

## Brief Reports

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Role of varying electronic density of states in the far-infrared behavior of V<sub>3</sub>Si

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Far-infrared measurements in a thin film of V<sub>3</sub>Si at 19 K are analyzed with new expressions for the ac conductivity for the case of a nonconstant electronic density of states  $N(\epsilon)$ . It is found that the infrared data can be fitted with a transport electron-phonon coupling function  $\alpha_{tr}^2 F$  which is proportional to the measured phonon density of states, and with an  $N(\epsilon) \neq \text{const}$ . Thereby, the discrepancy between the neutron scattering results and the previous analysis of the infrared behavior is resolved.

Different experimental probes of the electron-phonon (EP) coupling function  $\alpha^2(\Omega)F(\Omega)$  in the high superconducting  $T_c$  A-15 compound V<sub>3</sub>Si give conflicting results. Inelastic neutron scattering experiments<sup>1</sup> on V<sub>3</sub>Si at 4, 77, and 300 K give the phonon density of states  $F(\Omega)$  with peaks at 25 and 42 meV (Fig. 1). In contrast, far-infrared data taken by McKnight, Perkowitz, Tanner, and Testardi<sup>2</sup> (hereafter referred to as MPTT), when analyzed by Allen's theory<sup>3</sup> of infrared absorption, give the transport EP coupling function  $\alpha_{tr}^2(\Omega)F(\Omega)$  with peaks at 18 and 42 meV, and with entirely new structure at 6 meV (Fig. 1). Mitrović and Carbotte<sup>4</sup> have found that superconducting thermodynamic properties of V<sub>3</sub>Si could be fitted with an  $\alpha^2 F$  set

equal to  $\text{const} \times F(\Omega)$ , but not with the  $\alpha_{tr}^2 F$  deduced by MPTT. In general, the functions  $F(\Omega)$ ,  $\alpha^2(\Omega)F(\Omega)$  and  $\alpha_{tr}^2(\Omega)F(\Omega)$  do not have the same shape, but the difference between  $F$  and  $\alpha_{tr}^2 F$  in Fig. 1 is too large to be explained by  $\Omega$  dependence of  $\alpha_{tr}^2$ . In this paper we show that a correction to Allen's original formulation, to include the effect of structure in the electronic density of states  $N(\epsilon)$  very close to the chemical potential  $\mu (=0)$ , resolves the experimental discrepancy. Band-structure calculations,<sup>5</sup> the temperature dependence of magnetic susceptibility,<sup>6</sup> and the degradation of  $T_c$  with disorder<sup>7,8</sup> strongly suggest that  $N(\epsilon)$  in V<sub>3</sub>Si can vary on the scale of the maximum phonon frequency  $\Omega_{\text{max}}$  (or smaller) near  $\mu$ . A combination of

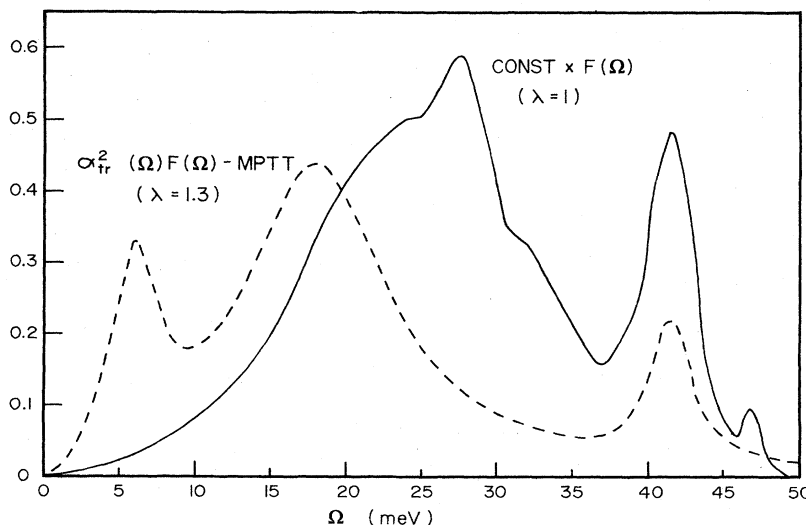


FIG. 1. Phonon density of states scaled by a constant factor (solid line) and  $\alpha_{tr}^2 F$  of McKnight *et al.* (Ref. 2) (dashed line).

