

Anisotropy of magnetic polarons bound to acceptors in $\text{Cd}_{1-x}\text{Mn}_x\text{Se}$

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Time-resolved donor-acceptor luminescence provides the main parameters of magnetic polarons bound to acceptors in $\text{Cd}_{1-x}\text{Mn}_x\text{Se}$. Time-resolved polarization of this emission with $\mathbf{H} \parallel \mathbf{c}$ in the Faraday geometry reveals the freezing of the polaron orientation at low temperature. This is related to the gyromagnetic factor $g_{\perp} = 0$ for the hole in wurtzite crystals, leading to a bistable magnetic polaron.

Among the properties of semimagnetic semiconductors,¹ one of the most noticeable is probably the formation of magnetic polarons bound to donors (D^0 -BMP)^{2,3} or acceptors (A^0 -BMP),⁴ caused by the exchange interaction between weakly bound carriers and the magnetic moments of Mn^{2+} ions. Up to now, BMP's were studied in cases where the exchange integrals (denoted usually $N_0\beta$ for free holes and $N_0\alpha$ for free electrons) were isotropic: Thus, these BMP's were free to orient their total magnetic moment in any direction. In wurtzite crystal, the top of the valence band is of Γ_9 symmetry, the gyromagnetic ratio vanishes for a magnetic field $\mathbf{H} \perp \mathbf{c}$ ($g_{\perp} = 0$),⁵ and that property is true also for the exchange integral ($N_0\beta_{\perp} = 0$). As a consequence, A^0 -BMP's in CdMnSe should have a strong tendency to align their magnetic moment parallel or antiparallel to the c axis. In a previous work, Heiman *et al.*⁶ studied the polarization of donor-acceptor (D - A) luminescence in CdMnSe in the Faraday geometry ($\mathbf{H} \parallel \mathbf{c}$) under dc conditions. They concluded that A^0 -BMP's did not have time to form below 10 K; a conclusion rather surprising considering the long lifetime of D - A emission.⁷

In this Rapid Communication, we present a time-resolved study of D - A luminescence in $\text{Cd}_{1-x}\text{Mn}_x\text{Se}$ which allows, from the shift of the band as a function of time and temperature T , to extract the exchange contribution $E_p(T)$ to the binding energy of the acceptor. With a magnetic field $\mathbf{H} \parallel \mathbf{c}$ applied, the time evolution of the circular polarization P_c ,⁸ which increases with time delay, gives evidence of the bistable character of A^0 -BMP's at low T .

The experiments are done on single crystals of $\text{Cd}_{0.95}\text{Mn}_{0.05}\text{Se}$ grown at the Institute of Physics of the Polish Academy of Sciences. The samples are analogous to those used for Raman spin-flip (RSF) experiments on D^0 -BMP's.² The excitation is provided by a dye laser modulated by an acousto-optic deflector (pulse width 200 ns, frequency 50 kHz, peak power 10 mW). The luminescence is analyzed by a double-grating monochromator and processed in the so-called "single photon counting" mode; a microcomputer programmed as a multichannel analyzer controls the data acquisition. Time-resolved spectra from 13000 to 15000 cm^{-1} with 10 cm^{-1} resolution were obtained during one hour of data accumulation. The precise line position and linewidth were obtained from calculations of the first and second moments.

Figure 1 shows the spectrum emitted at 4.8 K at different time delays. The D - A nature of the 14000 cm^{-1} band is already evidenced by the shift of the band with delay. The

line shape is somewhat broader at early time, but stabilizes after about 0.5 μs ; this is why we present quantitative analysis only for delay larger than 0.5 μs . Let us recall that the energy of a photon emitted by a D - A pair at separation R_{D-A} is given by

$$h\nu = E_G(T) - E_D - [E_A + E_p(T)] + e^2/KR_{D-A}, \quad (1)$$

where $E_G(T)$ is the band gap, E_D and E_A the binding energy of the donor and the acceptor, and e^2/KR_{D-A} the Coulomb interaction. Figure 2 gives the line position as a function of time delay at different temperatures. The time evolution, which depends only weakly on temperature, reflects the increase of $\langle R_{D-A} \rangle$ (from about 120 to 300 Å). The shift as a function of T reflects the evolution of $E_p(T)$, the polaron energy, which has been plotted in Fig. 3. To evaluate the main parameters of the A^0 -BMP, we use the so-called muffin-tin model,⁹ where the hole is coupled equally to N spins of $S = \frac{5}{2}$. In this approximation, the total energy is

$$E = \beta' \sigma M_z / 2\Omega + g \mu_B H M_z + A_1 M^2, \quad (2)$$

where M is the magnetization, M_z its component along the c axis, H the magnitude of the applied magnetic field parallel to c , $N_0\beta'$ the exchange integral for the acceptor, Ω the volume of the muffin tin, and $\sigma = \pm 1$ according to the two

