

## Long-range magnetic ordering in the high- $T_c$ superconductors $RBa_2Cu_3O_{7-\delta}$ ( $R = Nd, Sm, Gd, Dy, \text{ and } Er$ )

B. W. Lee, J. M. Ferreira,\* Y. Dalichaouch, M. S. Torikachvili,  
K. N. Yang, and M. B. Maple

*Department of Physics and Institute for Pure and Applied Physical Sciences,  
University of California, San Diego, La Jolla, California 92093*

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Low-temperature specific-heat  $C$  measurements have been made on the high- $T_c$  superconductors  $RBa_2Cu_3O_{7-\delta}$  ( $R = Nd, Sm, Gd, Dy, \text{ and } Er; \delta \approx 0.1$ ) for  $0.5 \lesssim T \lesssim 30$  K. Features in the specific heat associated with magnetic ordering of the trivalent  $R$  ions were observed for all of these compounds. The values of the magnetic ordering temperature  $T_M$ , defined as the temperature of the peak of the specific-heat anomaly due to magnetic ordering, are 0.52, 0.61, 2.25, 0.90, and 0.60 K for the compounds with  $R = Nd, Sm, Gd, Dy, \text{ and } Er$ , respectively. Calculations of the magnetic entropy from the  $C$  vs  $T$  data suggest that the  $R$  ions in these compounds have doublet ground states, except for  $R = Gd$ , which has an eightfold degenerate ground state. The values of  $T_M$  for the compounds with  $R = Nd, Sm, Dy, \text{ and } Er$  are in reasonable agreement with the deGennes factor scaling of  $T_M$  for the compound with  $R = Gd$ . The deGennes factor scaling of  $T_M$  is consistent with expectations based on the Ruderman-Kittel-Kasuya-Yosida interaction, although the agreement may be fortuitous since recent specific-heat measurements by Dunlap *et al.* on metallic and semiconducting (oxygen-deficient)  $GdBa_2Cu_3O_{7-\delta}$  suggest that dipole-dipole interactions are responsible for the magnetic order in these materials.

### INTRODUCTION

Following the discovery of superconductivity with a critical temperature  $T_c \approx 90$  K in  $YBa_2Cu_3O_{7-\delta}$ ,<sup>1</sup> the series of rare-earth ( $R$ ) barium-copper-oxide compounds  $RBa_2Cu_3O_{7-\delta}$  were also found to exhibit superconductivity with  $T_c \approx 90$  K, except for the compound with  $R = La$  for which  $T_c \approx 56$  K and the compounds with  $R = Ce, Pr, \text{ and } Tb$ , which do not exhibit superconductivity above 4.2 K.<sup>2,3</sup> The superconducting  $RBa_2Cu_3O_{7-\delta}$  compounds are isomorphic to the prototype  $YBa_2Cu_3O_{7-\delta}$  compound which has an oxygen-deficient orthorhombic perovskite-type crystal structure, except for  $LaBa_2Cu_3O_{7-\delta}$ , which has a related tetragonal structure. Normal-state magnetic susceptibility measurements on these compounds of  $R$  elements with partially filled  $4f$  electron shells revealed a Curie-Weiss-type behavior with effective magnetic moments derived from the Curie constant in good agreement with free ion values, except for the compound of  $R = Eu$  which has a nonmagnetic  $J = 0$  ground state, as expected from Hund's rules for  $Eu^{3+}$  (Ref. 2). However, the  $T_c$ 's of the  $RBa_2Cu_3O_{7-\delta}$  compounds are independent of the  $R$  ion, which is surprising in view of the relatively strong effect of paramagnetic ions on the  $T_c$  of conventional superconductors.<sup>4</sup> This suggests that the exchange interaction between the magnetic moments of the  $R$  ions and the spins of the superconducting electrons is very weak, or alternatively, that the  $RBa_2Cu_3O_{7-\delta}$  compounds exhibit an unconventional type of superconductivity that is insensitive to the presence of localized magnetic moments.<sup>5</sup> As part of a detailed investigation of the series of  $RBa_2Cu_3O_{7-\delta}$  compounds, we have performed low-temperature specific-heat measurements on these materi-

