# Temperature dependence of the phase diagram of C1/Ag(100)

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Using low-energy electron diffraction, we have determined the coverage at which overlayers of Cl adsorbed on Ag(100) order into a  $c(2\times 2)$  structure for sample temperatures ranging from 300 to 500 K. We find no evidence for a variation in the critical coverage  $\theta_c$  over this temperature range. However, experimental uncertainties in the values of  $\theta_c$  are too large to rule out the small variation predicted by an interacting-hard-square model with only next-nearest-neighbor repulsions. We find that the addition of modest third-neighbor repulsions to the model improves agreement of transfer-matrix scaling calculations with experimental measurements.

## **INTRODUCTION**

The interactions between chemisorbed surface atoms are clearly important to the understanding of many surface processes. In general, however, there is no reliable method for predicting these interactions. It is therefore desirable to determine the adatom-adatom interactions for as many systems as possible, with the hope of exposing underlying principles. Rather perversely, even though adatom-adatom interactions profoundly affect many surface processes, they are generally weak compared to adatom-substrate interactions, and are, therefore, difficult to quantify experimentally. One approach to estimating the interactions is to compare measured phase diagrams with model (lattice-gas) phase diagrams. The goal of this work is to measure the high-temperature phase boundary separating the  $c(2 \times 2)$  phase of Cl/Ag(100) from the disordered phase and to estimate from this the Cl-Cl interaction energies, or at least specify a model which gives a consistent phase diagram.

Cl/Ag(100) has been studied by many groups.<sup>1-4</sup> Chlorine molecules dissociate upon chemisorption and the only ordered structure seen is a  $c(2\times 2)$  overlayer. The Cl atoms are believed to form a simple overlayer: A controversy about the geometry of the  $c(2\times 2)$  structure has been recently resolved.<sup>4</sup> Figure 1 shows this structure and



FIG. 1. A schematic picture of the  $c(2\times 2)$  structure of Cl adsorbed on Ag(100) with relevant lattice-gas-model interactions. In this work,  $E_1$  is taken as infinitely repulsive.

relevant Cl-Cl interactions within a lattice-gas model.

Assuming the Cl Auger signal to be directly proportional to Cl coverage, which should be a good approximation at submonolayer quantities, a linear increase in coverage with exposure to Cl<sub>2</sub> up to a well-defined saturation coverage was observed. The work function of the surface also increased linearly with Cl coverage above  $\theta \cong 0.01$  monolayers (ML). The intensities of low-energy electrondiffraction features due to the  $c(2 \times 2)$  phase also reach a maximum at the saturation coverage. As the temperature of the saturated surface was raised. Cl began to desorb before the  $c(2 \times 2)$  phase disordered. These observations suggest that only one type of binding site is occupied, so that the system can be modeled by a square lattice gas, and that the saturation coverage is 0.5 ML; that is, that the nearest-neighbor interaction energy  $E_1$  is effectively infinitely repulsive and the Cl atoms act as hard squares in blocking out neighboring sites.

A number of other chemisorbed systems on square surfaces exhibit  $c(2\times 2)$  structures at 0.5 ML; the phase diagrams of several systems have been studied: Se/Ni(100) (Ref. 5); O/Ni(100) (Ref. 6); and O/Pd(100).<sup>7</sup> In addition to the  $c(2\times 2)$  phase at coverages near 0.5 ML, these systems have a  $p(2\times 2)$  phase at coverages near 0.25 ML. This is not surprising as further neighbor interactions can naturally stabilize lower coverage phases: third-neighbor attractions<sup>8</sup> or fourth-neighbor repulsions<sup>5</sup> can create a  $p(2\times 2)$  phase. No low-coverage phase is seen for Cl/ Ag(100), however, even for temperatures as low as 90 K. As we will discuss later in this paper, the absence of other phases at low coverages places restrictions on the values of the interaction energies consistent with experiment.

