Emergence of giant orbital Hall and tunable spin Hall effects in centrosymmetric transition metal dichalcogenides

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We demonstrate the formation of orbital and spin Hall effects (OHE/SHE) in the 1T phase of nonmagnetic transition metal dichalcogenides. With the aid of density functional theory calculations and model Hamiltonian studies on MX_2 (M = Pt, Pd; and X = S, Se, and Te), we show an intrinsic orbital Hall conductivity ($\sim 10^3 \hbar/e \ \Omega^{-1} \text{cm}^{-1}$), which primarily emerges due to the orbital texture around the valleys in the momentum space. The robust spin-orbit coupling in these systems induces a sizable SHE out of OHE. Furthermore, to resemble the typical experimental setups, where the magnetic overlayers produce a proximity magnetic field, we examine the effect of magnetic field on OHE and SHE and showed that the latter can be doubled in these class of compounds. With a giant OHE and tunable SHE, the 1T-TMDs are promising candidates for spin and orbital driven quantum devices such as SOT-MRAM, spin nano-oscillators, spin logic devices, etc., and to carry out spin-charge conversion experiments for fundamental research.

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I. INTRODUCTION

The generation of transverse orbital/spin/charge current with a longitudinal applied electric field is known as the orbital/spin/anomalous Hall effect (OHE/SHE/AHE) [1-3]. The effect is illustrated in Fig. 1. These transverse quantum phenomena have drawn significant attention due to their potential application in designing futuristic quantum devices. While the AHE can be observed by simply measuring the transverse charge current, in the case of OHE and SHE, the transverse magnetic moments are generally measured by passing orbital/spin current through a ferromagnet. The OHE is a fundamental effect, in the sense that it arises from the intrinsic orbital moment and does not require external magnetic field or interaction. On the other hand, the SHE is either intrinsically generated in a magnetic material or in a spin orbit coupling (SOC) active nonmagnetic material through SOC. In the latter case, the OHE induces a spin current via SOC [4-8]. Interestingly, several theoretical works [4–8] have proposed that the OHE is very large and is the dominant one in some materials.

In most of the experiments, OHE and SHE are manifested through the spin orbit torque (SOT), which arises due to the spin current [9–12]. Therefore, in the context of nonmagnetic materials, it is prudent to explore materials with large OHE and a strong SOC. For the former, the noncentrosymmetric systems are natural choices as the absence of inversion symmetry allows the spatial accumulation of orbital moments. From the materials point of view, keeping the large SOC in mind, Pt has been reported to exhibit large OHE and SHE. It has also been found that several low SOC metals show huge OHE even if the SHE is negligible. Such materials are of great interest as the large orbital current gives rise to strong SOT. In this context, the noncentrosymmetric monolayer TMDs are promising [6,7,13,14]. However, it is of practical interest to explore the bulk TMDs as potential candidates for SOT. A recent theoretical study [15] suggests that the orbital current in bulk PtSe₂ can give rise to large SOT in the permalloy. But, as the bulk TMDs are centrosymmetric, the quenching of the intrinsic orbital moment occurs, for which the OHE is expected to be negligible.

In this work, we carried out both density functional and model Hamiltonian calculation to propose that the bulk centrosymmetric TMDs ($1T-MX_2$; M = Pt and Pd; X = S, Se, and Te) can exhibit large OHE, when they are subjected to an applied electric field. In addition, we also consider an external magnetic field term in our model Hamiltonian to study the OHE, SHE, and AHE. This resembles the proximity magnetic field produced by the ferromagnetic overlayers, which are usually used in the experimental setups [16–18].

