# Thermoelectric power and transverse Nernst-Ettingshausen coefficient of  $Cd<sub>3</sub>As<sub>2</sub>$  at 300 K

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The thermoelectric power and the transverse Nernst-Ettingshausen coefficient of cadmium arsenide  $(Cd<sub>1</sub>As<sub>2</sub>)$  at room temperature have been calculated as a function of electron concentration, taking into account the HgTe-type inverted electronic-energy-band structure of this material. In the calculation, electron scattering due to polar-optical phonons, charged centers, and acoustical phonons has been considered. Since numerical values were available for every parameter involved except  $E_d$ , the acoustical-deformation-potential constant, the latter was treated as an adjustable parameter to fit the theoretical curves with experimental results. It was found that  $E_d$  lies between 10 and 20 eV consistent with the approximate value estimated in a previous paper.

#### I. INTRODUCTION

The electronic-energy-band structure of cadmium arsenide  $(Cd<sub>3</sub>As<sub>2</sub>)$ , after having been a question mark for some time, now appears to be similar to that of  $HgTe<sup>1</sup>$ . This point of view has been substantiated by several recent publications<sup>2,3</sup> which showed that this model of band structure for Cd,As, is consistent with all the available experimental data. The purpose of the present paper is to calculate the thermoelectric power  $\alpha$  and the transverse Nernst-Ettingshausen coefficient  $P_{\text{NE}}$  of Cd<sub>3</sub>As<sub>2</sub> at room temperature as a function of electron concentration, taking explicitly into account the HgTe-type inverted energy-band structure of this material. As in our previous work on the electrical resistivity of  $Cd<sub>3</sub>As<sub>2</sub>, <sup>4,5</sup>$ the calculation of  $\alpha$  and  $P_{NE}$  is carried out for the mixed mode of polar-optical phonon, chargedcenter, and acoustical-phonon scattering, using center, and acoustical-phonon scattering, using<br>the theoretical results of Zawadzki et al.<sup>6-10</sup> In the light of all the results we have recently obtained for  $Cd_3As_2$ ,  $2-5$  there is only one unknown in the calculation of  $\alpha$  and  $P_{NE}$ , which is the acoustical-deformation-potential constant $E_a$ . The latter is used in our procedure as an adjustable parameter to be determined by comparing the calculated results with all the available expericalculated results with all the a<br>mental data on  $\alpha,$   $^{11-23}$  and  ${P_{\rm NE}}$ .

## II. THEORY

n. Incoki<br>According to Zawadzki and co-workers,  $^{\rm 6-10}$  the general expressions to calculate  $\alpha$  and  $P_{\text{NE}}$  under high statistical degeneracy conditions are given by

$$
\alpha = A(R + 5 - 6l) \tag{1}
$$

and

$$
P_{\text{NE}} = A(\mu/c)(R + 2 - 6l), \qquad (2)
$$

where

$$
A = -\frac{1}{3} \left(\frac{\pi}{3}\right)^{2/3} \frac{k_B^2}{\hbar^2} \frac{T}{e} \frac{m^*}{n^{2/3}},
$$
 (3)

 $k_B$  is Boltzmann's constant, c is the speed of light, T is the absolute temperature,  $\hbar$  is Planck's constant divided by  $2\pi$ , e is the magnitude of the electronic charge, and  $m^*$  is the electron effective mass at the Fermi energy  $E_F$ . R is the effective scattering index which, for the combined scattering mode of polar-optical phonons (op), charged centers (cc), and acoustical phonons. (ac), is given by

$$
R = \mu \left( \frac{r'_{\rm op}}{\mu_{\rm op}} + \frac{r'_{\rm cc}}{\mu_{\rm cc}} + \frac{r'_{\rm ac}}{\mu_{\rm ac}} \right),\tag{4}
$$

where

$$
\mu = \left(\frac{1}{\mu_{\text{op}}} + \frac{1}{\mu_{\text{cc}}} + \frac{1}{\mu_{\text{ac}}}\right)^{-1}
$$
(5)

is the overall electron mobility calculated from the contributions of the three scattering mechanisms considered, namely, '

$$
\mu_{\rm op} = \frac{\hbar^3 k_{\rm F}}{2ek_{\rm B}T(1/\epsilon_{\infty}-1/\epsilon_0)(m^*)^2 F_{\rm op}},\tag{6}
$$

$$
\mu_{\rm cc} = \frac{\epsilon_0 \hbar^3 k_F^3}{2\pi e^3 (m^*)^2 N F_{\rm cc}},
$$
\n(7)

$$
\mu_{ac} = \frac{\pi e \hbar^3 dv_{\parallel}^2}{k_B T E_d^2 (m^*)^2 k_F F_{ac}} , \qquad (8)
$$

and

$$
r' = r - \frac{k_F}{F_r} \left(\frac{dF_r}{dk}\right)_{k=k_F}
$$
 (9)

denotes the effective scattering index for the electron-scattering mode in question. In Eqs.  $(6)-(9)$ ,  $\epsilon_0$  and  $\epsilon_{\infty}$  are the low- and high-frequency

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dielectric constants,  $k<sub>F</sub>$  is the wave number at the Fermi energy related to the electron concentration in a spherically symmetric degenerate band<sup>24,25</sup> by

$$
k_{\rm r} = (3\pi^2 n)^{1/3},\tag{10}
$$

 $N$  is the total concentration of ionized impurities, d is the material density,  $v_{\parallel}$  is the longitudinal velocity of sound in the material,  $E_d$  is the acoustical-deformation-potential constant, and  $r$  takes the values  $1, -1,$  and  $-3$  for charged-center scattering, polar-optical phonon scattering, and acoustical phonon scattering, respectively.

