Spontaneous recombination volumes of Frenkel defects in neutron-irradiated non-fcc metals

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Production and production-rate curves for the non-fcc metals Fe, Mo, Ta, W, Zr, and Sn are obtained by electrical-resistivity measurements taken at 4.6 K during reactor neutron irradiations. The saturation concentration of Frenkel defects, c_s , and the recombination volume v_o are evaluated. A parabolic relation between the spontaneous recombination volume v_0 and the compressibility κ for a series of bcc metals is found.

I. INTRODUCTION

In contrast to fcc metals, much less radiationdamage studies exist on bcc and hcp metals. Furthermore, data on production rate of Frenkel defects and spontaneous recombination volumes are not unique for the non-fcc metals. In a recent study of neutron-irradiated V and $Mo_j⁻¹$ it has been pointed out that the spontaneous recombination volumes of these two bcc metals differed by more than a factor of 3. These facts are contrary to the suggestion made by Horak and Blewitt² according to which bcc metals, in general, have an abnormally low recombination volume compared with fcc metals. In connection with this pared with ICC metals. In connection with the
problem, Biget *et al*.³ suggested a relationshi between the spontaneous recombination volumes v_0 of several bcc metals and their compressibilities. However, numerical results on recombination volumes were obtained, in general, from only low-dose experiments. Therefore, the parabolic relationship was, in our opinion, essentially qualitative. In the past, low-temperature fast-neutron irradiation experiments on supereonducting materials including Nb, V, and Ta were also performed by Brown et $al.^4$ However, the scatter of the experimental points in production-rate curves was too large to obtain reliable data on

saturation resistivities and recombination volumes.

In this work we report about damage-rate measurements during fast-neutron irradiation at 4.6 K on the bcc metals Fe, Mo, Ta, and W, the hcp metal Zr , and the tetragonal metal β -Sn. These measurements are related to a similar study on fcc metals.⁵ The irradiation were performed up to integrated doses of 2.39×10^{18} fast neutrons/ $cm²$, in two cases (Fe and Sn) to about $10¹⁹$ fast neutrons/cm'. The damage rate was monitored by electrical-resistivity measurements.

II. EXPERIMENTAL

All relevant details of the samples are collected in Table I. The polycrystalline sample wires (diameter D and length L) have been purchased from the indicated companies. The residual resistivity ratios (RRR) $\rho_{297\,\text{K}}/\rho_{4.6\,\text{K}}$ are given before and after the annealing treatment. Values of $\rho_0 = \rho_{4.6K}$ have been determined from the final RRR's using tabulated values⁶ of $\rho_{297 \text{ K}}$ $\Delta \rho_{\text{max}}$ is the maximum induced electrical resistivity and $\phi t_{\tt max}$ is the corresponding fast neutron dose (for $E > 0.1$ MeV). The residual-resistivity values givep in the table are without any size-effect corrections.

TABLE I. Sample specifications. The polycrystalline sample wires (diameter D and length L) have been purchased from the indicated companies. MRC is short for Materials Research Corporation. E.S.P.I. is short for Electronic Space Production, Inc. The residual-resistivity ratios (RRR) $\rho_{297K}/\rho_{4.6K}$ are given before and after the annealing treatment. Values of $\rho_0 = \rho_{4.6K}$ have been determined (always without any size-effect correction) from the final RRR's using tabulated values (Ref. 6) of ρ_{297K} . $\Delta\rho_{max}$ is the maximum induced electrical resis-
tivity and ϕt_{max} is the corresponding fast-neutron dose (for $E > 0.1$ M

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Irradiations were performed at 4.6 K in the liquid-helium irradiation facility of the Munich Research Reactor (FRM). The nominal value of the local fast-neutron flux ϕ_0 (E>0.1 MeV) was 1.3×10^{13} n/cm² sec; the corresponding resonance flux (related to the gold resonance) was 1.2×10^{12} $n/cm²$ sec and the thermal flux was 1.5×10^{13} $n/$ cm'sec. Details about the flux spectrum, the sample holder, and the resistivity measurement apparatus are given in Ref. 5. In order to record the evolution of the defect production with increasing neutron doses, we have irradiated Fe during 183 ^h 45 min (i.e., up to integrated doses of 8.25 \times 10¹⁸ fast neutrons/cm²), Sn during 213 h 30 min

 $(10.25 \times 10^{18}$ fast neutrons/cm²), and Mo, Ta, W, and Zr during 52 h 40 min $[(2.36 - 2.53) \times 10^{18}$ fastneutrons/cm']. More than 200 resistivity mea surements vere performed during the irradiations of Fe and Sn, and more than 80 measurements for Mo, Ta, W, and Zr.