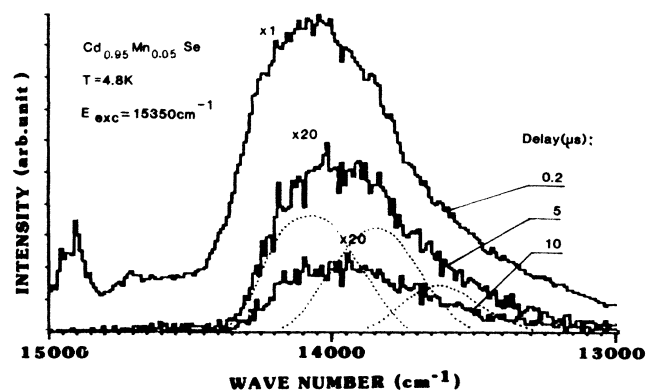


FIG. 1. Luminescence spectrum at different time delays (0.2, 5, 10 μs). The dotted curves suggest, for the 5 μs spectrum, a decomposition into a no phonon line and LO phonon replicas ($h\nu_{\text{LO}} \sim 26$ meV). The full width at half maximum of the no phonon line is about 46 meV.

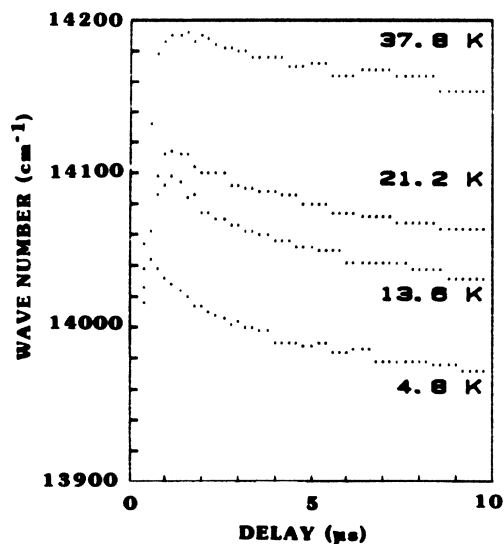


FIG. 2. Time evolution of the *D-A* line position at four different temperatures. The temperature dependence of E_G has been taken into account in order to display the temperature variation of $E_p(T)$.

possible hole states. The last term is an antiferromagnetic contribution, where $A_1 = 4kT_0/3N(S+1)S$. $E_p(T)$ is obtained as a thermal average of the first term in Eq. (2), which can be performed exactly. A good fit of $E_p(T)$, as shown on Fig. 3, is obtained by taking $N = 10$, the radius of the polaron 13.5 \AA ,¹⁰ and $N_0\beta' = -0.8 \text{ eV}$, a value lower than the free-hole value, $N_0\beta = -1.11 \text{ eV}$,¹¹ because a substantial mixing between *A* and *B* holes occurs in the acceptor wave function,¹² the *A-B* splitting being small with respect to E_A . The polaron energy $E_p(T)$ is larger than in $\text{Cd}_{1-x}\text{Mn}_x\text{Te}^4$ because β' is larger and the Bohr radius smaller [$E_p(0) = 50 \text{ meV}$]. Notice that a theoretical model is needed to place the base line in Fig. 3 and to determine E_A which is found equal to $100 \pm 5 \text{ meV}$. It was found that Li and Na give an acceptor level with $E_A = 109 \pm 6 \text{ meV}$ in CdSe.¹³

Time-resolved measurements of P_c were performed in a superconducting magnet up to 6 T, in the Faraday

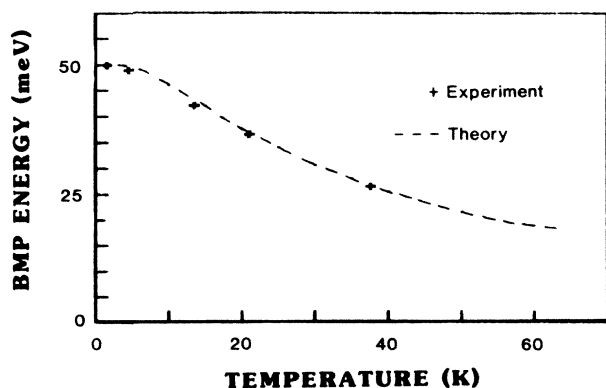


FIG. 3. Exchange contribution to $A^0\text{BMP}$ energy $E_p(T)$ has a function of T . \mp are experimental data. The dashed line is the theory.

