

## Optical properties of single-crystal rutile RuO<sub>2</sub> and IrO<sub>2</sub> in the range 0.5 to 9.5 eV

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We have measured the near-normal incidence reflectivity of single-crystal rutile RuO<sub>2</sub> and IrO<sub>2</sub> for  $\vec{E} \parallel c$  axis and  $\vec{E} \perp c$  axis at room temperature in the photon energy range 0.5–9.5 eV. From a Kramers-Kronig analysis of the reflectivity we have obtained the spectral dependence of the real and imaginary parts of the complex dielectric constant ( $\epsilon_1$  and  $\epsilon_2$ , respectively) and refractive index ( $n$  and  $k$ , respectively) for each material. Comparison with recent band-structure and density-of-states calculations and past experimental studies of related solids has enabled us to gain further insight into the nature of the oxygen  $p$  electrons and metal  $d$  electrons in these materials.

### I. INTRODUCTION

Ruthenium dioxide, RuO<sub>2</sub>, and iridium dioxide, IrO<sub>2</sub>, belong to the family of transition-metal dioxide compounds with rutile-type structure which possess an interesting variety of electrical and magnetic properties. RuO<sub>2</sub> is well known as a corrosion-resistant low-overpotential electrode for chlorine evolution.<sup>1,2</sup> Because of its low-anodic-oxygen overpotential, RuO<sub>2</sub> has been shown to be an equally effective electrode for oxygen evolution.<sup>3–5</sup> Furthermore, it has recently been reported that the catalytic photodecomposition of water into hydrogen and oxygen proceeds at a much higher rate when RuO<sub>2</sub> is added to a TiO<sub>2</sub> electrode.<sup>6</sup> These latter properties are particularly significant should hydrogen generation via water decomposition (either electrolysis or photoelectrolysis) become a part of any future energy program. In addition, because of its high electrical conductivity and chemical stability, RuO<sub>2</sub> shows great promise as an electrical contact material<sup>7</sup> and strip-line conductor in integrated circuits.<sup>8</sup>

The performance of an IrO<sub>2</sub> anode has also been found to be much superior to that of pure Pt for the oxygen evolution reaction.<sup>9,10</sup> Recently, the search for effective passive display devices has stimulated much interest in electrochromism,<sup>11</sup> a reversible color change induced electrochemically. An anodically grown iridium oxide film has been reported<sup>12,13</sup> to be a very promising electrochromic material and this has prompted several recent studies of their properties.<sup>14–20</sup> Its advantages over other electrochromic oxides such as WO<sub>3</sub> are shown to include (i) fast response, (ii) good open-

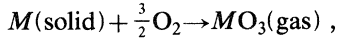
circuit memory, (iii) ability not to degrade in the presence of water, and (iv) the ability to grow and reform the oxide layer *in situ* in the electro-optic display cell.<sup>12</sup> As regards single crystals, the electrical-transport properties of RuO<sub>2</sub> and IrO<sub>2</sub> have been reported by Ryden *et al.*<sup>21</sup> and the conduction-electron screening effects have been demonstrated in IrO<sub>2</sub> by Wertheim and Guggenheim.<sup>22</sup> The above interesting properties of RuO<sub>2</sub> and IrO<sub>2</sub> are related to the nature of the metal  $d$  electrons. Although a considerable amount of applied research<sup>23</sup> has been performed on the properties of RuO<sub>2</sub> and IrO<sub>2</sub>, little work has been done on their fundamental aspects.

In this paper, we present the first comprehensive optical investigation of single-crystal RuO<sub>2</sub> and IrO<sub>2</sub>. We have measured the near-normal incidence ( $\sim 6^\circ$ ) reflectivity for the electric-field vector  $\vec{E}$  of the light polarized parallel ( $\parallel$ ) and perpendicular ( $\perp$ ) to the  $c$  axis in the energy range 0.5 to 9.5 eV at room temperature. Real and imaginary parts of the complex dielectric constant and refractive index have then been deduced for each crystal from a Kramers-Kronig analysis of the reflectivity. These quantities have been compared with some recent band-structure and density-of-states calculations as well as past experimental studies of related solids TiO<sub>2</sub> (Ref. 24) and VO<sub>2</sub> (Ref. 25) in order to gain further insight into the nature of the oxygen  $p$  electrons and metal  $d$  electrons in these materials.

### II. EXPERIMENTAL DETAILS

Single crystals of RuO<sub>2</sub> were grown in our laboratory by the method of chemical transport reac-

tion in a flowing system. This technique is similar to that used by Reames<sup>26</sup> and more recently by Shafer *et al.*<sup>27</sup> In the presence of oxygen at 800–1500 °C gaseous oxides (RuO<sub>3</sub> and IrO<sub>3</sub>) exist. The reaction takes place by the mechanism



where  $M = \text{Ru}$  or  $\text{Ir}$ . The volatile  $\text{MO}_3$  gas dissociates to  $\text{MO}_2$  in the cooler region. In our procedure, several grams of the Ru powder were contained in an alumina source boat. This boat was placed inside a Mullite tube at the center of the furnace which was raised to a temperature of 1400 °C. Oxygen at atmospheric pressure was passed through the Mullite tube at a flow rate of about 15 cm<sup>3</sup>/min. A second boat, which acted as a substrate, was placed 210 cm from the source boat in a cooler portion of the furnace (about 1000 °C). After several days, crystals of dimensions up to 6 × 4 × 2 mm<sup>3</sup> had formed in the substrate boat. Single crystals of IrO<sub>2</sub> were supplied by F. M. Reames.