The  $c(2\times 2)$  phase of Cl/Ag(100) appears only after the coverage has reached a particular critical value  $\theta_c$ . Taylor *et al.*<sup>1</sup> studied this order-disorder phase transition at 300 K. They estimated  $\theta_c$  to be  $0.394 \pm 0.007$  ML. If there were *only* first-neighbor exclusions, that is, if the system were equivalent to the much studied hard-square model, the value of  $\theta_c$  would be approximately 0.368 ML (Ref. 9) and it would be independent of temperature. It was found that the experimental value of  $\theta_c$  could be accounted for by assuming the presence of a secondneighbor repulsion of between 20 and 26 meV. If this model is correct, the phase boundary should exhibit some temperature dependence, with  $\theta_c$  varying from 0.388 ML

(1/2,1/2) intensity (arb. units)

at room temperature to 0.381 ML at 600 K for  $E_2=24$  meV. Smaller values of  $E_2$  would result in a weaker temperature dependence and smaller values of  $\theta_c$ . In this paper we report on measurements which test this prediction. We find no statistically significant evidence for a temperature variation in the phase boundary. To try to account for our observations, we introduce a third-neighbor repulsion. We emphasize at the outset that such an intricate interpretation of the experiment neglects many effects which could plausibly be present. For example, we neglect finite-size-induced shifts in the estimated  $\theta_c$  caused by the limitation of the size of the correlation length due to the finite distance between quenched defects, we ignore effects caused by the presence of impurities, and we do not consider effects of longer ranged interactions.

#### **EXPERIMENT**

Experiments were performed in a standard stainlesssteel UHV bell jar equipped with hemispherical retarding field LEED (low-energy electron diffraction)/Auger optics, a quadrupole mass spectrometer, and an Ar<sup>+</sup> sputtering gun. The base pressures were less than  $10^{-10}$  Torr. Cl<sub>2</sub> was admitted through a variable leak valve and the pressure measured with an ion gauge near the leak valve. The Cl<sub>2</sub> pressure at the sample was lower than measured at the ion gauge due to the pumping of the reactive Cl<sub>2</sub> by the chamber walls. The Ag(100) sample cleaning and preparation has been reported previously.<sup>1</sup> The sample was mounted on a resistive heater and temperature was monitored to within 5 K by a chromel-constantan thermocouple embedded in the sample.

LEED beam intensities were measured with a spot photometer consisting of a camera lens focusing the desired beam onto a small aperture located in front of a photomultiplier tube. To avoid distortions due to the heater current, the electron beam and heater current were chopped on alternate cycles at 170 Hz during measurement. Changes in the work function were measured using the diode method<sup>10</sup> using the electron gun in the LEED optics. A simple electronic feedback loop was used to monitor the work function change continuously during Cl<sub>2</sub> exposure. Shifts in work function could be measured with a resolution of 20 meV.

#### RESULTS

The critical coverage was determined from the intensity of the (1/2,1/2) beam of the chlorine  $c(2\times 2)$  LEED pattern at 65 eV as a function of Cl<sub>2</sub> exposure. To convert the measured exposures to absolute coverages, we made use of the constant sticking coefficient below saturation.<sup>1</sup> The measurements were begun at a coverage of around 0.25 ML as measured using Auger-electron spectroscopy (AES). The sample was then exposed to Cl<sub>2</sub> at a pressure of approximately  $2\times 10^{-9}$  Torr held constant to about 1%. The intensity was measured as a function of time and the exposure was ended at a coverage of about 0.45 ML. The final coverage was then measured precisely using AES. The coverages were interpolated from the measured

0.25 0.30 0.35 0.40 0.45 coverage (ML) FIG. 2. Sample plot of half-order diffracted intensity vs coverage. The method of coverage calibration is described in the text. The critical coverage is estimated from the point of inflection of this curve.

initial and final values resulting in traces of intensity versus coverage as shown in Fig. 2. The precision of the coverage measurement was determined from repeated measurements of the Auger signal to be  $\pm 0.007$  ML. The critical coverage was determined from the inflection point of the variation of intensity with coverage.<sup>11</sup> The inflection point was determined by numerically calculating the first derivative of the *I*- $\theta$  curve. The uncertainty in determination of the inflection point was much less than the uncertainty in the coverage measurements. Similar measurements were repeated for several temperatures between 300 K and 570 K in order to construct the temperature-dependent phase boundary shown in Fig. 3.

In making the coverage calibration we assumed that the sticking coefficient remains coverage independent at higher adsorption temperatures. To confirm this we measured the work-function shift, which is linear with coverage at room temperature, as a function of exposure.<sup>1</sup> We

600



FIG. 3. Experimental phase diagram (points) compared to model hard-square lattice-gas phase diagrams:  $E_2=24$  meV and  $E_3=0$  (dashed line), and  $E_2=23$  meV and  $E_3=3.5$  meV (solid line).



do not expect the work function to be temperature dependent. At the highest temperature measured, 620 K, deviations from linearity occur only above 0.475 ML, well above the maximum coverage used for calibration.