geometry. If the acceptor retains pure Γ_9 symmetry, P_c is given by

$$P_c = (P_e + P_h)/(1 + P_e P_h) \quad (3)$$

where P_e and P_h are the donor and acceptor polarizations. Most of the data were taken at the peak of the *D-A* band; a few spectroscopic data show that P_c decreases slowly with decreasing wave number, a feature that might be related to participation of LO phonon replicas. The remarkable point is the *increase* of P_c with time delay. This is observed only for H not too large, away from saturation. Figure 4 shows the time evolution of P_c at a constant H/T value, at several temperatures. One can clearly see that the rate of change of P_c becomes very slow at low temperature. Such a behavior can be easily explained by Eq. (2): When $H = 0$, the total $A^0\text{-BMP}$ energy presents two equivalent minima for $M_z = \pm NS$ separated by a saddle point at $M = 0$. Since the polaron involves a rather large number of particles, we assume that tunneling may be neglected; hence, transfer from one minimum to the other requires a thermal activation over a potential barrier of the order of $E_p(0)$. This explains why the time to reach equilibrium between the two states split by $2g\mu_B HNS$ becomes long at low T . A thorough analysis of P_c is certainly beyond the scope of this paper. We would like to discuss two points.

(i) How to extract P_h from the measurements of P_c ? The donor polarization P_e is well known from RSF experiments and is close to that of the free electron if $H \geq 0.1 \text{ T}$; so it can be easily calculated. If it is introduced in Eq. (3), one finds a value of P_c already larger than the experimental one, even if $P_h = 0$. In particular, the value of P_c at saturation, P_{sat} , is only 75–80%. We think that the hole in the $A^0\text{-BMP}$ no longer has a pure Γ_9 symmetry since it is subjected to perturbations which do not possess axial symmetry: The magnetic moment of $A^0\text{-BMP}$ has a large component along the *c* axis, but due to magnetic fluctuations, it has a nonzero transverse component; in addition, the acceptor is perturbed by the random substitution of a few Mn atoms inside its orbit. We present a phenomenological model with one fitting parameter δ . Equation (1) of Ref. 11 suggests that, for an oblique perturbation, mixing occurs mainly

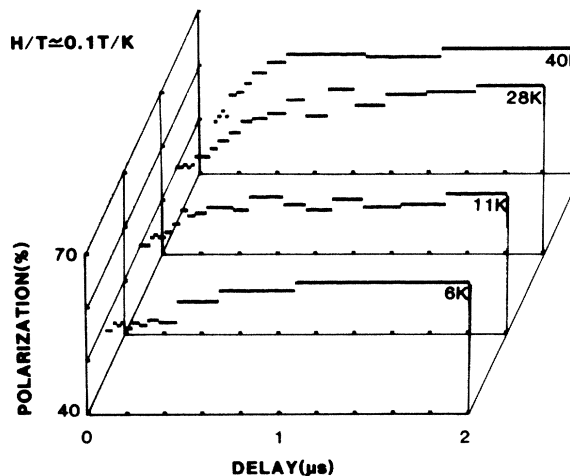


FIG. 4. Time evolution of the circular polarization P_c at different temperatures, for a constant ratio $H/T \sim 0.1 \text{ T K}^{-1}$.

between $|A, \frac{3}{2}\rangle$ and $|B, \frac{1}{2}\rangle$ holes. So we assume a hole state in the BMP of the following form: $|h+\rangle = (1-\delta^2)^{1/2} \times |A, \frac{3}{2}\rangle + \delta|B, \frac{1}{2}\rangle$ and $|h-\rangle$ its transform by time reversal. Then the new formula for P_c is

$$P_c = (GP_e + P_h)/(1 + GP_e P_h) \quad (4)$$

where $G = (3 - 4\delta^2)/(3 - 2\delta^2)$. Unfortunately, Eq. (4) implies a saturation $P_{c\text{sat}} = 1$, in contrast with experiment. We have to assume some kind of depolarization and define $P'_c = P_c/P_{c\text{sat}}$. Then, P_h can be obtained from Eq. (4), where P'_c is the experimental value and P_e the calculated one,