A number of crystals were examined by x-ray diffraction and Laue backscattering which indicated that they were of relatively good quality. Crystal faces were oriented perpendicular to the  $a$  axis by the x-ray diffraction method to  $\pm 1^\circ$ . They were then polished by using 12- $\mu\text{m}$  alumina powder, 6- $\mu\text{m}$  diamond paste, 3- and 0.3- $\mu\text{m}$  alumina powders and finally polish etched using Siton.<sup>28</sup>

A high-precision rotating-light pipe reflectometer<sup>29</sup> was used in order to record the reflectivity  $R$  as a continuous function of wavelength. The entire wavelength range was divided into three parts: near infrared (20000 to 7000 Å), visible (7000 to 2800 Å) and ultraviolet (2800 to 1200 Å). Light sources were a 150-W xenon lamp and tungsten-halogen lamp in the visible and infrared ranges, respectively. A McPherson Model 630 H<sub>2</sub>-gas-discharge lamp was used as the light source in the ultraviolet part. Polarization of the incident radiation was achieved by using appropriate Polaroid sheet polarizers in the visible and infrared. In the ultraviolet region, polarization was accomplished by reflection from a cleaved LiF plate at the Brewster angle. A photomultiplier was used as the detector in the visible range and PbS cell was employed in the infrared region. A prism pre-disperser was installed in front of the entrance slit of the monochromator in the visible part to avoid second-order effects and to minimize the scattered light, while in the infrared range the radiation below 7000 Å was filtered out with the help of a

high-pass filter. In the ultraviolet, measurements were carried out in vacuum ( $\sim 10^{-6}$  Torr). Mirrors coated with MgF<sub>2</sub> were used in this range which highly enhances the reflectivity of uv radiation down to 1200 Å. In this region, the front surface of the light pipe was coated with a thin and uniform film of sodium salicylate which converts ultraviolet radiation into visible light so that a photomultiplier could be used. Further experimental details are described in Refs. 30 and 31.

In the case of an isotropic crystal, when the angle of incidence of the incident radiation is not normal to the surface of the solid, then the reflected intensity is given by

$$R_n = \frac{(a - \cos\phi)^2 + b^2}{(a + \cos\phi)^2 + b^2} \quad (1)$$

and

$$R_p = R_n \frac{(a - \sin\phi \tan\phi)^2 + b^2}{(a + \sin\phi \tan\phi)^2 + b^2} \quad (2)$$

where  $R_n$  ( $R_p$ ) is reflected intensity of the solid when the polarization of the incident radiation is perpendicular (parallel) to the plane of incidence and  $\phi$  is the angle between the incident radiation and the normal to the surface of the solid. The parameters  $a^2$  and  $b^2$  are related to  $\varphi$  and the optical constants  $n$  and  $k$  by the relations

$$a^2 = \frac{1}{2} \{ [(n^2 - k^2 - \sin^2\phi)^2 + 4n^2k^2]^{1/2} + (n^2 - k^2 - \sin^2\phi) \},$$

$$b^2 = \frac{1}{2} \{ [n^2 - k^2 - \sin^2\phi]^2 + 4n^2k^2 \}^{1/2} - (n^2 - k^2 - \sin^2\phi) .$$

RuO<sub>2</sub> and IrO<sub>2</sub> are anisotropic crystals of the uniaxial type, i.e., they have dielectric constants of the form  $\epsilon_x = \epsilon_y \neq \epsilon_z$ . For these crystals,  $R_n$  as given by Eq. (1) can still be used if any one of the principal axes of the crystal is taken in the direction perpendicular to the plane of incidence and  $R_p$  in Eq. (2) can still be used if the  $c$  axis is in the direction perpendicular to the plane of incidence, as was the case in our experiments. Experimentally,  $R_n$  and  $R_p$  were measured at several values of  $\phi$  (from 5° to 75° in steps of 5°, depending upon the size of the crystal) for the laser energies 1.96, 2.53, and 2.73 eV. The values of  $a$  and  $b$  (and hence  $n$  and  $k$ ) were then obtained by a  $\chi^2$  fit between the theoretically expected and experimentally found reflectivity values. The values of  $\epsilon_1$  and  $\epsilon_2$  were then deter-

mined for each of the laser energies from the relations  $\epsilon_1 = n^2 - k^2$  and  $\epsilon_2 = 2nk$ .

### III. EXPERIMENTAL RESULTS

The polarization dependent near-normal incidence reflectivity at room temperature of single crystal  $\text{RuO}_2$  in the range 0.5–9.5 eV is shown in Fig. 1. The spectra for both  $\vec{E}||c$  and  $\vec{E}\perp c$  have four major features that are denoted by  $A$ ,  $B_1$ ,  $C_1$ , and  $E$ . In addition, there are smaller structures indicated by  $B_2$ ,  $B_3$ ,  $C_2$ , and  $D$ . At  $\sim 1$  eV the feature  $A$  has a well-resolved peak for  $\vec{E}||c$  and a shoulder for  $\vec{E}\perp c$ . Although the reflectivity curves for the two polarization directions are quite similar there are differences in energy positions for some of the features. For example,  $B_1^||$  and  $E^||$  occur at  $\sim 0.15$  eV below  $B_1^\perp$  and  $E^\perp$ , respectively. The feature  $B_2$  is present for both the polarizations at nearly the same energy but the shoulder  $C_2^||$  does not have its counterpart for  $\vec{E}\perp c$ ; the same is true for  $B_3^\perp$  which does not appear for  $\vec{E}||c$ .