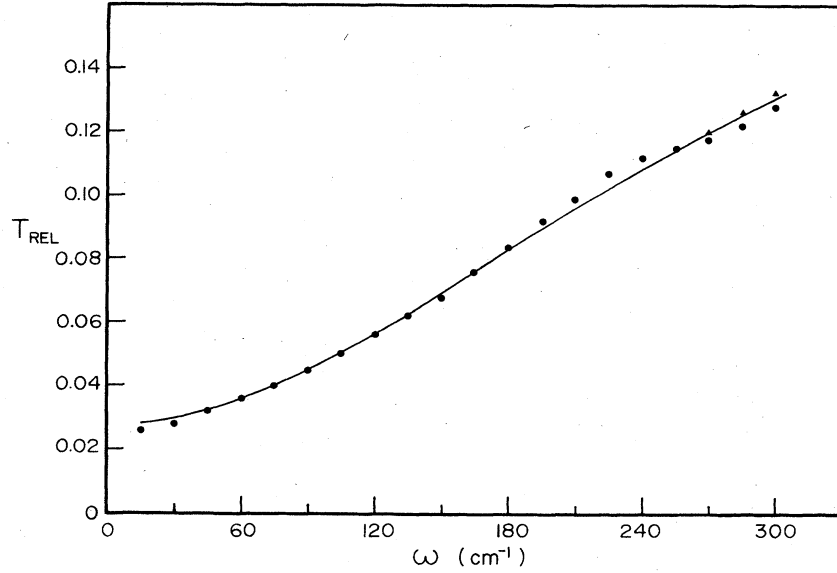


FIG. 2. Experimental values of  $T_{\text{rel}}$  (heavy dots) and theoretical fit (solid line). Triangles represent few points off the solid line which are calculated within the usual theory [ $N(\epsilon) = \text{const}$ ] from  $\alpha_{\text{tr}}^2 F$  given by the dashed curve in Fig. 1.

an  $\alpha_{\text{tr}}^2 F$  based on the neutron scattering data, and fine structure in  $N(\epsilon)$  satisfactorily reproduces the infrared results on  $\text{V}_3\text{Si}$  without any need to invoke shifts in the peak positions or the existence of new peaks.

MPTT analyzed data between 0.6 and 37 meV, taken in transmission through a 20-nm film grown on a sapphire substrate. The measurement was made in the normal state at 19 K. The measured quantity was  $T_{\text{rel}}$ , the transmission of the film and substrate (ss) normalized to that of the substrate alone. It is given by

$$T_{\text{rel}} = T_{\text{film+ss}}/T_{\text{ss}} = \left[ \left( 1 + \frac{y_1}{n+1} \right)^2 + \left( \frac{y_2}{n+1} \right)^2 \right]^{-1}, \quad (1)$$

where

$$y_1 + iy_2 = \frac{4\pi}{c} d \sigma(\omega). \quad (2)$$

Here  $4\pi/c$  is the impedance of free space,  $\sigma(\omega)$  the complex ac conductivity of the film,  $d$  the film thickness, and  $n$  the refractive index of the substrate. The ratio  $T_{\text{film+ss}}/T_{\text{ss}}$  eliminates almost completely all absorptive effects in the substrate, although at higher frequencies, where the sapphire absorption increases, there is about a 5% error. The measured values of  $T_{\text{rel}}$  are given in Fig. 2.