Our findings suggest that the OHE $(\simeq 800-1600 \ \hbar/e \ \Omega^{-1} \text{cm}^{-1})$ is nearly two orders of magnitude higher than the SHE ($\simeq 0.1-38 \ \hbar/e \ \Omega^{-1} \text{cm}^{-1}$) for the $1T-MX_2$. However, as the magnetic field is turned on, the SHE is nearly doubled, while the OHE changed a little. This result is significant since the spin current directly gives rise to SOT. Furthermore, since the OHE to SHE conversion factor, while the orbital current passes through a ferromagnetic overlayer [10], is $\simeq 2.5\%$, the large OHE itself provides a sizable contribution to the SOT. Hence, the present study opens up possibilities to tune the SOT experimentally with the aid of ferromagnetic overlayer, which provides a proximity magnetic field to the nonmagnetic material [16].

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FIG. 1. A schematic diagram illustrating orbital and spin Hall effect, where the electric field is applied along the x axis, and the orbital/spin current is produced along the y axis. Vertical arrows represent spins, while the circles indicate orbital magnetization.

II. BASIC FORMALISM AND COMPUTATIONAL METHOD

We study the 3D TMD compounds in the 1 T structure with the formula unit MX_2 , where M = Pt or Pd and X = S, Se, or Te. These compounds, with the Space Group No. 164 $(P\bar{3}1m)$, have a trigonal lattice structure [Fig. 2(a)] and are centrosymmetric. The band structure near the Fermi energy consists of d orbitals of the M atom and p orbitals of the Xatom, and has no band gap. Additionally, there is an electron pocket and a hole pocket at K and Γ points, respectively, as shown in Fig. 2(b) for PtSe₂. As we apply an external magnetic field, the spin degeneracy of the bands is broken. As a result, the bands with up and down characters cross the Fermi level at different energies, leading to a spin imbalance. As discussed later, this helps to tune the SHC of the material with the applied magnetic field. Detailed results for materials other than PtSe₂ are given in the Supplemental Material [19].

The orbital, spin, and anomalous Hall conductivities (OHC/SHC/AHC) reported here were computed within the framework of DFT by using the Quantum Espresso code [20], from which a TB model was constructed with the hopping parameters obtained from the WANNIER90 program [21]. The spin-orbit coupling (SOC) parameter in the TB Hamiltonian was extracted from the DFT band structure. From the eigenvalues and eigenfunctions of the TB Hamiltonian, the conductivities were computed using the Kubo formula as discussed later. For the DFT calculation, we have used the norm-conserving Perdew, Burke, and Ernzerhof (PBE) exchange-correlation functionals [22]. The self consistency calculation was carried out in a $30 \times 30 \times 30 k$ mesh.

We express the TB Hamiltonian as

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{SO} + \mathcal{H}_M,\tag{1}$$

where \mathcal{H}_0 is the electron kinetic energy, \mathcal{H}_{SO} is the SOC term, and \mathcal{H}_M describes the coupling of the external magnetic field to the spin and orbital moments of the electron. The kinetic energy term is

$$\mathcal{H}_{0} = \sum_{im\sigma} \varepsilon_{m} c_{im\sigma}^{\dagger} c_{im\sigma} + \sum_{ijmn\sigma} t_{im,jn} c_{im\sigma}^{\dagger} c_{jn\sigma}, \qquad (2)$$



FIG. 2. (a) Crystal structure of the 3D TMDs in the centrosymmetric 1 T phase, top and side views (left and right, respectively). (b) Comparison of the band structures of PtSe₂ obtained from the DFT and tight binding methods in the presence of SOC and without the magnetic field (B = 0). (c) Partial densities of state (PDOS), indicating Pt(d) and Se(p) to be the important orbitals near the Fermi energy. (d) Tight-binding band structure in the presence of both the magnetic field and SOC. The colored spin-split bands are not spin pure due to the SOC term, which mixes the two spins. Note that the hole pocket at Γ and the electron pockets at K as well as along the H - A line are the dominant contributors to the Hall conductivities due to the energy denominator in the Kubo expressions. (e) Sketch of the Brillouin zone.

