# Comparative optical study of the two-dimensional donor-type intercalation compounds graphite-KH<sub>x</sub> and their binary counterparts  $C_8K$  and  $C_{24}K$

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(Received 27 May 1986; revised manuscript received 17 February 1987)

We report the results of optical reflectivity studies of the stage-1 and -2 graphite- $KH_{x}$  intercalation compounds prepared by direct reaction of highly ordered pyrolytic graphite and KH powder. The stage-1 and -2 binary graphite-K compounds are studied for comparison. The optical data are analyzed in terms of a model involving two-dimensional (2D) graphitic  $\pi$  electrons and threedimensional  $(3D)$  nearly free  $K(4s)$  electrons. The model is used to interpret the observed values of the free-carrier unscreened plasma frequencies and the position of the interband absorption threshold to determine experimental values for the Fermi level  $(E_F)$  in the carbon  $\pi$  band(s) and the fractional occupation of the  $K(4s)$  band. For the hydrides, we find quantitative evidence that the hydrogen states lie below  $E_F$ . Thus, hydrogen is present as  $H^-$ , acting as an acceptor, thereby compensating the electron donation to the  $\pi$  bands from the K(4s) states. This assumption and the optical data for the stage-1 and -2 hydrides results in a  $[H]/[K]$  ratio of 0.8, in excellent agreement with chemical analyses reported by Guérard and co-workers, and leads to very small values for the fractional K(4s) band occupation  $f<sub>K</sub> < 0.03$  electrons per K atom. Within the framework of a superimposed 2D ( $\pi$ ) and 3D [K(4s)] rigid-band model, our experimental results support an empty K(4s) band (i.e.,  $f_K = 0$ ) in stage-2 C<sub>24</sub>K. In stage-1 C<sub>8</sub>K, the rigid-band model yields large values for  $f_K$  $(f<sub>K</sub> > 0.5$  electrons per K atom), unless the value of the optical mass of the electrons in the K(4s) states is larger than  $\sim$  2. The C<sub>8</sub>K results are also discussed in terms of more sophisticated energyband calculations.

# I. INTRODUCTION

It has been known for some time that gaseous hydrogen can be chemisorbed into the binary graphite intercalation compound (GIC)  $C_8K$  to form the ternary GIC hydride  $C_8KH_{2/3}$ .<sup>1-3</sup> The reaction rate is prohibitively slow in well-ordered graphite, even at several atmospheres of hydrogen pressures,<sup>4</sup> and is therefore carried out on  $C_8K$ powder. The binary GIC is a stage-1 compound, whereas the ternary hydride GIC is a stage-2 compound—the stage index refers to the number of carbon layers stacked between successive intercalate layers.<sup>5,6</sup> It has also been reported<sup>4</sup> that a larger  $[H]/[K]$  ratio of 0.8 can be accomplished by reacting pyrolytic graphite directly with KH powder to form either a stage-1  $(C_4KH_{0.8})$  or a stage-2  $(C_8KH_{0.8})$  compound, depending on the reaction temperature. We report here on the results of optical reflectivity studies of these hydride GIC's prepared from KH powder and highly oriented pyrolytic graphite which we refer to as graphite- $KH_{x}$ . Optical data of the binary graphite-K compounds  $C_8K$  and  $C_{24}K$  are presented and analyzed for comparison with the graphite- $KH_r$  compounds. The optical data indicate that the electron transfer from the K(4s) band to the lower-lying graphitic  $\pi^*$  and H(1s) levels (bands) is complete, or nearly so. The large thickness of the trilayer intercalate sandwich (K-H-K) serves to decouple the C-C interactions along the  $c$  axis resulting in a quasi-two-dimensional (2D) donor-type GIC, with a basal-plane conductivity associated with the  $\pi^*$  conduction band. The term donor type refers to the fact that the insertion of the intercalate layers raises the electron concentration in the carbon  $\pi$  conduction bands(s) due to a donation of electrons from the intercalate to the carbon 'ayers. $5,6$ 

The trilayer intercalate sandwich structure of graphite- $KH_{x}$  (K-H-K) is similar to that reported<sup>7</sup> for graphite-KHg (K-Hg-K). Using transmission electron microscopy TEM) both of these ternary GIC's have been found<sup>8,9</sup> to exhibit both the  $(2\times2)R0^\circ$  and  $(\sqrt{3}\times\sqrt{3})R30^\circ$  in-plane intercalate-layer superlattice phases. In the case of graphite  $KH_{x}$ , the TEM patterns are sensitive only to the position of the C and K atoms. On the basis of  $(hk0)$  diffraction studies, Guérard et  $al$ <sup>4</sup> have identified the presence of a  $2\sqrt{3}\times3$  rectangular ordering of the intercalate layer. Recent studies involving in-plane elastic neutron scattering measurements by Kamitakahara et al.<sup>10</sup> are consistent with the observations of Guérard et al. The neutron scattering results<sup>10</sup> on the hydride GIC's indicate that the H atoms themselves form an ordered sublattice, rather than randomly decorating the K superlattice. ac magnetic-susceptibility measurements<sup>11</sup> found  $C_8KH_{0.8}$ (stage 2) to be superconducting, but  $C_4KH_{0.8}$  (stage 1) was not found to superconduct for  $T>70$  mK at  $\sim$  1 atm. Resistivity studies<sup>12</sup> found a linear  $T$  dependence for  $4.2 < T < 300K$  for both stage-1 and -2 graphite KH<sub>x</sub>. This behavior is not observed in the binary donor-type GIC's, but has also been reported<sup>12</sup> in the stage-1 and -2 graphite-KHg compounds—which also superconduct<sup>11</sup>  $(T_c=0.77 \text{ K for C}_4 \text{ KHg}, T_c=1.90 \text{ K for C}_8 \text{ KH}_8).$  Further recent measurements on graphite  $KH_{x}$  which are relevant to the study presented here are magnetic susceptibility<sup>13</sup> and Raman scattering.<sup>14</sup> References to recent results on the related stage-2 hydride— $C_8KH_{2/3}$ , prepared by the reaction of powdered  $C_8K$  with gaseous hydrogen, can be found in Ref. 15.

