

# Large magnetodielectric coupling in layered perovskite $\text{Eu}_2\text{TiO}_4$

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Perovskite-type  $\text{EuTiO}_3$ , which is quantum paraelectric and  $G$ -type antiferromagnetic (AFM) in the bulk form, has attracted great attention due to its strong spin-lattice coupling and strain-induced multiferroic in thin film form. In this study, significant magnetodielectric (MD) coupling is demonstrated in  $\text{K}_2\text{NiF}_4$ -type ferromagnetic (FM) layered perovskite  $\text{Eu}_2\text{TiO}_4$ , which features alternating rocksalt (RS)-type  $\text{EuO}$  layers and perovskite (Pv)-type  $\text{EuTiO}_3$  layers. We find a dielectric anomaly as a local minimum of permittivity near the ferromagnetic transition temperature ( $T_C = 9.5$  K) in the temperature-dependent permittivity under zero magnetic field. Remarkably, an applied magnetic field induces a substantial increase in permittivity at  $T_C$  (approximately 22% at 3 T), which is three times larger than that observed in bulk  $\text{EuTiO}_3$ . Our experimental and first-principles studies reveal that the insertion of  $\text{EuO}$  layers in  $\text{Eu}_2\text{TiO}_4$  enhances the  $\text{Eu-}f/\text{Ti-}d$  orbitals hybridization through pseudotrain in the  $\text{EuTiO}_3$  layers, as well as modifies the magnetic exchange paths that favor ferromagnetism over antiferromagnetism. The enhanced hybridization highlights the role in the large MD coupling played by AFM superexchange interactions via the Ti  $3d$  state, which competes with indirect FM interactions via the Eu  $5d$  state. Our findings demonstrate the potential of layered structure to control MD coupling, paving the way for new strategies in designing MD materials.

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**Introduction.** The coupling between static electrical and magnetic properties is an interesting effect from the perspective of both fundamental physics and potential applications [1]. This coupling is exemplified by multiferroic materials where two or more primary ferroic orders—such as ferroelectrics, (anti)ferromagnetics, and ferroelastics—coexist. The interaction between these order parameters leads to many interesting effects [2–4]. Moreover, the growing interest in novel dielectric devices has spurred the exploration of the magnetodielectric (MD) coupling, wherein the dielectric properties are tunable by application of magnetic field [5]. This effect has been observed in various materials including  $\text{Gd}_2\text{CuO}_4$  [6],  $\text{YMnO}_3$  [7],  $\text{EuTiO}_3$  [8],  $\text{BiMnO}_3$  [9],  $\text{Pb}_2\text{MnO}_4$  [10], and  $\text{TbMnO}_3$  [11].

Among materials exhibiting MD coupling, perovskite oxides  $\text{EuMO}_3$  ( $M = \text{Ti, Zr, Hf}$ ) containing  $\text{Eu}^{2+}$  with  $4f^7$  spins ( $S = 7/2$ ) have attracted significant attention due to their manipulable magnetic properties and strong spin-lattice coupling [12–15]. For example, bulk  $\text{EuTiO}_3$  exhibits a  $G$ -type antiferromagnetic (AFM) ordering below the Néel temperature ( $T_N = 5.3$  K) [16,17], quantum paraelectric (PE) behavior, and a 7% change in permittivity at 2 K under a magnetic field of 1.5 T [8]. Subsequent theoretical and experimental studies have demonstrated switchable ground states between AFM-PE and ferromagnetic-ferroelectric (FM-FE) phases through

strain engineering in epitaxial  $\text{EuTiO}_3$  films. For instance, FM behavior can be induced by the one-dimensional (1D) out-of-plane elongation, while the FM-FE phase arises from 2D biaxial tension (e.g., due to a  $\text{DyScO}_3$  substrate) or from three-dimensional (3D) tension caused by negative pressure (e.g., due to the embedded  $\text{MgO}$  cylinders) [18–22]. Additionally, recent studies on bulk  $(\text{Eu,A})\text{ZrO}_3$  solid solutions ( $A = \text{Ca, Sr, Ba}$ ) have demonstrated that the 3D lattice expansion generated by chemical substitution at the  $A$  site can alter magnetic properties, inducing a transition from AFM to FM states [23].

Regarding the AFM-to-FM switching behavior of  $\text{EuMO}_3$ , Akamatsu *et al.* reported comprehensive computational studies, revealing the key role played by the hybridization between the  $\text{Eu } 4f$  orbitals and  $M nd$  orbitals. In  $\text{EuTiO}_3$ , the  $G$ -type AFM state consists of antiparallel spin alignments between the two-interpenetrating face-centered-cubic (fcc) sublattices of Eu ions. The magnetic interactions are primarily governed by nearest-neighbor (NN) AFM interactions ( $J_1 < 0$ ) and the next-nearest-neighbor (NNN) FM interactions ( $J_2 > 0$ ). The transition from AFM to FM ordering is linked to changes in lattice structure, such as 1D lattice expansion, 2D biaxial strain, or 3D strain-induced negative pressure as mentioned above. These structural changes modify the balance between FM indirect exchange through Eu  $5d$  states (Eu-Eu) and AFM superexchange via Ti  $3d$  states (Eu-Ti-Eu), which leads to a reversal in the sign of  $J_1$  from negative to positive that is favored by the FM state.