In the case of nonconstant  $N(\epsilon)$  ac conductivity in the local approximation and in the weak-coupling limit is given by

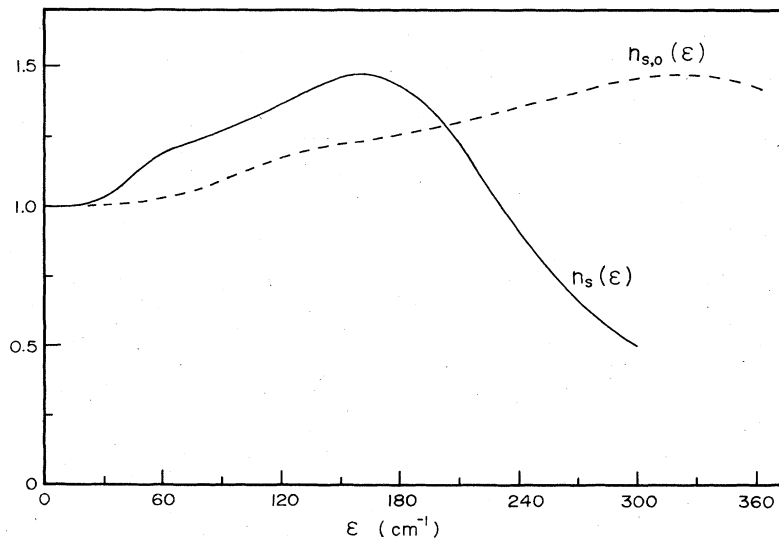


FIG. 3.  $n_s(\epsilon)$  which gives the fit in Fig. 2.  $n_{s,0}$  is obtained from  $n_s$  by eliminating the energy renormalization.

( $\hbar = 1$ )

$$\sigma(\omega) = \frac{\Omega_p^2 \tau^*(\omega)}{4\pi} \frac{1}{1 + \bar{\lambda}(\omega)} \frac{1}{1 - i\omega\tau^*(\omega)}, \quad (3)$$

where

$$1/\tau^*(\omega) = [1/\bar{\tau}_{ep}(\omega) + 1/\bar{\tau}_i(\omega)]/[1 + \bar{\lambda}(\omega)], \quad (4)$$

$$1/\bar{\tau}_{ep}(\omega) = \frac{2\pi}{\omega} \int_0^{\omega} d\Omega \alpha_{ir}^2(\Omega) F(\Omega) \int_0^{\omega-\Omega} d\epsilon n_s(\epsilon), \quad (5)$$

$$1/\bar{\tau}_i(\omega) = \frac{1}{\tau_i} \frac{1}{\omega} \int_0^{\omega} d\epsilon n_s(\epsilon), \quad (6)$$

$$\bar{\lambda}(\omega) = \bar{\lambda}_{ep}(\omega) + \bar{\lambda}_i(\omega), \quad (7)$$

$$\bar{\lambda}_{ep}(\omega) = \frac{2}{\omega^2} \int_0^{\Omega_{\max}} d\Omega \alpha_{ir}^2(\Omega) F(\Omega) \times \int_0^{+\infty} d\epsilon n_s(\epsilon) \ln \left| \frac{(\epsilon + \Omega)^2}{(\epsilon + \Omega)^2 - \omega^2} \right|, \quad (8)$$

$$\bar{\lambda}_i(\omega) = \frac{1}{\pi\tau_i\omega} \int_0^{+\infty} d\epsilon n_s(\epsilon) \ln \left| \frac{\epsilon^2}{\epsilon^2 - \omega^2} \right|, \quad (9)$$

$$n_s(\epsilon) = [N(\epsilon)/N(0) + N(-\epsilon)/N(0)]/2, \quad (10)$$

$$\tau_i = \tau_i(\omega=0). \quad (11)$$

Equations (3)–(11) can be derived<sup>9</sup> by using Allen's golden rule treatment<sup>3</sup> of EP and electron-impurity (EI) scattering plus the requirement that the conductivity satisfies the  $f$ -sum rule.<sup>10,11</sup> Also, it is assumed that the  $\epsilon$  dependence of the Drude plasma frequency  $\Omega_p(\epsilon)$  can be ignored. This approximation is justified by the band-structure calculations<sup>5,8</sup> for  $A$ -15 materials. It also underlies the analysis of the upper critical field data which yields the dependence of  $N(0)$  on disorder.<sup>7</sup> In the case of  $N(\epsilon) = \text{const}$  Eqs. (3)–(11) reduce to Allen's expression.<sup>3</sup> We point out that Eqs. (3)–(11) can also be obtained<sup>9</sup> from Holstein's theory<sup>12</sup> in the weak-coupling limit and in the local approximation.

