# Structural, electrical, and optical properties of  $a-Si_{1-x}Ge_x:H$ and an inferred electronic band structure

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Amorphous hydrogenated silicon-germanium alloys have been prepared over the full composition range by rf glow discharge of silane-germane mixtures at substrate temperatures between 200'C and 400 °C. A detailed description of the deposition apparatus, preparation procedures, and techniques of property measurement is given. The dependences on substrate temperature and germanium content of the optical-absorption, photoconductivity, and photoluminescence spectra and of the conductivity-temperature relation are reported and analyzed. Electronic band structures {density of states versus energy) are proposed which incorporate the changes in the optical energy gap with composition and the energies of the dangling-bond states on germanium and silicon atoms. The observed properties are examined in detail in relation to the proposed new density-of-states structure. The possibility is explored of explaining the poor photoelectronic properties with and without invoking a higher density of defects in the alloys. The occurrence of a two-phase heterostructure and the possibility of changes in its constitution, especially the location in it of the hydrogen, with changing substrate temperature and film composition are also discussed.

#### I. INTRODUCTION

Hydrogenated amorphous silicon-based binary alloys are currently a subject of much interest in the development of high-efficiency photovoltaic solar cells.<sup>1-4</sup> By alloying a-Si:H with such elements as Ge or Sn, it is possible to narrow the band gap and thus improve the longwavelength response. It appears that independent of the preparation method, rf sputtering,<sup>5,6</sup> cathodic sputtering,<sup>7</sup><br>dc glow discharge,<sup>8,9</sup> or rf glow discharge,<sup>1-3,10-12</sup> alloying Si with Ge leads to a deterioration of the photoelectronic properties. Such behavior is not peculiar to a- $Si_{1-x}Ge_x$ :H alloys or indeed narrow band-gap alloys. Similar findings have been reported for other alloy sys-<br>tems such as  $a-Si_{1-x}C_x:H^{13,14}$  and  $a-Si_{1-x}Sn_x:H^{15,16}$  At eported for other alloy sys-<br><sup>4</sup> and  $a-Si_{1-x}Sn_{x}$ :H.<sup>15,16</sup> At the time of writing, no solar cell utilizing a hydrogenated amorphous silicon-based binary alloy has a better efficiency than the best cells using a-Si:H. Indeed, no tandem solar cell incorporating such an alloy has a better efficiency than unalloyed nontandem solar cells. Paul and coworkers have already reported on the optical, electrical, and structural properties of  $a-Si_{1-x}Ge_x:H$  alloys prepared<br>by dc glow discharge<sup>8,9,17–19</sup> and rf sputtering.<sup>5,19,2</sup> '9,20 Some results have also been reported on unhydrogenated  $a-Si_{1-x}Ge_x$  produced by the latter method.<sup>5</sup> From the study of the dc glow discharge material, it was deduced that, normalized to the Si/Ge ratio, more H is bonded to the Si atoms than to the Ge.<sup>8,9,17,18</sup> (Similar findings have been recently reported for  $r f$  sputtered<sup>6</sup> and  $r f$  glow discharge<sup>21</sup>  $a-Si_{1-x}Ge_x:H$ .) It is therefore possible that Ge may be left with an associated higher density of (dangling-bond) defect states. Indeed, the ESR measurements of Morimoto et al.<sup>21</sup> indicate that the ratio of Ge dangling bonds to Ge atoms increases drastically with increasing  $x$ . However, it appears unlikely that this is the root cause of the inferior properties; work of von Roedern

et  $al$ <sup>9</sup> showed that the magnitudes of the photoconductivity and the photoluminescence (PL) are much larger than would be expected on this basis. (Recent work of Rudder *et al.*<sup>22</sup> using dual magnetron sputtering shows that the H attachment ratio can be normalized by varying the deposition conditions.) Another explanation has been put forward to explain the inferior properties. Paul but forward to explain the inferior properties. Paul *it al.*<sup>8,9,17,18</sup> inferred from hydrogen evolution experiments the existence of weakly bonded hydrogen in a-Ge:H and in  $a-Si_{1-x}Ge_x:H$  alloys containing a high Ge content. This suggested that the weakly bonded hydrogen could perturb the film structure resulting in heterostructure. The nature of the heterostructure may be responsible for the observed properties.

The present report concerns an investigation of the optical, electrical, and structural properties of  $a-Si_{1-x}Ge_x:H$ prepared by the rf glow discharge technique. Earlier work of this group<sup>20</sup> on the determination of the midgap density of states as a function of optical gap showed that for the same value of optical gap, sputtered  $a-Si_{0.7}Ge_{0.3}$ : H has a lower state density than sputtered unalloyed  $a$ -Si:H of different (lower) H content, and, again for the same optical gap, glow discharge  $a-Si:H$  has lower state density than sputtered a-Si:H. From this, it may be inferred that glow discharge  $a-Si_{1-x}Ge_x:H$  will possess a lower state density than sputtered  $a-Si_{1-x}Ge_x:H$  for the same optical gap. Thus, the present investigation is concerned with the properties of rf glow discharge  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>$ :H alloys as a function of substrate temperature and of  $a-Si_{1-x}Ge_x:H$  as a function of Ge content. All of the specimens were prepared in a deposition unit<sup>23</sup> which is capable of producing device grade a-Si:H as evidenced, for example, by' the low density of midgap states  $[-3 \times 10^{15} \text{ cm}^{-3} \text{eV}^{-1}$  by the space-charge-limited-current (SCLC) technique] $^{24}$  and the high sensitivity of the conductivity activation energy,<sup>25</sup> subband-gap absorption,<sup>24</sup>  $\mu\tau$  products,<sup>25</sup> and photoconductivity<sup>24</sup> to low levels (ppm range) of phosphorus doping. Care has been taken to eliminate or considerably reduce any known sources of impurities.

From correlations made between the optical, electrical, and structural properties new information is obtained about the alloys. A band structure for the  $x = 0.5$  alloy is suggested, which takes account of the different energies of electrons in Ge and Si dangling-bond states and of the shifts in the conduction- and valence-band edges with alloying. This new band structure is capable of rationalizing several of the observed photoelectronic properties, without requiring as large an increase in defect density as formerly for the best a-Si:H. The structural measurements support our earlier suggestion of increased heterostructure in the alloys, which implies that full understanding of the electrical and optical properties must eventually involve a more complete analysis of the band structures of both island and tissue material.

#### II. EXPERIMENTAL DETAILS

In this section, details are given'of our sample preparation and other experimental techniques.

#### A. Sample preparation

All of the samples were prepared as thin films by the rf glow-discharge decomposition of silane-germane mixtures. Figure <sup>1</sup> illustrates the main features of our deposition system.<sup>23</sup> A major consideration in the design of the system was the elimination or reduction of contamination from sources such as water vapor and oxygen that can result in inferior film properties.<sup>26–28</sup> Thus, the use of stainless-steel gas-feed lines which were short, a choice where possible of stainless-steel components in the deposition chamber, the baking of all stainless-steel parts including the joints, and the use of a turbomolecular pump capable of producing a high base vacuum were considered essential to reduce contamination to an acceptable level. As shown in Fig. 1, the deposition takes place within a plasma reactor that fits as an insert in an ultrahighvacuum (UHV) chamber. The plasma is confined to the reactor away from surfaces that could be sputtered. The majority of components of the reactor and the chamber are made from stainless steel and all joints are sealed by Cu gaskets. The short gas-feed lines to the system, the reactor, the joints, and the walls of the chamber are all bakeable. The reactor can be baked to a temperature of  $350-400$  °C. The system is evacuated by a turbomolecular pump which is backed by a rotary pump. Prior to deposition, after overnight bakeout, the base pressure is  $3 \times 10^{-8}$  Torr or better. During deposition, a residual gas analyzer  $(RGA)^{29}$  is used to monitor for impurities in the chamber. A qualitative analysis indicated that the main impurities detected,  $H_2O$  and  $CO_2$ , are present relative to the highest peak in the RGA spectrum  $(m/e=30,$  the main peak of  $SiH<sub>4</sub>$ ) in levels of 50 and 150 ppm, respectively. During deposition, with the main gate valve closed, the chamber is pumped via the throttle valve by the turbomolecular pump. The desired pressure in the chaxnber is set on a pressure controller unit which is electrically interfaced with the baratron pressure gauge and