als between  $\sim 0.5$  and 50 K. In a separate paper, we reported specific-heat data for compounds with  $R = Y, Eu, Ho, Tm, \text{ and } Yb$  which revealed the absence of magnetic ordering down to  $\sim 0.5$  K and the occurrence of electronic Schottky anomalies due to crystalline electric field (CEF) splitting of the energy levels of the  $R^{3+}$  ions,<sup>6</sup> although  $HoBa_2Cu_3O_{7-\delta}$  has been reported to exhibit magnetic ordering at  $\sim 0.17$  K.<sup>7</sup> In this paper, specific-heat data are presented for  $RBa_2Cu_3O_{7-\delta}$  compounds with  $R = Nd, Sm, Gd, Dy, \text{ and } Er$  which indicate that these compounds display magnetic ordering at temperatures of 0.52, 0.61, 2.25, 0.90, and 0.60 K, respectively. A brief account of the  $C(T)$  data for these compounds in the vicinity of the magnetic ordering temperatures  $T_M$  was recently given in an international conference.<sup>8</sup> In the process of preparing this manuscript, we received several preprints reporting evidence from low-temperature specific-heat measurements of magnetic ordering for  $RBa_2Cu_3O_{7-\delta}$  compounds with  $R = Sm,$ <sup>9</sup>  $Gd,$ <sup>9-15</sup>  $Dy,$ <sup>7,9,10,14</sup> and  $Er.$ <sup>7,10,14</sup>

### EXPERIMENTAL DETAILS

The method in which the samples were prepared can be found in previous reports.<sup>16</sup> Each sample has been characterized by means of powder x-ray diffraction, electrical resistivity,<sup>2</sup> and low-field magnetization measurements.<sup>16</sup> The powder x-ray diffraction patterns for each sample consisted predominantly of lines that could be indexed to the orthorhombic perovskite-type crystal structure of the prototype compound  $YBa_2Cu_3O_{7-\delta}$ . The electrical resistivity data for the  $RBa_2Cu_3O_{7-\delta}$  compounds studied in this work revealed superconducting transition

temperatures with  $T_c \approx 90$  K and transition widths  $\Delta T_c \lesssim 2$  K.<sup>2</sup> Low-field (10 Oe) magnetic susceptibility measurements in the superconducting state, reported elsewhere,<sup>16</sup> yielded magnetic susceptibilities  $\chi_m$  due to the Meissner effect and  $\chi_s$  associated with induced superconducting currents, respectively. The ratio of  $\chi_m/\chi_s$  is between 20% and 40% for each sample, while the value of  $\chi_s$  is very close to the theoretical value. The specific-heat measurements were performed in a <sup>3</sup>He semiadiabatic calorimeter at temperatures between  $\sim 0.5$  and 50 K using a standard heat pulse technique.

## RESULTS AND DISCUSSION

Specific-heat  $C$  versus temperature data for  $0.5 \lesssim T \lesssim 30$  K are shown in Fig. 1 for  $RBa_2Cu_3O_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, Dy}$ , and, for comparison, Y (indicated by the solid line) and in Fig. 3 for  $ErBa_2Cu_3O_{7-\delta}$ . The anomalies in  $C(T)$  due to magnetic ordering are shown in more detail in Fig. 2 for  $R = \text{Nd, Sm, Gd, and Dy}$  and in the inset of Fig. 3 for  $ErBa_2Cu_3O_{7-\delta}$ . The transition temperature  $T_M$  defined as the temperature of the peak in the specific-heat anomaly associated with magnetic order is  $0.522 \pm 0.005$  K for  $NdBa_2Cu_3O_{7-\delta}$ ,  $0.612 \pm 0.005$  K for  $SmBa_2Cu_3O_{7-\delta}$ ,  $2.25 \pm 0.03$  K for  $GdBa_2Cu_3O_{7-\delta}$ ,  $0.90 \pm 0.02$  K for  $DyBa_2Cu_3O_{7-\delta}$ , and  $0.599 \pm 0.003$  K for  $ErBa_2Cu_3O_{7-\delta}$ .

Distinct differences can be found between the magnetic specific-heat anomalies of the five compounds. The sharp specific-heat peak associated with the magnetic transition in  $NdBa_2Cu_3O_{7-\delta}$  is superimposed on a more rounded peak above  $T_M$ . The shapes of the specific-heat anomalies associated with the magnetic transition in the  $RBa_2Cu_3O_{7-\delta}$  compounds with  $R = \text{Sm, Dy, and Er}$  resemble those of  $RMo_6S_8$ ,  $RMo_6Se_8$ , and  $RRh_4B_4$  magnetic superconductors<sup>17</sup> in which the  $R$  ions exhibit antiferromagnetic order which coexists with superconductivity. Specific-heat measurements on  $GdBa_2Cu_3O_{7-\delta}$  (Ref. 15) and  $DyBa_2Cu_3O_{7-\delta}$  (Ref. 9) in applied magnetic fields are consistent with antiferromagnetic ordering of the  $R$  mo-