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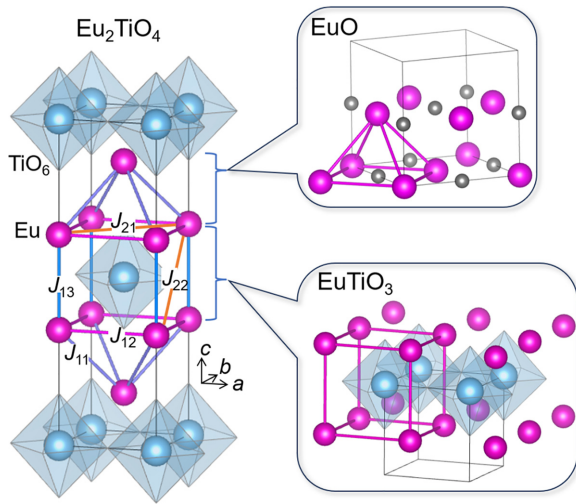


FIG. 1. Crystal structure of  $\text{Eu}_2\text{TiO}_4$  with RS-type EuO and Pv-type  $\text{EuTiO}_3$  layers. The NN interactions  $J_{1m}$  ( $m = 1, 2, 3$ ) and NNN interactions  $J_{2n}$  ( $n = 1, 2$ ) are shown with different color lines.

The hybridization of Eu-4*f*/Ti-3*d* states is also considered the dominant source of MD effects in  $\text{EuTiO}_3$ . The microscopic origin of MD effects has been discussed both theoretically and experimentally in terms of the spin-phonon coupling [24,25]. The soft phonon mode, which involves the vibration of  $\text{Ti}^{4+}$  ions against the  $\text{O}^{2-}$  octahedra, contributes the most to permittivity and thus dominates MD coupling. The spin alignments of  $\text{Eu}^{2+}$  ions can significantly impact permittivity through the Eu-Ti-Eu superexchange interactions [26]. In  $\text{EuTiO}_3$  thin films with 3D tensile strain, the MD coupling ( $\sim 0.1\%$  at 1.5 T) has been observed with a 3% lattice expansion [20], and the magnitude of the coupling is approximately 70 times weaker than that in bulk  $\text{EuTiO}_3$  ( $\sim 7\%$  at 1.5 T). This reduction can be attributed to the volume expansion, which weakens the Eu-Ti-Eu interactions and suppresses the MD coupling. The strong dependence of spin-phonon coupling on the energy levels of empty *d* states of *B*-site cations explains why strong spin-lattice coupling has not been observed in other related perovskite oxides, such as  $\text{EuZrO}_3$  ( $\sim 0.3\%$  at 5 T) [15,26,27].

$\text{Eu}_2\text{TiO}_4$ , a Ruddlesden-Popper (RP) perovskite oxide (space group  $I4/mmm$ ), features alternately stacked monolayers of perovskite (Pv)  $\text{EuTiO}_3$  and rocksalt (RS) EuO, as shown in Fig. 1. The insertion of the RS layers introduces additional exchange bridges between  $\text{Eu}^{2+}$  ions, enhancing the hybridization between Eu 4*f* and 5*d* orbitals. This facilitates indirect FM exchange interactions between neighboring  $\text{Eu}^{2+}$  ions [16]. The Pv units in  $\text{Eu}_2\text{TiO}_4$ , separated by RS layers, form a tetragonal unit cell. Compared to cubic  $\text{EuTiO}_3$  in bulk form (lattice parameter  $a = b = c = 3.905 \text{ \AA}$ ), the Pv units in  $\text{Eu}_2\text{TiO}_4$  are compressed by approximately 0.5% and 6.5% in the in-plane and out-of-plane directions, respectively. This compression can be interpreted as a pseudouniaxial strain resulting from the intrinsic chemical nature of the layered perovskite structure. Such pseudostrain is expected to enhance the overlap of Eu 4*f* and Ti 3*d* orbitals in the Pv layers and thus to strengthen the spin-lattice coupling. In this respect, we focus on the potential MD effect in  $\text{Eu}_2\text{TiO}_4$ .

In this study, we demonstrate substantial MD coupling ( $\sim 22\%$  at 3 T) near  $T_C$  in the layered perovskite  $\text{Eu}_2\text{TiO}_4$ . A combined study of structure analysis and first-principles calculations suggest that the enhanced Eu-4*f*/Ti-3*d* orbital hybridization in the Pv layers may be the origin of the large MD coupling. This strong spin-lattice coupling arises from the interplay between RS and Pv layers, allowing for the coexistence of FM interactions and strong MD coupling—a combination that is not achievable in the simple perovskite oxide  $\text{EuTiO}_3$ . The layered structure plays a unique role in integrating the magnetic and dielectric properties within this system.