The  $F_r$  factors for each electron scattering mode are rather involved functions defined in the abovementioned references.<sup>3-10</sup> It is worth mentioning, however, that the mixing of  $s$ - and  $p$ -like components in the total conduction-band wave function also allows a nonvanishing coupling of electrons to the transverse acoustical phonons, as is transparent in the following expression for  $F_{ac}$ :

$$
F_{ac} = F_{ac}^{\mu} + (v_{\mu}^2/v_{\mu}^2)F_{ac}^{\mu}, \qquad (11)
$$

where the symbols  $\parallel$  and  $\perp$  refer to the longitudinal and transverse modes, respectively.

Finally,  $l$  is a parameter which is defined as

$$
l = \frac{1}{3} \left[ 1 - \frac{m^*}{\hbar^2} \left( \frac{d^2 E}{d k^2} \right)_{k = k_F} \right] = \frac{k_F}{3m^*} \left( \frac{dm^*}{dk} \right)_{k = k_F}, \qquad (12)
$$

where  $E(k)$  is the dispersion relation for the conduction band. It is clear from Eq.  $(12)$  that  $l$  gives a measure of the degree of nonparabolicity at the Fermi level of the actual  $E(k)$  relation.

## III. NUMERICAL RESULTS AND DISCUSSION.

In order to calculate  $\alpha$  and  $P_{NE}$  from Eqs. (1) and (2), we must specify the explicit dependence of  $m^*$  and of  $E_F$  as a function of electron concentration *n* (in cm<sup>-3</sup>) for  $Cd<sub>3</sub>As<sub>2</sub>$  at room temperature. It has been found that<sup>2,5</sup>

$$
\left(\frac{m^*/m_0}{1-m^*/m_0}\right)^2 = 0.26 \times 10^{-3} + 1.1 \times 10^{-15} n^{2/3},\tag{13}
$$

where  $m_0$  is the free-electron mass, and

$$
E_F = 0.095[(1 + 4.4 \times 10^{-12}n^{2/3})^{1/2} - 1] + 0.00364 \times 10^{-12}n^{2/3} \text{ (eV)}, \qquad (14)
$$

when measured from the bottom of the conduction band.

The energy-band parameters of  $Cd<sub>3</sub>As<sub>2</sub>$  at room temperature which are required in the calculation are the  $\Gamma_{8} - \Gamma_{6}$  energy gap  $E_{0} = 0.19$  eV,  $E_{p} = P^{2}$  $(2m_0/\hbar^2)$  = 14 eV, where P is proportional to the  $\Gamma_{\rm s}$  –  $\Gamma_{\rm s}$  momentum matrix element, and the spinorbit splitting of the valence band at the  $\Gamma$  point  $\Delta = 0.30$  eV.<sup>2,5,26</sup> We also need the numerical



FIG. 1. Thermoelectric power  $\alpha$  in Cd<sub>3</sub>As<sub>2</sub> at 300 K as a function of electron concentration  $n$ . The three curves are calculated for electrons scattered by the mixed mode of polar-optical phonons, charged centers, and acoustical phonons, using three different values of the acoustical-deformation-potential constant  $E_d = 10$ , 20, and 30 eV. The data points reproduced for comparison are from Refs. 11 ( $\bullet$ ), 12( $\Diamond$ ), 13 ( $\triangledown$ ), 14 ( $\circ$ ), 15 and 19 ( $\Delta$ ), 16 and 23 (0), 17 and 18 ( $\bullet$ ), 20 (+), 21 ( $\times$ ), and 22  $(*)$ .

values for five material parameters. The latter are d, which is 6.21 g/cm<sup>3</sup> for  $Cd<sub>3</sub>As<sub>2</sub>,<sup>27</sup> v<sub>0</sub>$ , which is  $3.5 \times 10^5$  cm/sec according to Clavaguera, <sup>28</sup> who attributes this result to Lebourgeois, and according to our own measurements,  $v_{\perp}$ , which is reported to be equal to  $\frac{1}{2}v_{\parallel}$  in Cd<sub>3</sub>As<sub>2</sub> by various authors,  $29-31$  and  $\epsilon_0$  and  $\epsilon_{\infty}$  which are, respectively, 36 and 12 according to previous fits with experimental transport data.<sup>4,5</sup> Assuming that there is only one species of donor impurity and that it is singly ionized, and ignoring compensation effects [i.e.,  $N=n$  in Eq. (7)], the only parameter which



FIG. 2. Transverse Nernst-Ettingshausen coefficient  $P_{NE}$  in Cd<sub>3</sub>As<sub>2</sub> at 300 K as a function of electron concentration  $n$ . The three curves are calculated for the mixed mode of polar-optical phonon, charged-center, and acoustical phonon scattering, using three different values of the acoustical-deformation-potential constant  $E_d = 10$ , 20, and 30 eV. Experimental data are from Refs. 14 (o), 15  $(X)$ , and 20 ( $\bullet$ ).

