## Electronic structure and properties of  $CoSi<sub>2</sub>$

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The energy-band structure and related electronic properties of cubic  $\cos i_2$  have been calculated self-consistently with the use of the linear augmented-plane-wave method. The results are qualitatively similar to those determined previously for NiSi<sub>2</sub>, assuming a rigid-band adjustment of the Fermi level. The  $\cos i_2$  Fermi surface is quite simple, consisting of three nested hole sheets centered at the Brillouin-zone origin. The calculated Fermi-surface dimensions and topology are in excellent agreement with the de Haas-van Alphen data of Newcombe and Lonzarich (preceding paper). The calculated Drude plasma energy and Fermi velocity are combined with the observed resistivity to estimate transport properties such as low-temperature carrier mean free paths  $(l \approx 340 \text{ Å})$ . The kinematics of carrier transmission through Si/CoSi, interfaces and its dependence on interface orientation is analyzed in terms of the projected band structure.

Transition-metal silicides have received increased attention in recent years because of their practical importance in Si device applications.<sup>1</sup> This has been especially true in the case of the cubic disilicides  $\cos i_2$  and  $Nisi_2$ , which both crystallize with the well-known fluorite structure. In both materials, the bulk lattice parameters are close to those of Si. This proves to be favorable for the formation of sharp epitaxial silicon-silicide interfaces which are near perfect at an atomic scale.<sup>2</sup> This has led to detailed studies of their interface properties such as Schottky-barrier heights<sup>3,4</sup> and interface geometry,<sup>3</sup> as well as the fabrication of Si/CoSi<sub>2</sub>/Si heterostructures for use as metal-base transistors.

These developments have stimulated a parallel interest in the fundamental properties of the bulk silicide materials. For example, photoemission<sup>10-12</sup> and transpor measurements have been carried out on bulk and thinfilm samples of  $CoSi<sub>2</sub>$ , NiSi<sub>2</sub>, and related silicide compounds. Recently, Newcombe and Lonzarich<sup>14</sup> have observed de Haas-van Alphen oscillations in a high-quality  $\cos i_2$  sample. This provides an important opportunity to assess the accuracy of present state-of-the-art bandstructure methods and local-density theory in determining the electronic properties of this technologically interesting material.

There have been several previous calculations of the  $NiS_i$ <sub>2</sub> band structure ' $15$  and density of states 'which are found to be in reasonable agreement with the photoemission data.<sup>10-12</sup> The density-of-states results of Tersoff and Hamann<sup>17</sup> for CoSi<sub>2</sub> and NiSi<sub>2</sub>, derived from linear augmented-plane-wave (LAPW) calculations, predict a similar band structure for  $CoSi<sub>2</sub>$  except that the 3d-band binding energy is reduced by  $\sim$  2 eV, in accord with photoemission data.<sup>12</sup> Significantly different energy-band results for  $CoSi<sub>2</sub>$  have been obtained recently by Gupta and Chatterjee<sup>18</sup> using a composite-wave variational version of the APW method. In particular, these results predict a total valence-band width  $(-21.3 \text{ eV})$ which is  $\sim 60\%$  larger than the Tersoff-Hamann result.

In order to provide a more complete picture of the CoSi<sub>2</sub> band structure, Fermi surface, and related electronic properties, a scalar-relativistic LAPW calculation<sup>19</sup> has been carried out for the fluorite (C1) phase of this compound using the observed<sup>20</sup> lattice parameter,  $a = 5.356$  Å. The calculations assume nearly touching muffin-tin (MT) spheres which are centered at the Co and Si sites with radii  $R$ (Co)  $\approx$  2.34 a.u. and  $R$ (Si)  $\approx$  2.02 a.u., respectively. The basis functions included plane waves with energies below 10 Ry (approximately 140 LAPW's). All terms through  $l = 6$  have been included in the latticeharmonic expansion of the nonspherical contributions to the charge density and potential within the MT spheres. The corresponding Fourier expansions in the interstitial region contained about 2500 plane waves. The Brillouin-zone sampling included 28 k points in the  $\frac{1}{48}$  irreducible wedge of the full zone. Exchange and correlation effects have been treated using the Wigner interpolation formula.<sup>21</sup>