**Method.** The polycrystalline samples of  $\text{Eu}_2\text{TiO}_4$  were prepared by the solid-state reaction method. Reagent-grade  $\text{Eu}_2\text{O}_3$  and  $\text{TiO}_2$  (both 99.9% pure, sourced from Kojundo Chemical Laboratory Co, Ltd) were used as starting materials. Prior to use,  $\text{Eu}_2\text{O}_3$  was preheated at  $900^\circ\text{C}$  for 12 h to remove water and carbon dioxide. The solid-state synthesis was carried out in two steps. First, EuO precursors were prepared by the reduction of  $\text{Eu}_2\text{O}_3$  using graphite carbon (C):  $\text{Eu}_2\text{O}_3$  and C were mixed at a mole ratio of 1:1.2, pelletized, and heated at  $1400^\circ\text{C}$  under flowing of Ar gas for 6 h. Next, EuO and  $\text{TiO}_2$  were mixed, pelletized, and heated at  $1350^\circ\text{C}$  under flowing Ar gas for 6 h to get  $\text{Eu}_2\text{TiO}_4$ . We also prepared high-density ceramic samples ( $>98\%$  density) by spark plasma sintering (SPS). First,  $\text{Eu}_2\text{TiO}_4$  powder was loosely placed into a graphite die with a diameter of 10 mm. Then, the SPS treatment was carried out in a vacuum condition at a heating rate of  $100^\circ\text{C}/\text{min}$  under a uniaxial pressure of 90 MPa using a SPS machine (SPS1050, Fuji Electronic Industrial Co., Ltd, Japan). Finally, the sintering was conducted at  $1450^\circ\text{C}$  with a dwelling time of 1 min.

The phase purity of the final products, including SPS specimens, was checked by x-ray diffraction (XRD) using Smart-Lab diffractometer (Rigaku) with Cu  $K\alpha$  radiation ( $\lambda = 1.5418 \text{ \AA}$ ). High-resolution synchrotron x-ray diffraction (SXRD) was performed at room temperature using the large Debye-Scherrer cameras with MYTHEN solid-state detectors installed at the beamlines BL02B2 (SPring-8). The incident beam was monochromatized to  $\lambda = 0.774702 \text{ \AA}$ . Finely ground powder samples were sieved through a 32- $\mu\text{m}$  mesh sieve and put into a Pyrex capillary with 0.1 mm inner diameter. The sealed capillary was rotated during measurements to reduce the effect of preferential orientation. The SXRD data collected were analyzed by the Rietveld method [28] using a JANA program [29].

Magnetization measurements were carried out with a superconducting quantum interference device (SQUID) magnetometer (MPMS, Quantum Design). Temperature dependence of magnetic susceptibilities was measured in a range 2–300 K at an external magnetic field of 0.01 T. The field dependence of magnetization was recorded at 2 and 9.5 K in magnetic fields up to 5 T.

Dielectric properties were measured with an inductance, capacitance, and resistance (LCR) meter (Agilent E4980) in the temperature range 2–300 K in the magnetic field of 0–5 T utilizing a home-made dielectric measurements probe coupled with the physical property measurement system (PPMS, Quantum Design). 50-nm/20-nm Au/Ti electrodes were deposited on the top and bottom surface of an  $\text{Eu}_2\text{TiO}_4$  pallet

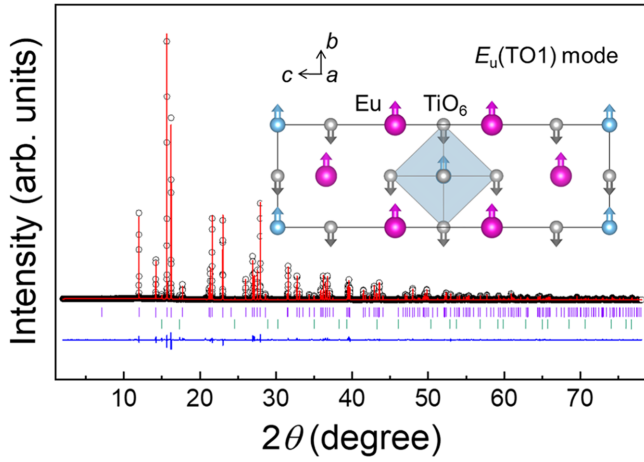


FIG. 2. SXR pattern ( $\lambda = 0.774702 \text{ \AA}$ ) of  $n = 1$  RP-type  $\text{Eu}_2\text{TiO}_4$  at 300 K and fitting curve obtained by Rietveld refinement with the  $I4/mmm$  structure model. Black circles and red solid curves represent the observed and the calculated intensities, respectively. The blue solid line at the bottom indicates the difference between the experimental and calculated patterns. Purple and green ticks show the peak positions of  $\text{Eu}_2\text{TiO}_4$  and  $\text{EuO}$ , respectively. The inset shows a schematic diagram for the movement of atoms in the  $E_u(\text{TO1})$  mode in  $\text{Eu}_2\text{TiO}_4$ .

(6 mm diameter) using electron beam evaporation (Hitachi, Japan).

First-principles density functional theory (DFT) calculations were carried out for  $\text{Eu}_2\text{TiO}_4$  (space group  $I4/mmm$ ) and  $\text{EuTiO}_3$  (space group  $Pm\bar{3}m$ ) using the projector augmented-wave (PAW) method [30,31] as implemented in the VASP code [32–37]. To reduce the computational costs, the generalized gradient approximation-PBESol (GGA-PBESol) [38–40] and HSE06 hybrid functional [41–43] were used for structural optimizations and electronic structure calculations, respectively. The PAW data sets with radial cutoffs of 1.5, 1.3, and 0.8  $\text{\AA}$  were used with a plane-wave cutoff energy of 550 eV. The following states were described as valence electrons:  $4f^7$ ,  $5s^2$ ,  $5p^6$ ,  $6s^2$  for Eu;  $3d^2$ ,  $4s^2$  for Ti; and  $2s^2$ ,  $2p^4$  for O. FM spin configurations were considered for  $\text{Eu}_2\text{TiO}_4$  and  $\text{EuTiO}_3$ . The lattice constants and internal coordinates were optimized until the residual stress and forces converged to 0.2 GPa and 1 meV/ $\text{\AA}$ , respectively. A phonon band structure was calculated for  $\text{Eu}_2\text{TiO}_4$  using the PHONOPY code [44]. The crystal orbital Hamilton population (COHP) between Eu and Ti atoms was calculated using the LOBSTER code [45,46]. The VESTA code was used to visualize crystal structures [47].