where $c_{im\sigma}^{\dagger}$ is the electron creation operator with $i/m/\sigma$ being the site/orbital/spin index. We kept the metal d^5 orbitals and the chalcogen p^3 orbitals in the basis set, so that we have a 22 × 22 Hamiltonian including spin, and, furthermore, we kept the hopping integrals beyond nearest neighbors as well. In the Bloch function basis, the matrix elements in the orbital space are spin diagonal and they are given by

$$\mathcal{H}_0^{mn}(\vec{k}) = \varepsilon_m \delta_{mn} + \sum_j t_{mn}^j e^{i\vec{k}\cdot\vec{d}_j},\tag{3}$$

where ε_m is the on-site energy of the *m*th orbital, and $t_{mn}^j = \langle 0, m | \mathcal{H} | d_j, n \rangle$ denotes the hopping energy between the *m*th orbital in the central cell and the *n*th orbital located at distance \vec{d}_j with respect to the position of the *m*th orbital. The SOC term in the familiar form is

$$\mathcal{H}_{SO} = \frac{2\lambda}{\hbar^2} \vec{L} \cdot \vec{S},\tag{4}$$

TABLE I. Effective spin-orbit coupling parameter (λ) for several TMD compounds obtained by fitting with the DFT results.

Material	PtS ₂	PtSe ₂	PtTe ₂	PdS ₂	PdSe ₂	PdTe
λ (eV)	0.28	0.34	0.38	0.22	0.25	0.30

and in the second quantization notation it is expressed as

$$H_{SOC} = \lambda \sum_{i\eta} \sum_{\alpha\beta\sigma\sigma'} c^{\dagger}_{i\alpha\sigma} L^{\eta}_{\alpha\beta} S^{\eta}_{\sigma\sigma'} c_{i\beta\sigma'}, \qquad (5)$$

where λ is the SOC constant; \vec{L} and \vec{S} are the orbital and spin angular momentum operators, *i*, (α, β) , and (σ, σ') are the site, orbital, and spin indices, respectively; and $\eta(=x, y, z)$ denotes the three Cartesian components.

For simplicity, we have considered an effective value of λ for each material (listed in Table I), so that the TB model reproduces the DFT band structure in a wide energy region around the Fermi energy. The electron spin is $\vec{S} = (\hbar/2)\vec{\sigma}$, where $\vec{\sigma}$ are the Pauli matrices $\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$, $\sigma_y = \begin{pmatrix} 0 & -i \\ i & -i \end{pmatrix}$, and $\sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$. The orbital angular momentum operators for the case of L = 1, in the basis set $\phi_p \equiv (p_x, p_y, p_z)$, are given by

$$L_{x}^{(p)} = \hbar \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{bmatrix}, \quad L_{y}^{(p)} = \hbar \begin{bmatrix} 0 & 0 & i \\ 0 & 0 & 0 \\ -i & 0 & 0 \end{bmatrix},$$
$$L_{z}^{(p)} = \hbar \begin{bmatrix} 0 & i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \tag{6}$$

while for L = 2, with the *d*-orbital basis set $\phi_d \equiv (z^2, x^2 - y^2, xy, yz, xz)$, they are

$$L_x^{(d)} = \hbar \begin{bmatrix} 0 & 0 & 0 & \sqrt{3}i & 0\\ 0 & 0 & 0 & i & 0\\ 0 & 0 & 0 & 0 & -i\\ -\sqrt{3}i & -i & 0 & 0 & 0\\ 0 & 0 & i & 0 & 0 \end{bmatrix},$$
$$L_y^{(d)} = \hbar \begin{bmatrix} 0 & 0 & 0 & 0 & -\sqrt{3}i\\ 0 & 0 & 0 & i & 0\\ 0 & 0 & -i & 0 & 0\\ \sqrt{3}i & -i & 0 & 0 & 0\\ \sqrt{3}i & -i & 0 & 0 & 0\\ 0 & 0 & -2i & 0 & 0\\ 0 & 2i & 0 & 0 & 0\\ 0 & 0 & 0 & 0 & i\\ 0 & 0 & 0 & -i & 0 \end{bmatrix}.$$
(7)

