Thermoelectric power and transverse Nernst-Ettingshausen coefficient of Cd₃As₂ at 300 K

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The thermoelectric power and the transverse Nernst-Ettingshausen coefficient of cadmium arsenide (Cd_3As_2) at room temperature have been calculated as a function of electron concentration, taking into account the HgTe-type inverted electronic-energy-band structure of this material. In the calculation, electron scattering due to polar-optical phonons, charged centers, and acoustical phonons has been considered. Since numerical values were available for every parameter involved except E_d , the acoustical-deformation-potential constant, the latter was treated as an adjustable parameter to fit the theoretical curves with experimental results. It was found that E_d lies between 10 and 20 eV consistent with the approximate value estimated in a previous paper.

I. INTRODUCTION

The electronic-energy-band structure of cadmium arsenide $(Cd_{3}As_{2})$, after having been a question mark for some time, now appears to be similar to that of HgTe.¹ This point of view has been substantiated by several recent publications^{2,3} which showed that this model of band structure for Cd₃As₂ is consistent with all the available experimental data. The purpose of the present paper is to calculate the thermoelectric power α and the transverse Nernst-Ettingshausen coefficient $P_{\rm NE}$ of $\rm Cd_3As_2$ at room temperature as a function of electron concentration, taking explicitly into account the HgTe-type inverted energy-band structure of this material. As in our previous work on the electrical resistivity of Cd₃As₂,^{4,5} the calculation of α and $P_{\rm NE}$ is carried out for the mixed mode of polar-optical phonon, chargedcenter, and acoustical-phonon scattering, using the theoretical results of Zawadzki et al.⁶⁻¹⁰ In the light of all the results we have recently obtained for Cd_3As_2 ,²⁻⁵ there is only one unknown in the calculation of α and $P_{\rm NE}$, which is the acoustical-deformation-potential constant E_d . The latter is used in our procedure as an adjustable parameter to be determined by comparing the calculated results with all the available experimental data on α , ¹¹⁻²³ and $P_{\rm NE}$.^{14, 15, 20}

II. THEORY

According to Zawadzki and co-workers, $^{6-10}$ the general expressions to calculate α and $P_{\rm NE}$ under high statistical degeneracy conditions are given by

$$\alpha = A \left(R + 5 - 6l \right) \tag{1}$$

and

$$P_{\rm NE} = A(\mu/c)(R+2-6l), \qquad (2)$$

where

$$A = -\frac{1}{3} \left(\frac{\pi}{3}\right)^{2/3} \frac{k_B^2}{\hbar^2} \frac{T}{e} \frac{m^*}{n^{2/3}} , \qquad (3)$$

 k_B is Boltzmann's constant, c is the speed of light, T is the absolute temperature, \hbar is Planck's constant divided by 2π , e is the magnitude of the electronic charge, and m^* is the electron effective mass at the Fermi energy E_F . R is the effective scattering index which, for the combined scattering mode of polar-optical phonons (op), charged centers (cc), and acoustical phonons (ac), is given by

$$R = \mu \left(\frac{r'_{\text{op}}}{\mu_{\text{op}}} + \frac{r'_{\text{cc}}}{\mu_{\text{cc}}} + \frac{r'_{\text{ac}}}{\mu_{\text{ac}}} \right), \qquad (4)$$

where

$$\mu = \left(\frac{1}{\mu_{op}} + \frac{1}{\mu_{cc}} + \frac{1}{\mu_{ac}}\right)^{-1}$$
(5)

is the overall electron mobility calculated from the contributions of the three scattering mechanisms considered, namely,⁵

$$\mu_{op} = \frac{\hbar^3 k_F}{2ek_B T (1/\epsilon_{\infty} - 1/\epsilon_0) (m^*)^2 F_{op}}, \qquad (6)$$

$$\mu_{\rm cc} = \frac{\epsilon_0 \hbar^3 k_F^3}{2\pi e^3 (m^*)^2 N F_{\rm cc}},\tag{7}$$

$$\mu_{ac} = \frac{\pi e \hbar^3 dv_{\parallel}^2}{k_B T E_d^2 (m^*)^2 k_F F_{ac}},$$
(8)

and

$$r' = r - \frac{k_F}{F_r} \left(\frac{dF_r}{dk} \right)_{k=k_F}$$
(9)

denotes the effective scattering index for the electron-scattering mode in question. In Eqs. (6)-(9), ϵ_0 and ϵ_{∞} are the low- and high-frequency

