Site Occupancy of the PbWO₄: Co and PbMoO₄: Co Systems

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In a previous investigation of Co-doped PbWO4 and PbMoO4, the EPR data were attributed to Co^{2+} ions occupying tetrahedral W (or Mo) sites of S₄ symmetry. Several years ago, Blasse proposed that the interstitial octahedral sites in scheelites could be occupied by U^{6+} ions. After reexamination of the g value and hyperfine-structure (hfs) data and from the 2D estimates, the case for interstitial site occupancy by Co^{2*} in these two scheelites can be made plausible. Although they are not conclusive, the optical data are compatible with this assignment.

In a previous EPR investigation of Co-doped PbWO₄, two of us (M. -C. Chen and J. O. Artman)¹ found this system to be characterized by an effective spin S of $\frac{1}{2}$ and the following spin-Hamiltonian parameters: $g_i = 4.50, 6.20, 2.07; |A_i| = 605,$ 970, 248 MHz (i = x, y, z); $I = \frac{7}{2}$. The resonance evidently occurred in a ground doublet state; in addition it was not observable at temperatures above 20 K. A 2D value of 83 cm^{-1} was estimated from spin-lattice relaxation data. This D value was larger than those previously reported for Co²⁺ in tetrahedral sites; the hfs parameters were unusually large also. Nevertheless we attributed the EPR to Co^{2*} occupying tetrahedral fourfold coordinated W sites of S_4 symmetry. This assignment was influenced in part by some optical-absorption spectra available to us which consisted of a band at 16130 cm^{-1} and three weaker bands at 15150, 18180, and $19\,230\,\mathrm{cm}^{-1}$; we associated these sequentially with the ${}^{4}A_{2} - {}^{4}T_{1}$ (⁴P) and the ${}^{4}A_{2} - {}^{2}E({}^{2}G), {}^{4}A_{2} - {}^{2}T_{1}({}^{2}G)$ absorptions expected for Co²⁺ in a tetrahedral scheelite site. Correspondences with the results of extensive optical observations on Co-doped garnets² were also made.

Recently one of us (J.C.M.H.) proposed, as an alternative explanation, that these EPR data were due to Co²⁺ occupying sites of octahedral symmetry. Although interstitial octahedral sites occur in scheelites (of which $PbWO_4$ and $PbMoO_4$ are two examples) it has generally been assumed that 3d, 4f, and 5f dopants occupy the divalent metal site (or possibly the hexavalent metal site) substitutionally. However Blasse,³ in an article on the fluorescence of uranium-activated compounds, proposed that U^{6+} ions in scheelites could occupy the

interstitial octahedral sites. The nominal centers of these sites are situated midway between each pair of next-nearest W (or Mo) neighbors. The symmetry of the six nearest oxygens corresponds to a highly distorted octahedron; odd components would be expected in the crystal-field expansion.

Qualitative indications in favor of octahedralsite occupation are the large g and A anisotropies and the extremely large value of the zero-field splitting; these would seem to be incompatible with an orbital singlet ground state. Moreover, one of the g-tensor principal axes should be along the tetragonal crystal axis if Co²⁺ occupied a W site substitutionally without further reduction in symmetry. The absence of any simple geometrical relation between the g tensor and the crystal axes makes an assignment to a substitutional site somewhat unplausible.

The argument may be made more quantitative by examining the relations between the g and A components within the framework of the Abragam-Pryce theory.^{4,5} For the octahedral case we have

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$$g_{x} = \frac{1}{3} (10 + 4a - 4r) + k(1 + a - r) \equiv (g_{s} + kg_{1}^{0})_{x} ,$$

$$g_{y} = \frac{1}{3} (10 + 4a + 4r) + k(1 + a + r) \equiv (g_{s} + kg_{1}^{0})_{y} ,$$

$$g_{z} = \frac{1}{3} (10 - 8a) + k(1 - 2a) \equiv (g_{s} + kg_{1}^{0})_{z} ,$$

where k is the orbital reduction factor and a and rare measures of the axial and rhombic fields, respectively:

$$a = 16A_{2}^{0} \langle r^{2} \rangle / 315\lambda, \quad r = -4A_{2}^{2} \langle r^{2} \rangle / 315\lambda$$

In this formalism we disregard all of the levels of the ${}^{4}F$ term except those of the ground orbital triplet ${}^{4}T_{1}$. The ${}^{4}T_{1}$ splittings due to spin-orbit

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coupling $\lambda \mathbf{L} \cdot \mathbf{S}$, orthorhombic crystal field, and Zeeman energy are calculated under the assumptions $A_4^m = 0$ and $\lambda \gg A_2^0$, A_2^2 . The hfs components are related to the g values through the formulas $A_i = P$ $(g_{ii}^0 - \frac{1}{2} \kappa g_{si})$, where P is a measure of $\langle r^{-3} \rangle$ and κ gives the unpaired s-electron admixture. We use values of P and κ identical to those found in hydrated Co salts, ⁴ 675 MHz and 0.325, respectively.