FIG. 1. (a) Schematic of the rf glow discharge deposition system. (b) Details of the plasma reactor.

the throttle valve. In the reactor, the substrates are mounted upside down (to reduce pinhole problems associated with dust) on a heated ungrounded (floating) electrode. The thermocouple used to measure the substrate temperature is embedded in the copper heater block on which the heated electrode is mounted. The  $SiH<sub>4</sub>$  and  $GeH<sub>4</sub>$  gases are admitted via separate electronic flow controllers into a short common mixing manifold before entering the reactor. The gas mixture flows radially inward between the heated electrode and the rf electrode below. The electrode configuration is asymmetric; the heated electrode is the larger and is 10 cm in diameter. As a matter of safety, the exhaust gases are diluted with nitrogen gas after the turbo pump then passed via the rotary pump into a furnace where they are decomposed at a temperature of about 800'C. The furnace is vented outside the laboratory. An oil filtering system on the rotary pump is used to remove the particulates created by the reaction of the gases and the hydrocarbon pump oil. The furnace and filtering system, together with the rotary pump, are enclosed in a fume cabinet while the toxic gases are located in a separate cabinet. The  $SiH<sub>4</sub>$  and  $GeH<sub>4</sub>$ gases are supplied by Matheson and both are 99.99% pure. Contamination, sometimes severe, of SiH<sub>4</sub> with chlorosilanes, has been reported by Corderman and Vanier.<sup>30</sup> However, RGA analysis shows no chlorosilanes in excess of the ppm level in the gases we have used.

All of the specimens were prepared at a frequency of 13.56 MHz. For the alloys, the chamber pressure was held constant at 0.25 Torr and the net rf power at 3 W. The  $a-Si_{0.5}Ge_{0.5}H$  alloys were prepared at various substrate temperatures covering the range 230 to 372'C. The  $SiH<sub>4</sub>$  and GeH<sub>4</sub> flow rates were kept fixed at 12 cm<sup>3</sup> at STP per minute (SCCM) and 3 SCCM, respectively. For this series of specimens, the average Ge content was  $52 \pm 1$ at. % as determined by electron microprobe. No correlation was found between Ge content and substrate temperature  $T_s$ . Films of a-Si<sub>1-x</sub>Ge<sub>x</sub>:H with x values ranging from 0.14 to 0.74 were grown at 300°C. The  $SiH<sub>4</sub>$ flow rate was kept at 12 SCCM and the GeH<sub>4</sub> flow rate varied from 0.48 to 6.17 SCCM. The unalloyed a-Si:H films were prepared at a net rf power of 4 W,  $T_s$  of 230'C, pressure of 0.20 Torr, and SiH4 flow rate of 20 SCCM; these are the conditions that give films of suitable quality for device applications. The unalloyed a-Ge:H specimens were prepared at a net rf power of 3 W,  $T_s$  of 260 °C, pressure of 0.25 Torr, and GeH<sub>4</sub> flow rate of 10 SCCM. Deposition rates were between 80 and 200  $\mathring{A}$  min<sup>-1</sup> and the specimen thicknesses ranged from 1 to 11  $\mu$ m. In each run, films were co-deposited on a selection of different substrates necessary for the different types of experiments described below. In all cases, the substrates, excluding the fragile microgrids used for electron microscopy, were ultrasonically cleaned in baths of trichloroethylene, acetone, and methanol and then dried with  $N_2$  gas before loading into the system.

Over 40 sets of films have been prepared for this work under the variety of deposition conditions described below. Good run-to-run reproducibility of the measured properties has been found for specimens prepared under nominally identical deposition conditions.

### B. Experimental techniques

In this section, brief details are given of the experimental techniques employed to study the alloys. These are electron microprobe analysis, photoluminescence, photoconductivity, dc conductivity, optical and ir absorption, and transmission electron microscopy. A more detailed description of the electron microprobe, photoluminescence, and photoconductivity apparati can be found in Refs. 9, 31, and 32, respectively.

Electron microprobe analysis<sup>9</sup> was used to determine x, the atomic concentration. of Ge relative to Si in the a- $Si_{1-x}Ge_x:H$  alloys. The measurements were performed using a Cameca MBX unit with Tracor Northern automation on films grown on Cr-coated Corning 7059 glass.

Probing several regions of each specimen indicated compositional nonuniformity of Si and Ge over areas  $16\times16$  $\mu$ m<sup>2</sup> of less than 1 at. %, the sensitivity of the probe.

Photoluminescence samples were deposited on 7059 glass substrates, which had been roughened so as to eliminate interference fringes. Steady-state photoluminescence spectra at 77 K were measured in reflection geometry using 2.41-eV Ar-ion laser excitation, a glass prism monochromator, and a thermoelectrically cooled PbS detector with lock-in detection. All spectra were corrected for system spectral response. The resolution of the measurement was approximately  $0.02$  eV.<sup>31</sup>

Room-temperature photoconductivity measurements<sup>32</sup> were carried out on films prepared on 7059 glass using a coplanar electrode configuration. Evaporated Cr contacts were found to have ohmic behavior both in the dark and under illumination over the range of the applied field used (50–500 V cm<sup>-1</sup>). The photoconductivity was measured under our standard conditions, i.e., flux of 10<sup>15</sup> phocons cm<sup>-2</sup>s<sup>-1</sup> at an energy of 1.96 eV. All values of photoconductivity in this paper are corrected for the penetration depth of the light in the samples as deduced from the optical-absorption spectra. The spectral dependence of the photoconductivity using the constant photocurrent method $^{33,34}$  was also investigated. These data were used to extend the optical-absorption spectra to lower energies. $32$  The temperature dependence of the dark dc conductivity was also studied on similar structures over the range from about 294 K to about 475 K.

The optical transmission of films prepared on 7059 glass was measured using a Varian model no. 2390 double-beam spectrophotometer over the wavelength range 0.6 to 2.6  $\mu$ m. Information was obtained on the optical-absorption edge, refractive index  $n$ , film thickness d, and the optical gap. We define the optical gap as  $E_{04}$ ,  $35-38$  the energy at which the optical-absorption coefficient,  $\alpha$ , is equal to  $10^4$  cm<sup>-1</sup>. From the transmission maxima, we obtain the position and order of the interference fringes in a nonabsorbing region of the spectra. To those we then fit a parabolic expression for  $n$  as a function of energy using an assumed approximate film thickness. The measured asymptotic transmission at 2  $\mu$ m is then used to scale the deduced value of  $n$  and to provide a correct film thickness. These values were then used in the calculation of the optical-absorption coefficient,  $\alpha$ , using standard optical formulae.<sup>39</sup>

The infrared-absorption spectra were recorded by a Perkin Elmer model no. 567 double-beam spectrometer. The spectra were obtained by placing a film (grown on roughened crystalline Si to eliminate interference fringes) in one beam and a matched piece of roughened crystalline Si in the reference beam. Spectra were taken in the frequency range between 200 and 4000  $cm^{-1}$ . An estimate of the total hydrogen content,  $C_H$ , was obtained from the integrated absorption associated with the Si-H/Ge-H wag modes centered in the region  $550-650$  cm<sup>-1</sup> using the expression

$$
C_{\rm H} = m A_w \t{1}
$$

where  $C_H$  is in at. %, m is constant, and  $A_w$  (eV cm<sup>-1</sup>) is the integrated absorption coefficient of the wag vibrations calculated by a Gaussian fit. Respective values for  $m$  of 0.62, 0.37, and 0.39 at. %/eV cm<sup>-1</sup> were taken for a-Si:H,  $a$ -Ge:H, and the alloys.<sup>40-42</sup>

Transmission electron microscopy was carried out on a variety of alloys prepared under different conditions using a Philips model no. EM 300 electron microscope. The films for this study were deposited directly on C-coated Ni microgrids. The C layer was about 100 A thick, and the films about 500 A, as deduced from the deposition rate and time.