## II. EXPERIMENTAL DETAILS

The graphite- $KH_{x}$  compounds were obtained by immersing plates ( $7\times7\times0.3$  mm<sup>3</sup>) of highly oriented pyrolytic graphite (HOPG, Union Carbide) in KH powder (Morton Thiokol/Alpha Inc.) at elevated temperature. The stage-1 and -2 compounds resulted, respectively, from reactions carried out for 7 days at  $T=350^{\circ}$ C and  $T = 250^{\circ}$ C. The KH powder, as received, was light gray in color and immersed in mineral oil. To separate the KH from the oil, the mixture was loaded into a glass vacuum apparatus above a clean sintered glass filter disk (Ace) with pore diameters in the range  $70-100 \mu m$ . The space above and below the filter disc was evacuated for  $\sim$  1 h to a pressure of 10  $\mu$ m using a liquid-nitrogen-trapped forepump. An overpressure of ultra high purity UHP grade  $N_2$  ( $\sim$ 2 atm) was then introduced above the KH-oil mixture to force the oil through the disk, leaving a residue of oil and the KH powder behind. Spectral-grade pentane was next admitted through a valve in a side arm above the disk to dissolve the oil residue. The solvated oil was then pushed through the disc by introducing UHP  $N_2$  again. The remaining KH powder was then pumped for  $\sim$  8 h to remove any remaining pentane. More details of the vacuum-line technique for separation of oil and airsensitive powders are available in the literature.<sup>16</sup>

Following the method of Guérard et al.,<sup>4</sup> the HOPG and KH powder was sealed off in 2-mm-wall Pyrex tubing (10-mm inside diameter) under a diffusion-pump vacuum ( $\sim 10^{-6}$  Torr). Some concern must be given to the wall thickness of the reaction ampoules—the walls are weakened somewhat by attack from K and can burst due to a gas overpressure which presumably occurs upon dissociation of the KH at the reaction temperature. Also, it should be denoted that KH is pyrophoric and therefore should not be handled in room air. The color of the HOPG plates reacted at 350'C (stage 1) and 250'C (stage 2) was observed to be violet and blue, respectively. The samples were removed from the reaction ampoules in a high-quality He-atmosphere glove box (Vacuum Atmospheres, Inc.,  $p_{\text{H}_2\text{O}}$  and  $p_{\text{O}_2}$  < 1 ppm), cleaved and transferred to rectangular cross section uv-quartz ampoules  $(0.4\times0.8\times8cm^3)$  (Vitrodynamics) which were sealed under vacuum ( $\sim 10^{-6}$  Torr) for the optical measurements.

The samples were characterized in the deep bulk and in the optical skin depth ( $\sim$ 1000 A), respectively, by (00*l*) x-ray diffraction and Raman scattering probes. The Raman results will be discussed later in the paper. A General Electric XRD6 diffractometer equipped with a Si:Li detector and Mo source was used to collect the (001) data which showed little or no evidence for stage impurity or inclusion of the K-based binary GiC's. We note that a pure stage-2 graphite-KH<sub>x</sub> is more difficult to achieve often times containing  $C_{24}K$  as a minority phase. The caxis separation of intercalate layers  $(I_c)$  was determined using Bragg's law and the method of least squares to be  $I_c = 8.53 \pm 0.02$  Å (stage 1) and  $I_c = 11.89 \pm 0.02$  Å (stage 2). These values agree, within experimental error, with the literature.<sup>4</sup> Our stage-1  $I_c$  value corresponds to the value reported<sup>4</sup> for the alpha phase; the beta phase  $(I_c=9.13 \text{ A})$  (Ref. 11) was not present in the samples studied in this work. We have, however, observed the beta and alpha hydride phases coexisting in some stage-1 samples. The stage-1 (alpha) and stage-2 hydride  $I_c$  values differ by 3.35  $\AA$ , which is the accepted value<sup>5,6</sup> for the thickness of a graphitic  $C$  layer. This suggests that the nature of the intercalate layers for these stage-1 and -2 compounds is similar, if not the same.