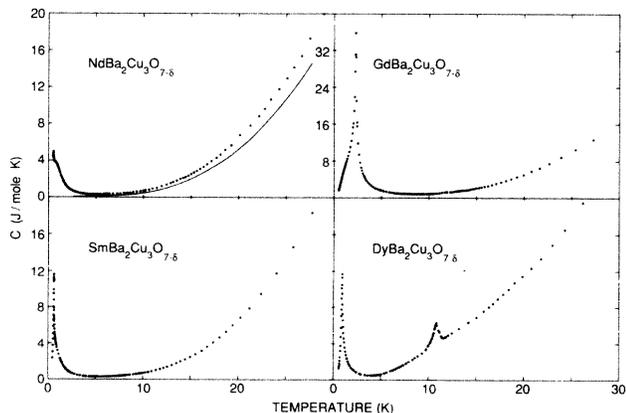


FIG. 1. Specific-heat  $C$  vs temperature for  $RBa_2Cu_3O_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, and Dy}$  for  $0.5 \lesssim T \lesssim 30$  K. The behavior of  $C(T)$  for  $YBa_2Cu_3O_{7-\delta}$  (solid line) is shown for comparison.

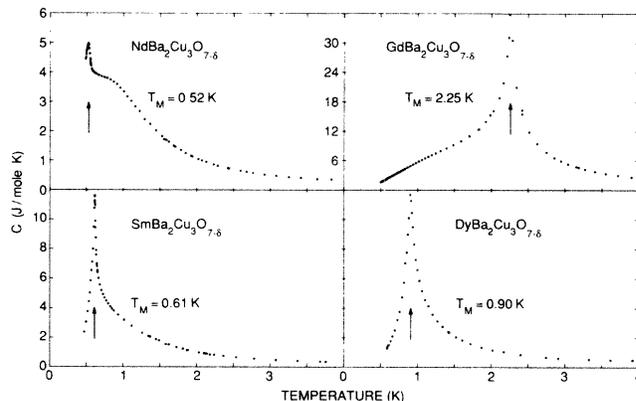


FIG. 2. Specific heat  $C$  vs temperature for  $RBa_2Cu_3O_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, and Dy}$  for  $0.5 \lesssim T \lesssim 4$  K.

ments in these compounds. Neutron scattering measurements have revealed  $c$ -axis antiferromagnetic ordering of the Gd (Ref. 18) and Dy (Ref. 19) moments in  $GdBa_2Cu_3O_{7-\delta}$  and  $DyBa_2Cu_3O_{7-\delta}$ , respectively, and  $a$ - $b$  plane antiferromagnetic ordering of the Er moments<sup>20</sup> in  $ErBa_2Cu_3O_{7-\delta}$ . The small specific-heat peak at  $\sim 10.8$  K in  $DyBa_2Cu_3O_{7-\delta}$  is probably associated with magnetic ordering in an impurity phase which we have not yet been able to identify.

Shown in Fig. 4 are entropy  $S$  versus  $T$  plots for the  $RBa_2Cu_3O_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, Dy, and Er}$  which were calculated using the specific-heat data according to the relation  $S(T) = \int_0^T [C(T')/T'] dT'$ . The entropy associated with the electronic and lattice vibrational degrees of freedom was estimated from the  $C(T)$  data of  $YBa_2Cu_3O_{7-\delta}$  (Ref. 6), and contributes less than  $0.003R$  ( $R$  is the gas constant) to the entropy and is negligible compared to the magnetic entropy. The value of the entropy  $S(T_0)$  below the lower-temperature limit  $T_0 \approx 0.5$  K of the specific-heat measurements was estimated from the area  $C(T_0)/T_0$  of a triangle on a  $C/T$  versus  $T$  plot with vertices at 0 K,  $T_0$ , and  $C(T_0)/T_0$ , and

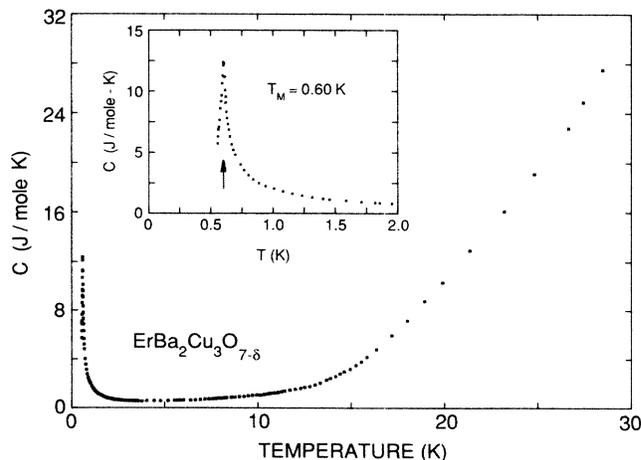


FIG. 3. Specific heat  $C$  vs temperature for  $ErBa_2Cu_3O_{7-\delta}$  for  $0.5 \lesssim T \lesssim 30$  K, and  $0.5 \lesssim T \lesssim 2$  K (inset).