Figure 2 shows the near-normal incidence room-temperature reflectivity spectra of single crystal  $\text{IrO}_2$  for both  $\vec{E}||c$  and  $\vec{E}\perp c$  in the photon energy range 0.5–9.5 eV. Curves for both the polarizations have four major features which are denoted by  $A$ ,  $B_1$ ,  $C_1$ , and  $E$ . In addition, there are smaller structures indicated by  $A_2$ ,  $A_3$ ,  $B_2$ ,  $C_2$ , and  $D$ . Although the reflectivity spectra for both  $\vec{E}||c$  and  $\vec{E}\perp c$  are quite similar there are significant differences in energy positions for most of the features. Almost all the features for  $\vec{E}||c$  appear at higher energies than their counterparts for  $\vec{E}\perp c$ . For ex-

ample,  $A_2^||$  is observed  $\sim 0.2$  eV above  $A_2^\perp$ ,  $B_1^||$  occurs at  $\sim 0.4$  eV above  $B_1^\perp$ ,  $C_1^||$  appears at  $\sim 0.7$  eV above  $C_1^\perp$  and  $E^||$  is present  $\sim 0.2$  eV above  $E^\perp$ . Small structure  $D^||$  is observed  $\sim 1$  eV above  $D^\perp$ . Some features appear for one of the polarizations only. For example,  $C_2$  appears only for  $\vec{E}||c$  having no counterpart for  $\vec{E}\perp c$ , while  $B_2$  is observed for  $\vec{E}\perp c$  only. Dotted lines represent extrapolations of the reflectivity down to 0 eV.

Quantities more relevant for the discussion of the electronic states of the solid are the optical constants rather than the reflectivity spectra. We have deduced the real ( $\epsilon_1$ ) and imaginary ( $\epsilon_2$ ) parts of the complex dielectric constant as well as real ( $n$ ) and imaginary ( $k$ ) parts of the complex refractive index by means of a Kramers-Kronig (KK) analysis of the reflectivity. An extrapolation scheme was used to evaluate the (KK) integral. In this method, the reflectivity  $R$  at an energy above the upper limit of the measurement ( $\sim 9.5$  eV) was taken to be  $R = R_1(\hbar\omega_1/\hbar\omega)^\beta$ , where  $\hbar\omega_1$  is the upper limit of the measurements,  $R_1$  is the reflectivity at  $\hbar\omega_1$ , and  $\beta$  is an adjustable parameter.<sup>31,32</sup> The parameter  $\beta$  was fit by requiring the optical constants to agree with values determined by angular reflectivity measurements at the laser energies 1.96, 2.53, and 2.73 eV.<sup>30,31</sup>

Room-temperature spectra of  $\epsilon_1$  and  $\epsilon_2$  for  $\text{RuO}_2$  are given in Figs. 3 and 4, respectively, both for  $\vec{E}||c$  and  $\vec{E}\perp c$  in the energy range 0.5–9.5 eV. Spectra of  $n$  and  $k$  for  $\text{RuO}_2$  are shown in Figs. 5 and 6, respectively. For  $\text{IrO}_2$ ,  $\epsilon_1$  and  $\epsilon_2$  spectra for  $\vec{E}||c$  and  $\vec{E}\perp c$  in the energy range 0.5–9.5 eV are plotted in Figs. 7 and 8, respectively. Figures 9 and 10 show the  $n$  and  $k$  spectra, respectively, for

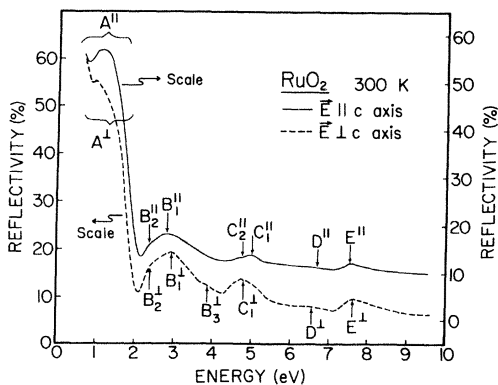


FIG. 1. Near-normal incidence reflectivity of single-crystal rutile  $\text{RuO}_2$  at room temperature for  $\vec{E}||c$  and  $\vec{E}\perp c$  in the energy range 0.5–9.5 eV.

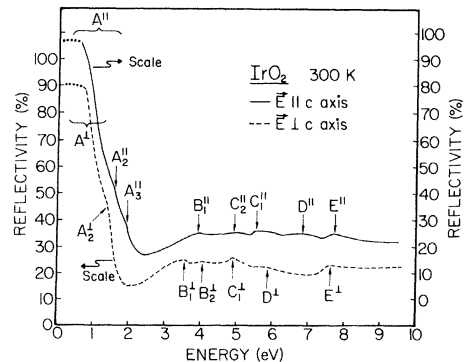


FIG. 2. Near-normal incidence reflectivity of single-crystal rutile  $\text{IrO}_2$  at room temperature for  $\vec{E}||c$  and  $\vec{E}\perp c$  in the energy range 0.5–9.5 eV. Dotted lines represent the extrapolation of the reflectivity.

