Memory and rejuvenation in glassy systems

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The memory effect in a single-crystal spin glass (Cu_{0.92}Mn_{0.08}) has been measured using 1 Hz ac susceptibility techniques over a temperature range of 0.4–0.7 T_g , and a model of the memory effect has been developed. A double-waiting-time protocol is carried out where the spin glass is first allowed to age at a temperature below T_g , followed by a second aging at a lower temperature, T_{w_2} , after it has fully rejuvenated. The model is based on calculating typical coincident growth of correlated regions at the two temperatures. It accounts for the absolute magnitude of the memory effect as a function of both waiting times and temperatures. The data can be explained by the memory loss being a function of the relative change in the correlated volume at the first waiting temperature because of the growth in the correlations at the second waiting temperature.

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Introduction. The origin and nature of memory and rejuvenation in spin glasses has been the subject of experimental and theoretical investigations for over two decades [1–16]. When held at a temperature below the glass temperature T_g , the state of a spin glass is well known to age with time [16–19]. Rejuvenation is the process where the spin glass appears to lose knowledge of its prior aging when the temperature is lowered. Memory, on the other hand, is displayed when the spin glass is reheated to the aging temperature and it recovers, at least partially, the aged state. Although there is some agreement to the origin of the aging phenomena, rejuvenation and memory present a conundrum that has eluded a satisfactory simultaneous explanation [16]. The appearance of these effects together is central to understanding the spin glass state, in particular, how one can understand memory observed *after* rejuvenation.

This begs the question—if the spin glass appears to have "forgotten" it aged during rejuvenation, how can it then "remember" its previous cooling history? Several explanations have been postulated, but never quantitatively tested experimentally [1,11,13,15,20–22]. As we will show, our double-waiting-time experiments and model answer this question.

In this Letter, we quantify spin glass memory loss in a single crystal of $Cu_{0.92}Mn_{0.08}$ and present a simple physical model which accounts for our results (see Paga *et al.* [23] for a complementary numerical study of memory). It is expected that this picture may provide an explanation for memory in other glassy systems, including biopolymers, granular media, and structural glasses [24–29].

Figure 1 shows a canonical low-frequency ac susceptibility measurement displaying these out-of-equilibrium phenomena [1]. The reference curve, where no aging is exhibited, is

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plotted alongside the curves that exhibit aging, rejuvenation, and memory. As in previous work [1,21], we focus on the imaginary part of the ac susceptibility $\chi''(\omega)$, because the size of these effects is more pronounced than in the real part, $\chi'(\omega)$ [30]. Hereafter, we drop the explicit frequency dependence on the susceptibility $\chi = \chi' + i\chi''$.

A significant feature is shown in Fig. 1, where upon returning to T_{w_1} , while the heating curve does have knowledge of the cooling curve, they do not lie on top of each other. Importantly, the spin glass exhibits "memory loss." Of the many previous works that see memory, some appear to see nearly perfect memory [1,20], while others see memory loss [11,15,21]. A common qualitative picture states that memory is an effect of spin glass droplets whose dynamics are organized in a hierarchy ordered by their size [1,11,21]. The distribution of droplet sizes corresponds to a distribution of different relaxation times measured in experiments. However, recent simulation results [31] indicate that temperature chaos drives rejuvenation as a random process of destroying locally correlated regions of spin overlap, or the local Edwards-Anderson order parameter, rather than just affecting the spin configurations themselves. These differing explanations again lead us to the question of how memory can follow rejuvenation, given that the system has gone chaotic and therefore lost knowledge of its previously grown correlated state.

Due to recent progress in understanding rejuvenation as a consequence of temperature chaos [31], we return to the observation of memory loss in spin glasses. We follow the so-called "double memory" experiments by Jonason *et al.* and Lefloch *et al.* [11,20], and focus on tuning the memory effect between two aging intervals at different temperatures separated by rapid temperature changes. In a similar spirit, we dub our protocols "double-waiting-time" experiments.