This approach indicates<sup>9</sup> that  $N(\epsilon)$  should be interpreted as the quasiparticle density of states<sup>13</sup>

$$N(\epsilon) = -\frac{1}{\pi} \text{Im} \sum_k G(k, \epsilon + i0^+), \quad (12)$$

where  $G$  is the Green's function, i.e., as the density of states which includes the self-energy effects (lifetime broadening plus the energy renormalization). The derivation is lengthy and will be presented elsewhere.<sup>9</sup> Note that in the case of  $N(\epsilon) \neq \text{const}$  the impurity contribution to  $1/\bar{\tau}(\omega)$  becomes frequency dependent, and thus impurities start contributing to the renormalization parameter  $\bar{\lambda}(\omega)$ . This fact was first pointed out by Pickett and Allen.<sup>11</sup>

In fitting the experimental data on  $T_{\text{rel}}$  we have used  $\alpha_{ir}^2(\Omega)F(\Omega) = CF(\Omega)$ , where  $F(\Omega)$  is the measured phonon density of states and the constant  $C$  was chosen so that  $\bar{\lambda}_{ep}(0) = 1$  (Fig. 1). The  $n_s(\epsilon)$  which gives the best fit to the data in Fig. 2 is shown in Fig. 3. The corresponding value of  $1/\tau_i$  was  $296 \text{ cm}^{-1}$  (i.e.,  $37 \text{ meV}$ ).  $\Omega_p^2$  was absorbed into the experimental value of  $\sigma(0)d$  (Ref. 2). The overall shape of  $n_s(\epsilon)$  does not depend much on the detailed shape of  $\alpha_{ir}^2F$  provided that the positions of the peaks in this function coincide with the positions of the peaks in  $F(\Omega)$ . [For example, an  $\alpha_{ir}^2F$  obtained by multiplying the solid curve in Fig. 1 with a factor which varies smoothly from 2 at  $\omega = 0$  to 0.5 at  $\omega = 42 \text{ meV}$  yields an  $n_s(\epsilon)$  which has the same overall shape as the  $n_s$  in Fig. 3.] We particularly note that the fit in Fig. 2 is identical to that obtained by MPTT with their modified  $\alpha_{ir}^2F$  (dashed line in Fig. 1) and  $N(\epsilon) = \text{const}$ . As pointed out by MPTT, the measured  $T_{\text{rel}}$  for  $\text{V}_3\text{Si}$  can be fitted within the usual formalism [ $N(\epsilon) = \text{const}$ ] only with an  $\alpha_{ir}^2F$  which is exhausted by  $25 \text{ meV}$ , i.e., with a major peak below this energy. Since the neutron scattering experiments down to  $4 \text{ K}$  do not give any significant shift of the broadest peak at  $25 \text{ meV}$ , such an  $\alpha_{ir}^2F$  is very unlikely. We emphasize that the most important effect of nonconstant  $N(\epsilon)$  on infrared behavior comes via EI scattering [ $1/\bar{\tau}_i(\omega)$  and  $\bar{\lambda}_i(\omega)$ ]. In Fig. 4 we show