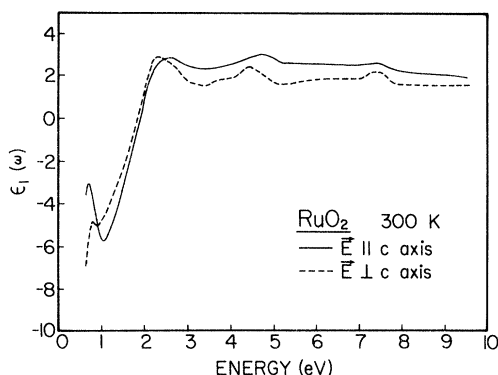


FIG. 3. Real part of the dielectric constant  $\epsilon_1$  of single-crystal rutile RuO<sub>2</sub> for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

IrO<sub>2</sub>. We have denoted the structural features in  $\epsilon_2$  related to those in the reflectivity spectra.

#### IV. DISCUSSION OF RESULTS

In the rutile structure each metal atom is surrounded by a nearly octahedral array of six oxygen atoms. The octahedral component of the ligand field causes metal  $d$  levels to be split into triply degenerate  $t_{2g}$  and doubly degenerate  $e_g$  components.<sup>33</sup> The  $t_{2g}$  and  $e_g$  degeneracies are lifted by the orthorhombic distortion. In these materials, the ten metal-atom  $d$ -states, which form the conduction bands, are separated by an energy gap from the 12 oxygen  $2p$  states, which constitute the valence bands. The position of the Fermi level depends on the number of  $d$  electrons. In RuO<sub>2</sub> with four  $d$  electrons and in IrO<sub>2</sub> with five  $d$  electrons per metal atom the Fermi level will lie in the  $d$ -band complex.

In order to analyze our experimental results, we have made use of two recent theoretical works as

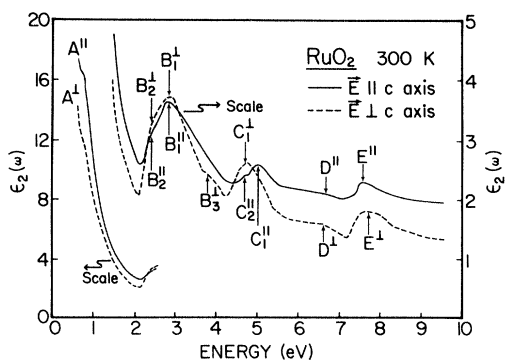


FIG. 4. Imaginary part of the dielectric constant,  $\epsilon_2$  of single-crystal rutile RuO<sub>2</sub> for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

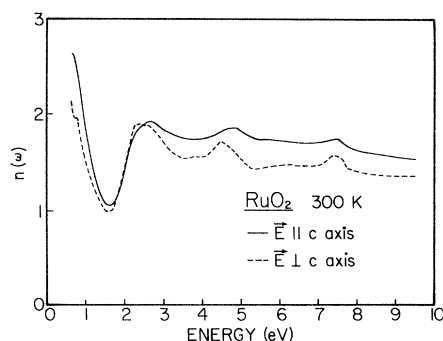


FIG. 5. Real part of refractive index  $n$  of single-crystal rutile RuO<sub>2</sub> for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

well as past experimental studies of related materials such as TiO<sub>2</sub> and VO<sub>2</sub>. Mattheiss has calculated the band structure as well as the density of states of the valence and conduction bands of RuO<sub>2</sub> and IrO<sub>2</sub>.<sup>34</sup> Posternak *et al.* have calculated the joint density of states for rutile NbO<sub>2</sub>, which has one  $d$  electron per metal atom.<sup>35</sup> They have also determined the band structure and individual density of states for this material.<sup>35</sup> Reflectivity and  $\epsilon_2$  spectra of rutile TiO<sub>2</sub> have been reported by Cardona and Harbeke who have studied in detail the optical properties and band structure of wurtzite-type crystals and rutile.<sup>24</sup> Finally, Verleur *et al.* have carried out a detailed optical investigation of VO<sub>2</sub>, which undergoes a sharp semiconductor to metal(rutile) transition at 68 °C.<sup>25</sup>

#### A. RuO<sub>2</sub>

Shown in Fig. 11 are the valence (oxygen  $p$  states) and conduction (Ru metal  $d$  states) band density of states for RuO<sub>2</sub> from Ref. 34. The effect of the crystal-field splittings of the  $d$  electron states

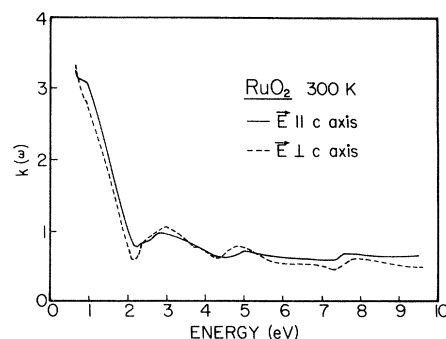


FIG. 6. Imaginary part of refractive index  $k$  of single-crystal rutile RuO<sub>2</sub> for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