**Results.** According to laboratory XRD data, the main phase of the synthesized products was identified as  $\text{Eu}_2\text{TiO}_4$  with an  $n = 1$  RP ( $\text{K}_2\text{NiF}_4$ )-type structure. The  $^{151}\text{Eu}$  Mössbauer spectrum shows that almost all the europium ions exist as  $\text{Eu}^{2+}$  (see Fig. S1 and Table S1 in the Supplemental Material (SM) [48]). Figure 2 shows the SXR pattern at room temperature. The main reflections can be indexed by a tetragonal unit cell with lattice parameters of  $a = b = 3.88619(1) \text{ \AA}$ , and  $c = 12.54039(4) \text{ \AA}$ . The observed reflection conditions indicate the tetragonal symmetry (space group  $I4/mmm$ ), in agreement with previous observation on  $\text{Eu}_2\text{TiO}_4$  [16]. A negligibly small amount of  $\text{EuO}$  impurities (less than 1 wt %)

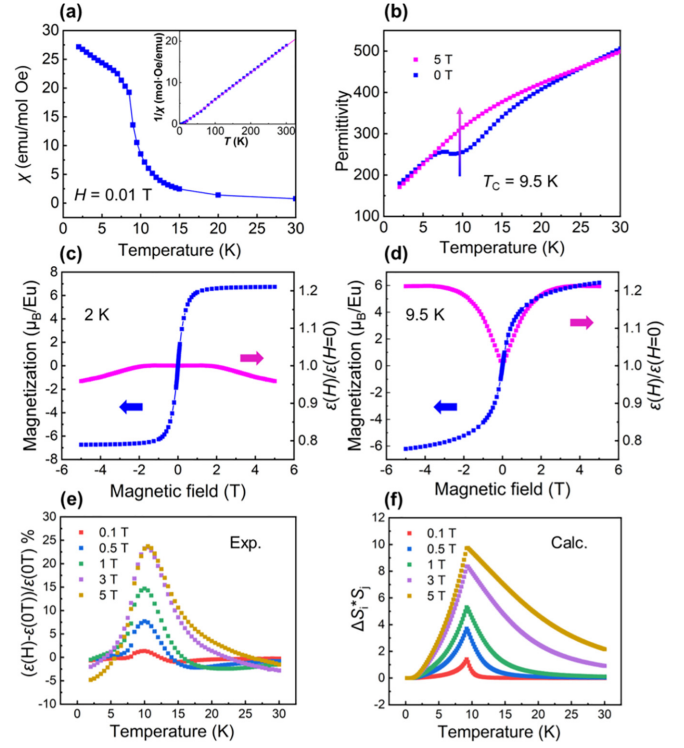


FIG. 3. (a) Temperature dependence of magnetic susceptibility  $\chi (= M/H)$  of  $\text{Eu}_2\text{TiO}_4$  collected at 0.01 T. The inset shows the inverse susceptibility  $1/\chi$  with Curie-Weiss fitting (pink line). (b) The permittivity of  $\text{Eu}_2\text{TiO}_4$  as a function of temperature ( $2 \text{ K} \leq T \leq 30 \text{ K}$ ) measured at 0 and 5 T under a frequency of 1 MHz. (c), (d) Variation of magnetization and  $\varepsilon(H)/\varepsilon(H=0)$  of  $\text{Eu}_2\text{TiO}_4$  with magnetic field at (c) 2 K and (d) 9.5 K. (e), (f) Temperature dependence of (e)  $[\varepsilon(H) - \varepsilon(H=0)]/\varepsilon(H=0)\%$  and (f)  $\Delta(S_i \cdot S_j)$  obtained by subtracting  $\langle S_i \cdot S_j \rangle$  data at 0 T from those at 0.1, 0.5, 1, 3, and 5 T.

is detected. Rietveld refinement with the  $I4/mmm$  structure model converges to a good reliability index  $R_{\text{wp}}$  (weighted profile  $R$  factor) of 6.65%. Separate occupancy refinement reveals no deviation from the ideal composition. Detailed structural parameters obtained from the refinement are summarized in Table S2 in the SM [48].

The crystal structure of  $n = 1$  RP-type  $\text{Eu}_2\text{TiO}_4$  can be interpreted as alternating layers of  $\text{TiO}_2$  and  $\text{EuO}$  planes stacked along the  $c$  axis, as illustrated in Fig. 1. The stacking sequence follows a  $\text{TiO}_2\text{-EuO-EuO}$  pattern, with the second  $\text{EuO}$  layer being shifted by  $1/2a$  along the  $[110]$  direction relative to the first  $\text{EuO}$  layer. From the structural refinement, the  $\text{EuTiO}_3$  unit in the Pv layer shows lattice parameters of  $a_{\text{Pv}} = b_{\text{Pv}} = 3.88619(1) \text{ \AA}$ ,  $c_{\text{Pv}} = 3.65819(1) \text{ \AA}$ , indicating a compressed  $c$  axis compared to its in-plane dimensions.