The last term of the Hamiltonian Eq. (1) is the coupling of the applied magnetic field to the electron magnetic moment. In the conventional form it is written as

$$\mathcal{H}_M = \vec{B} \cdot (g_l \vec{L} + g_s \vec{S}), \tag{8}$$

and in the second quantization notation it takes the form

$$H_M = B_z \Biggl[\sum_{i\alpha\beta\sigma} c^{\dagger}_{i\alpha\sigma} L^z_{\alpha\beta} c_{i\beta\sigma} + 2 \sum_{i\alpha\sigma\sigma'} c^{\dagger}_{i\alpha\sigma} S^z_{\sigma\sigma'} c_{i\alpha\sigma'} \Biggr].$$
(9)

Here, $\vec{B} \equiv \mu_B B_0 / \hbar \hat{z}$, where B_0 is the magnetic field along the z direction, μ_B is the Bohr magneton, and $g_l = 1$ and $g_s \approx 2$ are the orbital and spin gyromagnetic ratios, respectively. The magnetic field term in this model study represents an applied external magnetic field. It could also come from the proximity magnetic field of the overlayer in the experiment [16–18]. However, we note that for actual material systems, additional effects such as the exchange interaction of the electrons with the magnetic moments of the overlayer atoms may need to be considered.

The TB band structure obtained from Eq. (1), with parameters extracted from DFT, is compared with the DFT band structure in Fig. 2(b), where SOC was present but the magnetic field was zero. The two band structures agree very well over the entire Brillouin zone. There is no spin splitting as both the time reversal as well as the inversion symmetries are present. With a nonzero magnetic field, the time reversal symmetry is broken, producing the spin splitting in the band structure [Fig. 2(d)].

III. MAGNETIC MOMENTS AND ANOMALOUS HALL CONDUCTIVITY IN PRESENCE OF A MAGNETIC FIELD

Due to the presence of both time reversal and inversion symmetries in the TMDs, the momentum space spin/orbital moments as well as the Berry curvature are all zero in the Brillouin zone, but they all become nonzero when the magnetic field is applied, which breaks the time reversal symmetry. As it is well known, the nonzero Berry curvature leads to the anomalous Hall effect. In this section, we study these quantities and evaluate the magnitude of the AHC, to be later compared with the SHC and the OHC.

A. Spin/orbital magnetic moment

In the semiclassical formulation, the orbital magnetic moment is expressed as [23,24]

$$\vec{m}^{\text{orb}}(\vec{k}) = \frac{e}{2\hbar c} \sum_{n} f_{n\vec{k}} \left\langle \partial_{k} u_{n\vec{k}} \right| \times \left(\mathcal{H}_{k} + \varepsilon_{n\vec{k}} - 2\mu \right) \left| \partial_{k} u_{n\vec{k}} \right\rangle,$$
(10)

where $f_{n\vec{k}}$ is the Fermi function, *n* is the band index, \vec{k} is the Bloch momentum, -e < 0 is the electron charge, $\varepsilon_{n\vec{k}}$ is the band energy, and $u_{n\vec{k}}$ is the corresponding wave function. Also, here ∂_k represents $(\partial/\partial k_x \hat{x} + \partial/\partial k_y \hat{y})$. It is known that in presence of the inversion symmetry, the orbital magnetic moment follows $m^{\text{orb}}(\vec{k}) = m^{\text{orb}}(-\vec{k})$, whereas when the time reversal symmetry is present, one gets $m^{\text{orb}}(\vec{k}) = -m^{\text{orb}}(-\vec{k})$. Hence, the presence of both the time reversal and inversion symmetries nullifies the magnetic moment throughout the BZ. However, by breaking one of the two symmetries (in our case breaking the time reversal symmetry with the magnetic field), a nonzero distribution of the moments can be obtained in the momentum space. The same is true for both the spin moment as well as for the Berry curvature. We compute the spin moment from the expectation value of the spin