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dielectric constants, k_F is the wave number at the Fermi energy related to the electron concentration in a spherically symmetric degenerate band^{24,25} by

$$k_{\rm F} = (3\pi^2 n)^{1/3} \,, \tag{10}$$

N is the total concentration of ionized impurities, d is the material density, v_{\parallel} is the longitudinal velocity of sound in the material, E_d is the acoustical-deformation-potential constant, and r takes the values 1, -1, and -3 for charged-center scattering, polar-optical phonon scattering, and acoustical phonon scattering, respectively.

The F_r factors for each electron scattering mode are rather involved functions defined in the abovementioned references.³⁻¹⁰ It is worth mentioning, however, that the mixing of *s*- and *p*-like components in the total conduction-band wave function also allows a nonvanishing coupling of electrons to the transverse acoustical phonons, as is transparent in the following expression for F_{ac} :

$$F_{ac} = F_{ac}^{\parallel} + (v_{\parallel}^2 / v_{\perp}^2) F_{ac}^{\perp}, \qquad (11)$$

where the symbols || and \perp refer to the longitudinal and transverse modes, respectively.

Finally, l is a parameter which is defined as

$$l = \frac{1}{3} \left[1 - \frac{m^*}{\hbar^2} \left(\frac{d^2 E}{dk^2} \right)_{k=k_F} \right] = \frac{k_F}{3m^*} \left(\frac{dm^*}{dk} \right)_{k=k_F}, \quad (12)$$

where E(k) is the dispersion relation for the conduction band. It is clear from Eq. (12) that *l* gives a measure of the degree of nonparabolicity at the Fermi level of the actual E(k) relation.

III. NUMERICAL RESULTS AND DISCUSSION.

In order to calculate α and $P_{\rm NE}$ from Eqs. (1) and (2), we must specify the explicit dependence of m^* and of E_F as a function of electron concentration n (in cm⁻³) for Cd₃As₂ at room temperature. It has been found that^{2,5}

$$\left(\frac{m^*/m_0}{1-m^*/m_0}\right)^2 = 0.26 \times 10^{-3} + 1.1 \times 10^{-15} n^{2/3}, \qquad (13)$$

where m_0 is the free-electron mass, and

$$E_F = 0.095[(1 + 4.4 \times 10^{-12} n^{2/3})^{1/2} - 1] + 0.00364 \times 10^{-12} n^{2/3} \text{ (eV)}, \qquad (14)$$

when measured from the bottom of the conduction band.

The energy-band parameters of Cd_3As_2 at room temperature which are required in the calculation are the $\Gamma_8 - \Gamma_6$ energy gap $E_0 = 0.19$ eV, $E_P = P^2$ $(2m_0/\hbar^2) = 14$ eV, where *P* is proportional to the $\Gamma_8 - \Gamma_6$ momentum matrix element, and the spinorbit splitting of the valence band at the Γ point $\Delta = 0.30$ eV.^{2, 5, 26} We also need the numerical



FIG. 1. Thermoelectric power α in $\operatorname{Cd}_3\operatorname{As}_2$ at 300 K as a function of electron concentration n. The three curves are calculated for electrons scattered by the mixed mode of polar-optical phonons, charged centers, and acoustical phonons, using three different values of the acoustical-deformation-potential constant $E_d = 10$, 20, and 30 eV. The data points reproduced for comparison are from Refs. 11 (\bullet), 12(\diamond), 13 (∇), 14 (\Box), 15 and 19 (\triangle), 16 and 23 (O), 17 and 18 (\bullet), 20 (+), 21 (\times), and 22 (*).

values for five material parameters. The latter are d, which is 6.21 g/cm³ for Cd₃As₂,²⁷ v_{\parallel} , which is 3.5×10^5 cm/sec according to Clavaguera,²⁸ who attributes this result to Lebourgeois, and according to our own measurements, v_{\perp} , which is reported to be equal to $\frac{1}{2}v_{\parallel}$ in Cd₃As₂ by various authors,²⁹⁻³¹ and ϵ_0 and ϵ_{∞} which are, respectively, 36 and 12 according to previous fits with experimental transport data.^{4,5} Assuming that there is only one species of donor impurity and that it is singly ionized, and ignoring compensation effects [i.e., N=n in Eq. (7)], the only parameter which



FIG. 2. Transverse Nernst-Ettingshausen coefficient $P_{\rm NE}$ in Cd₃As₂ at 300 K as a function of electron concentration *n*. The three curves are calculated for the mixed mode of polar-optical phonon, charged-center, and acoustical phonon scattering, using three different values of the acoustical-deformation-potential constant $E_d = 10, 20, \text{ and } 30 \text{ eV}$. Experimental data are from Refs. 14 (o), 15 (X), and 20 (\bullet).