Before presenting the dielectric properties and MD coupling of  $\text{Eu}_2\text{TiO}_4$ , it is crucial to first examine the magnetic characteristic of our  $\text{Eu}_2\text{TiO}_4$  samples. Temperature dependence of magnetic susceptibility ( $\chi$ - $T$ ) exhibits an FM transition around  $T_C = 9.5 \text{ K}$  [see Fig. 3(a)]. A Curie-Weiss analysis in the temperature range  $15 \text{ K} \leq T \leq 300 \text{ K}$  yields effective magnetic moment  $\mu_{\text{eff}} = 7.84(1)\mu_B$ , consistent with the expected  $7.8\mu_B$  for  $\text{Eu}^{2+}$  ions in a  $4f^7$  ( $J = S = 7/2$ ) configuration. The analysis also reveals a Weiss temperature



$\theta_W = 10.05(2)$  K, indicating that FM interactions are dominant. These values of  $\mu_{\text{eff}}$  and  $\theta_W$  are in good agreement with those reported previously for polycrystalline  $\text{Eu}_2\text{TiO}_4$  samples [49].

Temperature-dependent dielectric permittivity  $\varepsilon(T)$  under zero magnetic field at 1 MHz is displayed in Fig. 3(b). Below 30 K, we observed a negligible dependence of permittivity on frequency between 1 kHz and 1 MHz, along with a relatively low dielectric loss ( $\tan\delta < 0.3$ ). The permittivity decreases with decreasing the temperature, indicating that  $\text{Eu}_2\text{TiO}_4$  behaves distinctly from quantum paraelectric  $\text{EuTiO}_3$ . As the temperature further decreases, a local minimum of permittivity is observed near 9.5 K, corresponding to the  $T_C$ . This anomaly of permittivity is smeared out when the magnetic field of 5 T is applied, suggesting the presence of MD coupling in this system.

The magnetic field dependence of magnetization ( $M$ - $H$ ) and permittivity ( $\varepsilon$ - $H$ ) at 2 and 9.5 K is comparatively shown in Figs. 3(c) and 3(d), respectively. At 2 K [see Fig. 3(c)], the magnetization increases with the magnetic field increasing and reaches its saturation around 1.2 T. The saturation magnetization is  $6.7\mu_B/\text{Eu}^{2+}$ , which is close to the full moment of free  $\text{Eu}^{2+}$  ( $7\mu_B/\text{Eu}^{2+}$ ). Meanwhile, the permittivity is independent of the magnetic field and slightly decreases beyond 1.2 T. The slight decrease in the permittivity under high fields can be attributed to magnetostriction [50], similar to what was observed in the strain-induced FM  $\text{EuTiO}_3$  thin films [20]. The field-independent permittivity at low magnetic fields could result from the cancellation of positive contribution from magnetic structure changes and negative contribution from magnetostriction (see Fig. S5).

Remarkably, at  $T = 9.5$  K [see Fig. 3(d)], both magnetization and permittivity increase simultaneously when the magnetic field is applied up to 3 T. This is indicative of significant MD coupling, and the permittivity enhancement is about 22% at 3 T, which is three times larger than that observed in  $\text{EuTiO}_3$  (7% at 1.5 T) [8]. Note that the resistivity in our samples exceeds  $10^6\Omega\text{cm}$  below 30 K. In addition, a high frequency (1 MHz) was employed for the dielectric measurements in this study to mitigate the influence of charge carriers. Therefore, the contribution from the magnetoresistance could be negligible.

In bulk  $\text{EuTiO}_3$ , permittivity as a function of temperature and magnetic field can be represented using the following equation [8]:

$$\varepsilon(T, H) = \varepsilon(T, 0) (1 + \alpha \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle), \quad (1)$$

where  $\varepsilon(T, 0)$  is the permittivity at zero magnetic field.  $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle$  is the spin pair correlation between nearest-neighbor  $\text{Eu}^{2+}$ , and  $\alpha$  is the coupling constant between spin correlation and permittivity [8]. To estimate  $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle$  in  $\text{Eu}_2\text{TiO}_4$ , molecular-field calculations were conducted based on a Heisenberg model under an assumption that the  $4f$  spins of  $\text{Eu}^{2+}$  ( $S = 7/2$ ) are located on a tetragonal lattice with FM ordering. The Heisenberg Hamiltonian of the spin system is given by

$$H^{\text{me}} = \sum_{ij} J_{ij} \cdot \mathbf{S}_i \cdot \mathbf{S}_j, \quad (2)$$