#### DISCUSSION

In using the experimentally determined phase diagram to deduce values for the adatom interaction, it is crucial that the measured values of the coverage be accurate. We have estimated the precision of the coverage measurements to be  $\pm 0.007$  ML. However, it is also necessary to consider the possible effect of any systematic error on the accuracy of the measurement. We feel the most obvious source of systematic error to be adsorption of Cl into defect sites. Three cases are possible: (1) the ordered  $c(2\times 2)$  structure may fill first, followed by the defect sites; (2) the  $c(2\times 2)$  and defect sites may fill simultaneously; and (3) the defect sites may fill first, followed by the  $c(2\times 2)$  sites.

In the first case, the measured coverage would be lower than the true value in the ordered regions. However, the LEED intensity would also reach its maximum before the AES intensity, which is not observed. Therefore, we can rule out this case. In the second case, the total surface coverage would be greater than one half a monolayer, but the local coverage in the ordered regions would agree with the measured value. In the third case, the measured values would be larger than the true coverage in the ordered regions. The small nonlinearity observed in the change in work function with coverage<sup>1</sup> at small coverages allows us to estimate the maximum value of this effect to be  $\sim 0.01$  ML. Therefore, if there is a systematic error in the coverage calibration, the measured values are larger than the true value by at most 0.01 ML.

Figure 3 compares two model phase diagrams with experiment. The dashed line shows the diagram for the hard square model with only second-neighbor repulsions with  $E_2$  chosen equal to 24 meV. This value gives the best agreement with experiment: Making  $E_2$  larger does shift the critical coverages to higher values<sup>12</sup> but at the expense of causing a (2×1) phase, which occurs around 1/4 of a monolayer,<sup>12</sup> to appear at temperatures above 90 K, which is not observed.<sup>1</sup> The accuracy of the transfermatrix scaling calculation, which produced this phase diagram,<sup>12</sup> is probably better than the resolution of Fig. 3. This model phase diagram is not grossly inconsistent with experiment. However, if one neglects the possibility of systematic error in the absolute coverage calibration, the model does tend to underestimate  $\theta_c$ .

This small discrepancy can be repaired by introducing a small repulsive  $E_3$ . The solid line in Fig. 3 shows our estimate of the phase diagram for  $E_2=23$  meV and  $E_3=3.5$  meV. This phase diagram was computed in essentially the same manner as in Ref. 12; exact information from semiinfinite strips of sites was extrapolated to the infinite system limit. However, because of the larger range of the interactions smaller strip widths were used. The curve for nonzero  $E_3$  was constructed by extrapolating results<sup>13</sup> from strips 4, 6, 8, and 10 sites wide. By studying the ac-

curacy of the calculation for  $E_2 = 0$  for these widths we estimate the accuracy of the critical coverages to be approximately 0.001.13 Unfortunately it is much more difficult to generate accurately the low coverage parts of the phase diagram when  $E_3$  is nonzero. For even quite large positive values of  $E_3$  (0.25 $E_2$ ), transfer-matrix scaling yields a high-temperature part of the low coverage phase diagram which is very similar to the case  $E_3 = 0$ :<sup>12</sup> There is a narrow (2×1) phase between 0.24 and 0.26 ML. The maximum transition temperature is difficult to determine, however. For example, for the interaction set of Fig. 3, comparison of strips of width 4 and 6 give a maximum 2×1 transition temperature of 74 K, 4 and 8 give 70 K, but 6 and 8 give 63 K: There is no sign of convergence. We also searched for a low-temperature  $c(4 \times 2)$  phase which should occur when  $E_3$  is repulsive. There is no sign of this phase above T = 20 K. By performing Monte Carlo simulations for the two models on  $24 \times 24$  lattices (being careful that averages were independent of starting configurations, which required waiting on the order of 10<sup>4</sup> Monte Carlo steps per site for equilibration) we established that there was also no significant short-range  $(2 \times 1)$  order at 90 K, so that both the interaction sets are consistent with experimental observations at low T. Because of metastability problems, however, the Monte Carlo calculations were unable to provide equilibrium properties much below 90 K.