For the tetrahedral case the ground state is an orbital singlet ${}^{4}A_{2}$; we have simply $A_{i} = P[(g_{i} - 2) - \kappa]$, where the g_{i} refer to the "intrinsic" g values of the ${}^{4}A_{2}$ multiplet. (These intrinsic g values were found to be¹ 2.82, 2.52, and 2.10, respectively.) In this case the orbital contribution P(g - 2) and the core polarization P_{κ} tend to compensate; we therefore expect lower hfs values for the tetrahedral case.

If we assume that the Co^{2*} ion is situated on an octahedral site, we find k = 0.92, a = 0.485, r = 0.378, and A_i values of 366, 765, and -205 MHz, respectively. On the other hand if the Co^{2*} ion is assumed to be on a tetrahedral site, we have $A_i = 334$, 132, and -152 MHz. We see that the A_i values calculated on the basis of octahedral-site occupancy appear to be the more reasonable ones. (The EPR experiments do not distinguish between positive and negative A_i values.) For octahedrally coordinated Co²⁺, Gladney⁶ has reported the following parameters in the MgF₂:Co²⁺ case: $g_i = 6.03$, 2.30, 4.24; $A_i = 637$, 123, 210 MHz. Gladney⁶ cites similar data for $\operatorname{Zn} F_2$: Co^{2*} , $\operatorname{Ti}O_2$: Co^{2*} , and $\operatorname{Na} F$: Co^{2*} . For octahedral Co^{2+} in YGaG, g_{\parallel} and g_{\perp} values of 7.027 and 2.665, respectively, were reported.⁷ The hfs constants |A| and |B| were 922 and 45 MHz, respectively. Such values indeed are comparable to our data.

As we had mentioned earlier, our estimated 2D value of 83 cm^{-1} is unusually large for tetrahedrally coordinated Co²⁺ (${}^{4}A_{2}$ ground state). A recent EPR study⁷ of tetrahedrally coordinated Co²⁺ in YGaG did yield a 2D value of -36 cm^{-1} , g_{\parallel} and g_{\perp} values of 2.42 and 2.19, respectively, and hfs constants less than 120 MHz in value. Tetrahedral site Co²⁺ 2D values of $-8.60 \text{ and} -10.7 \text{ cm}^{-1}$ have been reported in CoCs₃Cl₅ and CoCs₃Br₅, respectively.⁸ The g values cited were about 2.4, the hfs constants did not exceed 100 MHz.⁹

Clearly, from the aspect of the hfs splittings the data for tetrahedral Co^{2*} (Refs. 7-9) do not correspond too well to ours. (It should also be noted

that the EPR spectra for tetrahedral Co^{2*} were all observable at temperatures up to 77 K at least.) On the other hand, fluorescence studies in the octahedral MgF: Co^{2*} system¹⁰ have indicated that the lowest excited state is 152 cm⁻¹ above the ground state, which is not too far from our estimate of 83 cm⁻¹.

Evidence for site occupancy from the gross features of the PbWO₄: Co optical-absorption data is still incomplete. Judging from Refs. 2, 7, 11, and 12 we would expect in the tetrahedral Co^{2+} case to see ${}^{4}A_{2}({}^{4}F) - {}^{4}T_{2}({}^{4}F)$, ${}^{4}T_{1}({}^{4}F)$, ${}^{4}T_{1}({}^{4}P)$ at 4500, 7000, 16 000 cm⁻¹, respectively. (The ${}^{4}A_{2} - {}^{4}T_{2}$ absorption would be relatively weak.) In the octahedral Co^{2*} case, we would expect (Refs. 2, 13, 14) to see ${}^{4}T_{1}({}^{4}F) - {}^{4}T_{2}({}^{4}F)$, ${}^{4}A_{2}({}^{4}F)$, ${}^{4}T_{1}({}^{4}P)$ at 7500, 18000, and 20000 cm^{-1} , respectively. (The ${}^{4}T_{1} \rightarrow {}^{4}A_{2}$ transition is relatively weak.) We had previously reported¹ observation of a band at 16130 cm⁻¹. Upon reexamination at room and liquidnitrogen temperatures of some Co-doped PbWO₄ and $PbMoO_4$ samples, we have found an additional band centered at 4400 cm⁻¹. No absorption was found in the $7000 - \text{cm}^{-1}$ region.