where  $J_{ij}$  represents the exchange constants between spins  $\mathbf{S}_i$  and  $\mathbf{S}_j$ , with a restriction on considering only the NN and NNN interactions. This approach helps us evaluate the magnetic exchange interactions and their impact on the dielectric properties of  $\text{Eu}_2\text{TiO}_4$ . We used the exchange interaction parameters obtained with the previous first-principles calculations [51] (see Fig. 1, and Fig. S2 and Table S3 in the SM [48]):  $J_{11}/k_B = 0.2$  K,  $J_{12}/k_B = 0.08$  K, and  $J_{13}/k_B = 0.0$  K for NN interactions,  $J_{21}/k_B = 0.08$  K and  $J_{22}/k_B = 0.04$  K for NNN interactions, where  $k_B$  is the Boltzmann constant. In the molecular-field calculation,  $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle$  is obtained as the product of  $\langle \mathbf{S} \rangle$  on two sublattices. To further analyze the impact of a magnetic field on the dielectric properties, we calculated the change in spin pair correlation:

$$\Delta \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle = \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_H - \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_0, \quad (3)$$

where  $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_H$  and  $\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle_0$  are the spin pair correlations under finite and zero magnetic field, respectively. Figure 3(e) illustrates the relative permittivity change:

$$\frac{[\varepsilon(H) - \varepsilon(0)]}{\varepsilon(0)} \times 100\%, \quad (4)$$

in comparison with  $\Delta \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle$  [Fig. 3(f)]. The calculated results show remarkable agreement with the experimental findings, indicating that the MD effect in  $\text{Eu}_2\text{TiO}_4$  is primarily governed by the pair correlation of the  $\text{Eu}^{2+}$  spins. The magnetodielectric coupling constant is  $\alpha = 2.4 \times 10^{-2}$  which, obtained by Eq. (1) for  $\text{Eu}_2\text{TiO}_4$ , is the largest among perovskite-type oxides with  $\text{Eu}^{2+}$  occupying the A sites, e.g.,  $\text{EuZrO}_3$  ( $\alpha = 1.1 \times 10^{-4}$ ) [15] and  $\text{EuTiO}_3$  ( $\alpha = 2.74 \times 10^{-3}$ ) [8], highlighting the unique magnetodielectric properties of  $\text{Eu}_2\text{TiO}_4$ .

*Discussion: Magnetic properties of  $\text{Eu}_2\text{TiO}_4$ .* We start with a brief survey of the magnetic properties of  $\text{Eu}_2\text{TiO}_4$ . For perovskite and related oxides with  $\text{Eu}^{2+}$  occupying the A sites, both AFM and FM interactions coexist between the nearest-neighbor (NN)  $\text{Eu}^{2+}$ - $\text{Eu}^{2+}$  pairs. Hence, the magnetism of these oxides alters depending on the relative strength of the competing magnetic interactions, i.e., the sign of  $J_1$ . In bulk  $\text{EuTiO}_3$ ,  $\text{Eu}^{2+}$  ions have six nearest neighbors within the cubic lattice, where the indirect FM exchange via the Eu 5d states and the AFM superexchange via the Ti 3d states coexist. The G-type AFM state of bulk  $\text{EuTiO}_3$  appears due to the AFM superexchange via the Ti 3d states. Moreover, it was also suggested that the third nearest-neighbor magnetic exchange ( $J_3$ ) may play a crucial role in the MD coupling in  $\text{EuTiO}_3$  [52]. In the case of  $J_3$ , the exchange occurs between Eu ions at opposite corners of a cube through the central Ti ion, forming a  $180^\circ$  Eu-Ti-Eu superexchange pathway, further highlighting the significance of Eu-Ti-Eu superexchange interactions.

In contrast, the layered structure in  $\text{Eu}_2\text{TiO}_4$  introduces significant changes in the magnetic exchange paths: the number of NN  $\text{Eu}^{2+}$ - $\text{Eu}^{2+}$  pairs increases from 6 in  $\text{EuTiO}_3$  to 9 in  $\text{Eu}_2\text{TiO}_4$ . Specifically, the insertion of an RS layers between the Pv units introduces four additional  $\text{Eu}^{2+}$ - $\text{Eu}^{2+}$  pairs along the  $\langle 11\sqrt{2} \rangle$  direction (exchange constant  $J_{11}$ ), maintaining four  $\text{Eu}^{2+}$ - $\text{Eu}^{2+}$  interactions along the  $\langle 100 \rangle$  and  $\langle 010 \rangle$  directions (exchange constant  $J_{12}$ ), while it eliminates one of two  $\text{Eu}^{2+}$ - $\text{Eu}^{2+}$  pairs along the  $\langle 001 \rangle$  direction (exchange constant  $J_{13}$  for the remaining pair) (see Table S3 in the SM [48]).

The absence of Ti atoms in the RS-type EuO layers results in the exclusive presence of FM indirect exchange (positive  $J_{11}$ ). Namely, the additional magnetic exchange pathways in  $\text{Eu}_2\text{TiO}_4$  leads to the FM ground state.