III. RESULTS AND DISCUSSION

The experimental results for the increase $\Delta \rho$ of residual resistivity with irradiation dose ϕt are given in the Figs. 1-6. The derived resistivity damage rates $d\Delta\rho/d\phi t$ as a function of $\Delta\rho$ are also given in these figures.

FIG. 2. Dose-curve results for Mo. For the presentation of the data see caption of Fig. 1.

FIG. 3. Dose-curve results for Ta. Both two series of plots of $\Delta \rho$ vs ϕt and two differentiated plots are shown. For the presentation of the data see caption of Fig. 1.

As was shown in Ref. 5, the production-rate curves can be analyzed in terms of a third-order polynomial,

$$
\frac{d\Delta\rho}{d\phi t} = A + B\Delta\rho + C\Delta\rho^2 + D\Delta\rho^3 \t\t(1)
$$

or a second-order polynomial,

$$
\frac{d\Delta\rho}{d\phi t} = A + B\Delta\rho + C\Delta\rho^2 \tag{2}
$$

According to the theory of Lück and Sizmann⁷ also

a linear relation between $d\Delta\rho/d\phi t$ and $\Delta\rho$ is obtained,

$$
\frac{d\Delta\rho}{d\phi t} = A \left(1 - 2v_o \frac{\Delta\rho}{\rho_F} \right),\tag{3}
$$

where ρ_F is the Frenkel-defect specific resistivity and v_o is the spontaneous recombination volume.

For Fe and Sn both quadratic and linear fits were applied (for cubic fits, see Ref. 5). In the case of other samples, in addition to the relatively small neutron doses and great "tail" in the beginning of the irradiation, the scatter of the experi-

FIG. 4. Dose-curve results for W. For the presentation of the data see , caption of Fig. 1.

FIG. 5. Dose-curve results for Zr. Two series of plots of $\Delta \rho$ versus ϕt are shown (right-hand-side and top scales) and the differentiated plots $d\Delta\rho/d\phi t$ vs $\Delta \rho$ are shown for two samples. For $Zr(1)$, the ordinate is shifted up by 1.0×10^{-25} Ω cm³. For the other presentation of the data, see captions of Fig. 1.

mental points was too large to permit a preference as to the linear or quadratic fit; thus, we have made only a linear evaluation for these metals. The linear fit was done for all but the first "tail" points.

The extrapolation of the damage rate curves towards zero-change rate leads to the saturation resistivity $\Delta \rho_s$ which is given in Table II. In this case one obtains from Eq. (3) for the spontaneous recombination, volume the expression

$$
v_0 = \rho_F / 2 \Delta \rho_s \tag{4}
$$

Using Eq. (2) one obtains for the spontaneous re-

combination volume according to Refs. 5 and 8

$$
v_0 = \rho_F / \Delta \rho_s \tag{5}
$$

Thus calculated values of the spontaneous recombination volumes are given in Table II together with values taken from the literature.

By the way, the characteristic resistivity of a Frenkel pair, ρ_F , is a fundamental parameter in these studies, so the significance of its choice has been discussed in great detail in Hefs. 1 and 9. However, we prefer to choose ρ_r values same as in Ref. 3 to simplify the comparison with results in the past.

FIG. 6. Dose-curve results for Sn. For the presentation of the data see caption of Fig. 1.