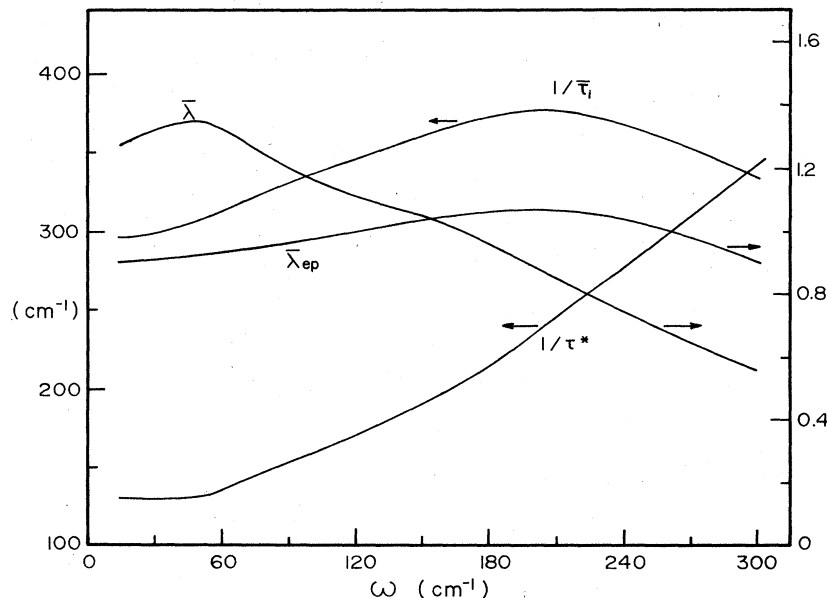


FIG. 4. Calculated renormalization parameters and scattering times.

$1/\tau^*$ ,  $1/\bar{\tau}_i$ ,  $\bar{\lambda}_{ep}$ , and  $\bar{\lambda}$  calculated with  $n_s(\epsilon)$  from Fig. 3. Note that with our input  $\alpha^2 F$  (solid curve in Fig. 1)  $\bar{\lambda}_{ep}$  is almost constant, whereas  $\bar{\lambda}_i$  is rapidly decreasing, giving a rapidly decreasing  $\bar{\lambda}$ . The original  $\alpha^2 F$  of MPTT (dashed curve in Fig. 1) would yield an  $\bar{\lambda}_{ep}$  very similar to  $\bar{\lambda}$  in Fig. 4.

The question arises as to whether the impurity scattering parameter  $1/\tau_i = 37$  meV is compatible with the structure in  $n_s(\epsilon)$  in Fig. 3. First, the lifetime broadening due to EI scattering is given by<sup>13</sup>

$$\Gamma_i(\epsilon) = \frac{1}{2\tau_i} \frac{N(\epsilon)}{N(0)},$$

where  $N$  is defined by Eq. (12). Thus,  $\Gamma_i$  is about a factor of 2 smaller than  $1/\tau_i$ . Second, the quasiparticle density of states [Eq. (12)] includes the energy renormalization due to interactions and thus displays a sharper structure within  $\pm \Omega_{\max}$  of  $\mu$  than its bare band-electron counterpart.<sup>13</sup> Roughly speaking,  $N(\epsilon) = N_0[\epsilon(1+\lambda)]$ , where  $N_0$  is the band-electron density of states broadened by the lifetime effects and  $\lambda$  is the (energy-dependent) electron mass renormalization parameter.<sup>13</sup> In Fig. 3 we also show  $n_{s,0}(\epsilon) = n_s[\epsilon/(1+\lambda)]$ . The structure in  $n_{s,0}(\epsilon)$  is not incompatible with  $\Gamma_i$  of about 20 meV. We also point out that with  $\Omega_p = 3.1$  eV (Ref. 7) and  $1/\tau_i = 37$  meV we get the residual resistivity of  $\rho_0 = 29 \mu\Omega \text{ cm}$  for this sample of  $V_3\text{Si}$ . This

value of  $\rho_0$  correlates well<sup>7</sup> with the measured  $T_c = 15 \pm 0.5$  K.

Finally, we comment that the study of effects of nonconstant  $N(\epsilon)$  on superconducting thermodynamic properties<sup>14</sup> indicates that an  $n_{s,0}(\epsilon)$  from Fig. 3 does not have to be accounted for in the calculation of thermodynamics. Therefore, the results obtained in Ref. 4 remain valid. In contrast, the analysis of the effects of  $N(\epsilon) \neq \text{const}$  on superconducting tunneling<sup>15</sup> indicates that an  $n_{s,0}$  from Fig. 3 would influence the  $\alpha^2 F$  obtained from the tunneling. At the moment, there is no information about  $\alpha^2 F$  in  $V_3\text{Si}$  from the tunneling experiments. We predict that even if the tunneling junction is free of the proximity effect, the inverted  $\alpha^2 F$  for a high  $T_c$   $V_3\text{Si}$  sample would contain a negative tail for  $\Omega \geq \Omega_{\max}$ ,<sup>15</sup> provided that no constraint is imposed on the upper cutoff in  $\alpha^2 F$  during the inversion procedure.

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