FIG. 3. Momentum space distribution of (a) orbital moment and (b) spin moment for $B_z = 0.1$ eV in PtSe₂ in the $k_z = 0$ plane. The units are in Bohr magneton (μ_B). The moments are prominent around the K and the Γ points on this plane, contributing a principal amount to the SHC/OHC. Panels (c) and (d) show the total orbital and spin moments (BZ sum) as a function of the magnetic field. Without a magnetic field, the net moments, as well as the moments everywhere in the BZ, are zero due to the existence of both the inversion and the time reversal symmetry.

operator \vec{S} ,

$$\vec{m}^{\rm spin}(\vec{k}) = -g_s \frac{e}{2m_e} \sum_n f_{n\vec{k}} \left\langle u_{n\vec{k}} | \vec{S} | u_{n\vec{k}} \right\rangle. \tag{11}$$

The computed values of the spin/orbital moments for PtSe₂ in the presence of a magnetic field are shown in Fig. 3. As expected, they are zero everywhere in the BZ in the absence of a magnetic field. Note that the spin moments disappear if the two spin-split bands are both occupied. Thus as may be inferred from the band structure of Fig. 2(b), there is spin moment only near the Γ and K points in the BZ, as seen from Fig. 3(b).

B. Anomalous Hall conductivity

Before we study the SHC and OHC, we compute the magnitude of the AHC, which can be expressed as the sum of the Berry curvatures over the occupied band states in the Brillouin zone [23], viz.,

$$\sigma_{\alpha\beta}^{\text{AHE}} = -\frac{e^2}{\hbar N_k V_c} \sum_{n\vec{k}}^{\alpha cc} \Omega_{n\vec{k}}^{\gamma}, \qquad (12)$$

where (α, β, γ) are cyclic permutations of (x, y, z), V_c is the unit cell volume, and N_k is the number of k points in the BZ. As usual, the conductivity is defined from the expression for the current density $j_{\alpha\beta} = \sigma_{\alpha\beta}E_{\beta}$, where the current density $j_{\alpha\beta}$ is along the α direction, generated by the electric field along the β direction. The Berry curvature may be expressed



FIG. 4. Anomalous Hall conductivity in PtSe₂ in the presence of the magnetic field. (a) Berry curvature $\Omega^{z}(\vec{k})$ (units of Å²), defined as the sum of $\sum_{n} \Omega_{n\vec{k}}^{z}$ over the occupied bands *n*, on the $k_{z} = 0$ plane with the scaled magnetic field $\mu_{B}B_{0}/\hbar \equiv B_{z} = 0.1$ eV. (b) Different components of the AHC in units of $\hbar/e \Omega^{-1}$ cm⁻¹ as a function of the magnetic field.

using the Kubo formula

$$\Omega_{n\vec{k}}^{\gamma} = -2\hbar^2 Im \sum_{m\neq n} \frac{\langle u_{n\vec{k}} | v_{\alpha} | u_{m\vec{k}} \rangle \langle u_{m\vec{k}} | v_{\beta} | u_{n\vec{k}} \rangle}{(\varepsilon_{m\vec{k}} - \varepsilon_{n\vec{k}})^2}, \quad (13)$$

where $v_{\alpha} = \hbar^{-1}(\partial \mathcal{H}/\partial k_{\alpha})$ is the velocity operator. Note that the Berry curvature also follows similar symmetry arguments as for the spin/orbital magnetic moment, already discussed above. It therefore vanishes in the absence of the magnetic field, since the system has both time reversal and inversion symmetries. However, an applied magnetic field will break the time reversal symmetry and create a nonzero Berry curvature. This leads to a nonzero anomalous velocity given by $e\hbar^{-1}\vec{E}$ × $\vec{\Omega}_{n\vec{k}}$, causing a transverse flow of electrons, resulting in the anomalous Hall effect (AHE). Since the charges also carry intrinsic orbital and spin magnetic moments, this also leads to an orbital/spin accumulation across the material, leading to the OHE/SHE, which we will study in the next section. The computed Berry curvature and the AHC are shown in Fig. 4. From the figure, we see that large values of the Berry curvature occur at the momentum points, where bands cross the Fermi energy [Fig. 2(d)] due to the energy denominator in the Kubo formula. The AHC is nonzero only when a magnetic field is present, as expected.