FIG. 1. The imaginary part of the ac magnetic susceptibility, $\chi''(\omega = 2\pi \text{ Hz}, T)$. The dashed data are the reference curve measured while continuously cooling the sample. The dot-dashed data include waiting at $T_{w_1} = 22.5 \text{ K}$ for $t_{w_1} = 1$ hour and rejuvenation upon lowering the temperature. The solid curve is the heating data that exhibit the memory effect back at T_{w_1} . All heating and cooling rates are 1 K/min. The inset shows a double-waiting-time experiment. $\Delta \chi_C''$ is the change in susceptibility during aging and $\Delta \chi_H''$ is the difference from the reference curve upon heating. For these data, the cooling and heating rate is 35 K/min between the two waiting temperatures.

We quantify the memory, \mathcal{M} , by computing the ratio

$$\mathcal{M} \equiv \frac{\Delta \chi_H''}{\Delta \chi_C''} = \frac{\chi_R''(T_{w_1}) - \chi''(t_{w_1} + t_{w_2}, T_{w_1})}{\chi_R''(T_{w_1}) - \chi''(t_{w_1}, T_{w_1})}, \qquad (1)$$

shown pictorially in Fig. 1. This quantity is a dimensionless parameter that compares the three measured susceptibilities. The numerator, $\Delta \chi_{H}^{"}$, is the difference between the reference curve $\chi_{R}^{"}$ at $T_{w_{1}}$ and the susceptibility upon returning to $T_{w_{1}}$ after aging for an additional $t_{w_{2}}$ at the lower temperature. The denominator, $\Delta \chi_{C}^{"}$, is the difference between the reference curve $\chi_{R}^{"}$ at $T_{w_{1}}$ and the dynamic susceptibility at $T_{w_{1}}$ after aging for $t_{w_{1}}$. Perfect memory ($\mathcal{M} = 1$) occurs when $\chi^{"}(t_{w_{1}} + t_{w_{2}}, T_{w_{1}}) = \chi^{"}(t_{w_{1}}, T_{w_{1}})$. If there is no memory ($\mathcal{M} = 0$), the heating curve follows the reference curve, $\chi^{"}(t_{w_{1}} + t_{w_{2}}, T_{w_{1}}) = \chi_{R}^{"}(T_{w_{1}})$.

We ascribe rejuvenation to temperature chaos, first described in Ref. [32], and recently observed [33] in a sample of Cu_{0.92}Mn_{0.08} cut from the same boule as our sample. As shown computationally in Refs. [13,31], when the temperature is lowered to T_{w_2} such that the spin glass has gone chaotic, then spin glass correlations develop over regions with a new length scale, with the growth of new correlations at T_{w_2} occurring as if there were no correlations grown at T_{w_1} . We have ensured that our temperature drop of $\Delta T \equiv T_{w_1} - T_{w_2} = 4$ K is large enough to guarantee rejuvenation (see Fig. 1).

From this argument, memory is an interplay between correlation lengths, as recently confirmed [34]. We increase the correlation lengths by varying the waiting time. If t_{w_1} (t_{w_2}) increases while t_{w_2} (t_{w_1}) is fixed, more (less) memory is expected at T_{w_1} . This argument is akin to the "temperature microscope model" (TMM) of Bouchaud *et al.* [35] used to describe locally ordered spin configurations within the droplet picture, as well as the phenomenological picture presented in Ref. [11]. Importantly, the TMM implies that memory in the double-waiting-time experiments are a function of a single variable: the ratio between the dynamical correlation lengths grown at either temperature. Meanwhile, models like the "ghost domain" picture [15] are similar to the TMM, but have correlated growth with finite spatial extent. Still other pictures, such as in Ref. [32], imply that any growth of any correlated regions at T_{w_2} will lead to memory loss. In what follows, we scrutinize these arguments by measuring how the memory, defined in Eq. (1), varies throughout our doublewaiting-time experiments.

Methods. The following describes our systematic, quantitative study of the memory effect. All ac susceptibility measurements were taken using a magnetic property measuring system (MPMS) 3 [36]. The measurement frequency was 1 Hz, with a field amplitude of 10 Oe, sufficient to observe out-of-equilibrium effects while staying in the linear regime. The glass temperature was found through dc magnetization measurements to be $T_g = 41.6$ K [37].