### III. VARIATION WITH  $T_s$  OF THE ELECTRICAL AND OPTICAL PROPERTIES OF  $a-Si_{0.5}Ge_{0.5}H$

It has been well established that the optical and electrical properties of glow discharge  $a$ -Si:H and  $a$ -Ge:H depend critically on the deposition temperature as a result of changes in the hydrogen content and the density of defects, which alter the size of the optical gap and the distribution of states in the band gap. Our first step in the study of  $a-Si_{1-x}Ge_x:H$  was to determine the optimum deposition temperature for films of roughly equal Si and Ge concentrations. We produced a series of samples holding all parameters constant except  $T_s$ , which was varied over the range 230 to 372 °C. The samples had good surface continuity, few pinholes, and excellent adhesion. The measurements described in Sec. IIB were made on codeposited samples. In Fig. 2, data are presented for the optical gap,  $E_{04}$ , the energy of the photoluminescence peak,  $E_{PL}$ , and the full width at half maximum of the peak,  $\Delta E_{PL}$ , for the sample series.  $E_{04}$  and  $E_{PL}$  show the same linear decrease with increase of  $T_s$ .  $\Delta E_{PL}$  is not a strong function of  $T_s$ . The hydrogen content,  $C_H$ , for these specimens was calculated from the integrated absorption of the infrared wag modes using Eq. (1). As shown in Fig. 3,  $C_H$  decreases monotonically from about 13 at. % at 230 °C to about 4 at. % at 372 °C.



FIG. 2. Energy gap  $E_{04}$ , energy  $E_{PL}$ , and width  $\Delta E_{PL}$  of the photoluminescence peak versus substrate temperature  $T_s$  for a- $Si<sub>0.5</sub>Ge<sub>0.5</sub>:H.$ 



FIG. 3. Hydrogen content  $C_H$  versus substrate temperature  $T_s$  for  $a-Si_{0.5}Ge_{0.5}$ :H.



FIG. 4. (a) Photoconductivity  $\Delta \sigma$  versus substrate temperature  $T_s$  for a-Si<sub>0.5</sub>Ge<sub>0.5</sub>:H. (b) Photoluminescence peak intensity  $I_{PL}$  versus substrate temperature  $T_s$  for  $a-Si_{0.5}Ge_{0.5}H$ .

In Fig. 4, we show the photoconductivity,  $\Delta \sigma$ , and the photoluminescence peak intensity,  $I_{PL}$ , for the same series of samples. The magnitude of  $\Delta \sigma$  is known to depend critically on the Fermi-level position. In the present series of specimens, the Fermi level is essentially independent of  $T<sub>g</sub>$ , lying close to midgap, and we choose to use  $\Delta \sigma$  as an indicator of the relative photoelectronic quality of the specimens. As shown in Fig. 4, the magnitudes of both  $\Delta \sigma$  and  $I_{PL}$  initially rise by about an order of magnitude as a function of  $T_s$  and peak at around 300°C. Above about 300 $^{\circ}$ C,  $I_{PL}$  decreases by an order of magnitude and  $\Delta \sigma$  by a factor of 2. Because  $I_{PL}$  has been shown to correlate with the density of states near midgap in a- $Si_{1-x}Ge_x$ :H (Ref. 20) and because  $\Delta\sigma$  and  $I_{PL}$  are general indicators of the photoelectronic quality of the films, we use the deposition temperature of 300'C, which provides close to the highest values of both these quantities in this film series, as the optimized substrate temperature for the  $a-Si_{1-x}Ge_x$ :H films prepared subsequent to this series.

We have also determined that the photoelectronic properties improved somewhat as the rf power was reduced below 3 W, but the improvement was not considered sufficient to offset the disadvantage of a decreased deposition rate ( $\lt$  80 Å min<sup>-1</sup>). Powers of 5 W, on the other hand, tended to produce samples with inferior physical properties. In consequence, a power level of 3 W was adopted for the study of alloys of different  $x$ .

# IV. VARIATION WITH x OF THE ELECTRICAL AND OPTICAL PROPERTIES OF  $a-Si_{1-x}Ge_x:H$

After optimization of the deposition parameters for a- $Si<sub>0.5</sub>Ge<sub>0.5</sub>$ :H films, we kept these parameters fixed and varied the flow rate of the GeH4 to produce samples of



FIG. 5. Absorption coefficient  $\alpha$  versus photon energy  $h\nu$  for the  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>:H$  alloys indicated. The solid lines and symbols denote the respective regions of the spectra deduced from optical transmission and from photoconductivity.

various compositions in the range of  $x$  from 0.14 to 0.74. We again measured the optical, electrical, and structural properties of the co-deposited samples.

In Fig. 5, absorption spectra are shown for a series of  $a-Si_{1-x}Ge_x:H$  alloys of different x prepared at 300°C, together with data for an  $a-Si_{0.98}Ge_{0.02}$ : H alloy prepared at 230 $^{\circ}$ C, and an unalloyed a-Ge:H specimen prepared at 260'C. The spectra of the alloys were extended to subband-gap energies using the constant photocurrent method.  $3\overline{3}$ ,  $3\overline{4}$  The photoconductivity-derived part of the absorption spectrum was normalized to the part from direct optical transmission measurements in the range of overlap at higher photon energies in the band tails near an  $\alpha$  of 10<sup>3</sup> cm<sup>-1</sup>. In Fig. 5, the solid lines and the symbols denote the respective regions of the spectra deduced from optical transmission and from photoconductivity. The absorption spectrum of the  $a-Si_{0.98}Ge_{0.02}$ : H alloy is almost the same as that of a-Si:H. The spectra are observed to shift smoothly to lower energies and the subband-gap absorption to increase with Ge content. Also, the. slope of the exponential edge, which can be accurately measured up to  $x$  of about 0.5, decreases with increasing Ge content by about 30%. We take this as an indication that alloying leads to an increase in the width of the valence-band tail. The oscillations observed in these spectra are caused by optical interference effects in the thin samples.

In Fig. 6, dark conductivity versus inverse temperature data are presented for some of the specimens from Fig. 5 and for representative samples of unalloyed a-Si:H and a-Ge:H. All specimens were heated under vacuum to about 210'C before the measurements were performed, in order to ensure that any photoproduced defects (Staebler-Wronski effects<sup>43</sup>) were annealed out. All specimens exhibited activated transport and the conductivity,  $\sigma$ , is observed to increase with Ge content. For the alloys,  $\sigma$  is singly activated over almost 4 orders of magnitude. Figure 7 shows the variation with  $x$  of the transport activa-



FIG. 6. Dark conductivity  $\sigma$  versus inverse temperature. The numbers in parentheses identify the samples.







tion energy  $(E_c - E_F)_0$ , deduced by a fit of the conductivity data to the relation

$$
\sigma = \sigma_0 \exp[-(E_c - E_F)_0 / kT]. \tag{2}
$$

A downward kink in  $ln \sigma(1/T)$  is observed for temperatures greater than 150-160°C (i.e.,  $10^3/T$  less than 2.31–2.36 K<sup>-1</sup>) for alloys of composition  $x = 0.14$  to 0.64 prepared at 300 °C and also for the  $a-Si_{0.98}Ge_{0.02}$ :H film prepared at 230'C. The unalloyed specimens, particularly a-Ge:H, show signs of slight curvature in  $ln\sigma(1/T)$ .