IV. ORBITAL AND SPIN HALL CONDUCTIVITIES

The key quantities we study in this paper are the orbital and spin Hall conductivities in the presence of a magnetic field, which are important ingredients in the generation of the spin-orbit torque in the TMD heterostructures with magnetic materials, which has been studied in several experiments [16,25].

We compute the OHC and SHC from the momentum sum of the orbital/spin Berry curvatures (OBC/SBC)

$$\sigma_{\alpha\beta}^{\gamma,\text{orb/spin}} = -\frac{e}{N_k V_c} \sum_{\vec{k}} \Omega_{\alpha\beta}^{\gamma,\text{orb/spin}}(\vec{k}), \qquad (14)$$

where $\Omega_{\alpha\beta}^{\gamma,\text{orb/spin}}(\vec{k}) = \sum_{n=1}^{\infty} \Omega_{n,\alpha\beta}^{\gamma,\text{orb/spin}}(\vec{k})$ is the sum over occupied bands *n* at a specific momentum point \vec{k} . The OBC for



FIG. 5. (a) Orbital and (b) spin Hall conductivity for PtSe₂, with B = 0, as a function of the Fermi energy. (c) and (d) Orbital and spin Berry curvature sums $\Omega_{yx}^{z,orb/spin}(\vec{k})$, defined as the sum over occupied bands of the corresponding Berry curvature at a specific \vec{k} point, in units of Å² in the $k_z = 0$ plane for the case $E_F = 0$. Contours of constant OBC/SBC values are shown in Panels (c) and (d). We note that while the SBC (d) preserves the sixfold rotational symmetry of the crytal, it is broken in the case of OBC (c). This is attributed to the distortion of the hybridized orbitals due to the electric field.

the Bloch state $n\vec{k}$ is computed using the Kubo formula

$$\Omega_{n,\alpha\beta}^{\gamma,\text{orb}}(\vec{k}) = 2\hbar \sum_{n' \neq n} \frac{\text{Im}[\langle u_{n\vec{k}} | \mathcal{J}_{\alpha}^{\gamma,\text{orb}} | u_{n'\vec{k}} \rangle \langle u_{n'\vec{k}} | v_{\beta} | u_{n\vec{k}} \rangle]}{(\varepsilon_{n'\vec{k}} - \varepsilon_{n\vec{k}})^2}, \quad (15)$$

where $v_{\alpha} = \frac{1}{h} \frac{\partial \mathcal{H}}{\partial k_{\alpha}}$ is the velocity operator, and the orbital current operator is $\mathcal{J}_{\alpha}^{\gamma,\text{orb}} = \frac{1}{2} \{v_{\alpha}, L_{\gamma}\}$, with L_{γ} being the orbital angular momentum. For the SBC, the orbital current operator is replaced by the spin current operator $\mathcal{J}_{\alpha}^{\gamma,\text{spin}} = \frac{1}{2} \{v_{\alpha}, S_{\gamma}\}$ in Eq. (15). Sufficient number of *k* points are taken in the momentum sum in Eq. (14) to ensure convergence, which typically required a *k* mesh of $120 \times 120 \times 120$ points in the full BZ.