The Raman scattering measurements on the intercalant-perturbed graphitic intralayer phonons  $({\sim}1600 \text{ cm}^{-1})$  were carried out in the Brewster angle<br>backscattering geometry under low laser power (4880 Å at  $\sim$  20 mW).<sup>17</sup> Reflectivity measurements (R) were carried out at near-normal incidence using a prism monochromator and a standard  $MgF_2$ -overcoated Al mirror calibrated against a Ag film below 3 eV and calibrated absolutely for  $E > 3$  eV. Spectra were obtained in the range of transmission of the quartz ampoule  $(0.5 < \hbar \omega < 6$  eV). Details of the Raman and reflectance apparatus are available in the literature.<sup> $17,18$ </sup> The absolute scale of the reflectance data was checked at  $E = 1.96$  eV using a He-Ne laser. To perform Kramers-Krönig  $(KK)$  analyses, the spectra were extended in the ir as a Drude metal, and in the uv as a density-scaled spectrum of pristine graphite. The KK transform of the reflectance (R) data (i.e., the phase integral) was then calculated to obtain the dielectric functions  $\epsilon_1$  and  $\epsilon_2$ . Further details of the KK transformation and the data analysis are given in a recent review.<sup>19</sup>

#### III. RESULTS AND DISCUSSION

Raman scattering studies of the intercalant-perturbed graphitic phonon at  $\sim 1600 \text{ cm}^{-1}$  provide an important stage-specific characterization<sup>20</sup> of the bulk in the optical skin depth  $({\sim}1000 \text{ A})$ . In Fig. 1 we display the Raman spectra in the vicinity of the  $\sim 1600$ -cm<sup>-1</sup> graphitic intralayer phonons for the same samples whose reflectance spectra are analyzed below. The solid lines in the lower three spectra are the result of least-squares fits to a single Lorentizian line shape. The  $C_8K$  spectrum appears in the inset in the figure because an otherwise narrow peak associated with the intralayer phonon is broadened and downshifted by a Breit-Wigner or Fano resonance characteristic 'of the stage-1  $C_8K$ ,  $C_8Rb$ , and  $C_8Cs$  compounds.<sup>21,2</sup>  $C_{24}K$ ,  $C_{4}KH_{0.8}$ , and  $C_{8}KH_{0.8}$  exhibit a Lorentzian rather than Breit-Wigner line shape, indicating that in these compounds the coupling between the graphitic phonons  $(E_{2g}, \Gamma \text{ point})$  and a Raman-active continuum is much weaker. The strong coupling which occurs in the stage-1 GIC's  $C_8K$ ,  $C_8Rb$ , and  $C_8Cs$  downshifts the graphitic inthe stress expects and experiments the graphics in error  $\approx 1600$  to  $\sim 1500$  $cm^{-1}$ ,  $^{17,20,21}$  It is evident in Fig. 1 that the linewidth for the  $C_{24}K$  binary GIC [full width at half maximum (FWHM) of 12  $\text{cm}^{-1}$ ] is noticeably less than the ternary hydrides (FWHM of  $\sim$  23 cm<sup>-1</sup>). This might be interpreted as evidence for a generally poorer in-plane order, or poor stacking fidelity in the ternaries. However,

In Fig. 2 we display the reflectance spectra  $R(E)$  of  $C_8K$ ,  $C_{24}K$ ,  $C_4KH_{0.8}$ , and  $C_8KH_{0.8}$ . The spectra are characteristic of metals, exhibiting a sharp Drude edge in the visible region. The edge position, which is located near the screened plasma frequency  $\tilde{\omega}_p$ , is largely responsible for the characteristic color of the compounds. The rise in the reflectance with increasing energy from the minimum is associated with the threshold for interband absorption. The broad peak in the range <sup>4</sup>—<sup>5</sup> eV is the GIC analog of the *M*-point absorption<sup>25</sup> observed in pristine graphite.<sup>26</sup> The binary GIC spectra  $(C_{24}K, C_8K)$  are in good agreement with that observed previously.<sup>27,28</sup>

analyses (Sec. II). The stage-1 compounds  $C_8K$  and  $C_4KH_{0.8}$ , and the stage-2 compounds  $C_{24}K$  and  $C_8KH_{0.8}$ are compared in Figs. 3 and 4, respectively. The insets to the figures show the zero crossing of  $\epsilon_1$  which locates the screened plasma frequency  $\tilde{\omega}_p$  and thus the position of the ntraband plasmon observable in electron-energy-loss specroscopy.<sup>29-31</sup> The downshift of  $\tilde{\omega}_p$  we observe for the ternary hydride relative to the parent binary GIC indicates a decrease in the Fermi energy  $E_F$  in the carbon  $\pi$ band. This can be understood as result of the introduction of low-lying  $H(1s)$ -states in the graphite-KH compounds.

Our schematic density of states (DOS) model for  $C_4KH_{0.8}$  and  $C_8KH_{0.8}$  is shown in Fig. 5. The position of the low-lying H states is consistent with the large electronegativity of hydrogen. Electrons must empty from the  $\pi$  conduction band and the K(4s) band to fill these low-lying H(1s) levels (band). Our data also support the placement of  $E_F$  below the K(4s) band minimum. We discuss the evidence for an empty  $K(4s)$  band in the hy-

In Figs. 3 and 4 we display  $\epsilon_2$  data obtained by KK

TABLE I. Results of 001 x-ray diffraction  $(I_c)$ , Raman scattering  $(\omega, \Gamma)$  and optical reflectivity  $(\omega_p, \omega_p \tau, \epsilon_x, E_T/2)$  studies of C<sub>8</sub>K,  $C_4KH_{0.8}$ ,  $C_{24}K$ ,  $C_8KH_{0.8}$ . The various parameters are defined in the text.