For the double-waiting-time experiments, we approximate a quench with a cooling rate of 35 K/min to reduce unintended aging effects. For consistency in the measurements, the temperature was allowed to settle at each waiting temperature before recording the first measurement. While the temperature change from T_{w_1} to T_{w_2} was only about 10 seconds, the first data point taken was around 100 seconds. For each recorded point, 10 measurements were averaged. First, the system was quenched from $T = 60 \text{ K} > T_g$ to an aging temperature $T_{w_1} < T_g$ and was allowed to relax for a time t_{w_1} . Then, the system was quenched to a lower temperature $T_{w_2} < T_{w_1}$ where it evolved for time t_{w_2} . Finally, the system was rapidly heated back to T_{w_1} where the susceptibility was compared to the reference system (inset of Fig. 1).

Results. Our experiments were designed to test the effects of waiting time (and therefore the correlation length) on \mathcal{M} . In Fig. 2, we see that the double-waiting-time protocol significantly impacts \mathcal{M} . The trend is clear—the longer t_{w_1} , the greater \mathcal{M} is, but the longer t_{w_2} , the smaller \mathcal{M} is. Additionally, in experiments with a lower T_{w_1} , \mathcal{M} is always larger than in ones that have a higher T_{w_1} . Furthermore, the fact that \mathcal{M} *increases* with t_{w_1} means that the memory loss seen is more complicated than the picture presented in Ref. [32], where any growth at T_{w_2} for a fully chaotic system is expected to decrease \mathcal{M} . Indeed, this increase suggests that the degree to which temperature chaos erases the spin glass's memory is a gradual, rather than an abrupt, process.

There are at least two length scales at play—the size of correlations at T_{w_1} , and those at T_{w_2} . We estimate the correlation length based on the relationship developed by Kisker and Rieger [38],

$$\frac{\xi(t,T)}{a_0} = c_1 \left(\frac{t}{\tau_0}\right)^{c_2 T/T_g},\tag{2}$$

where $a_0 = 6.6$ Å is the average spacing between manganese ions, $\tau_0 \approx 2 \times 10^{-13}$ s is the timescale of microscopic fluctuations, $c_1 \approx 1$, and $c_2 \approx 0.1$. These estimates have been compared to three experimentally extracted correlation



FIG. 2. Memory versus waiting time with four different first waiting temperatures. For both (left) and (right), the first and second waiting temperatures are the same: $T_{w_1} = (18, 22.5, 27.5, \text{ and } 30 \text{ K})$ and $T_{w_1} - T_{w_2} = 4 \text{ K}$. In both cases either t_{w_1} (left) or t_{w_2} (right) were varied from 0 to 6 hours (the horizontal axis), while the other waiting time was fixed at 3 and 1 hours, respectively. Closed (open) markers with statistical error bars indicate a variation of t_{w_1} (t_{w_2}). The lines are predictions based our model described by Eq. (5). As discussed in the text, the vertical dashed lines are where we expect a crossing if memory only depends on the ratio of the spin glass correlation lengths.

lengths (starred points in Fig. 3) using dc protocols pioneered by [39,40].

At first glance, our experimental results in Fig. 2 are qualitatively consistent with the TMM, which posits that the memory loss is only controlled by the ratio $\alpha \equiv \xi_2/\xi_1$. An increase in ξ_1 (ξ_2) leads to a decrease (increase) in memory loss. However, quantitatively, this is not borne out in the data. To illustrate this, consider when $t_{w_1} = t_{w_2}$. α will then depend only on the *difference* between waiting temperatures, ΔT , meaning the curves in Fig. 2 should cross when $t_{w_1} = t_{w_2}$ since all the ΔT s are identical (for more details, see the Supplemental Material [41]). Experimentally, however, we find that \mathcal{M} varies by about 40%. Even when the temperature dependence of c_2 is taken into account, only a 2.4% difference in \mathcal{M} is expected. This demonstrates that the physics of memory has a more intricate dependence on spin glass correlations than what is currently discussed in the literature.