A natural question now is "Can one place meaningful restrictions on the values of  $E_3$  and  $E_2$  consistent with the experimental phase diagram?" The answer turns out to depend critically on the size of the errors in the phase diagram. Figure 4 (solid line) shows the allowed values of  $E_2$  and  $E_3$  if one interprets the experimental data in Figure 3



FIG. 4. Values of  $E_2$  and  $E_3$  which are consistent with the experimental phase diagram: Assuming the phase boundary is between 0.387 and 0.401 ML between 300 and 600 K gives the region enclosed by the solid line; and assuming it is between 0.386 and 0.401 ML gives the region determined by the dashed line.

as requiring the phase boundary to lie between 0.387 and 0.401 ML in the temperature range 300 to 600 K. The requirement that there be no low coverage phase above 90 K (Ref. 14) restricts the system to be beneath the line with positive slope. The allowed range of  $E_2$  and  $E_3$  is rather small: Smaller values of  $E_3$  are ruled out because of the appearance of  $(2 \times 1)$  order, larger values are not allowed because then the model phase diagrams fall outside of the specified coverage range. If, however, one changes the allowed coverage range by just 0.001 ML so that coverages from 0.386 to 0.401 are allowed, the range of allowed values of  $E_2$  and  $E_3$  increases dramatically (dashed lines in Fig. 4; note that the accuracy of the finite-size scaling calculation is not negligible here). So, even ignoring other complications, as discussed in the Introduction, not a lot can be quantitatively said about the sizes of  $E_2$  and  $E_3$ , given the ambiguities in interpreting the experimental uncertainty in the phase boundary. Given Fig. 4, however, it seems reasonable to say that  $E_2$  is on the order of 10 meV and  $E_3$  is less than 10 meV.

In contrast, if we take into account the possibility of systematic error in the coverage calibration, then the observed phase diagram can be explained without recourse to a third-neighbor interaction. The average value of  $\theta_c$  measured between 300 and 600 K is 0.391 ML. If we assume this is too large by 0.01 ML due to systematic error, then the true value would be 0.381 ML. With this value of  $\theta_c$ , the phase diagram could be explained with an interaction set of  $E_2 \cong 15$  meV and  $E_3 = 0$ . This results in a temperature variation of  $\theta_c$  of only 0.006 ML between

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300 and 600 K, which is in better agreement with the data. It also suppresses the formation temperature of the  $(2 \times 1)$  phase to  $\sim 50$  K, well below the lowest temperature of observation.

### CONCLUSION

We have presented the temperature dependence of the phase diagram for  $c(2\times 2)$  Cl/Ag(100), and have shown that there is no difficulty in interpreting the results in terms of an interacting-hard-square lattice-gas model. Unfortunately, the featurelessness of the phase diagram and uncertainties in the coverage calibration do not allow us to unambiguously determine the Cl-Cl interaction energies beyond the observation that values of the repulsive interaction  $E_2$  on the order of 10 meV and values of  $E_3$ less than 10 meV are consistent with the experimental phase diagram. To determine the interactions more accurately, or to test the model more fully, one needs an even more accurate determination of the phase boundary or observations of the predicted low-T phases.

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- <sup>13</sup>As an example of the convergence we list the results for  $E_2 = 1$ ,  $E_3 = 0.15$ , and T = 1.0: comparing strips of width 4 and 6 gave  $\theta_c = 0.40275$ ; 6 and 8 gave  $\theta_c = 0.40233$ ; and 8 and 10 gave  $\theta_c = 0.40210$ . Extrapolating these values in the standard way by a power-law fit gives the final estimate of  $\theta_c$  as 0.4014. For comparison the sequence of estimates for the case  $E_2 = E_3 = 0$  for the same strip widths is 0.36939, 0.36839, and 0.36807 which extrapolates to 0.3678. This compares with the estimate of 0.367743(1) using strip widths up to 22 (see Ref. 9).
- <sup>14</sup>The estimate of the maximum transition temperature of the  $(2 \times 1)$  phase was taken from the comparison of strip widths 4 and 6: This comparison gave higher estimates of the transition temperature than those using strips of width 6 and 8, and 10 and 12, as described in the text.



FIG. 1. A schematic picture of the  $c(2\times 2)$  structure of Cl adsorbed on Ag(100) with relevant lattice-gas-model interactions. In this work,  $E_1$  is taken as infinitely repulsive.