Nominal formula	<b>Stage</b> index		Raman line-shape parameters		Drude Parameters <sup>a</sup>					
		$I_c$ (Å)	Peak position $\rm (cm^{-1})$	<b>FWHM</b> $(cm^{-1})$	$\hslash \omega_p^{\;\;b}$ (eV)	$\omega_p \tau$	$\epsilon_{\infty}$	$f_c^b$	$E_F{}^b$ (eV)	$E_T/2^{\rm a,b}$ (eV)
$C_8K$	1	$5.35 \pm 0.02$ 5.35 <sup>c</sup>	$1522 \pm 2^{d}$		$4.51 \pm 0.1$ $4.5^{\rm f}$ 4.65 $^{d}$	14	3.6	$-1/8^d$ $\sim 0.6/8^g$ $-0.6/8h$	$1.4^{d}$ $1.4^{g}$ 1.4 <sup>h</sup>	1.60 1.50 <sup>f</sup> 1.45 <sup>d</sup> 1.45 <sup>g</sup>
$C_4KH_{0.8}$	$\mathbf{1}$	$8.53 \pm 0.02$ $8.53^{j}$ 8.56 <sup>m</sup>	$1596 \pm 2$ $1596 \pm 3^{k}$	$25 + 2$ $23 \pm 3^k$	$3.31 \pm 0.1$	17	3.0	$0.050 \pm 0.006$ <sup>i</sup> $0.054 \pm 0.005$ <sup>1</sup> 0.020 <sup>m</sup>	$1.53 \pm 0.09$ <sup>i</sup> $1.62 \pm 1^{1}$ $0.65^{\rm m}$	1.40
$C_{24}K$	$\overline{2}$	$8.74 \pm 0.02$ 8.74 <sup>e</sup>	$1601 \pm 2$ 1599 <sup>n</sup>	$13\pm2$ 13 <sup>n</sup>	$4.2 \pm 0.1$	21	6.3	$0.042 \pm 0.004$ $0.042^{\circ}$	$1.42 \pm 0.07$ <sup>1</sup>	1.40
$C_8KH_{0.8}$	$\overline{2}$	$11.89 \pm 0.02$ $11.88^{j}$ 11.93 <sup>m</sup> 12.08 <sup>k</sup>	$1598 \pm 2$ $1598 \pm 3^{k}$	$26 + 2$ $12 \pm 3^k$	$3.26 \pm 0.1$	20	4.3	$0.026 \pm 0.003$ 0.033 <sup>m</sup>	$1.13 \pm 0.7$ <sup>1</sup> 1.15 <sup>m</sup>	1.10

<sup>a</sup>Obtained from fits of Eq. (1) to both R and  $\epsilon_2$  data.

<sup>b</sup>Purely theoretical values obtained from band-structure calculations are underlined.

'This feature exhibits a Breit-Wigner line shape, the remaining Raman data in the table refer to Lorentzian line shapes.

DiVincenzo and Rabii (Ref. 37).

'Parry and Nixon (Ref. 40).

fFischer et al. (Ref. 27).

Ohno et al. (Ref. 36).

<sup>h</sup>Tanuma et al. (Ref. 42).

'Obtained from our value for  $\omega_p$  and the band model of Holzwarth, Ref. 33.

<sup>j</sup>Guérard et al. (Ref. 4).

 $k$ Yeh et al. (Ref. 14).

Obtained from our value for  $\omega_p$  and the band model of Blinowski *et al.* ( $\gamma_0$ =2.9 eV,  $\gamma_1$ =0.375 eV), Ref. 32.

"Enoki et al. (Ref. 39).

"Dresselhaus and Dresselhaus (Ref. 20).

'Dresselhaus et al. (Ref. 41).



FIG. 1. Raman spectra associated with the high frequency  $(-1600 \text{ cm}^{-1})$  graphitic intralayer phonons for the stage-1 and -2 binary ( $C_8K$ ,  $C_{24}K$ ) and ternary ( $C_4KH_{0.8}$ ),  $C_8KH_{0.8}$ ) GIC's. The  $C_8K$  spectrum (inset) exhibits a Breit-Wigner line shape typical of the C<sub>8</sub>M ( $M = K$ ,Cs,Rb) compounds while C<sub>24</sub>K,  $C_4KH_{0.8}$ , and  $C_8KH_{0.8}$  spectra exhibit a Lorentzian line shape. Data are shown as points while the solid lines represent the results of least-square fits of the spectra to Lorentzian line shapes.



FIG. 2. Reflectance data (300 K) measured at near-normal incidence to the c face for C<sub>8</sub>K, C<sub>24</sub>K, C<sub>4</sub>KH<sub>0.8</sub>, and C<sub>8</sub>KH<sub>0.8</sub>. Data are displayed as solid lines while the dashed lines are calculated from Drude parameters obtained from Fig. 6. Values of the corresponding unscreened or bare plasma frequencies  $(\omega_p)$ are displayed beside each spectrum.



FIG. 3. Real  $(\epsilon_1)$  and imaginary  $(\epsilon_2)$  dielectric functions for  $C_4KH_{0.8}$  (solid line) and  $C_8K$  (dashed line). The inset shows the zero crossing of  $\epsilon_1$  which approximately locates the screened plasma frequency ( $\tilde{\omega}_p$ ). The arrows associated with energy  $E_T$ indicate the midpoint of the interband threshold. The threshold is broadened by electron-electron scattering (Ref. 38).

drides in detail below.