Figure 5 shows the computed OHC and SHC for PtSe₂ as a function of the Fermi energy. Once again, the major contribution to the conductivity comes from the Γ and K valleys of the BZ as indicated from the Berry curvatures shown in Figs. 5(c) and 5(d), as well as from Fig. 6, which shows the Berry curvatures along the symmetry lines in the BZ. The last figure also shows additional substantial contributions from momentum points along the H-A line. One point to note from Fig. 5 is that the SHC is an order of magnitude less than the OHC. In fact, the OHC dominates the SHC even when a magnetic field is present, as summarized in Fig. 7.

However, in spite of its smaller magnitude, the spin current is thought to play the dominant role in magnetic torque experiments in typical nonmagnet/FM bilayers. For example, in the torque experiments on FM/Pt bilayers [12], it has been



FIG. 6. Orbital and spin Berry curvature sums along the high symmetry lines for PtSe₂.

estimated that the orbital-to-spin conversion efficiency is typically only a few percent (1-5%), so that overall, the orbital current is not as effective as the spin current in producing the torque, though it is much stronger in magnitude.

We note in passing that the OHE is considered more fundamental than the SHE in the sense that it can exist without the SOC λ . The OHE can originate from the orbital texture, created in response to the electric field [4], and neither the SOC nor a magnetic field is necessary for its existence. In contrast, one of these two needs to be present for the SHE, simply because otherwise there is no coupling between the spin space and the real space. This is clearly seen from Fig. 8, where we have shown the dependence of the OHC and the SHC on the SOC strength λ and the magnetic field. The SHC is zero unless there is a nonzero λ or a magnetic field.



FIG. 7. Orbital, spin, and anomalous Hall conductivities for PtSe₂ as a function of the magnetic field. Note that the magnitude of the OHC is by far the largest as compared to the other two, and of course the AHC is nonzero only when a magnetic field is present. The conductivities are in units of $\hbar/e \ \Omega^{-1} \text{cm}^{-1}$.



FIG. 8. (a) Dependence of the OHC and SHC for PtSe₂ (units of $\hbar/e \ \Omega^{-1}$ cm⁻¹) on the SOC strength λ . Here, $B_z = 0$. (b) The same as a function of the magnetic field but with $\lambda = 0$. The SHC is zero, if both λ and B_z are zero.

The Hall conductivities for several TMD compounds without any magnetic field are listed in Table II. In all cases, we find that the OHC is much higher than the SHC by many orders of magnitude.

Effect of a magnetic field

Since in the magnetic torque experiments on the nonmagnetic/FM bilayers, a strong magnetic field exists in the nonmagnetic material due to the proximity effect, it is important to consider how the magnetic field might affect the Hall conductivities. A main result of this section is that we find the SHC to increase by as much as a factor of two for typical fields that are present near the interface, while the OHC increases only by a modest amount. The substantial effect of the proximity magnetic field on the spin current must therefore be taken into account in interpreting the experiments, since the spin current is expected to be important in the generation of the magnetic torque.

In our calculations, we applied a magnetic field in the z direction, i.e., along the c axis of the material. The magnetic field has two effects that enhance the Hall conductivities. First, it creates a net orbital/spin moment in the sample, with momentum dependent values over the BZ, as indicated in Fig. 3. Second, a strong spin polarization is produced near the valley points K, and to some extent also at the Γ point, where the bands cross the Fermi energy, due to the Zeeman spin splitting produced by the magnetic field. It turns out that this spin imbalance has a strong effect on the SHC, which is enhanced by a factor of two or so for magnetic fields that exist

TABLE II. Orbital and spin Hall conductivities (in units of $\hbar/e \ \Omega^{-1} \text{cm}^{-1}$) for several TMD compounds with B = 0. Note that OHC \gg SHC for all cases.