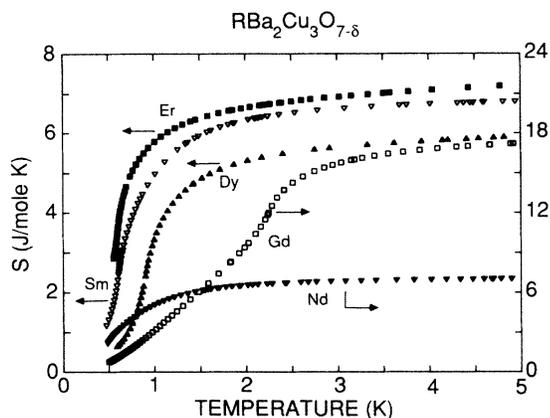


FIG. 4. Entropy  $S$  due to magnetic ordering vs temperature for  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, Dy, and Er}$  for  $T \leq 5$  K. The estimation of  $S$  below the low-temperature limit  $T_0 \approx 0.5$  K of the specific-heat experiments is explained in the text.

is responsible for most of the uncertainty in the calculation of  $S(T)$ . The values of  $S$  at  $T_0$ ,  $T_M$ , and 5 K, which is well above  $T_M$  for all the  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  compounds, are given in Table I. The values of  $S(5 \text{ K})$  for the compounds with  $R = \text{Nd, Sm, Dy, and Er}$  are close to  $\mathcal{R} \ln 2 = 0.693 \mathcal{R}$ , considering the error in the estimate of  $S_0$ , which indicates that each of these compounds has a doublet ground state in the CEF. The rounded feature in the specific heat of  $\text{NdBa}_2\text{Cu}_3\text{O}_{7-\delta}$  is reminiscent of a Schottky anomaly arising from a low-lying excited state produced by the splitting of the  $\text{Nd}^{3+}$  Hund's rules ground-state multiplet by the CEF. However, the entropy associated with the specific-heat anomaly up to 5 K indicates a doublet ground state for  $\text{Nd}^{3+}$  in the CEF. It is interesting to note that there are two peaks in the specific heat of another Nd compound,  $\text{NdRh}_4\text{B}_4$ , corresponding to two different antiferromagnetically ordered states that coexist with superconductivity in zero applied magnetic field.<sup>21</sup> The value of  $S(5 \text{ K})$  for  $\text{GdBa}_2\text{Cu}_3\text{O}_{7-\delta}$  is very close to  $\mathcal{R} \ln 8 = 2.08 \mathcal{R}$ , the value expected for the eightfold-degenerate  $J = \frac{7}{2}$  Hund's rules ground state for  $\text{Gd}^{3+}$ , and indicated by low-temperature magnetization measurements on the  $\text{GdBa}_2\text{Cu}_3\text{O}_{7-\delta}$  compound.<sup>22</sup>

The magnetic ordering temperatures  $T_M$  for the  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, Dy, and}$

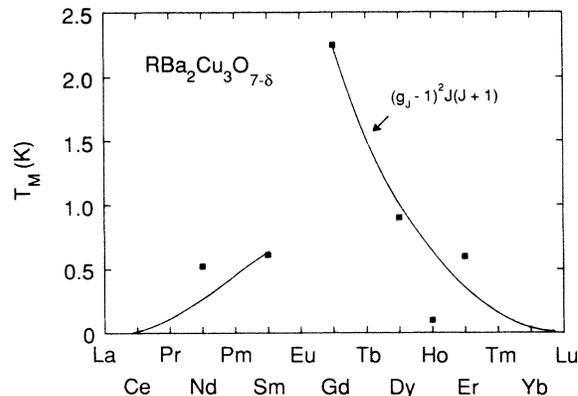


FIG. 5. Magnetic ordering temperature  $T_M$  vs  $R$  for  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, Dy, and Er}$  (this work) and  $\text{Ho}$  (Dunlap *et al.*, Ref. 7). The solid line represents the value of  $T_M$  expected from a scaling of  $T_M$  for  $R = \text{Gd}$  by the deGennes factor  $(g_J - 1)^2 J(J + 1)$ , where  $g_J$  and  $J$  are, respectively, the Landé  $g$  factor and total angular momentum of the Hund's rules ground-state multiplet of the  $R^{3+}$  ion under consideration (after Ref. 8).