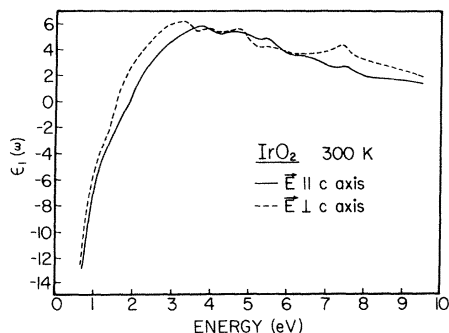


FIG. 7. Real part of the dielectric constant  $\epsilon_1$  of single-crystal rutile  $\text{IrO}_2$  for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

into  $t_{2g}$  and  $e_g$  bands is indicated. As shown by the position of the Fermi level,  $E_F$ , the  $t_{2g}$  orbitals are partially filled, while the  $e_g$  orbitals are empty. We note that the width of the  $t_{2g}$  bands is nearly 2.4 eV and the  $p$ - $d$  band gap is approximately 2.3 eV. However, Mattheiss has pointed out his calculations tend to overestimate the  $p$ - $d$  gap by several electron volts.

As shown in Fig. 4, the first major structure in  $\epsilon_2(\omega)$  is the large peak  $A$  which is observed for both polarizations below  $\sim 2$  eV. This pronounced feature is due primarily to free-carrier absorption with some contribution from  $d$ -electron intraband transitions (indicated by the small structure) within the  $t_{2g}$  manifold ( $d_1 \rightarrow d_2$  in Fig. 11). Evidence for this assignment of  $A$  comes from several considerations including the optical properties of  $\text{VO}_2$ , which undergoes a sharp transition at  $68^\circ\text{C}$  ( $T_c$ ) from the semiconducting monoclinic phase to the metal rutile phase (with one  $d$  electron per metal atom). In this material the corresponding low-energy peak appears at temperatures above  $T_c$  and

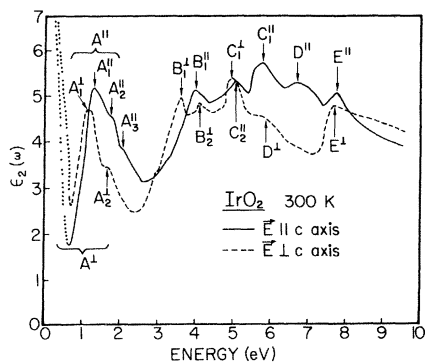


FIG. 8. Imaginary part of the dielectric constant  $\epsilon_2$  of single-crystal rutile  $\text{IrO}_2$  for  $\vec{E}||c$  and  $\vec{E}\perp c$ . Dotted lines correspond to extrapolated regions of Fig. 2.

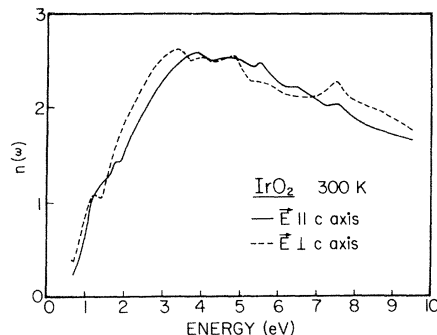


FIG. 9. Real part of refractive index  $n$  of single-crystal rutile  $\text{IrO}_2$  for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

is absent below it<sup>25,36</sup> and hence is clearly related to the  $d$  electrons. Also such a low-energy feature is not observed in the optical constants of  $\text{TiO}_2$ ,<sup>24</sup> which has the rutile structure with no  $d$  electrons. The joint-density-of-states calculation for  $\text{NbO}_2$  shows a pronounced bump in the region below 2 eV (with a maxima around 1.5 eV) which is a result of  $d$  electron intraband transitions within the  $t_{2g}$  manifold.<sup>35</sup> Thus, these intraband transitions are probably responsible for the peak ( $\vec{E}||c$ ) and shoulder ( $\vec{E}\perp c$ ) on the large- $A$  feature (see Fig. 4). The spectral dependence of the  $\epsilon_1(\omega)$  curve (see Fig. 3) below about 3 eV is similar to that for materials which have both free-electron and  $d$ -band contributions to the optical properties.<sup>32</sup>

The structure at photon energies above about 2.5 eV is due to  $p \rightarrow d$  interband transitions. Similar features are seen for both phases of  $\text{VO}_2$ .<sup>25,36</sup> The first  $p \rightarrow d$  peak in  $\epsilon_2$ , represented by  $B_1$ , appears at approximately 2.8 eV. However, in the basis of Fig. 11 we expect it to be due to transitions from the valence states  $p_1$  to conduction states  $d_2$  and should occur at about 3.9 eV. This discrepancy be-

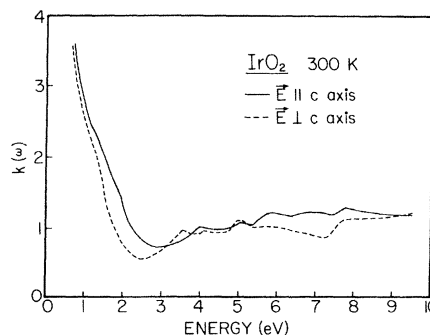


FIG. 10. Imaginary part of refractive index  $k$  of single-crystal rutile  $\text{IrO}_2$  for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