Previous first-principles studies of  $\text{Eu}_2\text{TiO}_4$  have suggested competition between FM and AFM exchanges within the Pv layers (near zero  $J_{13}$ ) and in the RS-Pv interlayers (slightly positive  $J_{12}$ ) [51]. To compare such competition in  $\text{Eu}_2\text{TiO}_4$  with those in  $\text{EuTiO}_3$ , we checked the refined structure data: in  $\text{Eu}_2\text{TiO}_4$ , the Pv layers, sandwiched by the RS layers, have a tetragonal unit cell ( $a_{\text{Pv}} = b_{\text{Pv}} = 3.88619(1) \text{ \AA}$ ,  $c_{\text{Pv}} = 3.65819(1) \text{ \AA}$ ), which is compressed by approximately 0.5% and 6.5% in the in-plane and out-of-plane directions, respectively, relative to the cubic unit cell of bulk  $\text{EuTiO}_3$  (lattice parameter  $a = b = c = 3.905 \text{ \AA}$ ). This uniaxial compression effectively reduces the Eu-Ti distance in  $\text{Eu}_2\text{TiO}_4$  (3.301  $\text{\AA}$ ) compared to that in bulk  $\text{EuTiO}_3$  (3.382  $\text{\AA}$ ). This pseudostrain along the  $c$  axis caused by the insertion of the RS layers works to enhance the overlap between Eu 4*f* and Ti 3*d* orbitals in the Pv layers, potentially strengthening the spin-lattice coupling.

**Magnetodielectric effect of  $\text{Eu}_2\text{TiO}_4$ .** The observation of large MD coupling constant in the  $\text{Eu}_2\text{TiO}_4$  raises two questions: What is the origin of MD coupling in FM  $\text{Eu}_2\text{TiO}_4$ ? Additionally, why is the magnitude of MD coupling even larger than bulk  $\text{EuTiO}_3$ ?

According to Lyddane-Sachs-Teller (LST) relation, the permittivity is connected to the optical phonon frequency:

$$\frac{\varepsilon_0}{\varepsilon_\infty} = \frac{\omega_{\text{LO}}^2}{\omega_{\text{TO}}^2}, \quad (5)$$

where  $\varepsilon_0$  is the static permittivity, which includes the lattice contribution,  $\varepsilon_\infty$  is the electronic contribution, and  $\omega_{\text{LO}}$  and  $\omega_{\text{TO}}$  are the zone-center longitudinal and transverse optical (LO and TO) phonon frequencies, respectively. The  $\varepsilon_0$  of a material is primarily influenced by the lowest-energy TO phonon mode. Although  $\text{Eu}_2\text{TiO}_4$  is a multimode system, Eq. (5) is used here for a qualitative discussion based on a simplified single-mode approximation. Our first-principles calculations on  $\text{Eu}_2\text{TiO}_4$  (see Table S4 in the SM [48]) identify this as the  $E_u(\text{TO1})$  mode, which involves  $\text{Ti}^{4+}$  and  $\text{Eu}^{2+}$  ions vibrating against the  $\text{O}^{2-}$  octahedra within the  $a$ - $b$  plane (see the inset of Fig. 2), analogous to the behavior observed in  $n = 1$  RP-type  $\text{Sr}_2\text{TiO}_4$  [53]. This finding suggests that the  $E_u(\text{TO1})$  mode plays a crucial role in the dielectric properties of  $\text{Eu}_2\text{TiO}_4$ . Specifically, the application of an external magnetic field near  $T_C$  can align the Eu spins in the field direction, which may soften the  $E_u(\text{TO1})$  mode and increase permittivity. Note that the in-plane movement of the  $E_u(\text{TO1})$  mode in the Pv layers of  $\text{Eu}_2\text{TiO}_4$  closely resembles the  $T_{1u}$  mode in  $\text{EuTiO}_3$  [25], where changes in Eu spin configuration under a magnetic field alter the phonon frequency through modified hybridization between the Eu 4*f* and Ti 3*d* orbitals [26]. More detailed analyses of the phonon modes using infrared and Raman spectroscopy [54] should be performed in future work to reveal its phonon nature.

To estimate the Eu/Ti orbital hybridization in  $\text{Eu}_2\text{TiO}_4$ , we calculated the electronic state by site-projected partial density of states (PDOS). The valence band mainly consists of O