Samples Fe	$\Delta\rho_{\rm max}$ 4208.2	$\Delta \rho_{s}$ (fit) $(n\Omega$ cm)	ρ_F $(\mu \Omega \text{ cm}/\text{at. } \%)$		$c_s = \Delta \rho_s / \rho_F$ $(10^{-3}$ at. fraction)	Ours v_0 $(at. vol.)$.	Literature v_0 (at, vol.)		κ $(10^{-12}$ cm ² /dyn)
		6300 ± 200 (lin.) 5800 \pm 100 (quadr.)	19	Ref. 2	3.32 ± 0.10 3.05 ± 0.05	151 ± 5 328 ± 6	105 $43 \sim$ - 67	Ref. 3 Ref. 2	0.589
Mo	948.2	5260 ± 760 (lin.)	13 ± 2	Ref. 9	4.05 ± 0.58	124 ± 18	30 $200 \pm$ $120 \sim 155$	Ref.3 Ref. 2	0.383
Ta(1) Ta(2)	689.8 645.8	4450 ± 200 (lin.)	17.5	Ref. 18	2.54 ± 0.11	197 ± 9	$240 \pm$ 40 280	Ref.3 Ref. 20	0.510
W	922.8	7140 ± 680 (lin.)	13	Ref. 3	5.49 ± 0.52	91 ± 9	190	Ref. 3	0.321
Zr(1) Zr(2)	4819.2 4625.2	20000 ± 500 (lin.) 20500 ± 500 (lin.)	40	Ref. 22	5.00 ± 0.13 5.10 ± 0.13	100 ± 3 98 ± 3	195 ± 17	Ref. 21	\dddotsc
Sn	491.8	10 (lin.) 536 \pm 558 \pm 10 (quadr.)	1.1	Ref. 23	4.87 ± 0.09 5.07 ± 0.09	103 ± 2 197 ± 4	\cdots		\cdots

TABLE II. Results of the quadratic (for Fe and Sn) and linear fits to the production rate curves. The values ρ_F (defined by $\Delta \rho = c \rho_F$) are taken from the literature. $\Delta \rho_s$ is the extrapolated saturation resistivity and v_0 is the recombination volume as calculated from Eq. (4) or (5). The compressibility κ is taken from Ref. 24.

A. Iron (Fig. 1)

The striking feature of the production rate curve
Fe is the negative (convex) curvature.¹⁰ This of Fe is the negative (convex) curvature.¹⁰ This behavior, indeed, represents a realistic physical effect and not, for example, an experimental artifact. The sample temperature was always that of liquid helium. Any possible (although probably negligible) change of the local neutron spectrum during a period of continuous reactor operation should be much more pronounced during the first 30 h of operation (buildup of the $135Xe$ poisoning) than in the remaining 170 h. Note that the defect production curves of other metals as Al, which according to Ref. 5 were contained in the same sample holder as the Fe sample of this paper. are perfectly regular and exhibit the usual positive (concave) curvature without any particularity around $\phi t = 1.4 \times 10^{18}$ n/cm² (corresponding to 30 h) as mentioned above); this also demonstrates that our continuous local-fast-neutron-flux monitor, which uses the $^{16}O(n, p)^{16}N$ reaction and so measures only the fastest neutrons having energies above 10 MeV, indeed provides a realistic information about the "fast-flux" ϕ and that changes of the neutron spectrum within a reactor operation period are insignificant.

Previously, Horak and Blewitt² obtained results for the differentiated dose curve of reactor-irradiated Fe which are also consistent with a negative curvature, although the larger scatter of the data and the much smaller irradiation dose did not allow them to clearly recognize this effect. More recently the convex curvature has been confirmed

in independent low-temperature reactor irradiain independent low-temperature reactor irradia-
tions of Fe in Garching-Munich¹¹ and Paris.¹² The magnitude and dose range of the convex curvature seems to depend on the purity of the Fe samples and on the type of irradiating particles since the effect obviously does not occur during electron 12 or fission-fragment¹³ irradiation. The negative curvature of the differentiated dose curve of Fe, which has also been observed during reactor irwhich has also been observed during reactor Γ . within the framework of usual defect production theory since the overlap of recombination volumes $v₀$ would always lead to a positive (concave) curvature.¹⁴ Very probably the negative curvature is caused by a decrease of the electrical resistivity per Frenkel defect, when the individual displacement cascades overlap during high-dose reactor irradiation leading to the growth and to configura
tion changes of the defect clusters.^{5,11}

