Erratum: Nonreciprocal charge transport and subharmonic structure in voltage-biased Josephson diodes [Phys. Rev. B 109, 024504 (2024)]

A. Zazunov, J. Rech, T. Jonckheere, B. Grémaud, T. Martin, and R. Egger 10

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A mistake has been made in Sec. IV of the original paper when taking the zero-temperature limit of the general expression for the conductance (47) of a normal-superconducting (NS) junction. The correct form of Eq. (48) in the original paper must read

$$\frac{G(V)}{G_0} = \frac{1}{2} [\tilde{I}_1(eV) - \tilde{I}_2(-eV)], \tag{1}$$

such that electron- and hole-type scattering channels (s = 1, 2) contribute to G(V) with opposite signs of V. Since our results in Secs. IV B and IV C are based on Eq. (48), they have to be corrected accordingly. In particular, Eq. (50) should be replaced by

$$\frac{G(V)}{G_0} = 1 + \frac{1}{2} \sum_{\alpha = \pm} e^{-2\tilde{\gamma}_{\alpha}(\alpha eV)} = 1 + |a_1(eV)|^2,$$
(2)



FIG. 1. Zero-temperature nonlinear conductance G(V) (in units of $G_0 = 2e^2/h$) for a NS junction with several values for the dimensionless Cooper pair momentum parameter $q\xi$. This figure corrects Fig. 3 in the original paper. (a) is for transparency $\mathcal{T} = 1$ and was obtained from Eq. (3). (b)–(d) are for $\mathcal{T} = 0.9, 0.5, 0.1$, respectively, and were obtained from Eqs. (1) and (2).

where we took into account that $|a_1(eV)| = |b_2(-eV)|$, and hence Eq. (51) should read

$$\frac{G(v,q\xi)}{G_0} = 1 + \Theta(1 - |v - q\xi|) + \frac{\Theta(|v - q\xi| - 1)}{[|v - q\xi| + \sqrt{(v - q\xi)^2 - 1}]^2}.$$
(3)

This equation clearly reveals an asymmetry of $G(V) \neq G(-V)$ under voltage reversal for $q \neq 0$, and hence one can find rectification in the NS case. The corrected version of Fig. 3 in the original paper is shown in Fig. 1.

Unfortunately, we have missed this effect in our general expression (47) in the original paper for G(V). The subsequent analysis at zero temperature, due to the above mistake in Eq. (48), led us to the erroneous conclusion that the symmetry relation G(V) = G(-V) is always satisfied. Our corrected results agree with the results of Ref. [1].

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[1] M. Davydova, M. Geier, and L. Fu, Nonreciprocal superconductivity, arXiv:2407.01681.