The LAPW results for  $CoSi<sub>2</sub>$  are plotted along symmetry lines of the fcc Brillouin zone in Fig. 1. They consist of broad low-lying Si 3s-3p bands which merge with the relatively narrow Co 3d bands just below  $E_F$ . The open circles at symmetry points in Fig. <sup>1</sup> identify those states with predominant 3d character within the Co MT spheres. Though there is some evidence of broadening due to hybridization effects, the principa1 Co 3d-band contribution to the density of states is expected to occur in the energy range  $1-3$  eV below  $E_F$ , in agreement with previous results.<sup>17</sup>

The CoSi, Fermi level cuts through a hybrid portion of the band structure where the broad 3s-3p bands are beginning to reemerge. The resulting Fermi surface is relatively simple, consisting of three nested hole pockets that are located at the Brillouin-zone center  $\Gamma$ . These are labeled  $h_7$ ,  $h_8$ , and  $h_9$  since they represent holes in the seventh, eighth, and ninth bands, respectively. The intersection of these three Fermi-surface sheets with the (001) and  $(110)$  symmetry planes is shown in Fig. 2. As indicat-



FIG. 1. LAPW energy-band results for  $CoSi<sub>2</sub>$ .

ed, symmetry-induced band degeneracies ( $\Delta_5$  and  $\Lambda_3$ ) along the  $\Delta(\Gamma X)$  and  $\Lambda(\Gamma L)$  lines cause the  $h_7-h_8$  and  $h_8-h_9$  surfaces to contact in these directions. Although these degeneracies are removed by spin-orbit effects, the resulting splittings are expected to be small since Co and Si are both light elements with small  $(-0.02-0.09 \text{ eV})$ spin-orbit parameters. $22$  This leads to the likelihood of magnetic breakdown for orbits that pass near these contacts.

Three-dimensional sketches of the individual  $h_7$ ,  $h_8$ , and  $h_9$  Fermi-surface sheets are shown in Fig. 3. From their shapes, one expects that the extremal orbits which are observed in the de Haas-van Alphen effect will generally involve central orbits (i.e., orbits confined to a plane through the origin). Two exceptions involve  $h_8$ and  $h_9$  when the magnetic field direction **H** is near [001]. For  $h<sub>8</sub>$ , a pair of noncentral extremal orbits can exist in which the orbit trajectories pass over the four upper and lower [111] bulges. These noncentral orbits enclose an area which is about 15% larger than that of the central orbit when H is along [001]. Similar noncentral extremal orbits appear to be possible on the  $h_9$  surface, although this has not been confirmed by means of detailed calculations.

The variation with angle of the central extremal areas and cyclotron masses for orbits on the  $CoSi<sub>2</sub>$  Fermi surface have been calculated using the Mueller inversion scheme.<sup>23</sup> In this procedure, 19 Fermi radii  $k_F$  have been fit (with an accuracy of  $1-2\%$ ) using an eight-term cubic-harmonic expansion ( $l_{\text{max}}$  = 14). The results, which are shown in Fig. 4, have an estimated accuracy of 5 and 15% for the calculated areas and cyclotron masses, respectively. The average  $(h_7-h_9)$  calculated cyclotron mass ratio is about 1.0, reflecting the presence of relatively steep bands at  $E_F$  in Fig. 1.

As shown by the results summarized in Table I, there is excellent ( $\sim$  5%) agreement between the calculated and



FIG. 2. Calculated central (001) and (110) cross sections of the CoSi<sub>2</sub> Fermi-surface sheets  $h_7$ ,  $h_8$ , and  $h_9$ .