The contribution to the optical dielectric function  $\epsilon(0,\omega) = \epsilon_1 + i\epsilon_2$  from free carrier (or intraband) absorption is given in the Drude approximation by the wellknown expression

$$
\varepsilon_{\text{Drude}} = \epsilon_{\infty} - \omega_p^2 (\omega^2 + i\omega/\tau)^{-1} \,, \tag{1}
$$

where  $\omega_p$  is the *unscreened* plasma frequency,  $\tau$  is the average carrier lifetime, and  $\epsilon_{\infty}$  if the core dielectric constant. If there is more than one partially occupied band, then the standard approximation is to assume  $\tau_i \approx \tau_0$ , independent of band index j. Then the plasma frequency in Eq.  $(1)$  is given by

$$
\omega_p^2 = \sum_j \omega_{p,j}^2 \tag{2}
$$

where

$$
\omega_{p,j}^2 = 4\pi N_j e^2 / m_{\text{opt},j} \tag{3}
$$

 $N_j$  is the carrier concentration,  $m_{\text{opt},j}$  is the optical mass, and e is the electronic charge. The alternative to this procedure is to assign different  $\tau_j$  and adjust all  $\omega_{p,j}$  and  $\tau_j$ parameters to fit the data. This proliferation in the number of parameters is seldom justified, and we do not pursue it here.



FIG. 4. Real  $(\epsilon_1)$  and imaginary  $(\epsilon_2)$  dielectric functions for  $C_8KH_{0.8}$  (solid line) and  $C_{24}K$  (dashed line). See caption to Fig. 3.



In Fig. 2 the dashed lines indicate the reflectance calculated from Eq. (1) using a single  $\omega_p$  and  $\tau$ , and are in good agreement with the low-energy data below the reflectance minimum. The disagreement near, and just above, the minimum occurs because the presence of nearby interband absorption is inadequately described by a core dielectric constant  $\epsilon_{\infty}$ . In Fig. 6 we examine the Drude fit in a different way. We plot  $(\omega \epsilon_2)^{-1}$  versus  $\omega^2$ . This analysis yields a linear plot for a Drude metal [Eq. (1)], whose slope and intercept depend on the unscreened or "bare" plasma frequency  $\omega_p$  and  $\tau$  only, and not on  $\epsilon_\infty$ . The linear behavior at low energies is evident, the deviation from linearity at higher energy is due to the onset of interband absorption. The parameters obtained from the Drude analyses of R and  $\epsilon_2$  are found in Table I.

Referring to the schematic DOS diagram of Fig. 5, it is evident that charge neutrality and a stoichiometry  $C_{4n}KH_{x}$  (where  $n = 1,2$  is the stage index) (Ref. 4) yield the following relationship relationship among the fractional band occupations  $f_X$ 

$$
(fK - 1) + x(fH - 1) + 4nfC = 0 , \t\t(4)
$$

where  $f_X$  (X=K,H,C) represents the number of electrons per X atom in the respective K(4s), H(1s), and  $C(\pi^*)$ 



Density of States

FIG. 5. Schematic density of states for  $C_4KH_{0.8}$  and  $C_8KH_{0.8}$ . The H(1s) levels lie below the Fermi level  $E_F$  (dashed line) indicating the hydrogen is present as  $H^-$ .

FIG. 6. Plot of  $(\omega \epsilon_2)^{-1}$  vs  $(\hbar \omega)^2$  for C<sub>8</sub>K, C<sub>24</sub>KH<sub>0.8</sub>, and  $C_8KH_{0.8}$ . A linear curve indicates Drude behavior [Eq. (1)]. The corresponding values of the Drude parameters  $\omega_p$  and  $\omega_p \tau$ are given in Table I and are independent of the choice for the core dielectric constant  $\epsilon_{\infty}$  used to calculate R (dashed curve in Fig. 2).

bands(s). The reaction of KH with graphite has been reported to lead to a [H]/[K] ratio  $x=0.8$  for both the stage-1 and -2 hydrides.<sup>4</sup> If we adopt this value of x for the moment, and assume that the H levels (or band) lie below the Fermi level (i.e.,  $f_H = 2$ ), then Eq. (4) can be written as

$$
f_{\rm C} = (0.2 - f_{\rm K})/4n \tag{5}
$$

We can describe the stage-1 two-dimensional (2D)  $\pi^*$ conduction-band either by the tight-binding band model of Blinowski et  $al$ .<sup>32</sup> or the linear combination of atomic orbitals model of Holzwarth.<sup>33</sup> Previous work<sup>34</sup> has shown that both these models yields approximately the same values for  $m_{\text{opt}}$  for stage-1 GIC's, provided a value of the C-C intralayer interaction  $\gamma_0$  ~ 2.9 eV is used in the model of Blinowski et al.<sup>32</sup> The bare plasma frequency for the stage-1 GIC is given in the Blinowski model by

$$
\omega_p^2 = 4e^2 E_F / \hbar^2 I_c \quad \text{(stage 1)}\,,\tag{6}
$$

where  $E_F$  is given by

$$
E_F = \gamma_0 (\sqrt{3} \pi f_C)^{1/2} \text{ (stage 1 and 2)}.
$$
 (7)

