  $\rho/\rho_0=1$  to 3. Other anisotropic molecular interactions of shorter range as well as coupling to the phonons are not effective.

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