Discussion. To this end, we developed an experimentally motivated model of our data whose derivation is given in the Supplemental Material [41]. We consider a growing correlated region of size ξ_1 at waiting temperature T_{w_1} , encapsulated by a volume $V_{\ell} = \ell \ell_1^2$. Here, we take ℓ and ℓ_{\perp} as length scales that



FIG. 3. The data from Fig. 2 collapse as a function of memory loss modeled in Eq. (4). Additionally, the three starred data points use correlation lengths extracted from dc experiments with the ac values of memory. T_{w_1} (18, 22.5, 27.5, and 30 K) and $T_{w_1} - T_{w_2} = 4$ K. In both cases either the first (closed markers) or second (open markers) waiting times are varied from 0 to 6 hours, while the other waiting time is fixed at 3 (1) hours.

are parallel and perpendicular to the ac field, and require that they be large enough to consider different volumes of size V_{ℓ} as statistically independent. In equilibrium, and in the absence of a real-space anisotropy, we would expect that these scales are both equal to a static, isotropic correlation length which we assume is always larger than the dynamical correlation length in our experiments.

Next, we consider a quench to T_{w_2} . Because we have ensured full rejuvenation, the spin glass energy landscape at T_{w_2} does not have the same set of minima as it does at T_{w_1} . We model this as a single correlated region of volume V_{ξ_1} growing within V_{ℓ} , with secondary correlated regions of volume V_{ξ_2} growing independently from the first. Thus, upon quenching to T_{w_2} , the new regions can appear anywhere within V_{ℓ} with an assumed uniform probability. If any new growth at T_{w_2} coincides with the original correlated region during the waiting time t_{w_2} , we assume memory is reduced upon returning to T_{w_1} .

Within this model, memory loss is the average relative change in V_{ξ_1} within V_{ℓ} after randomly developing new correlated regions at T_{w_2} . Thus, we must compute $\overline{\Delta V}/V_{\xi_1}$, where the overbar denotes statistical averaging over all independent volumes of size V_{ℓ} . Further details can be found in the Supplemental Material [41] and Ref. [42] therein, but the main point is that the average change in volume $\overline{\Delta V}$ depends on where V_{ξ_2} grows: within, at the edge of, or outside V_{ξ_1} . The final expression for a spherical correlated volume, $\overline{\Delta V}/V_{\xi_1}$, is proportional to

$$\frac{\overline{\Delta V}}{V_{\xi_1}} \propto \frac{V_{\xi_1}}{V_\ell} \left(\frac{\xi_2}{\xi_1}\right)^3 = \frac{V_{\xi_1}}{V_\ell} \alpha^3.$$
(3)

Comparing Eq. (3) to Fig. 2, we identify two cases that help ascertain the behaviors of ℓ and ℓ_{\perp} . The first case would be if there is no independent length scale at the first waiting temperature other than ξ_1 , implying both ℓ and $\ell_{\perp} \sim \xi_1$. Thus, Eq. (3) predicts that memory loss only depends on α (TMM). This is incompatible with the data shown in Fig. 2, as discussed above. In the second case, there is still real-space isotropy, $\ell = \ell_{\perp}$, but both ℓ_{\perp} and ℓ are independent of ξ_1 . In this case, Eq. (3) implies that memory loss does not depend on ξ_1 at all, again incompatible with the experimental results—were this true, each curve in Fig. 2 (left) would be constant. Hence, from our experimental data, we conclude that only one length scale must indeed scale with ξ_1 , while the other is independent of it.

By substitution into Eq. (3), we have

$$\frac{\overline{\Delta V}}{V_{\xi_1}} \propto \frac{4\pi}{3} \frac{\xi_1}{\ell} \left(\frac{\xi_2}{\xi_1}\right)^3 = \frac{4\pi}{3} \frac{\xi_1}{\ell} \alpha^3. \tag{4}$$

With this expression, we combine all data from Fig. 2 into a single plot shown in Fig. 3, with the measured memory being the vertical axis, and the calculated value of $\xi_1 \alpha^3$ being the horizontal. We see clear evidence of data collapse from all of the double-waiting-time experiments, indicating that the memory effect is not solely a scaling function of α , but rather memory depends on *both* length scales explicitly. The only way the dimensionless quantity of memory can be a function of both lengths is if there is at least another independent length scale present: ℓ . Our model provides an interpretation for this length. Its size, compared to ξ_1 , controls how probable it is for new correlated regions grown at T_{w_2} to coincide with those at T_{w_1} . For it is only growth at T_{w_2} that coincides with the original growth at T_{w_1} , rather than any growth at all, that leads to memory loss.