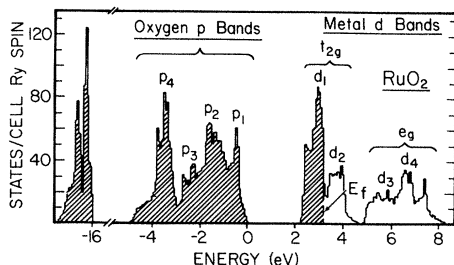


FIG. 11. Density of states for the valence (oxygen  $p$  levels) and conduction (metal  $d$  levels) bands of RuO<sub>2</sub> from Ref. 34. The ligand field splitting of the  $d$  levels into  $t_{2g}$  and  $e_g$  complexes is indicated.

tween the theoretically calculated density of states and our experimental results can be resolved if the  $p$ - $d$  band gap is reduced by  $\sim 1$  eV. After such a band-gap adjustment is made we can tentatively assign the peaks in  $\epsilon_2$  at about 5 eV (see Fig. 4) to transitions from  $p_3$  states to  $d_2$  states and the peaks at about 7.5 eV to transitions from  $p_2$  to  $d_4$  states.

### B. IrO<sub>2</sub>

The valence (oxygen  $p$  states) and conduction (Ir  $d$  states) band density of states for IrO<sub>2</sub> from Ref. 34 are shown in Fig. 12. The effect of the crystal field splittings of the  $d$  states into  $t_{2g}$  and  $e_g$  bands is also indicated. We see that in IrO<sub>2</sub>, having five  $d$  electron per metal atom, the  $t_{2g}$  bands are more filled compared to those in RuO<sub>2</sub> which has four  $d$  electrons per metal atom. The  $d_2$  manifold which is empty in the RuO<sub>2</sub> (see Fig. 11) is partially filled in IrO<sub>2</sub>; the filled and empty parts have been indicated by  $d_2'$  and  $d_2''$ , respectively (see Fig. 12). However, the  $e_g$  bands are empty in IrO<sub>2</sub> as well

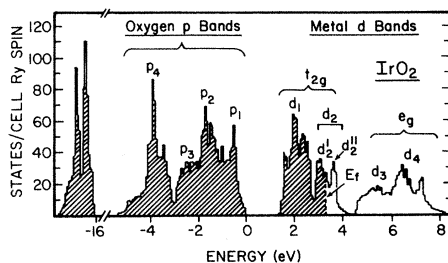


FIG. 12. Density of states for the valence (oxygen  $p$  levels) and conduction (metal  $d$  levels) bands of IrO<sub>2</sub> from Ref. 34. The ligand field splitting of the  $d$  levels into  $t_{2g}$  and  $e_g$  complexes is indicated.

Here, the width of the  $t_{2g}$  bands is nearly 2.8 eV and the  $p$ - $d$  band gap as calculated by Mattheiss is approximately 1.5 eV.

Figure 8 shows the  $\epsilon_2$  spectra for  $\vec{E}||c$  and  $\vec{E}\perp c$  for IrO<sub>2</sub> in the energy range 0.5 to 9.5 eV. The dotted line corresponds to that in the reflectivity curves and is similar to  $\epsilon_2$  due to absorption by free charges only. The small features marked  $A_2$  and  $A_3$  are related to intraband electronic transitions within the  $t_{2g}$  complex, i.e., from filled  $d_1$  and  $d_2'$  to empty  $d_2''$  states shown in Fig. 12. The assignment of the  $A$  feature to free-carrier and intraband  $d$ -band effects is made since no  $p \rightarrow d$  interband transitions are expected below 2 eV as indicated by the  $\epsilon_1$  curves<sup>32</sup> (see Fig. 7) and also by Fig. 12 which shows that the width of the filled  $t_{2g}$  band is  $\sim 2$  eV. However, intraband transitions within the  $t_{2g}$  complex can occur up to  $\sim 2.8$  eV.

Above  $\sim 3$  eV, the structure in  $\epsilon_2$  is due to  $p \rightarrow d$  interband transitions. We see from Fig. 8 that the first  $p \rightarrow d$  peak in  $\epsilon_2$  appears at 4 eV for  $\vec{E}||c$  but at  $\sim 3.5$  eV for  $\vec{E}\perp c$ . On the basis of Fig. 12, however, we would expect it to occur at  $\sim 4$  eV resulting from transitions from  $p_1$  states to  $d_2''$  states. This difference between the theoretically expected and experimentally observed results can be resolved if we reduce the theoretically  $p$ - $d$  band gap for IrO<sub>2</sub> by  $\sim 5$  eV. Our reductions of the calculated band gaps for both RuO<sub>2</sub> and IrO<sub>2</sub> are consistent with the observation made by Mattheiss that his calculations tend to overestimate the band gap by several electron volts. After this band-gap adjustment is made, we can, as in the case of RuO<sub>2</sub>, tentatively assign the features  $C_2^||$  and  $C_1^\perp$  at about 5.2 eV and  $C_1^||$  at  $\sim 5.5$  eV (see Fig. 8) to transitions from  $p_3$  states to  $d_2''$  states (see Fig. 12) and the structures denoted by  $E^||$  and  $E^\perp$  at about 7.7 eV to transitions from  $p_2$  to  $d_4$  states. We note that the  $B_2$  peak is narrower in IrO<sub>2</sub> than in RuO<sub>2</sub>. This is probably because only the  $d_2''$  part of the  $d_2$  manifold is available as final states for transitions that give rise to this peak in IrO<sub>2</sub>, whereas the whole  $d_2$  manifold is available in RuO<sub>2</sub>.