Using Eqs. (2), (3) and  $(5)$ - $(7)$  we express the bare plasma frequency as a sum of contributions from the  $\pi^*$  and  $K(4s)$  bands in terms of the fractional occupation of the K(4s) band  $f<sub>K</sub>$ . The first and second terms on the righthand side in Eq. (8) are, respectively, from the  $\pi$  and  $K(4s)$  bands,

$$
\hat{\hbar}^2 \omega_p^2 (eV^2) = 7.87 \gamma_0 (0.2 - f_K)^{1/2} + 15.4 f_K / m_K \ (C_4 K H_{0.8}) ,
$$
 (8)

where  $m_K = m_{\text{opt}, K} / m_e$ , and  $m_e$  is the electronic mass. We note that if  $f<sub>K</sub> = 0$ , the  $K(4s)$  band is empty, and if  $f_K = 0.2$  the  $\pi$  band is empty (assuming [H]/[K]=0.8). In the left-hand panel of Fig. 7 we plot on an expanded vertical scale the square of the calculated plasma frequency versus  $f_K$  [Eq. (8)] for two choices of  $m_K$  and  $\gamma_0$ .  $\omega_p^2$ decreases for increasing  $f<sub>K</sub>$  because the optical mass of the  $\pi$  electrons is considerably less than the free-electron mass values  $m_K = 1-2$  chosen for the K(4s) electrons. The values of  $\gamma_0$  used are consistent with Holzwarth<sup>33</sup> and those used previously to describe optical results in graphite-SbCl<sub>5</sub> (Ref. 18) and graphite-H<sub>2</sub>SO<sub>4</sub> (Ref. 34). However, St. Jean et al.<sup>35</sup> report somewhat lower values of  $\gamma_0$  (2.6 eV for stage 1 and 2.8 eV for stage 2) on the basis of similar reflectance studies of graphite- $H_2SO_4$ . As is evident from the left-hand panel of Fig. 7, values for  $\gamma_0$  < 2.9 eV strengthen the argument that the K(4s) band is empty in  $C_4KH_{0.8}$ . The upper and lower arrows on the ordinate indicate, respectively, our experimental values for the most probable value of  $\omega_p^2$  and the lower bound for  $\omega_p^2$ , consistent with an experimental uncertainty in the plasma frequency of  $\pm 0.1$  eV. The most probable experimental value for  $\omega_n^2$  lies above the uppermost calculated curve, indicating the  $K(4s)$  band is probably empty. However, our estimate for the lower bound on  $\omega_p^2$  cuts the upper curve at a very small value  $f_{K}$  ~0.02 electrons per K atom which represents the maximum occupation in the  $K(4s)$  band in the stage-1 hydride consistent with the in-



FIG. 7. Square of the plasma frequency  $(\omega_p^2)$  vs  $f_K$ , where  $f<sub>K</sub>$  is the fractional occupation of the K(4s) band. The lefthand panel is for stage-1  $C_4KH_{0,8}$  and the right-hand panel is for  $C_8KH_{0.8}$ . The curves are calculated according to the model described in the text for the values of the parameters ( $\gamma_0, m_K$ ) shown.  $\omega_p^{\text{expt}}$  indicates the most probable value of the experimental plasma frequency.  $\omega_p^2$  is uncertain to  $\pm \Delta$ .  $\omega_p^2 - \Delta$  cuts the calculated curves as shown and leads to the corresponding estimate for the upper bound of  $f<sub>K</sub>$  for the stage-1 and -2 hydrides.

traband optical data and  $\Delta \omega_p = \pm 0.1$  eV. This small value of  $f<sub>K</sub>$  coupled with a large value of  $I<sub>c</sub>$  indicate that  $C_4KH_{0.8}$  should exhibit a high electrical anisotropy, more in line with a typical stage-1 acceptor GIC rather than a typical stage-1 binary donor GIC.

Our stage-1 value for  $\omega_p(C_4KH_x) = 3.31$  eV may be interpreted from another perspective. We assume the  $K(4s)$ band is empty and calculate the value  $x = [H]/[K]$  consistent with a 2D analysis for the  $\pi^*$  band [Eqs. (6) and (7) and  $\gamma_0$ =2.9 eV) and H levels which lie below  $E_F$ . We then find that  $x=0.79\pm0.02$  using the model of Blinowski et al.<sup>32</sup> Using the results of Holzwarth<sup>33</sup> we find  $x=0.80\pm0.02$ . Both values of x are in excellent agreement with the reported experimental value ( $x = 0.8$ ) based on chemical analysis.<sup>4</sup> In Table I we list the value for  $E_F$ for  $C_4KH_{0.8}$  obtained from the experimental bare plasma frequency and the models of Holzwarth ( $E_F=1.53$  eV) and Blinowski ( $E_F = 1.62$  eV). The Blinowski model<sup>32</sup> result is higher due to the K point expansion used as an approximation to recover explicit formulas which relate  $E_F$  to  $f_C$ .