We emphasize that the collapse shown in Fig. 3 comes from 52 independent double-waiting-time experiments [43], and the horizontal axis represents a protocol-dependent, *calculated* value from Eq. (4). The fact there is a distinct data collapse represents agreement between these independent trials and implies the existence of another physical length scale relevant for memory. This is the additional structure that has been missing in our understanding of the memory effect.

Now, we revisit the conundrum where some spin glasses exhibit significant memory loss (typically metallic spin glasses) while others do not (typically insulating spin glasses). If a system has $\xi_1/\ell \rightarrow 0$, we expect nearly perfect memory regardless of correlated growth at T_{w_2} . Meanwhile, whenever ξ_1/ℓ is sizable, there will always be a substantial amount of memory loss. In both cases, random competition between the independent growth of ξ_1 and ξ_2 drives memory loss, and ℓ controls the severity.

We can be more precise with our modeling. As discussed in Refs. [44–47], an increase in ξ is attributed to growing spin glass order. In the case of ac susceptibility measurements, this is seen in the reduction of χ'' . As derived in the Supplemental Material [41], the relation between \mathcal{M} and $\overline{\Delta V}/V_{\xi_1}$ can then be shown to have the form

$$\mathcal{M} = w \left[1 - \frac{4\pi}{3} \frac{\xi_1}{\ell} \left(\frac{\xi_2}{\xi_1} \right)^3 \right]^{p/d},\tag{5}$$

where $w \sim O(1)$, ℓ , and p are unknown fitting parameters. For Fig. 3, the values of w, ℓ , and p are found to be $w = 1.2 \pm 0.02$, $\ell = 100 \pm 24 a_0$, and $p/d = 2.4 \pm 0.7$, where d = 3 is the spatial dimension.

This predicted fit is shown in Fig. 3, and we find that the data in Fig. 2 are well represented by this model. Notably, the same three fitting parameters are used for all 52 independent trials of the eight curves in Fig. 2.

Conclusions. Using quantitative measures of memory loss in spin glass systems, we have elucidated the mechanism responsible for the memory effect. By performing a

"double-waiting-time" experiment, and varying either t_{w_1} or t_{w_2} while holding the other fixed, we have shown that we can tune the amount of memory loss. This has allowed us to quantitatively test previously proposed qualitative explanations of memory loss and develop an experimental model which explains our results. By modeling the amount of memory retained as a function of dynamical correlation length growth, we find that an additional spatial length scale, ℓ , controls the impact that independent, but coincident, growth of correlations at T_{w_2} have on established correlated regions grown at T_{w_1} .

Our modeling relies on the existence of separate, uncorrelated anisotropic volumes of size $V_{\ell} = \ell \ell_{\perp}^2$, where ℓ_{\perp} , measured in the plane normal to the ac field, scales with the dynamical correlation length grown at the first waiting temperature $\xi_1(t_{w_1}, T_{w_1})$, and ℓ is independent of it. While the cause of the spatial anisotropy is unclear, our data (Fig. 2), and subsequent collapse of all 52 independent trials (Fig. 3), strongly support its presence. There are several mechanisms which could generate a spin-space anisotropy in spin glasses like an external magnetic field acting as an effective uniaxial random field [48], or magnetic anisotropies inducing chiral order [49]. At present, it is unclear how these would present in real space and will be the subject of further study, but such spin-space mechanisms exist. For example, extended defects are known to play a similar role in disordered magnetic systems [50-54]. Our model assumes the spin-space anisotropy produced by the ac field generates an equivalent real-space anisotropy.

We emphasize that the spin glass correlated volumes as described in this Letter are not spin-spin correlations as suggested in the droplet picture [55]. Instead, given the recent numerical results on temperature-chaos-driven rejuvenation [31], these correlated volumes are grown in the local Edwards-Anderson overlap. Crucially, this allows a description of memory following rejuvenation. When the temperature is lowered, it is the Edwards-Anderson overlap, rather than the spin configurations, which are frozen in, or "imprinted." Once the system goes chaotic, the growth of correlations at either waiting temperature will be independent of the growth of correlations at the other waiting temperature. However, the correlations at the lower temperature could form in the same location in real space as the original correlated regions. When this coincident growth occurs, the volume of the original correlated region decreases, leading to the memory loss observed. We anticipate this study will allow for quantitative comparisons of the memory effect in other glassy systems [56].

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