In Fig. 8 are presented the measured  $E_{04}$ ,  $E_{PL}$ , and  $\Delta E_{\text{PL}}$  for samples of the same series as reported in Fig. 5. There is a single photoluminescence band for all samples, except for the films with  $x = 0.74$  and  $x = 1$ , where no photoluminescence was detected. Linear dependences on x are found:



x. (b) Energy  $E_{PL}$  and width  $\Delta E_{PL}$  of the photoluminescence peak of  $a-Si_{1-x}Ge_x:H$  as a function of x.

FIG. 9. (a) Variation of the pbotoluminescence peak intensity  $I_{PL}$  with x for  $a-Si_{1-x}Ge_x:H$ . (b) Variation of the photoconductivity  $\Delta \sigma$  with x for a-Si<sub>1-x</sub>Ge<sub>x</sub>:H.

$$
E_{04} = 1.92 - 0.79x \, (eV) \tag{3}
$$

$$
E_{\rm PL} = 1.33 - 0.84x \, \text{(eV)} \,, \tag{4}
$$

$$
\Delta E_{\rm PL} = 0.291 - 0.038x \, \text{(eV)} \,. \tag{5}
$$

It is essential to comment immediately that the influence of varying  $C_H$  on these relations is not clear. When the procedure to determine  $C_H$  from the integrated intensity of the wag modes in the infrared-absorption spectra is followed (see Sec. II B)  $C_H$  remains constant at about 8 at. % for x between 0 and 0.5. For  $x > 0.5$ ,  $C_H$  decreases and, in the unalloyed  $a$ -Ge:H samples, is only about 2 at. %. Given the sensitivity of  $E_{04}$  and  $E_{PL}$  to  $C_H$  in a-Si:H, one is surprised to find these parameters linearly dependent on x for  $x > 0.5$ . Discussion of this will be taken up in Sec. VI B.

In Fig. 9 we show the photoluminescence peak intensity,  $I_{PL}$ , and the photoconductivity,  $\Delta \sigma$ , for these samples as a function of Ge content.  $I_{PL}$  initially falls off gradually with Ge content up to  $x \sim 0.3$  then decreases rapidly by almost 3 orders of magnitude.  $\Delta \sigma$  exhibits a similar behavior with x. However, beyond  $x = 0.74$ ,  $\Delta \sigma$  is observed to increase. It is interesting that alloying  $a$ -Si:H with as little as 2 at. % Ge leads to a large improvement in  $\Delta \sigma$ . In considering an explanation of these results we must bear in mind that between  $x = 0$  and  $x = 0.02$  and between  $x = 0.74$  and  $x = 1.0$  the Fermi level (as deduced from the activation energy for conductivity) approaches the conduction-band edge.

# V. STRUCTURAL PROPERTIES OF THE  $a-Si_{1-x}Ge_x$ : H ALLOYS

In this section, results are presented on a structural examination of the  $a-Si_{1-x}Ge_x:H$  alloys using infrared spectroscopy and transmission electron microscopy. In particular, results are presented on the structural properties of  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>$ :H as a function of  $T_s$  and also  $a-Si<sub>1-x</sub>Ge<sub>x</sub>$ :H prepared at 300 °C as a function of  $x$ .

Figure 10 shows the infrared-absorption spectra of a- $Si<sub>0</sub>$ ,  $Ge<sub>0</sub>$ ,  $H$  grown at (a) 230 °C, (b) 275 °C, and (c) 312 °C. The three alloys are of similar thickness. The main absorption features are labeled in (a). The modes at 2000 and 2090 cm<sup>-1</sup> are stretch modes associated with Si-H entities. The corresponding stretch modes for Ge-H are at 1875 and 1975 cm<sup> $-1,44-\bar{51}$ </sup> The features near 845 and 885 cm<sup>-1</sup> are bending modes related to  $(SiH_2)_n$  complexes. The wagging modes from which  $C_H$  was calculated are centered at about 630 cm<sup>-1</sup>. At the lowest  $T_s$  of 230 °C, the Si—<sup>H</sup> bending modes are at their largest. The Si—<sup>H</sup> stretch mode is mainly centered at 2090  $cm^{-1}$ . Increasing  $T_s$  results in an increase in the intensity of 2000-cm<sup>-1</sup> absorption relative to the 2090-cm<sup>-1</sup> mode. At  $T_s$  of  $312^{\circ}$ C, the 2000-cm<sup>-1</sup> mode is now dominant over the  $2090 \text{-cm}^{-1}$  modes and the Si-H bending modes are much less prominent. The infrared-absorption spectra of the a- $Si_{1-x}Ge_x$ :H alloys prepared at 300°C have also been studied. The addition of 14 at. % Ge to  $a$ -Si:H does not lead to any appreciable changes in the absorption spectra, i.e, the Si-H stretch mode at 2000 cm<sup>-1</sup> is dominant and the Si—<sup>H</sup> bending modes are very small. With increasing Ge



FIG. 10. Infrared spectra of  $a-Si_{0.5}Ge_{0.5}H$  prepared at  $T_s = (a)230$ °C, (b) 275°C, and (c) 312°C. The main absorption features are labeled in (a). The numbers in parentheses identify the samples.

content, the Ge—<sup>H</sup> stretch modes increase, as does the  $2090\text{-cm}^{-1}$  mode, however, the  $2000\text{-cm}^{-1}$  mode remains dominant. The Si—<sup>H</sup> bending modes remain very small.

The spectra of the  $a-Si_{1-x}Ge_x:H$  alloys are recorded immediately upon removal from the UHV deposition chamber. The spectra of several different types of specimens have been monitored closely as a function of time after the initial measurement. It is found that when the  $2090$ -cm<sup>-1</sup> mode is dominant over the 2000-cm<sup>-1</sup> mode, e.g.,  $a-Si_{0.5}Ge_{0.5}H$  prepared at  $T_s = 230^{\circ}C$ , films show signs of oxygen incorporation from the atmosphere. Figure 11 shows the changes in the measured absorption spectra with time of an  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>$ :H specimen grown at 230'C. After a few days a broad absorption band between  $800$  and  $1200 \text{ cm}^{-1}$  becomes evident and then is observed to rapidly increase in magnitude with time. This band has been attributed to oxygen incorporation.<sup>53</sup> Superimposed on this band are modes at 980 and 1050 cm $^{-1}$  which are associated with Si-0 entities. On some samples, a distinct distortion in the Si—<sup>H</sup> bending modes is observed. This may be due to the presence of <sup>a</sup> Ge—0 vibrational mode at 860 cm<sup> $-1.54$ </sup> (The unalloyed *a*-Ge:H films prepared for



FIG. 11. Changes in the infrared spectrum with time of an  $a\text{-Si}_{0.5}\text{Ge}_{0.5}$ :H sample prepared at 230 °C.

this work showed strong evidence of a vibrational mode at  $860 \text{ cm}^{-1}$ . The intensity of this absorption is observed to grow rapidly with time.) An estimate of the oxygen content in the  $a-Si_{0.5}Ge_{0.5}H$  alloy was calculated from the expression,

$$
C_0 = m A_0 \t{6}
$$

where  $C_0$  is the atomic percentage of oxygen, *m* is a con-<br>stant (=0.156 at. %/eV cm<sup>-1</sup>),<sup>55</sup> and  $A_0$  is the measured integrated absorption coefficient of the Si—0 bond centered at  $1050 \text{ cm}^{-1}$ . Figure 12 shows the estimated oxygen content of the  $a-Si_{0.5}Ge_{0.5}H$  sample from Fig. 11 as a function of time. The oxygen content is of the order of a few percent. Also included in the figure for comparison are results for an  $a-Si_{0.5}Ge_{0.5}$ : H specimen prepared similarly but covered with about 1000  $\AA$  of  $a$ -Si:H. The  $a$ -Si:H layer reduces the rate of oxygen uptake, demonstrating the atmospheric origin of the oxygen.