It is interesting to compare the  $\epsilon_2$  spectra of RuO<sub>2</sub> and IrO<sub>2</sub>. Table I summarizes the energy positions of the major features in  $\epsilon_2$  of both RuO<sub>2</sub> and IrO<sub>2</sub> and our assignments of the interband transitions related to them. The comparison shows that both in RuO<sub>2</sub> and IrO<sub>2</sub>, the  $\epsilon_2$  spectra above 2.5 and 3 eV, respectively, have three major features denoted by  $B$ ,  $C$ , and  $E$  which can be accounted for by similar  $p \rightarrow d$  transitions occurring in the two materials. For example, the  $B_1$  features

TABLE I. Energy positions of the major structures in the  $\epsilon_2$  spectra of RuO<sub>2</sub> and IrO<sub>2</sub> (see Figs. 4 and 8) and our assignment of the interband transitions.

Structure denoted by	RuO <sub>2</sub> <sup>a</sup>	IrO <sub>2</sub> <sup>b</sup>
<i>B</i> <sub>1</sub>	~2.8 eV ( <i>p</i> <sub>1</sub> → <i>d</i> <sub>2</sub> )	~3.7 eV ( <i>p</i> <sub>1</sub> → <i>d</i> ' <sub>2</sub> )
<i>C</i> <sub>1</sub>	~5.0 eV ( <i>p</i> <sub>3</sub> → <i>d</i> <sub>2</sub> )	~5.5 eV ( <i>p</i> <sub>3</sub> → <i>d</i> ' <sub>2</sub> )
<i>E</i>	~7.5 eV ( <i>p</i> <sub>2</sub> → <i>d</i> <sub>4</sub> )	~7.7 eV ( <i>p</i> <sub>2</sub> → <i>d</i> <sub>4</sub> )

<sup>a</sup>After reduction of band gap by ~1 eV.

<sup>b</sup>After reduction of band gap by ~0.5 eV.

are associated with *p*<sub>1</sub>→*d*<sub>2</sub> (or *d*'<sub>2</sub> in IrO<sub>2</sub>) transitions, the features denoted by *C*<sub>1</sub> represent *p*<sub>3</sub>→*d*<sub>2</sub> (or *d*'<sub>2</sub>) transitions and the structures indicated by *E* have been assigned the *p*<sub>2</sub>→*d*<sub>4</sub> transitions.

For a free-electron gas and in the absence of any interband transitions, the real part of the dielectric constant [ $\epsilon_1 = 1 - (\omega_p^2/\omega^2)$ ] becomes zero at the plasma frequency given by  $\omega_p = (4\pi Ne^2/m^*)^{1/2}$ , where *N* is the density of free electrons, *e* is the electronic charge, and *m*<sup>\*</sup> is the effective mass of the electron inside the metal. However, in the presence of interband transitions, experimental  $\epsilon_1$  has free and bound contributions and, starting from negative values, becomes zero at a frequency  $\omega_i < \omega_p$  where  $\hbar\omega_i$  indicates the threshold energy for interband transitions.<sup>32</sup> The  $\epsilon_1$  spectra for RuO<sub>2</sub> and IrO<sub>2</sub> in the energy range 0.5–9.5 eV are shown in Figs. 3 and 7, respectively. We note that the values of  $\hbar\omega_i$  in the two cases are nearly 1.8 and 2.0 eV, respectively. Effective masses of the electron in RuO<sub>2</sub> and IrO<sub>2</sub> are not available in literature at present. Therefore, the exact values of the plasma frequencies for them cannot be estimated. However, it can be said that these will be well above the respective  $\hbar\omega_i$  values.

We can calculate  $n_{\text{eff}}$ , an effective number of electrons per atom contributing to the optical properties in the finite energy range 0 to  $\omega_0$  with the help of a sum rule expressed by Phillip and Ehrenreich<sup>37</sup>:

$$n_{\text{eff}}(\omega_0) = \frac{m}{2\pi^2 Ne^2} \int_0^{\omega_0} \omega \epsilon_2(\omega) d\omega, \quad (3)$$

where  $\omega$  is the angular frequency of the light, *m* is the free electron mass, *e* is the electronic charge, and *N* is the number of atoms per unit volume. To

apply Eq. (3) to RuO<sub>2</sub> (or IrO<sub>2</sub>), it is more appropriate to define *N* as the number of Ru (or Ir) atoms per unit volume, in which case  $n_{\text{eff}}$  becomes the effective number of electrons pre Ru (or Ir) atom contributing to the optical absorption up to a frequency  $\omega_0$ .