The band at 16130 cm^{-1} can be attributed equally well to ${}^{4}T_{1}({}^{4}F) \rightarrow {}^{4}T_{1}({}^{4}P)$ of octahedral Co²⁺ or, as was done in our earlier work, ¹ to ${}^{4}A_{2}({}^{4}F) \rightarrow {}^{4}T_{1}({}^{4}P)$ of tetrahedral Co²⁺. The absence of any absorption in the 7000-cm⁻¹ region, however, suggests assignment of the relatively strong 4400-cm⁻¹ band to the ${}^{4}T_{1}({}^{4}F) \rightarrow {}^{4}T_{2}({}^{4}F)$ transition of octahedrally coordinated Co²⁺. Our spectra closely resemble those of $CoWO_4$, ¹³ in which Co^{2*} occupies a significantly distorted octahedral site with symmetry C_2 . The value of Dq may be obtained by comparing our spectral data with the crystal-field calculations of Ferguson, Wood, and Knox.¹³ We find a Dq value of $500 \pm 50 \text{ cm}^{-1}$. This Dq value represents a reduction of about 35% from those commonly listed¹³ for Co²⁺ at regular octahedral sites. This may not be astonishing when we remember that this scheelite interstitial site has two positively charged W⁴⁺ (Mo⁴⁺) ions nearby.

In summary, from examination of the g value and hfs data and from the 2D estimates, the case for interstitial octahedral-site occupancy for the $PbWO_4:Co^{2*}$ and $PbMoO_4:Co^{2*}$ systems can be made plausible. Although they are not conclusive, the optical data are compatible with this assignment.

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Electron-Phonon Interaction in Transition Metals

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We point out that an expression for the electron-phonon matrix element in transition metals recently derived by Barisic, Labbé, and Friedel from a "Hubbard-Hamiltonian" formulation, and of particular interest in understanding the superconducting properties of these materials, follows from the more basic "modified-tight-binding" approximation of Fröhlich and Mitra.

In a recent publication Barisic, Labbé, and Friedel¹ have indicated that the order of magnitude of the electron-phonon interaction required to explain the superconducting properties of transition metals can be obtained by considering the electronphonon coupling between *d*-band states. Barisic et al. have used a Hubbard-Hamiltonian formulation in which the electron-phonon coupling arises from the dependence on interatomic distance of a "hopping" or overlap integral as encountered in tight-binding band theory. Here we wish to point out that their expression for the electron-phonon interaction is not limited to the Hubbard-Hamiltonian model, but rather follows from the assumption that the electron wave function rigidly follows the motion of the ions, an assumption in the spirit of the tight-binding approximation. In particular, their result for the electron-phonon matrix element can be rederived by considering instead the matrix elements of the electron-phonon operator between modified-tight-binding wave functions as introduced by Fröhlich² and used by Mitra.³

Fröhlich's assumption is that the tight-binding wave function corresponding to the ions in staticdisplaced positions a distance \vec{X}_{μ} from their equilibrium-lattice positions \vec{R}_{μ} can be written in a modified-tight-binding form

$$\psi(\mathbf{\vec{r}}) = \sum_{\mu} e^{i\mathbf{\vec{k}}\cdot\mathbf{\vec{R}}_{\boldsymbol{u}}} \phi(\mathbf{\vec{r}}-\mathbf{\vec{R}}_{\mu}-\mathbf{\vec{X}}_{\mu}), \qquad (1)$$

where $\phi(\vec{r})$ is the localized orbital from which the tight-binding band arises. Using the Born-Oppen-heimer formulation of the electron-phonon interaction leads to the electron-phonon matrix element [Eq. (2.18) of Ref. 3]

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$$g_{kq}^{\nu} = M_1 + M_2 , \qquad (2)$$

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where

$$M_{2} = i \left(\frac{\hbar}{2MN\omega_{qv}^{0}}\right)^{1/2} \times \vec{\epsilon}_{q}^{v} \cdot \sum_{n} \nabla J(\vec{u}) \left[\sin\vec{k}\cdot\vec{u} - \sin(\vec{k}+\vec{q})\cdot\vec{u}\right]$$
(3)

in the notation of Ref. 1. Here M_1 involves degenerate three-center integrals, ignored by Barisic *et al.* (We note that these terms are not obviously negligible, since in the Garland-Bennemann⁴ theory of the electron-phonon interaction they yield the principal contribution, although it should be noted that the latter have employed the Bloch rather than the Born-Oppenheimer viewpoint.)

Applying Eq. (3) to the case considered by Barisic *et al.*, in which the near-neighbor environment is orthorhombic, and using the expression of Ref. 1 for ∇J , we obtain

$$g_{kq}^{\nu} \cong M_{2} = 2iq_{0} \left(\frac{\hbar}{2NM\omega_{q\nu}^{0}}\right)^{1/2} \times \sum_{\alpha} J(\bar{a}_{\alpha}) \frac{\bar{a}_{\alpha} \cdot \bar{\epsilon}_{q}^{\nu}}{a_{\alpha}} \left[\sin k_{\alpha}a_{\alpha} - \sin(\bar{k} + \bar{q})_{\alpha}a_{\alpha}\right],$$
(4)

which is just the result of Barisic *et al.* [see Eq. (6) of Ref. 1].

In conclusion we note that this more basic foundation for the electron-phonon matrix element to some extent reinforces the validity of the Barisic *et al.* calculation, and also indicates clearly its extension to a more realistic, degenerate *d*-band case.

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