Figure 13 shows transmission electron microscopy (TEM) photographs of  $a-Si_{0.5}Ge_{0.5}H$  prepared at 230°C and 300'C. Both specimens exhibit microstructure in the form of noncoalescing regions of high electron density in a honeycomb network of lower density material. These regions are of the order of <sup>100</sup>—<sup>500</sup> <sup>A</sup> in size. On average, the dimensions of the regions in the specimen prepared at 300'C are much smaller than for the films deposited at 230 C. No clearly discernible microstructure

 $(a)$ 





FIG. 12. Estimated oxygen content  $C<sub>0</sub>$  as a function of time for the  $a-Si_{0.5}Ge_{0.5}H$  sample from Fig. 11. For comparison, results are shown for a similarly prepared a1loy capped with a-Si:H. The numbers in parentheses identify the samples.

of this nature was observed in our unalloyed a-Si:H films. However, the unalloyed a-Ge:H samples showed microstructure on a scale of about 200 A.

#### VI. DISCUSSION

### A. Variation with  $T_s$  of the electrical and optical properties of  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>H$

The effect of an increase of preparation substrate temperature,  $T_s$ , on the properties of unhydrogenated a-



FIG. 13. Bright field TEM images of  $a-Si_{0.5}Ge_{0.5}H$  prepared at (a) 230°C and (b) 300°C.

Ge,<sup>5,56–58</sup> a-Si,<sup>5</sup> and a-Si<sub>1–x</sub>Ge<sub>x</sub>,<sup>5</sup> has already been studied. Among the results universally reported are a sharpening and a shift to higher photon energies of theoptical-absorption edge, and an increase in the photoconductivity. These and other results are consistent with a decrease in the density of states (DOS) near the edges of the valence and conduction bands, in the band tails, and in the band gap, and these in turn are consistent with the healing of the disordered network, both to decrease the topological disorder of the completely coordinated structure and to reduce the number of defects such as dangling bonds. It seems reasonable to expect the same effects for increases in  $T<sub>s</sub>$  for hydrogenated material.

The effect of an increase in  $T_s$  for hydrogenated material must, however, also take account of any changes in  $C_H$ with  $T_s$ . The variation of  $C_H$  with  $T_s$  for our samples of  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>$ :H is shown in Fig. 3. While this variation may be expected to depend in its detail on the method of preparation, the decrease in  $C_H$  with increase in  $T_s$  is qualitatively consistent with published data on  $a$ -Si:H.<sup>59</sup> It is also consistent with studies of the evolution of hydrogen when  $a$ -Si:H is annealed.<sup>60</sup>

The effect of *increased*  $C_H$  alone on the topological disorder, the defect density, and the electronic band structure is essentially equivalent to that of increased  $T_s$  for the unhydrogenated material: The hydrogen compensates dangling bonds, thus reducing the midgap state density; the hydrogen also forms <sup>a</sup> Si—<sup>H</sup> alloy, with reduced densities of states at the former valence- and conduction-band edges; and, by reducing the average coordination number, it facilitates a structure with smaller topological disorder. The overall results for changes with  $T<sub>s</sub>$  of the properties of the present hydrogenated alloys, taking into account both the effects of changing  $C_H$  and the explicit temperature effect, should be interpreted within this general framework.

We discuss first the linear decreases, at the same rate, of  $E_{04}$  and  $E_{PL}$  between 230 and 372 °C shown in Fig. 2. Apparently, for this range of  $T_s$ , the effect of a decrease in  $C_H$  with  $T_s$  is more important than the effect of network healing. This result is qualitatively consistent with earlier work that may be taken to estimate the two effects of  $T_s$  separately. (1) The explicit effect of  $T_s$  may be estimated from the change in optical gap of unhydrogenated a-Si, a-Ge, and  $a$ -Si<sub>1-x</sub>Ge<sub>x</sub>. Thus, Connell *et al.*<sup>58</sup> found a change of 0.2 eV for a  $T_s$  increase from 25 °C to 350 °C for a-Ge, while Paul et al.<sup>5</sup> found an increase of at most 0.08 eV for a  $T_s$  increase from 200 °C to 550 °C for a-Si, and of 0.1 eV for a  $T_s$  increase from 100 °C to 350 °C for  $a-Si_{0.45}Ge_{0.55}$ . (2) The effect of decrease in  $C_H$  with increase in  $T_s$  may be estimated from the change in optical gap of a-Si:H when  $C_H$  is changed at fixed  $T_s$ , as happens when the partial pressure of  $H_2$  is changed in the sputtering method of preparation. Such studies by ourselves suggest<sup>61</sup> a decrease in gap of about  $0.5$  eV when  $C_H$  is decreased from 15 at. % to 2 at. %, while Morel and Moustakas $^{62}$  find a decrease of about 0.25 eV for a similar decrease in  $C_H$ .

Combining these (admittedly) disparate sources of data suggests that an increase in  $T_s$  from 230 °C to 372 °C would lead to an increase in gap of about 0.06 eV due to the explicit  $T<sub>s</sub>$  effect, and a decrease of about 0.17 to 0.35 eV due to the  $C_H$  decrease. Thus, the actual experimental finding is rationalized.

Next we consider the changes with  $T_s$  of the electron photoconductivity,  $\Delta \sigma$ , and the photoluminescence peak intensity,  $I_{PL}$ , for  $a-Si_{0.5}Ge_{0.5}H$  shown in Fig. 4. The existence of an optimum  $T_s$  for the photoconductivity of rf glow discharge  $a-Si_{1-x}Ge_x:H$  alloys has also been report-<br>ed by Nakamura *et al.*<sup>63</sup> (200–250°C) and by Bullot ed by Nakamura *et al.*<sup>63</sup> (200–250°C) and by Bullot *et al.*<sup>11</sup> (280°C). We expect that the optimum  $T_s$  will depend on the method of preparation, the deposition system, and the Ge content. Taking into account also that the deposition temperature  $T_s$  is measured in different ways, the experimental observations in the literature may be taken as self-consistent.

The magnitude of  $\Delta \sigma$  depends on the electron trapping lifetime which is determined by the DOS distribution above the Fermi level and so by the energetic position of the Fermi level below the conduction band. However, for the  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>:H films investigated, the transport activa$ tion energy decreases by only 0.14 eV as  $T<sub>s</sub>$  is varied from  $230^{\circ}$ C to 372 °C. This small change suggests that the *ini*tial rapid increase of  $\Delta \sigma$  with  $T_s$  is attributable to a decrease in the DOS just above  $E_F$ . The initial rapid increase in  $I_{PL}$  is similarly consistent with a decrease in gap DOS; this correlation has been recently explicitly demonstrated for  $a-Si_{0.7}Ge_{0.3}H$  (Ref. 20) and  $a-Si:H$  (Ref. 31) through a comparison of PL magnitudes and the midgap state densities. Much recent work demonstrating that  $\Delta \sigma$ and  $I_{PL}$  increase with decreasing density of dangling bonds is suggestive of a decrease in such density in the present instance, but we have no explicit experimental proof identifying this defect as the cause.

The *initial* increases in  $\Delta \sigma$  and  $I_{PL}$  are consistent with the explicit effect of temperature  $(T_s)$  rise in reducing the midgap DOS, and they imply that this effect overrides the effect of an increase in midgap DOS consequent on a decrease in  $C_{\text{H}}$ . We recall that the net result on  $E_{04}$  and  $E_{\text{PL}}$  of the two effects of an increase in  $T_s$  favored the dominance of the  $C_H$  decrease in the temperature range of 230'C to 300'C. These results may be reconciled if we infer that the explicit  $T_s$  effect is less important than the decrease in  $C_H$  in affecting the DOS near the valence- and conduction-band edges, but more important in affecting the midgap DOS.