We next analyze the stage-2 plasma frequencies in the same way, using the stage-2 relationship for  $\omega_{n}(E_{F})$  (Ref. 32) and Eqs.  $(2)$ – $(5)$  and  $(7)$ , to develop a numerical relationship between  $\omega_p$  and  $f_K$  the fractional K(4s) band occupation. For the case of the binary  $C_{24}K$  compound, the experimental value of  $\omega_p = 4.20 \pm 0.1$  eV results in  $f_K = 0$ (i.e., complete charge transfer) and  $f_c = 1/(23.7 \pm 0.12)$ , in excellent agreement with the expected average

stoichiometry for stage-2 graphite- $K^{5,6}$ . For the stage-2 hydride, the numerical relation  $\omega_p^2$  versus  $f_K$  is plotted in the right-hand panel of Fig. 7 for (1) the values of  $\gamma_0$  and the K electron optical mass  $m_K$  shown, (2)  $I_c = 8.53 \text{ Å}$ ,<br>and (3)  $\gamma_1 = 0.375 \text{ eV}^{32,18}$  where  $\gamma_1$  is the C-C *interlayer* interaction. As in the case of the stage-1 hydride, the most probable experimental value for  $\omega_p^2 = (3.26 \text{ eV})^2$  lies slightly above the curves. Our lower estimate for  $\omega_p^2$ , consistent with an experimental uncertainty  $\Delta \omega_p = \pm 0.1$  eV, sistem with an experimental uncertainty  $\Delta \omega_p = \pm 0.1$  eV,<br>cuts the upper curve  $\gamma_0 = 3$  eV,  $m_K = 1$ . In this latter case we obtain  $f_{\rm K}$  ~0.03 electrons per K atom for an upper bound for the fractional occupation of the K(4s) band for the stage-2 hydride with stoichiometry  $C_8KH_{0.8}$ .

On the other hand, if we (1) assume the  $K(4s)$  band is empty and the H(1s) levels lie below  $E_F$ , (2) use the stage-2 band model of Blinowski *et al.*,  $32$  and (3) use our value for  $\omega_p = 3.26 \pm 0.1$  eV, we find  $x = [H]/[K]$  $=0.78\pm0.02$ , in excellent agreement with  $x=0.8$  determined by Guérard et al. using chemical analysis.<sup>4</sup>

The presence of the hybridized graphitic states in  $C_8K$ which are zone folded to the  $\Gamma$  point by the  $(2\times2)R0$  K superlattice probably overextends the application of a simple two-carrier model to interpret a value for  $\omega_p$  in this compound. Nevertheless, we proceed as follows to see what values of  $f<sub>K</sub>$  are obtained. For the  $\pi$  band we use the numerical results for the optical mass obtained from Holzwarth<sup>33</sup> because the K point expansion of Blinowski et al.<sup>32</sup> is expected to break down for large  $f<sub>C</sub>$  or large Fermi wave vector  $k_F$ . For the  $\Gamma$  point K(4s) [or K(4s)- $\pi$  hybridized] electrons we use an isotropic mass  $m<sub>K</sub>$ , and for charge neutrality we assume the relation  $8f_C+f_K=1$ (i.e., 1 e/K atom residing in either the  $\pi$  or K(4s) band]. The plasma frequency  $\omega_p$  is given [Eq. (2)] by  $[(\omega_p^{\mathbf{K}})^2 + (\omega_p^{\pi})^2]^{1/2}$ , where  $\omega_p^{\pi}$  and  $\omega_p^{\mathbf{K}}$  are the  $\pi$  and  $\mathbf{K}(4s)$ contributions. We find via numerical methods the selfconsistent solutions for C<sub>8</sub>K: (1)  $f_K = 0.55$  for  $m_K = 2m_e$ , and (2)  $f_{\text{K}} = 0.85$  for  $m_{\text{K}} = m_e$ . Thus we arrive at values for the  $K(4s)$  band population in  $C_8K$  larger than the theoretical results by Ohno et al.  $(f_{K} = 0.4)$ , <sup>36</sup> and much larger than that obtained by DiVincenzo and Rabii<sup>37</sup>  $(f_{K}-0)$  (Table I). We note that the values for which we could obtain  $f<sub>K</sub>$  by our simple two-band analysis would decrease further if increasingly larger values of  $m<sub>K</sub>$  are used in the model. It is important to note that the values of  $f_{\rm K}$  we have just obtained from the bare plasma frequency for  $C_8K$  are derived from a rigid-band model superimposing  $2D \pi$ -electron bands and a  $3D$  band for the  $K(4s)$  electrons ( $m_{opt}$  for the  $\Gamma$ -point carrier pocket is the adjustable parameter). This model necessarily ignores altogether the potentially important effects of  $K(4s)$ - $\pi$  hybridization near the K and M points in the  $\pi^*$  band, which is a central issue in the debate between the more complete band models of  $C_8K$ .<sup>36,37</sup> Using their bandstructure results ( $f_{K}$  ~0), DiVincenzo and Rabii<sup>37</sup> calculate a bare plasma frequency of 4.65 eV in good agreement with both our experimental value of  $\omega_p=4.5$  eV and the experimental value  $\omega_p=4.5$  eV obtained by Fischer et al.