Electron concentration					
$\rm (cm^{-3})$	$1\times10^{17}$	$5 \times 10^{17}$	$1 \times 10^{18}$	$5 \times 10^{18}$	$1\times10^{19}$
$E_F$ (eV)	0.0387	0.0927	0.131	0.272	0.365
$m*/m_0$	0.0220	0.0304	0.0362	0.0567	0.0695
$\mu_{\rm cc}$ (m <sup>2</sup> /V sec)	36.8	17.8	12.3	4.75	3.10
$\mu_{ac}$ (m <sup>2</sup> /V sec)	97.3	47.7	33.9	13.6	8.66
$\mu_{\rm op}$ (m <sup>2</sup> /V sec)	2,21	2.31	2.14	1.52	1.26
$\mu$ (m <sup>2</sup> /V sec)	2.04	1.96	1.73	1.06	0.812
$r_{cc}'$	0.809	0.881	0.895	0.914	0.920
$r_{ac}'$	$-2.30$	$-2.00$	$-1.97$	$-2.13$	$-2.27$
$r'_{\rm op}$	$-0.712$	$-0.779$	$-0.870$	$-1.03$	$-1.06$
ı	0.158	0.237	0.262	0.292	0.296
$\alpha$ ( $\mu$ V/K)	$-349$	$-142$	$-100$	$-50.1$	$-38.7$
$P_{\text{NF}}(10^{-5} \text{ m}^2/\text{sec K})$	$-8.17$	0.669	1.56	0.896	0.524

TABLE I. Calculated coefficients at  $T = 300$  K for different electron concentrations, assuming  $E_d=10$  eV.

remains to be specified is  $E_d$ . A rough estimate of this parameter which is  $\tilde{E_d}$  ~10 eV comes from our previous electronic- energy- band-structure calculations.<sup>3</sup> This value of  $E_d$  was subsequently used in all our electron-mobility calculations in  $Cd<sub>3</sub>As<sub>2</sub>$ , <sup>5</sup> as well as in the  $Cd<sub>3-x</sub>Zn<sub>x</sub>As<sub>2</sub>$  alloy system  $(x \le 1.5)$ .<sup>32</sup> In the following, we treat  $E_d$  as an adjustable parameter to be determined by comparing the calculated results of  $\alpha$  and  $P_{NE}$  with all the available experimental data. This procedure has been used successfully by Zawadzki and co-<br>workers<sup>6,8,10</sup> for the determination of the de workers<sup>6,8,10</sup> for the determination of the deformation-potential constant of InSb. Figure 1 illustrates the 300-K thermoelectric -power results illustrates the 300-K thermoelectric-power respectively by various authors<sup>11-23</sup> on a number of Cd,As, samples, as well as theoretical curves computed from the equations of Sec. II for three different values of  $E_d$ , namely, 10, 20, and 30 eV, respectively. The same is done in Fig. 2 for the transverse Nernst-Ettingshausen coefficient of  $Cd<sub>3</sub>As<sub>2</sub>$  at 300 K. Table I summarizes a few of the results leading up to the  $E_d = 10$  eV curves for  $\alpha$ and  $P_{\text{NE}}$ . It is clear from Fig. 1 that the predicted behavior of  $\alpha$  with n is consistent with the experimental results. The small spacing between the curves illustrates the weak dependence of the thermoelectric power on acoustical phonon scattering. This insensitivity is due to the factor 5 which appears in the expression  $R+5-6l$  of Eq.

(I) and which dominates small possible changes of  $R$  resulting from different relative importances of the various sqattering modes. Taking also into account the scatter of the data, it can only be stated that  $E_d$  lies between 10 and 30 eV.

On the other hand, Eg. (2) contains the factor  $(R+2-6l)$ . Since for high electron energies in a nonparabolic band such as the conduction band of  $Cd<sub>3</sub>As<sub>2</sub> 2-6l \sim 0$  (see, for example, Table I), the Nernst-Ettingshausen coefficient is almost directly proportional to the scattering index  $R$ . This explains the larger spacing between the curves of Fig. 2 which even predict a change in sign of the Nernst-Ettingshausen coefficient at sufficiently low carrier densities. With the available data, it may reasonably be stated that  $E_a$ lies between 10 and 20 eV. A much more precise value of  $E_d$  could be obtained from samples with value of  $E_d$  coald be obtained from Bampies with  $n < 10^{18}$  cm<sup>-3</sup> since then the Nernst-Ettingshaus coefficient would approach zero (see Fig. 2). It now<br>appears that such samples are available.<sup>33</sup> appears that such samples are available.

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