Figure 13 shows  $n_{\text{eff}}$  determined from the optical data of RuO<sub>2</sub> for both  $\vec{E}||c$  and  $\vec{E}\perp c$  in the energy range 0.5 to 9.5 eV. Near a photon energy of 2.5 eV there is an abrupt increase in the slope of  $n_{\text{eff}}$  which indicates the onset of interband transitions between the oxygen *p* bands and the ruthenium *d* bands. This conforms to our assignment of the structure in  $\epsilon_2$  above 2.5 eV to interband *p*→*d* optical transitions and that below 2.5 eV to free-electron absorption and intraband *d*→*d* transitions. For IrO<sub>2</sub>,  $n_{\text{eff}}$  for both polarizations is shown in Fig. 14. In this case we seen an abrupt increase in the slope of  $n_{\text{eff}}$  at about 3 eV which again confirms our identification of the features in  $\epsilon_2$  above

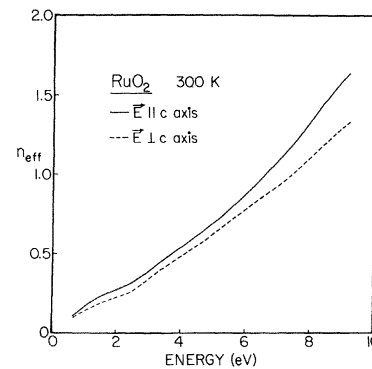


FIG. 13. Effective number of electrons per Ru atom,  $n_{\text{eff}}$ , contributing to the optical absorption in RuO<sub>2</sub> at room temperature for  $\vec{E}||c$  and  $\vec{E}\perp c$ .

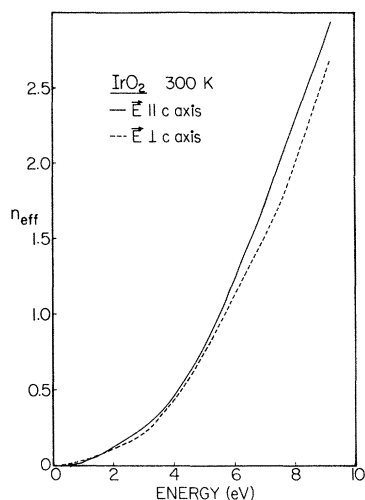


FIG. 14. Effective number of electrons per Ir atom,  $n_{\text{eff}}$ , contributing to the optical absorption in IrO<sub>2</sub> at room temperature for  $\vec{E} \parallel c$  and  $\vec{E} \perp c$ .

3 eV with interband transitions and those below 3 eV to intraband  $d$  transitions in addition to free-carrier absorption. The reason why the interband transitions in IrO<sub>2</sub> start at a higher energy than in RuO<sub>2</sub> is due mainly to the fact that the Fermi level  $E_F$  is higher in the former material.

More understanding of the nature of optical processes in RuO<sub>2</sub> and IrO<sub>2</sub> can be gained by comparison of our  $\epsilon_2$  spectra for those two materials with that of TiO<sub>2</sub> as obtained by Cardona and Harbeke.<sup>24</sup> It will be noticed that the structures in RuO<sub>2</sub> and IrO<sub>2</sub> are not nearly as sharp or as strong as in TiO<sub>2</sub> at  $\sim 4$  eV. This is a very striking effect and could be explained in several possible ways. Lifetime broadening is perhaps the least likely explanation because of the very large broadening required. A more satisfactory explanation of the difference in the magnitude of the absorption is that, in TiO<sub>2</sub>, the final states associated with the absorption peaks lie in the lowest conduction band whereas in RuO<sub>2</sub> and IrO<sub>2</sub>, the lowest conduction bands are partially occupied by extra  $d$  electrons. Cardona and Harbeke<sup>24</sup> have suggested that in TiO<sub>2</sub>, some of the optical structure up to 10 eV may arise from exciton effects. These effects are

expected to give rise to sharp structure near critical points as observed near 4 eV. Such exciton effects would, however, be suppressed in RuO<sub>2</sub> and IrO<sub>2</sub> due to the screening by the large number of free carriers in these materials.

## V. CONCLUSIONS

We have performed the first comprehensive optical investigation of the single-crystal rutile RuO<sub>2</sub> and IrO<sub>2</sub>. The near-normal incidence reflectivity has been measured for  $\vec{E} \parallel c$  and  $\vec{E} \perp c$  in the energy range 0.5–9.5 eV and we have deduced the optical constants from Kramers-Kronig analyses combined with angular reflectivity measurements. The imaginary part of the dielectric constant ( $\epsilon_2$ ) has been compared with the band-structure and density-of-states calculations of Mattheiss as well as the theoretical work of Posternak *et al.*

For RuO<sub>2</sub>, the structure in  $\epsilon_2$  below 2 eV is assigned to free-carrier absorption and  $d \rightarrow d$  electron transitions. Above about 2.5 eV, all the features in  $\epsilon_2$  represent  $p \rightarrow d$  interband transitions. Our results indicate that the calculation of Mattheiss has overestimated the  $p$ - $d$  band gap in RuO<sub>2</sub> by  $\sim 1$  eV.

For IrO<sub>2</sub>, the structure in  $\epsilon_2$  below 2.5 eV is assigned to free-carrier absorption and  $d \rightarrow d$  intraband transitions. Above about 3 eV, all the features in  $\epsilon_2$  represent  $p \rightarrow d$  interband transitions. Our results indicate that the calculation of Mattheiss has overestimated the  $p$ - $d$  band gap in IrO<sub>2</sub> by  $\sim 0.5$  eV.

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