For  $T_s \ge 300$ °C,  $E_{04}$ ,  $E_{PL}$ ,  $\Delta \sigma$ , and  $I_{PL}$  all decrease. This is consistent with the overriding effect of decreasing  $C_H$  in increasing the DOS throughout the entire energy gap. The monotonic decrease of  $E_{04}$  and  $E_{PL}$  over the full range of  $T_s$ , and the maxima in  $\Delta \sigma$  and  $I_{PL}$  near 300 C, are therefore assigned to a change in the relative effects of decrease in  $C_H$  and increase in network and defect healing. We may proceed further, in more speculative fashion. Early work by Paul et  $al.^{56-58}$  and Paesler et  $al$ .<sup>64</sup> on unhydrogenated  $a$ -Ge showed that a sharp change in a variety of properties (density, refractive index, porosity, internal stress, and free spin density) occurred for  $T_s$  near 300°C, and this was attributed to a rapid change in the structure of the films near this  $T_s$ . This rapid change was related to the probability that an adatom configuration on the growth surface would transform to a lower energy adatom configuration during the time for deposition of a monolayer. We may therefore speculate that up to a  $T_s$  of about 300°C a major effect is the removal of defects associated with Ge, which more than compensates for any loss in hydrogen content, but that, after this process is completed, the effect of hydrogen content reduction dominates the outcome.

# B. Variation with  $x$  of the electrical and optical properties of  $a-Si_{1-x}Ge_x:H$

The observed changes in optical and transport properties as x is varied are consistent with our earlier reports<sup>8,9</sup> on this subject and with publications by other workers. ' In this section we shall try to advance the interpretation, using our extensive data on co-deposited samples, and appealing to new knowledge about the energies of defect levels. We recall from Secs. IV and V the principal findings. (1) As x is increased, the energy gap,  $E_{04}$ , and the photon energy,  $E_{\text{PL}}$ , corresponding to the peak of the photoluminescence spectrum decrease linearly and almost exactly at the same rate. (2) As  $x$  is increased from 0 to 0.64 the magnitude of the PL intensity,  $I_{PL}$ , decreases by a factor of about 250. Beyond  $x = 0.64$ , we are unable to detect PL. (3) As x is increased from 0 to 0.74, the magnitude of the photoconductivity response for  $h\nu = 1.96$  eV decreases rapidly. For pure a-Ge:H, it is nearly 2 orders of magnitude larger. (4) As  $x$  is first increased to about 0.37, the magnitude of the subband-gap absorption [for brevity referred to as  $\alpha(1.2)$ ] increases, until the effect is obscured at small values of the energy gap. (5) As  $x$  is in-<br>creased, the infrared-vibrational-absorption spectra infrared-vibrational-absorption spectra change in a way suggesting structural alterations. (6) For high Ge content and low  $T_s$ , there is evidence of oxygen contamination and in-diffusion with time. (7) Electron microscopy studies suggest the existence of heterostructure in the  $a-Si_{0.5}Ge_{0.5}H$  films. We recall also (1) a demonstrated correlation between decreased  $I_{\text{PL}}$  and increased midgap DOS (derived from SCLC measurements) in  $a-Si<sub>0.7</sub>Ge<sub>0.3</sub>$ :H alloys,<sup>20</sup> which suggests that the midgap states (dangling bonds?) act as nonradiative recombination channels, (2) a demonstrated correlation for a-Si:H between the magnitude of midgap DOS (derived from admittance measurements) and the subband-gap absorption  $\alpha(1.2)$ ,<sup>65</sup> (3) preliminary SCLC measurements on the alloys which suggest an increase in midgap DOS with increasing Ge content.<sup>66</sup> For unalloyed  $a$ -Si:H prepared at 230 °C the DOS is about  $3 \times 10^{15}$  cm<sup>-3</sup> eV<sup>-1</sup>, for  $x = 0.02$ the DOS is about a factor of 4 higher, while for  $x = 0.5$  $(T_s = 300 \degree C)$  the DOS is about  $10^{17}$  cm<sup>-3</sup> eV<sup>-1</sup>. We recall also (4) that increases in the DOS in the gap on Ge alloying have been deduced by Huang et  $al^{67}$  from SCLC measurements and by Senemaud et  $al.^{68}$  from a combination of photoemission and subband-gap absorption.

The linear decrease of energy gap (in whatever manner it is estimated) with  $x$  has been the conclusion of most published work.<sup>69</sup> The parallel decrease of  $E_{\text{PL}}$  with x is consistent with the interpretation of the radiative transition as conduction-band tail to valence-band tail. The linear decrease of  $\Delta E_{PL}$  with x, taken together with the (small) increase in width of the valence-band tail inferred

from the decrease in slope of the exponential part of the absorption edge, suggests a (slight) sharpening of the tail to the conduction-band edge.

These simple conclusions are vitiated to some extent by doubts concerning the possible influence of  $C_H$  variation with x. Some of the work reported in the literature did not consider, or at least did not discuss, the determination of  $C_H$ .<sup>8,9</sup> In the present work (see Sec. IV)  $C_H$  remains constant for  $0 \le x \le 0.5$ , but decreases for  $x > 0.5$ . We have no fully satisfactory explanation for the continued (rather good) linear dependence of  $E_{04}$ ,  $E_{PL}$ , and  $\Delta E_{PL}$  on x for  $x > 0.5$ , but the following observations may be pertinent. First, the procedure of obtaining  $C_H$  from infrared-absorption calibrated by nuclear reaction results may be inappropriate if the latter experiments measure all H, strongly and weakly bonded, while the former measures only the strongly bonded fraction. Second, there is good evidence that the films are heterogeneous, which may imply a nonuniform distribution of H over those regions determining the optical-absorption properties and the regions which do not. Third, there appears to be a difference between the gap increase caused by hydrogenation of  $a$ -Ge and  $a$ -Si. Thus, films of  $a$ -Ge prepared at high temperatures have values of  $E_{04}$  of about 1.1 eV.<sup>70</sup> Addition of  $\sim$  8 at. % H was estimated to increase  $E_{04}$  to 1.2 eV by Connell and Pawlik<sup>71</sup> and addition of  $\sim$  10 at. % H to increase  $E_{04}$  to 1.2 eV by Rudder et al.<sup>72</sup> On the other hand, unhydrogenated  $a$ -Si prepared at 200 $^{\circ}$ C has an  $E_{04}$  of about 1.4 eV, and hydrogenation to  $\sim$  10 at. % increases  $E_{04}$  to 1.9 eV.<sup>61</sup>

Clearly, however, more work is needed to clarify the dependences of the energy gap on  $x$  and  $C_H$  described here. We note in passing that it is essential that the value of  $x$  be determined from examination of the films by electron microprobe (as was done here) or similar measure, and not by the ratio of GeH<sub>4</sub> to  $SiH_4$  in the plasma.<sup>73</sup>