FIG. 3. Three-dimensional sketch of the  $CoSi<sub>2</sub>$  Fermi-surface sheets  $h_7$  (a),  $h_8$  (b), and  $h_9$  (c).



FIG. 4. Calculated central extremal areas and cyclotron masses for magnetic field directions  $H$  in the (110) and (001) planes.

observed<sup>14</sup> Fermi-surface areas for  $CoSi<sub>2</sub>$ . The larger variations exhibited by the ratio of experimental and calculated cyclotron masses is consistent with the decreased accuracy of the calculated values. This ratio provides an estimate of the electron-phonon coupling parameter  $\lambda$ ~0.7±0.3 for CoSi<sub>2</sub> which is in the range expected for a superconductor with  $T_c \approx 1.3$  K (Ref. 24).

The calculated  $\cos i_2$  density of states is shown in the top panel of Fig. 5. It has been calculated using tetrahedral interpolation on a mesh of  $44$  k points in the  $\frac{1}{48}$  irreducible Brillouin-zone wedge. It is in good agreement with previous results calculated using a discrete sampling procedure.<sup>17</sup> It agrees equally well with the



FIG. 5. (a) Calculated density of states, (b) Drude plasma energy, and (c) Fermi velocity for CoSi<sub>2</sub>.

features exhibited by photoemission data,<sup>12</sup> though the binding energy of the main calculated peak is  $\sim 0.3$  eV larger than the observed value.

The lower panels in Fig. 5 contain the calculated Drude plasma energy  $\Omega_p(E)$  and Fermi velocity  $v_F(E)$ , quantities which are useful for analyzing the transport properties<sup>13</sup> of bulk  $\cos i_2$ . The calculated carrier density  $n = 2.6 \times 10^{22}$  holes/cm<sup>3</sup> is in excellent agreement with Hall data.<sup>13</sup> Combining the calculated values for  $\Omega_n(E_F)=6.2$  eV and  $v_F=0.7\times10^8$  cm/sec with the observed low-temperature resistivity  $\rho$ (4 K) = 2.6  $\mu\Omega$  cm, one can estimate the mean free path I by use of the relation  $l \sim v_F / \Omega_p^2 \rho$  (Ref. 25). The calculated value  $l \approx 340 \text{ Å}$ 

Н		Area $(\mathring{A}^{-2})$			Mass $(m_c/m)$		
	<b>Sheet</b>	Calc.	Obs.	Ratio	Calc.	Obs.	Ratio
$[100]$	h <sub>7</sub>	0.647	0.655	1.01	0.54	0.78	1.4
	$h_{\rm R}$	0.805	0.857	1.06	0.82	1.36	1.7
	$h_{\rm g}$	$0.923$ <sup>a</sup>	0.963	1.04		1.34	
	$h_{9}$	1.730	1.747	1.01	1.28	2.00	1.6
$[110]$	h <sub>7</sub>	0.524	0.545	1.04	0.51	0.70	1.4
	$h_{\rm R}$	1.216	1.230	1.01	1.06	1.55	1.5
	$h_{9}$	1.900	1.948	1.03	1.25	2.47	2.0
$[111]$	$h_{7}$	0.503			0.49		
	$h_8$	0.954			1.03		
	$h_{9}$	2.280			1.53		

TABLE I. Comparison of the calculated CoSi<sub>2</sub> Fermi-surface areas and cyclotron masses with the de Haas-van Alphen results of Newcombe and Lonzarich (Ref. 14).