$$P_h = (P'_c - GP_e)/(1 - GP'_c P_e) \quad (5)$$

That procedure gives satisfying results at least for $T \geq 5$ K,¹⁴ assuming δ^2 of the order of 0.4. On Fig. 5, as a function of H , we compare the values of $P_h(2)$ at a delay of 2 μs with the thermodynamic equilibrium $P_{h,\text{th}}$ obtained by an appropriate average on Eq. (2). The values of $P_h(0)$ at zero delay are compared to the following model: Our sample is n type, so A^0 is photo-created when the field H is already present. The N spins in the box around A^- undergo magnetic fluctuations and one can readily calculate $P_{M_z}(H, T)$, the rate of "magnetic polarization." Figure 5 shows that, to a good approximation, $P_h(0) = P_{M_z}$. This means that if at the time of the hole capture, M_z points towards a given direction, then A^0 -BMP will develop its magnetization towards the same direction, independent of the spin polarization of the captured hole.¹⁵ $P_h(2)$ is found to be smaller than $P_{h,\text{th}}$ and the discrepancy seems to increase at low T . This is consistent with the model of A^0 -BMP orientation freezing.

(ii) How to justify the order of magnitude of the time constant of P_c as a function of T ? The rate of transfer U from one valley to the other is proportional to the probability of reaching the saddle point, assuming the polaron is in a given valley. With the model leading to Eq. (2), U is thermally activated by an energy $E_{ac} = 42$ meV at $H = 0$. Such a value of E_{ac} would probably induce a rather abrupt change in the P_c time constant at a temperature higher than observed. In fact, the property $g_{\perp} = 0$ for the hole is valid

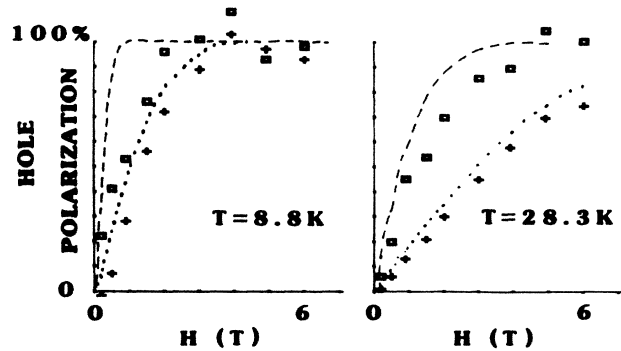


FIG. 5. Initial A^0 BMP polarization $P_h(0)$ (O) (+) compared to calculated P_{M_z} (dotted curve) and final A^0 BMP polarization $P_h(2)$ (□) compared to the calculated value at equilibrium $P_{h,\text{th}}$ (dashed curve), at two temperatures.

only to first order, i.e., for small transverse field. For large transverse magnetization, a type- A hole can gain exchange energy,¹¹ so that the saddle point does not occur at $M = 0$ but rather at $M = NS$, $M_z = 0$, with a substantial reduction of E_{ac} , maybe by a factor of 2. In addition, since the mean number of spins in the A^0 -BMP is 10, N should fluctuate from 6 to 14, inducing a broad distribution of E_{ac} values. These two facts justify probably the temperature range (10–40 K), where the P_c time constant is in the μs range.

To conclude, we have shown that, in wurtzite semimagnetic semiconductors (SMSC's), despite the fact that Mn^{+2} ions of S -like electronic configuration have essentially no anisotropy, the strong anisotropy of the Γ_9 hole is transferred to A^0 -BMP. If one could grow p -type $\text{Cd}_{1-x}\text{Mn}_x\text{Se}$, the component of magnetization related to A^0 BMP should exhibit magnetocrystalline anisotropy and hysteresis at low T . More theoretical studies of acceptors in wurtzite SMSC's are needed in order to bring interpretation on a more quantitative basis.

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⁸In this paper, the polarization rate P_i ($i = c, e, h, M_z$) is defined as $P_i = (P_i^+ - P_i^-)/(P_i^+ + P_i^-)$.

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¹⁰This radius corresponds to about $1.8a_B$, where a_B is the Bohr radius of an hydrogenic envelope function; after R. Planel, T. H. Nhung, G. Fishman, and R. Nawrocki, *J. Phys. (Paris)* **48**, 1071 (1984).

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¹⁴In addition to thermal excitation processes, the time evolution of P_h depends on preferential recombination on polarized electrons, which is dominant at 2 K: Then P_c (and thus P_h) decreases with time delay.

¹⁵A somewhat different situation, namely, the direct creation of localized excitons by polarized light (site selection) and subsequent development of a magnetic polaron was considered by J. Warnock, R. N. Kershaw, D. Ridgely, K. Dwight, A. Wold, and R. R. Galazka, *J. Lumin.* **34**, 25 (1985).