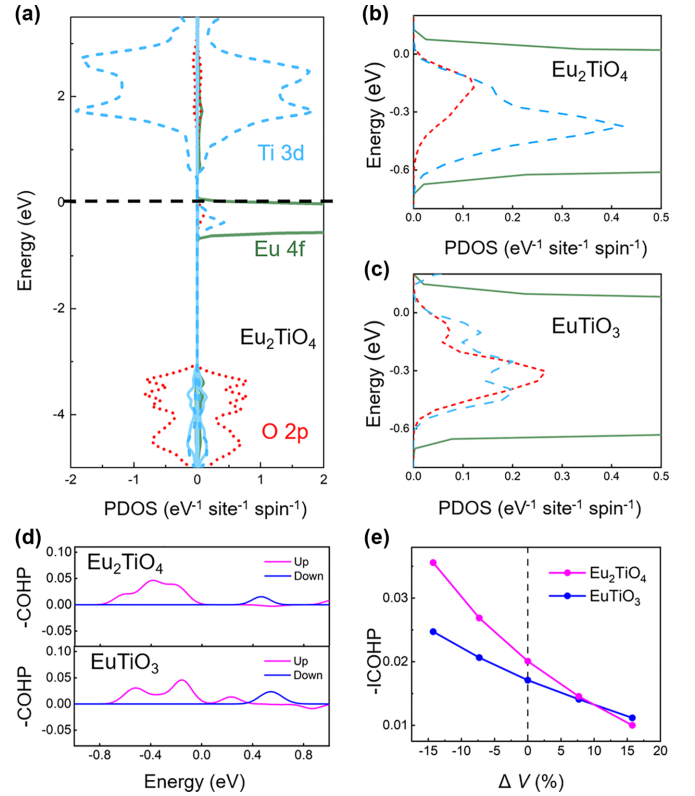


FIG. 4. (a) Site-projected PDOS of  $\text{Eu}_2\text{TiO}_4$ . The zero of energy is placed at the highest occupied state. (b),(c) Magnified view of the up-spin component of the PDOS in the energy region near the Eu 4*f* band in (b)  $\text{Eu}_2\text{TiO}_4$  and (c)  $\text{EuTiO}_3$ . (d) Comparison of  $-\text{COHP}$  between  $\text{Eu}_2\text{TiO}_4$  and  $\text{EuTiO}_3$  without volume change ( $\Delta V = 0\%$ ) and (e) variations of integral  $-\text{COHP}$  ( $-\text{ICOHP}$ ) between  $\text{Eu}_2\text{TiO}_4$  and  $\text{EuTiO}_3$  with isotropic volume change ( $\Delta V = -14.3\%$ ,  $-7.3\%$ ,  $0\%$ ,  $+7.7\%$ , and  $+15.8\%$ ).

2*p* states, while the conduction band chiefly has Ti 3*d* and Eu 5*d* characters. The occupied Eu 4*f* bands lying between these bands are narrow, indicating their localized nature [see Fig. 4(a)]. The enlarged view of the PDOS in the energy region near the Eu 4*f* band is shown in Figs. 4(b) and 4(c) for  $\text{Eu}_2\text{TiO}_4$  and  $\text{EuTiO}_3$ , respectively. The Eu 4*f* states, which possess the localized spins near the Fermi level, are hybridized with the Ti 3*d* and O 2*p* states [see Fig. 4(b)]. Compared to  $\text{EuTiO}_3$  [Fig. 4(c)], the PDOS for Ti in  $\text{Eu}_2\text{TiO}_4$  is significantly larger, indicating a stronger hybridization between Eu 4*f* and Ti 3*d* orbitals.

To further illustrate the covalent bonding interactions between Eu 4*f* and Ti 3*d* orbitals, we employed the COHP method [33]. In COHP analysis, the negative value represents bonding interactions, while the positive value corresponds to antibonding interactions. A comparison of the  $-\text{COHP}$  in the energy range  $-1 \text{ eV}$  to  $1 \text{ eV}$  near the Fermi level between  $\text{Eu}_2\text{TiO}_4$  and  $\text{EuTiO}_3$  is displayed in Fig. 4(d). Integrating the  $-\text{COHP}$  curves up to the Fermi level provides the integral  $-\text{COHP}$  ( $-\text{ICOHP}$ ) value, which qualitatively correlate with the strength of corresponding bonds. The larger positive value of  $-\text{ICOHP}$  in  $\text{Eu}_2\text{TiO}_4$  ( $0.2 \text{ band}^{-1}$ ) than in  $\text{EuTiO}_3$  ( $0.17 \text{ band}^{-1}$ ) indicates the stronger bonding between Eu and Ti atoms in  $\text{Eu}_2\text{TiO}_4$ , implying the enhanced AFM interaction

within the Pv layers. We expect that this stronger bonding interaction can contribute to the large MD coupling observed in  $\text{Eu}_2\text{TiO}_4$ . Moreover, Fig. 4(e) plots the variation in  $-\text{ICOHP}$  against the isotropic lattice volume change ( $\Delta V$ ). For both  $\text{Eu}_2\text{TiO}_4$  and  $\text{EuTiO}_3$ , the  $-\text{ICOHP}$  increases with lattice volume decreasing. Interestingly, the variation in  $-\text{ICOHP}$  with  $\Delta V$  is pronounced in  $\text{Eu}_2\text{TiO}_4$  compared to  $\text{EuTiO}_3$ , which indicates that the layered structure of  $\text{Eu}_2\text{TiO}_4$  offers a more volume-sensitive mechanism for tuning the bonding interaction between Eu 4*f* and Ti 3*d* orbitals. Namely, the intrinsic physical nature of the layered perovskite structure provides a versatile platform to study the complex interplay between static electrical and magnetic properties. It is interesting to explore the possibility of inducing ferroelectricity in  $\text{Eu}_2\text{TiO}_4$  by epitaxial strain or chemical substitution, though care must be taken to mitigate potential conductivity issues.

**Conclusions.** In conclusion, an FM layered perovskite oxide,  $n = 1$  RP-type  $\text{Eu}_2\text{TiO}_4$ , exhibits a large MD coupling around  $T_C$ . The magnitude of the MD coupling (approximately 22% at 3 T) is three times larger than that of bulk  $\text{EuTiO}_3$ . A combined study of structure analysis and first-principles calculations suggests that the enhanced MD coupling in  $\text{Eu}_2\text{TiO}_4$  arises from the interplay of RS and Pv layers in the quasi-2D structures. The AFM superexchange interactions via the *B*-site

Ti 3*d* state, which compete with indirect FM interactions via the Eu 5*d* state, are crucial to the mechanism responsible for the enhanced MD coupling. Our study highlights that this layered structure provides a distinctive approach to regulating MD coupling, opening interesting possibilities for innovative MD material design.

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**Data availability.** The data supporting this study's findings are available within the article.

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