<sup>a</sup>Noncentral orbit in plane at height  $\sim \frac{1}{6} \overline{\Gamma} \overline{X}$ .

is about a factor of 2 smaller than empirical estimates by Hensel et  $al$ .<sup>13</sup> that are derived from transport data

An important consideration in the potential application of  $Si/CoSi<sub>2</sub>/Si$  heterostructures for use as metal-base transistors concerns the transmission characteristics of the  $Si/CoSi<sub>2</sub>$  interface. Transmission across a wellordered epitaxial interface requires that strict kinematical conditions be satisfied. The transmitted state in one material must have the same energy and parallel component of its Bloch wave vector,  $k_{\parallel}$ , as the incident state in the other. For the usual case where Si is *n* type,  $k_{\parallel}$  is determined by the position of the conduction-band minimum along  $\Delta$  ( $\sim$ 0.85 $\Gamma X$ ). Because of band bending at the interface, energy matching involves projected  $\cos i_2$  bands at a Schottky-barrier height<sup>3</sup> ( $\sim$  0.7 eV) above  $E_F$ .

The kinematical conditions for  $Si/CoSi$ , are illustrated in Fig. 6 for three low-index interfaces, (111), (100), and (110). The CoSi<sub>2</sub> bands<sup>26</sup> are plotted versus  $k_1$  for a set of  $k_{\parallel}$  determined by the projections of the Si conductionband minima on each interface plane. There are six equivalent  $(0.85,0,0)$  minima in Si. For the  $(111)$  interface, all of these generate equivalent  $k_{\parallel}$ , so only one band plot, Fig. 6(a), needs to be considered. Transmission of a Si electron near the conduction-band minimum requires that the dashed line at  $E_F+0.7$  eV intersect a  $\cos i_2$ band. It does not. We conclude that transmission at this interface requires phonon or impurity scattering to break  $k_{\parallel}$  conservation, or highly excited electrons ( $\sim$ 0.6 eV) which can reach the first available  $\cos i_2$  band.

For the (100) interface, (0.85,0,0) and (0,0,0.85) produce inequivalent  $k_{\parallel}$ , and the appropriate band plots for these are shown in Figs. 6(b) and 6(c), respectively. For the  $(0,0,0.85)$  case in Fig.  $6(c)$ , the kinematical transmission conditions are again unsatisfied. For (0.85,0,0), there appear to be allowed bands. The bands in Fig. 6(b), however, are along the  $\Delta$ -symmetry line and we must consider the symmetry of the states in each material. From Fig. 1, we see that one of the bands crossing the dashed line has  $\Delta_1$  symmetry, which is the same as that of the Si conduction-band states, so that direct transmission is allowed. Finally, for a (110) interface, (0.85,0,0) and (0,0,0.85) are again inequivalent, the bands are not on symmetry lines, and the results in Figs.  $6(d)$  and  $6(e)$  show that transmission is allowed.

We note that satisfying the kinematical conditions does not guarantee a high rate of transmission through an in-



FIG. 6. CoSi<sub>2</sub> band plots vs  $k_1$  for  $k_1$  values appropriate for n-type Si and low-index interfaces, as described in the text. The abscissae are  $k_1$  ranging from 0 to the indicated vector, in units of  $(2\pi/a)$ .

terface. A dynamical calculation of transmission and refiection coefficients is needed for quantitative predictions.

In conclusion, the results of LAPW calculations for  $CoSi<sub>2</sub>$  are in good agreement with Fermi-surface and photoemission data. Arguments based on projected bulk bands indicate favorable  $Si/CoSi<sub>2</sub>$  transmission conditions for  $(100)$  and  $(110)$  but not  $(111)$  interfaces.

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- <sup>26</sup>The bands in Fig. 6 were recalculated with the lattice constant of  $CoSi<sub>2</sub>$  set equal to that of Si, a 1.2% compression.

![](_page_5_Figure_0.jpeg)

FIG. 2. Calculated central (001) and (110) cross sections of the CoSi<sub>2</sub> Fermi-surface sheets  $h_7$ ,  $h_8$ , and  $h_9$ .

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FIG. 3. Three-dimensional sketch of the CoSi<sub>2</sub> Fermi-surface sheets  $h_7$  (a),  $h_8$  (b), and  $h_9$  (c).