Material	OHC			SHC		
	$\overline{\sigma_{zy}^{x,\mathrm{orb}}}$	$\sigma_{xz}^{y,\mathrm{orb}}$	$\sigma_{yx}^{z, \text{orb}}$	$\sigma_{zy}^{x,{ m spin}}$	$\sigma_{xz}^{y, { m spin}}$	$\sigma_{yx}^{z, \text{spin}}$
PtS ₂	799	1545	1049	0.07	-0.91	-1.12
PtSe ₂	1021	1601	1037	12.8	11.9	-29.4
PtTe ₂	602	819	1168	-38.2	-27.07	-50.7
PdS ₂	858	-146	-880	-0.01	0.49	0.05
PdSe ₂	840	-126	-803	-5.48	20.05	7.42
PdTe ₂	824	-112	-784	-35.4	-22.1	15.04



FIG. 9. Magnitudes of the OHC (left) and the SHC (right) as a function of the applied magnetic field for several TMD compounds.

near the interface with a FM. The OHC is also enhanced, but by a much smaller amount.

To be more specific, in these systems, the band structure, shown in Fig. 2, has an electron pocket at the K point and a hole pocket at Γ , except for PtS₂, which is an insulator. As the magnetic field is applied, it induces spin splitting of the band structure, creating an imbalance between up and down spins near these high symmetry points. Since the SBC for the bands with spin up character is almost opposite to that of the spin down bands for a specific k point, the imbalance created by the magnetic field leads to a net increase of the SBC and in turn of the SHC.

The computed values of the OHC/SHC as a function of the magnetic field for several TMD compounds are shown in Fig. 9. As we have already mentioned, the OHC is significantly larger than the SHC for all compounds and for all magnetic fields. A second point to note is that one might naively think that the larger the SOC, the larger would be the SHC. This would be generally true if the SOC strength λ can be increased within a certain material as was shown in Fig. 8(a) for PtSe₂, however, this is not the case while comparing between different materials. This is because the details of the band structure, in particular, the band crossings at the Fermi energy, have a dominant effect on the SHC. As a result, though the effective λ as seen from Table I are not that different, the magnitudes of the SHC are different, as seen from Table II and Fig. 9, by an order of magnitude between the materials considered. The observed increase in SHC due to the proximity magnetic field is in contrast to the case of pure metallic systems such as Pt and Pd where the SHC decreases with the increase in the proximity induced magnetic moment [26]. The decrease is attributed to the chemical potential dependence of SHE in these metals.

V. SUMMARY AND OUTLOOK

In summary, we studied the orbital and spin Hall effects in a series of bulk 1T transition-metal dichalcogenides (TMDs) of the form MX_2 : M = Pt, Pd and X = S, Se, and Te, in the presence of a magnetic field. Our work was motivated by the fact that many spintronics experiments involve nonmagnetic/ferromagnetic heterostructures, where the spin Hall effect of the nonmagnetic material is used to inject spin current into the ferromagnet. We used the TMDs as a prototype because these have been proposed to be effective nonmagnetic materials in such devices. In all materials we studied, the orbital Hall conductivity (OHC) was found to be two to three orders of magnitude larger than the SHC. Concenring the SHC, it is large in $PtTe_2$ and $PdTe_2$ as compared to the other compounds, suggesting the usefulness of these materials for spintronics devices. In magnetic torque experiments involving the nonmagnetic/ferromagnetic heterostructures so far studied, due to weak effective spin-orbit correlation in the ferromagnetic domain, the orbital current has been found rather inefficient in producing the torques, even though it may be much larger in magnitude. If this issue can be resolved, this may make the TMDs with large OHC be important materials for a variety of spintronics devices.

In the presence of a magnetic field, such as the proximity field of the ferromagnet in the heterostructure, we found the SHC to be enhanced by quite a large amount, as much as a factor of two, while the OHC increased by a modest amount. Thus, in device applications, the effect of any magnetic field present must be taken into account in determining the magnitude of the SHC/OHC. Additionally, in free standing samples, the OHC/SHC may be tuned by the application of an external magnetic field. Our work would be important in the interpretation of the spin-charge conversion experiments in spintronic devices such as SOT-MRAM, spin nano-oscillators, spin logic devices etc., involving the TMD materials.

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