.The results of a computer fit for Eq. (2) was best with $B/A = -9.91 \times 10^{-5}$ (nQ cm)⁻¹ best with $B/A = -9.91 \times 10^{-5}$ (n Ω cm)⁻¹ and C/A
= -1.25 × 10⁻⁸ (n Ω cm)⁻², and for $\Delta \rho$ >70 n Ω cm the
fit deviation was always smaller than 0.04 × 10⁻²⁵ fit deviation was always smaller than 0.04×10^{-25} Ω cm³. From this high-dose fit we obtained the saturation resistivity $\Delta \rho_s = 5800 \text{ n}\Omega \text{ cm}$, a value which is significantly smaller than the low-dose extrapolation result ($\Delta \rho_s = 9230$ n Ω cm) of Horak extrapolation result ($\Delta \rho_s = 9230 \text{ n}\Omega \text{ cm}$) of Horak
and Blewitt.² Assuming $\rho_F = 19 \mu\Omega \text{ cm/at.} \%$, ¹⁵ we obtain from Eq. (5) $v_0 \approx 330$ at. vol.

Horak and Blewitt used the value ρ_F = 12.5 $\mu\Omega$ cm/ at. % and obtained $v_0 = 43-67$ at. vol. (i.e., 65-101) at. vol., if $\rho_F^{}$ = 19 $\mu\Omega$ cm/at. $\%$ is applied). Biget *et al.* adopted the value $v_0 = 105$ at. vol. In any case, our result $v_0 \approx 330$ at. vol. for the spontaneous recombination volume of Fe is larger by a factor 3 to 5 than the other.

For reference, the results of the computer fit for Eq. (3) (linear fit) are also listed on the upper row in third, fifth, and sixth columns in Table II. In case of the linear fit, we obtain from Eq. (4) $v₀ \approx 150$ at. vol.

On the other hand, an irradiation experiment at 20 K by fission fragments¹⁶ shows $\Delta \rho_s = 3000 4000 \text{ n}\Omega \text{ cm}$ (quadratic fit) for Fe and suggests much larger recombination volume, though as discussed in Ref. 5 radiation damage by fission fragments might be different from that by neutrons.

B. Molybdenum (Fig. 2)

There are some experimental data to be compared with our results. Maury $et al.^9$ determined the Frenkel pair resistivity from the results of their experiments; $\rho_F = 13 \pm 2 \mu \Omega \text{ cm/at. } \%$. Applying the value determined thus, they get v_o $= 200 - 250$ at. vol. Recently, Biget et al. modified this value and adopted $v_0 = 200 \pm 30$ at. vol. in Ref. 3, as listed in Table II. On the other hand, Horak and Blewitt² obtained $v_0 = 120-155$ at. vol., assuming $\rho_r = 10 \mu \Omega \text{ cm/at.} %$

As seen in Fig. 2, Mo shows a great "tail" which is interpreted as stemming from $long-range$ collision sequences.¹⁷ From the rest of the points, lision sequences.¹⁷ From the rest of the points we have calculated the saturation resistivity by a linear fit, leading to the recombination volume v_0 = 124 at. vol. This value is smaller by factor of $\frac{2}{3}$ than that of Biget et al.³

C. Tantalum (Fig. 3)

Biget et al.³ have taken $\rho_F = 17.5 \mu \Omega \text{ cm/at. } \%$ as determined by Jung and Schilling¹⁸ and obtained $v_0 = 240 \pm 40$ at. vol. using the saturation resistivity $v_{\rm o}$ = 240 ± 40 at. vol. using the saturation resistivi
of Ta irradiated by electrons.¹⁹ Biget *et al*. have also listed $\rho_r = 24 \mu \Omega \text{ cm/at. } \% \approx 2 \rho_0$ in their table. However, in our opinion, the relation $\rho_r \approx 2\rho_0$ is only a criterion for unestablished values of elements. On the other hand, Faber²⁰ has obtained $v_0 = 280$ at. vol., assuming $\rho_F = 17 \mu \Omega \text{ cm/at. } \%$. Our result v_0 = 197 at. vol. for Ta is smaller by factor of $\frac{2}{3}$ than that of Ref. 20.