We next discuss the important question of the energy of the defect states. In principle, there can be a variety of defects in the band-gap dangling bonds, reconstructed bonds longer in spatial extent and weaker in bond strength than the normal Si—Si covalent bonds, bipolaron reconstructions, and the like.<sup>74</sup> Much recent work has shown that, to a high degree of probability, the dominant defect giving states in the upper half of the gap of  $a$ -Si:H is the dangling bond, either neutral  $D^0$  or doubly occupied  $D^-$ . We feel that it is very likely that the lower half of the gap of a-Si:H contains states attributable to the other types of defects, not yet fully explored. It is not clear whether this neat division of roles for dangling bonds vis-a-vis with the rest pertains in the alloys and in a-Ge:H, but we shall tentatively assume this is so, and concentrate our attention on the dangling-bond states. Although the assembly of resu1ts just described appears to suggest an increase in dangling-bond density with  $x$ , it behooves us to consider first effects that may ensue from changes in the gap density of states (GDOS) distribution relative to the Fermi lev e/, independent of changes in the total integrated GDOS. We suppose that the "absolute" energy (with respect to, say, the vacuum level) of a dangling-bond state  $D^0$  or  $D^$ on either a Si or a Ge atom remains essentially constant as  $x$  is changed. The fact that the g values for the singly-

occupied dangling bonds do not change with  $x$  supports this contention.<sup>21</sup> We suppose also that the widths of the  $D^0$  and  $D^-$  bands do not change with x, since the topologies of a-Si:H and a-Ge:H are similar, and we shall assign to them a FWHM of 0.2 eV. Further, we suppose that the correlation energies  $[E(D^-)-E(D^0)]$  remain unchanged at 0.35 eV for Si (Ref. 75) and 0.<sup>1</sup> eV for Ge (Ref. 76) as x is varied. Also, we place the  $D^0$  band at 1.0 eV below  $E_c$  in Si (Refs. 77–81) and at 0.5 eV below  $E_c$ <br>in Ge.<sup>82</sup> in Ge.

Finally, it is necessary to include the variation with  $x$ of the absolute energies of  $E_c$  and  $E_v$ . We have found it to be quite difficult to estimate these accurately by considering the results of photoemission from valence-band and core levels. The problem is the same as that faced by workers on valence- and conduction-band discontinuities in semiconductor heterostructures. After following an iterative process of postulating the variations of  $E_c(x)$  and  $E<sub>v</sub>(x)$  which fitted the observed  $E<sub>04</sub>(x)$ , and considering the inferences for the photoconductivity, we concluded that it was most reasonable to suppose that  $E_v$  increased, and  $E_c$  decreased, at the same rate with  $x^{83}$ 

Figure 14 thus shows the variation of  $E_v$ ,  $E_c$ , and the  $E(D^0)$  and  $E(D^-)$  for Ge and Si dangling bonds as x is varied from 0 to l. It should be emphasized that this diagram is a schematic of the distribution of states in these materials, showing only the band-edge energies, the centers of the, dangling-bond bands, and the Fermi energy as a function of x. We have assumed  $E_c - E_v$  to be 1.8 eV for a-Si:H and 1.0 eV for a-Ge:H; there is a certain arbitrariness to this choice (see Ref. 35), but it fits with our conclusion from previous research that the band gap is probably a little smaller than  $E_{04}$  (1.9 eV for our a-Si:H and 1.<sup>1</sup> eV for our a-Ge:H).

We have also sketched in Fig. 14 the variation of  $E_F$ , which is assumed to be given by the value of the transport activation energy from Fig. 7. The important point, which may then be noted from Fig. 14, is that there is a change in the relative filling of the dangling-bond states with x. Thus, as  $E_F$  approaches closer to the valenceband [because of the small change in  $(E_c - E_F)_0$ ], more dangling-bond states become more positively charged.

In Fig. 15 we have schematized the band structure for



FIG. 14. The variation of  $E_v$ ,  $E_c$ , and the  $E(D^0)$  and  $E(D^-)$ for Ge and Si dangling bonds as  $x$  is varied from 0 to 1. The dashed line and points indicate the variation of  $E_F$  with x deduced from the conductivity activation energy  $(E_c-E_F)_0$ .



FIG. 15. Schematic band structure for  $a-Si_{0.5}Ge_{0.5}H$  showing the location of the Si and Ge  $D^0$  and  $D^-$  dangling-bond centers with respect to the conduction and valence bands (CB and VB).

the  $a-Si_{0.5}Ge_{0.5}H$  alloy, assuming the same dangling-bond density of  $10^{17}$  cm<sup>-3</sup> for Si and Ge. We emphasize two points. First, several tentative assumptions have entered into the construction of Figs. 14 and 15, but we believe that only modifications of these diagrams will be required, as better estimates of parameter variation with  $x$  are established, and not abandonment of the overall approach. Second, there is good reason to believe that increases in defect density and changes in microstructure with  $x$  must also be considered in developing an overall description. We consider this next.

Increases in the defect density with  $x$  are suggested not only by the decreases in  $\Delta \sigma$  and  $I_{PL}$ , but also by the subband-gap absorption and direct SCLC measurement. However, it must be noted that subband-gap absorption has two origins, one a transition from the valence band into empty states above  $E_F$  and the other a transition from below  $E_F$  into the conduction band. These two optical transitions do not necessarily have the same matrix element. Deductions about the DOS from spectra of  $\alpha(h\nu)$  [and also, of course, deductions of  $\alpha(h\nu)$  from  $\Delta\sigma(h\nu)$ ] must be considered in the framework of Figs. 14 and 15. Similar remarks apply to the DOS determined by SCLC or indeed any other such measurements: while the DOS at a specified energy may be determined, its meaning in terms of defect density requires a consideration of the changes with x in placement of  $E_v$ ,  $E_c$ , and the defect energy levels.

We consider finally the implications for the photoelectronic properties of Figs. 14 and 15. The variations with x of  $E_{04}$ ,  $E_{PL}$ , and  $\Delta E_{PL}$  have, of course, been incorporated into the figures. The most important point is that, as an increasing fraction of a constant density of dangling-bond states become more positively charged with increase of  $x$ , the magnitude of the photoluminescence and the photoconductivity will decrease. An increase of dangling-bond density with  $x$  will simply increase this effect. The magnitude of the subband-gap absorption will

change, even for constant density of dangling bonds, if the matrix elements for transitions from valence-band states to empty dangling-bond states and from filled danglingbond states to conduction-band states are different. Again, an increase in density of dangling bonds will emphasize this effect. That such an increase in defects is very plausible is strongly suggested by the structural studies based on infrared spectroscopy and transmission electron microscopy. We discuss these in more detail next.

#### C. Variation with  $T_s$  and x of the positive evidence for structural heterogeneity

In this section we shall argue that lower  $T_s$  and higher  $x$  lead to greater heterogeneity in the films, that is, more specifically, to a greater difference in physical properties between growth islands and the tissue connecting them.<sup>84</sup>

# 1. Infrared vibrational absorption

Wagner and Beyer<sup>51</sup> have shown for  $a$ -Si:H that the ocwagner and Beyer. have shown for a-Shift that the oc-<br>currence of  $a$ Si-H stretch mode near 2100 cm<sup>-1</sup> correlates with structural inhomogeneity.<sup>85</sup> Our results are consistent with their findings. The infrared-absorption spectra displayed in Fig. 10 for  $a-Si_{0.5}Ge_{0.5}H$  indicate the appearance, increase in intensity, and eventual dominance of the 2090-cm<sup>-1</sup> mode over the 2000-cm<sup>-1</sup> mode as  $T_s$ is decreased from 312 °C to 230 °C. Moreover, films grown at  $T_s < 300$ °C show signs of continuous oxygen incorporation from the atmosphere (Fig. 12). Presumably the oxygen diffuses into the film more readily via low atomic density tissue and some of it chemically bonds to the Si. Knights et  $al^{86}$  and Ross and Messier<sup>87</sup> have previously reported oxygen incorporation in a-Si:H when the  $2090 \text{ cm}^{-1}$  mode and bending modes between 800 and 900 cm $^{-1}$  are present

A strong  $2090$ -cm<sup>-1</sup> mode and much oxygen indiffusion become more likely as  $x$  is increased. Thus, unalloyed a-Si:H and  $a-Si_{0.98}Ge_{0.02}$ :H prepared at 230°C show no sign of either, while for unalloyed a-Ge:H the 1975-cm<sup>-1</sup> high-frequency component of the Ge-H stretch doublet is usually present (this corresponds to the  $2090$ -cm<sup>-1</sup> Si-H stretch mode) and oxygen incorporation occurs.