We next turn to the quantitative information which can be obtained from the interband absorption threshold. The threshold for interband absorption is identified with the

rise in  $\epsilon_2$  with increasing  $\omega$  after the fall due to the freecarrier contribution, and is evident Figs 3 and 4. The arrows in the figures indicate the midpoint of the respective interband threshold, which we refer to as  $E<sub>T</sub>$ . If the interband threshold is due to transitions between carbon  $\pi$ (valence) and  $\pi^*$  (conduction) bands which have approximate mirror symmetry, then  $E_T \sim 2E_F$ . The bands near the K point in the model of Blinowski et al.<sup>32</sup> exhibit exact mirror symmetry (i.e.,  $E_T = 2E_F$ ), while the Holzwarth model<sup>33</sup> exhibits a slight asymmetry which introduces a correction  $\delta E$  at high charge transfer for donor-type GIC's (i.e.,  $E_T \sim E_F - \delta E$ , where  $\delta E$  increases with increasing  $E_F$  ( $\delta E \sim 0.1$  eV at  $E_F \sim 1.4$  eV). Thus the  $\pi$ - $\pi$ <sup>\*</sup> interband threshold represents another optical measure of  $E_F$ , independent of that obtained from the free-carrier plasma frequency. The  $\pi$ - $\pi$ <sup>\*</sup> interband threshold has been shown by Shung<sup>38</sup> to be theoretically broadened about  $\sim 2E_F$  due to electron scattering. Accordingly, we display in Table I the interband threshold energy  $E_T$  as the position of the midpoint of the initial rise in the interband contribution to  $\epsilon_2$ . Good agreement is thereby obtained between  $E_F$  obtained from  $\omega_p$  and that obtained from  $E_T/2$  for C<sub>24</sub>K, C<sub>4</sub>KH<sub>0.8</sub> and C<sub>8</sub>KH<sub>0.8</sub>, indicating that in these compounds the interband thresholds are properly identified with  $\pi$ - $\pi$ <sup>\*</sup> transitions. Values for  $f_c$  (number of electrons in  $\pi^*$  band per C atom) obtained from  $\omega_p$  also appear in Table I. We note (Table I) that in the case of the stage-1 hydride, where  $E_F$  is large, the agreement between  $E_F$  (determined by  $\omega_p$ ) and  $E_T/2$  is better within the Holzwarth model than in the Blinowski model. This is symptomatic of a breakdown of the Kpoint expansion approximation in the Blinowski model. We can compare our results for  $f_c$  and  $E_F$  in hydrides  $C_4KH_{0.8}$  and  $C_8KH_{0.8}$  to those obtained from Shubnikov—de Haas experiments by Enoki et al.<sup>39</sup> (Table I). Good agreement is obtained for the stage-2 hydride. However, agreement is not obtained for the stage-1 compound. The large disagreement in stage <sup>1</sup> may stem from he difficulty involved in observing the higher<br>Shubnikov—de-Haas-frequencies.<sup>43</sup>

For the case of C<sub>8</sub>K, we find  $(E_T/2)=1.6$  eV. Using the value  $\delta E \sim 0.1$  yields a value for  $E_F \sim 1.65$  eV, as compared to the value  $E_F = 1.4$  eV obtained from both  $C_8K$  band-structure calculations.<sup>36,37</sup> Disagreement between  $\pi$ -electron-derived values of  $E_F$  and  $E_T/2$  would be expected for  $C_8K$  on theoretical grounds because of the strong  $\pi$ -K(4s) band hybridization near  $E_F$  and interband transitions near  $\Gamma$  to K(4s)-derived states.<sup>36,37</sup> Our value of  $E_T = 3.2$  eV compares reasonably well with the theoretical value of 2.9 eV calculated by both DiVincenzo and Rabii<sup>37</sup> and Ohno et al.<sup>36</sup> Fischer et al.<sup>27</sup> report an experimental value of 2.7 eV for the onset, rather than the midpoint, of the interband threshold. From their data<sup>27</sup> we estimate  $E_T \sim 3.0$  eV in good agreement with our value.

### IV. CONCLUSIONS

We find the graphite- $KH_{x}$  optical data support the single-particle density of states shown in Fig. 5 in which the H(1s) levels lie below  $E<sub>F</sub>$ . The reflectance data were analyzed in terms of contributions from graphitic  $\pi$  elec-

In the case of  $C_8K$ , the observed bare plasma frequency and position of the interband threshold are in good agreement with a previous experimental study<sup>27</sup> as well as band-structure calculations by DiVincenzo and Rabii.<sup>37</sup> The optical results for  $C_{24}K$ ,  $C_4KH_{0.8}$ , and  $C_8KH_{0.8}$  are found to be well described by a 2D graphitic  $\pi$ -electron model. A rigid, nonhybridized band model used to interpret the optical results in C<sub>8</sub>K leads to values of  $f<sub>K</sub> < 0.5$ for values of the K(4s) electron optical mass  $m<sub>K</sub> > 2$ , compared to theoretical estimates of  $f_{\text{K}} = 0$  (DiVincenzo compared to theoretical estimates of  $f_{\text{K}}$  and Rabii<sup>37</sup>) and  $f_{\text{K}} = 0.4$  (Ohno *et al.*<sup>36</sup>).

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#### ACKNOWLEDGMENTS

We thank Dr. A. W. Moore of Union Carbide for his generous gift of the highly oriented pyrolytic graphite (HOPG) used in this study, Professor N. A. W. Holzwarth for original figures from her work in Ref. 33, and Professor J. P. Seleague for his guidance in preparing the KH powder for reaction. We are grateful to Professor H. Inokuchi and Dr. T. Enoki at the Institute for Molecular Science, Okazaki, for their efforts in organizing the recent topical conference on hydrogen in GIC's which we found very informative. The research was supported by the U.S. Department of Energy at the University of Kentucky (No. DE-EF05-84ER45151) and at Oak Ridge National Laboratory (No. DE-AC05-84OR2100), where one of us (P.C.E.) was on sabbatical leave during part of this research.

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