$\text{Er}$  determined from the specific-heat measurements reported here, and for  $\text{HoBa}_2\text{Cu}_3\text{O}_{7-\delta}$  from recent specific-heat measurements by Dunlap *et al.*<sup>7</sup> are plotted in Fig. 5, which also appeared in Ref. 8. Except for  $\text{HoBa}_2\text{Cu}_3\text{O}_{7-\delta}$ , the variation of  $T_M$  with  $R$  conforms reasonably well to the values (solid line in Fig. 5) that have been "scaled" from the value for  $\text{Gd}$  according to the deGennes factor  $(g_J - 1)^2 J(J + 1)$ , where  $g_J$  and  $J$  are, respectively, the Landé  $g$  factor and total angular momentum of the Hund's rules ground-state multiplet of the  $R^{3+}$  ion under consideration. A deGennes factor variation of  $T_M$  with  $R$  would be expected in an isostructural series of  $R$  compounds in which the magnetic moments of the  $R$  ions are coupled by the Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction and CEF effects are relatively unimportant. However, the agreement between the observed and deGennes scaled values of  $T_M$  may be misleading. The  $R$  ions appear to be rather well isolated from the  $\text{CuO}$  layers which are, in turn, situated between two  $\text{BaO}$  layers in the  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  crystal structure, and are thought to be responsible for the superconductivity. Alp *et al.*<sup>23</sup> reported the results of an investigation of superconducting

TABLE I. Magnetic transition temperature  $T_M$ , magnetic entropy  $S(T_0)$  at the lower-temperature limit  $T_0 \approx 0.5$  K,  $S(T_M)$  at  $T_M$ , and  $S(5 \text{ K})$  for  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, Dy, and Er}$ .

$R$ ion in $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$	$T_0$ (K)	$T_M$ (K)	$S(T_0)$ ( $\mathcal{R}$ )	$S(T_M)$ ( $\mathcal{R}$ )	$S(5 \text{ K})$ ( $\mathcal{R}$ )
Nd	0.484	$0.522 \pm 0.005$	0.267	0.311	0.850
Sm	0.471	$0.612 \pm 0.005$	0.142	0.309	0.819
Gd	0.497	$2.25 \pm 0.03$	0.094	1.441	2.066
Dy	0.587	$0.90 \pm 0.02$	0.077	0.289	0.711
Er	0.553	$0.599 \pm 0.003$	0.344	0.428	0.871

$\text{GdBa}_2\text{Cu}_3\text{O}_{7-\delta}$  utilizing  $^{155}\text{Gd}$  Mössbauer spectroscopy measurements that provide direct evidence for an absence of conduction electrons at the Gd sites in  $\text{GdBa}_2\text{Cu}_3\text{O}_{7-\delta}$  and hence no interaction between the localized  $4f$  electrons and the conduction electrons responsible for superconductivity. This explains why the replacement of Y ions by R ions does not reduce  $T_c$  and superconductivity coexists with the magnetically ordered states in the  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  compounds with  $R = \text{Nd, Sm, Gd, Dy, and Er}$ . According to recent low-temperature specific-heat experiments by Dunlap *et al.*,<sup>12</sup> the feature in  $C(T)$  due to magnetic ordering and the value of  $T_M$  are virtually identical for both nearly stoichiometric metallic orthorhombic and oxygen-deficient semiconducting tetragonal  $\text{GdBa}_2\text{Cu}_3\text{O}_{7-\delta}$ . This suggests that the magnetic ordering is not due to the RKKY interaction, which is mediated by the conduction electrons, but is rather due to dipole-dipole interactions, and perhaps even superexchange, that could be operative in metals as well as insulators. The quantitative agreement between the values of  $T_M$  and the variation

predicted by the deGennes factor may be a fortuitous consequence of the effect of the reduced degeneracy of the ground states of the  $R^{3+}$  ions in the CEF on the values of  $T_M$  which are due to dipole-dipole interactions (and perhaps superexchange), rather than the RKKY interaction.

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\*Permanent address: Departamento de Física, Universidade Federal de Pernambuco, 50000 Recife, Brazil.

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