#### 2. Transmission electron microscopy

Direct evidence of structural inhomogeneity in a- $Si<sub>0.5</sub>Ge<sub>0.5</sub>$ :H is seen in the TEM micrographs shown as Fig. 13. The high-density regions are of the order of <sup>100</sup>—<sup>500</sup> <sup>A</sup> across. On average, the dimensions of these regions in the specimens grown at  $300^{\circ}$ C are much smaller than in films prepared at 230'C, implying that the higher  $T_s$  films are more structurally homogeneous. The a-Ge:H also showed discernible microstructure on a scale of 200 A but, by contrast, no clearly discernible structure was found in our unalloyed a-Si:H. We emphasize that this does not rule out the possibility of its presence and, in fact, microstructure has been observed elsewhere in high quality  $a-Si:H.^{88}$  We are of the view that it is always present as a consequence of the mechanism of film

growth under our preparation conditions. The question is one of the discernibility in a TEM which has to do with differences in atom density between island and tissue.

#### 3. High-temperature kinks in  $ln \sigma$  versus  $1/T$

Decreases in the slope of  $\ln \sigma$  versus  $1/T$  plots at high temperature ( $10^3/T \leq 2.4$  K<sup>-1</sup>) have been found by many workers,<sup>89</sup> and further examples may be seen in Fig. 6. Anderson and Paul<sup>90</sup> have proposed to explain these socalled kinks on the basis of a model $91$  of a heterogeneous film structure consisting of high atom density islands interconnected by low atom density tissue. In the islands, most of the dangling bonds are compensated by hydrogen, probably in the monohydride Si-H configuration. In the tissue, there is a larger density of defects and a greater variety of Si—<sup>H</sup> bonding entities. Island and tissue therefore have different structure, chemistry, and transport properties. In a heterogeneous film, it is supposed that neither phase is likely to form a continuous (electrical) channel between electrical contacts. In their model, the measured conductivity is determined by the island material below the "kink", and by the tissue material at high temperatures. The kink occurs because island and tissue possess different  $\sigma$  versus  $1/T$  characteristics.

A different explanation for these kinks has been put forward by Overhof and Beyer.<sup>92</sup> In their model, the kink is produced by a rapid change of the dependence of the Fermi level on temperature near the kink temperature. This rapid change is linked to the occurrence of fluctuations in the potential. It is to be noted that the presence of heterostructure in the form of islands and tissue is a very likely cause of potential fluctuations on the scale desired, so that both explanations for the kinks in  $ln \sigma$ correlate them with increasing heterogeneity.

The present results on  $a-Si_{1-x}Ge_x:H$  are only partly supportive of the suggested connection between heterogeneity and kinks in  $\ln \sigma$  versus  $1/T$ . Thus, in Fig. 6, unalloyed  $a$ -Si:H does not show a kink, while the Si-Ge alloys do, in agreement with our hypothesis that increasing x induces heterostructure. On the other hand, the  $a$ -Ge:H sample of that figure does not show a kink. It is also to be noted that a sample of  $a-Si_{0.98}Ge_{0.02}$ : H prepared at  $T_s = 230^{\circ}\text{C}$  shows a kink, yet its infrared spectrum is very similar to that of unalloyed a-Si:H viz. a dominant  $2000-cm<sup>-1</sup>$  mode and no bending modes near 800-900 cm<sup>-1</sup>. Further, a sample of  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>$ :H prepared at 230 C does not show a kink, yet has a dominant absorpion at 2090  $cm^{-1}$  and strong bending modes. We are forced to conclude from this confusion of indicators that this transport anomaly is a poor guide concerning structure for the present set of films.

#### 4. Evolution of hydrogen

Although not reported in detail in this paper, it is pertinent to draw attention to our earlier work<sup>17</sup> on the thermal evolution of hydrogen from films of a  $Si_{1-x}Ge_x$ :H of different x produced by dc glow discharge at different  $T_s$ . The general conclusion of that work firmly supported the present interpretation viz. that low

 $T<sub>s</sub>$  and increased x produced films which showed evolution of H at low temperatures (order of  $200^{\circ}$ C), which implied the existence of easy exit pathways for  $H_2$ molecules—presumably through low-density tissue.

#### VII. CONCLUSIONS

The principal conclusions from this work are the following.

(1) Increased substrate temperature  $T_s$  affects the properties of  $a-Si<sub>0.5</sub>Ge<sub>0.5</sub>$ : H both through increased network healing and decreased H incorporation. The observed results include a linear decrease of the optical energy gap and the peak energy of photoluminescent emission over the full range of  $T_s$  and a maximum in the magnitude of photoluminescence intensity and photoconductivity response for  $T_s$  near 300 °C.

(a) For  $T_s$  increasing below 300°C, the network healing effect reduces the state density in the energy gap (GDOS), while the decrease in H content increases it. In this temperature range, the former effect is more important in causing a net decrease in GDOS near midgap and the latter effect more important in producing a net increase in GDOS near the valence- and conduction-band edges.

(b) For  $T_s$  increasing beyond 300°C the increase in DOS throughout the band gap caused by decreasing the H content is the overriding effect.

(c) The maximum in photoconductivity and photoluminescence near  $T_s = 300$ °C, supposedly caused by a change in the relative importance of network healing and H removal in affecting the midgap DOS, may be connected with a critical  $T<sub>s</sub>$  for the elimination of a fundamental defect primarily associated with the Ge.

(2) Increased substrate temperature favors the production of films which have less visible heterostructure, as inferred from studies of infrared vibrational absorption, transmission electron microscopy, and hydrogen evolution. Also, the films produced at high  $T_s$  ( $\approx 300\degree$ C) show less evidence of oxygen contamination and in-diffusion with time.

(3) For  $T_s = 300 \degree C$ , increased Ge content x produces the following changes: (a) The optical energy gap and the peak energy of photoluminescent emission decrease linearly at the same rate; (b) the magnitude of the intensity of photoluminescence decreases by 3 orders of magnitude (by  $x = 0.74$ ) and falls below our detection limit; (c) the magnitude of the photoconductivity decreases rapidly but re-

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covers near  $x = 1$ ; (d) the magnitude of the subband-gap absorption increases; (e) the infrared-vibrationalabsorption spectra change in a way suggesting alterations of structure.

(4) A band structure may be constructed for a  $Si_{1-x}Ge_x$ :H alloys based on the following observations and assumptions: (a) The energy gap decreases linearly with  $x$  from 1.8 eV to 1.0 eV; (b) the principal defect states, at least in the upper half of the band gap, are caused by dangling bonds on the Ge and Si atoms. The energies of the singly-occupied  $(D<sup>0</sup>)$  and doubly-occupied  $(D^-)$  dangling-bond states may be taken, with some uncertainty, from current work on spin resonance, deep-level transient spectroscopy, and doping studies in unalloyed  $a$ -Si:H and  $a$ -Ge:H; (c) the energies of the dangling-bond states remain constant with respect to the vacuum level for all compositions; (d) the absolute energies of the valence- and conduction-band edges increase and decrease linearly at the same rate between pure a-Si:H and pure a-Ge:H; (e) the position of the Fermi level may be found approximately from the activation energy for conduction.

(5) The band structure constructed according to the scheme outlined in (4) may be exploited to rationalize the observed changes in photoluminescence and photoconductivity in the alloys.

(6) There is strong direct evidence that the poorer photoelectronic properties in the Ge-rich alloys are caused only partly by the band-structure changes outlined in (4), and that a major additional cause is the occurrence of increased heterostructure in the films.

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