D. Tungsten (Fig. 4)

Biget *et al*. have taken $\rho_F = 13 \mu \Omega \text{ cm/at. } \%$ of Frenkel pairs, in view of the close resemblance in the electrical properties of Mo and W and presented the value v_0 = 190 at. vol.³ Our result v_0 $= 91$ at. vol. for W is much smaller by a factor of $\frac{1}{2}$ than that of the above-mentioned low-dose data.

The fission-fragments irradiation experiment¹⁶ gave the saturation resistivity $\Delta \rho_s \sim 8000 \text{ n}\Omega \text{ cm}.$ Assuming $\rho_F=13 \mu\Omega \text{ cm/at.}$ % one obtains $v_0=80$

at. vol. , which closely resembles our result.

E. Zirconium (Fig. 5)

E. Zirconium (Fig. 5)
Vialaret *et al*.²¹ performed electrical-resistiv measurements to study the creation and annealing out of defects in Zr irradiated at 24 K by fast neutrons. They obtained an apparent recombination volume of 195 ± 17 at. vol. independent of oxygen content using the resistivity per Frenkel pair ρ_F =40 $\mu\Omega$ cm/at. % after Biget *et al*.²² The maximum induced resisitivity was about $2500 \text{ n}\Omega \text{ cm}$, which was only a half of ours.

Although a large scatter of the experimental points exists in our measurement, we obtain v_o $= 98 \times 100$ at. vol. from the linear fit as listed in Table II. The discrepancy between ours and Vialaret $et al.'s$ values of a factor of 2 may come from the difference of the irradiation temperature. Further experiments on Zr and on other hcp metals, such as Mg, Ti, Co, and Zn, are very desirable.

F. Tin $(\beta$ -Sn) (Fig. 6)

Tin has no other data to be compared with our results. In this experiment, the fluctuation of the data was not small, so we could not choose decidedly between quadratic and cubic fits. Saturation values from above fits are 558 and 544 n Ω cm for quadratic and cubic fits, respectively. Assuming the resistivity of Frenkel pair $\rho_r = 1.1$ suming the resistivity of Frenkel pair $\rho_F = 1.1$
 $\mu\Omega$ cm/at. %, ²³ we obtain $v_0 = 200$ at. vol. In the cases of the linear fit, for reference, we obtain from Eq. (4) v_0 = 103 at. vol. as listed in Table II.

G. Parabolic relation between the spontaneous recombination volume and the compressibility

It was suggested by Biget $et \ al.^3$ that there is a relationship between the spontaneous recombination volumes and the compressibility of the bcc metals. For W, Mo, Ta, Nb, and V they found a power law of roughly second order. In Pig. 7 we have now plotted our values of the spontaneous

FIG. 7. Spontaneous recombination volume v_0 of several bcc metals as a function of their compressibility κ .

recombination volumes v_0 as a function of the compressibility κ . The values of κ are taken from Ref. 24 (see Table II). We can also put one curve through our points which is roughly of second order, though our values for the recombination volume differ from those of Biget $et al.^3$ However, such an analysis has to be taken with caution keeping in mind the uncertainty of the spontaneous recombination volumes due to the uncertainty of the values of ρ_r .

IV. SUMMARY

Polycrystalline wires have been irradiated at 4.6 K by reactor neutrons $(E > 0.1 \text{ MeV})$ to a dose of $(2.3-2.5) \times 10^{18}$ n/cm² for Mo, Ta, W, and Zr, 8.25×10^{18} n/cm² for Fe, and 10.25×10^{18} n/cm² for Sn. Production and production rate curves were obtained by electrical-resistivity measurements taken at 4.6 K. Saturation concentration of Frenkel defects c_s and spontaneous recombina-

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tion volumes $v_{\rm o}$ were evaluated. For Mo, Ta, W, and Zr, v_0 values are by a factor of $\frac{1}{2}$ to $\frac{2}{3}$ smaller whereas for Fe v_0 is a factor 3 to 5 larger than the values given-in the literature for low-dose experiments. A parabolic relation between the spontaneous recombination volume v_0 and the compressibility κ for Fe, Mo, Ta, and W is found.

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