Electron					
(cm ⁻³)	1×10 ¹⁷	5×10 ¹⁷	1×10 ¹⁸	5×10 ¹⁸	1×10 ¹⁹
E_F (eV)	0.0387	0.0927	0.131	0.272	0.365
$m*/m_0$	0.0220	0.0304	0.0362	0.0567	0.0695
$\mu_{\rm cc}~({ m m}^2/{ m Vsec})$	36.8	17.8	12.3	4.75	3.10
$\mu_{\rm ac}~({ m m}^2/{ m Vsec})$	97.3	47.7	33.9	13.6	8.66
$\mu_{\rm op}({ m m}^2/{ m Vsec})$	2.21	2.31	2.14	1.52	1.26
μ (m ² /V sec)	2.04	1,96	1,73	1.06	0.812
r'cc	0.809	0.881	0.895	0.914	0.920
r'ac	-2.30	-2.00	-1.97	-2.13	-2.27
r'op	-0.712	-0.779	-0.870	-1.03	-1.06
l	0.158	0.237	0.262	0.292	0.296
$\alpha ~(\mu V/K)$	-349	-142	-100	-50.1	-38.7
$P_{\rm NE}(10^{-5} {\rm m}^2/{ m sec} {\rm K})$	-8.17	0.669	1.56	0.896	0.524

TABLE I. Calculated coefficients at T = 300 K for different electron concentrations, assuming $E_d = 10$ eV.

remains to be specified is E_d . A rough estimate of this parameter which is $\vec{E_d} \sim 10$ eV comes from our previous electronic-energy-band-structure calculations.³ This value of E_d was subsequently used in all our electron-mobility calculations in Cd_3As_2 ,⁵ as well as in the $Cd_{3-x}Zn_xAs_2$ alloy system $(x \le 1.5)$.³² In the following, we treat E_d as an adjustable parameter to be determined by comparing the calculated results of α and $P_{\rm NE}$ with all the available experimental data. This procedure has been used successfully by Zawadzki and coworkers^{6,8,10} for the determination of the deformation-potential constant of InSb. Figure 1 illustrates the 300-K thermoelectric-power results obtained by various authors¹¹⁻²³ on a number of Cd₃As₂ samples, as well as theoretical curves computed from the equations of Sec. II for three different values of E_d , namely, 10, 20, and 30 eV, respectively. The same is done in Fig. 2 for the transverse Nernst-Ettingshausen coefficient of Cd₃As₂ at 300 K. Table I summarizes a few of the results leading up to the $E_d = 10$ eV curves for α and $P_{\rm NE}$. It is clear from Fig. 1 that the predicted behavior of α with *n* is consistent with the experimental results. The small spacing between the curves illustrates the weak dependence of the thermoelectric power on acoustical phonon scattering. This insensitivity is due to the factor 5 which appears in the expression R + 5 - 6l of Eq.

(1) and which dominates small possible changes of R resulting from different relative importances of the various scattering modes. Taking also into account the scatter of the data, it can only be stated that E_d lies between 10 and 30 eV.

On the other hand, Eq. (2) contains the factor (R+2-6l). Since for high electron energies in a nonparabolic band such as the conduction band of $Cd_3As_2 2 - 6l \sim 0$ (see, for example, Table I), the Nernst-Ettingshausen coefficient is almost directly proportional to the scattering index R. This explains the larger spacing between the curves of Fig. 2 which even predict a change in sign of the Nernst-Ettingshausen coefficient at sufficiently low carrier densities. With the available data, it may reasonably be stated that E_d lies between 10 and 20 eV. A much more precise value of E_d could be obtained from samples with $n < 10^{18}$ cm⁻³ since then the Nernst-Ettingshausen coefficient would approach zero (see Fig. 2). It now appears that such samples are available.³³

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