## Terahertz spin-light coupling in proximitized Dirac materials

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The two-dimensional (2D) materials are highly susceptible to the influence of their neighbors, thereby enabling the design by proximity phenomena. We reveal a remarkable terahertz (THz) spin-light interaction in 2D Dirac materials that arises from magnetic and spin-orbital proximity effects. The dynamical realization of the spin-charge conversion, the electric dipole spin resonance (EDSR), of Dirac electrons displays distinctive THz features upon emerging spin-pseudospin proximity terms in the Hamiltonian. To capture the effect of fast pseudospin dynamics on the electron spin, we develop a mean-field theory and complement it with a quantum-mechanical treatment. As a specific example, we investigate the THz response of a single graphene layer proximitized by a magnetic substrate. Our analysis demonstrates a strong enhancement and anomalous polarization structure of the THz-light absorption, which can enable THz detection and efficient generation and control of spins in spin-based quantum devices. The identified coupled spin-pseudospin dynamics is not limited to EDSR and may influence a broad range of optical, transport, and ultrafast phenomena.

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Heterostructures combining two-dimensional (2D) van der Waals (vdW) materials offer innovative approaches for tailoring material properties [1,2]. The atomically thin 2D layers imply that many phenomena can be dominated by proximity effects [3,4]. This scenario is exemplified in spin-dependent properties of graphene-vdW heterostructures [3–7]. Transition metal dichalcogenides imprint spin-pseudospin-valley splitting and spin-orbit coupling (SOC) onto graphene [4,8–11], leading to spin filtering [12–14] as well as enhanced spin-to-charge interconversion [15–19]. An exchange field and ensuing carrier spin splitting can be further induced in graphene through magnetic proximity [20–25].

These added functionalities can pave the way to novel topological phases and devices that merge spin injection, detection, and manipulation into a single graphene platform [4,7,26]. Graphene and other Dirac materials have a great potential for THz (opto)electronics. Fast, room-temperature THz detectors made of graphene exhibit excellent sensitivity, high dynamic range, and broadband operation [27]. Massless Dirac fermions in graphene and topological insulators have large nonlinear optical coefficients and harmonic conversion efficiencies, suitable for THz high-power harmonic generation [28–30].

In this work, we investigate the spin-charge THz dynamics in proximitized 2D Dirac material with spin splittings, as shown in Fig. 1, and describe the resulting spin-light interaction including SOC. Our results demonstrate an unexplored realization of the spin-charge conversion from the electric dipole spin resonance (EDSR) [31,32], the excitation of electron spin precession by an ac electric field, which is a versatile tool from probing SOC, inhomogeneous magnetism, and topological states to realizing spin injection and controlling qubits [33–43]. In the presence of SOC, the EDSR is driven by a unique mechanism due to coupled spin-pseudospin dynamics [44,45]. Previously overlooked, this phenomenon becomes crucial at frequencies  $\omega$  in the THz range, where  $\omega \tau_p \gg 1$ , with  $\tau_p$  the momentum relaxation time. We calculate the absorption in proximitized graphene, using realistic SOC and magnetic exchange parameters, and demonstrate that the predicted EDSR leads to a remarkable increase of both the spin susceptibility and THz absorption. We reveal an anomalous polarization structure of EDSR controlled by the coupled spin-pseudospin dynamics and transformed for massive Dirac electrons upon lowering the Fermi energy,  $\mu$ . Our findings (i) provide striking differences from prior mechanisms [37,38,46,47] and (ii) highlight their relevance for THz detection and spin manipulation.



FIG. 1. Electric field of THz radiation causes intersubband spinflip transitions in a graphene on a substrate with a magnetization, **M**. The Dirac spectrum with a proximity-induced spin splitting,  $\Delta$ , wave vector, **k**, and the Fermi energy,  $\mu$ .

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The electron spin resonance (ESR) [36,48] is a wellestablished technique for studying spin phenomena in solids. It requires a static magnetic field that defines the direction of an equilibrium spin polarization, ac-magnetic field, that induces spin-flip transitions, which are detected by the absorption close to the Larmor frequency. The EDSR is essentially identical, but with the spin-flip transitions induced by acelectric field, allowed in the presence of SOC [31,32,49]. In nanostructures the SOC symmetry and magnitude can be designed to increase the efficiency of spin-flip absorption for a stronger spin-light interaction in the EDSR than in ESR. This is very desirable for semiconductor qubits [39,42,43] and to resonantly enhance the spin-charge conversion.

We analyze the EDSR for the low-energy Hamiltonian of Dirac electrons in a hexagonal system near the K and K' valleys, including magnetic exchange and SOC

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{\text{ex}} + \mathcal{H}_{\text{so}},\tag{1}$$

where  $\mathcal{H}_0 = \hbar \Omega_k \cdot \tau$  defines the Dirac spectrum,  $\hbar$  is the Planck constant, with  $\tau$  the lattice pseudospin operator [50],  $\Omega_k = 2v_F(\xi k_x, k_y, U/2\hbar v_F)$  the Larmor frequency, k the electron wave vector,  $v_F$  the Fermi velocity, and  $\xi = \pm 1$  the valley index. In *z* component of  $\Omega_k$ , *U* is the strength of the staggered potential, due to the on-site asymmetry between two inequivalent sublattices in 2D hexagonal lattices deriving from different atoms in the unit cell or from the effect of a substrate.  $\mathcal{H}_{ex} = \mathbf{\Delta} \cdot \mathbf{s}$  describes the magnetic exchange, where *s* is the spin operator, and  $\Delta$  the spin splitting in the meV (THz) range [4], whereas  $\mathcal{H}_{so} = \hbar \Omega_{so}(\tau) \cdot \mathbf{s}$  characterizes the SOC, where we assume a *k*-independent  $\Omega_{so}(\tau)$ . For a graphene/TMD,  $\mathcal{H}_{ex}$  is the valley-dependent splitting  $\xi \mathbf{\Delta} \cdot \mathbf{s}$ .

A hallmark of Dirac materials is the spin-pseudospin coupling and their entanglement [4,10,44,45] arising from  $\mathcal{H}_{so}$ . To model the spin-pseudospin dynamics driven by an electromagnetic wave, we consider the interaction  $\mathcal{V} = \hbar \Omega_{int}(t) \cdot \tau$ , where  $\Omega_{int} = -2(e/\hbar c)v_F(\xi A_x, A_y)$ , with *A* the vector potential. At normal incidence, we focus on the spin-light coupling emerging via an electric field component  $E_{\omega} = (i\omega/c)A_{\omega}$ .

We describe the coupled spin-pseudospin dynamics by the mean-field equations of motion for the classical vectors  $\tau$ , *s* [51]

$$\dot{\boldsymbol{\tau}} = ([\boldsymbol{\Omega}_k + \boldsymbol{\Omega}_{so}'(\boldsymbol{s})] \times \boldsymbol{\tau}) + [\boldsymbol{\Omega}_{int}(t) \times \boldsymbol{\tau}], \quad (2)$$

$$\dot{\boldsymbol{s}} = ([\boldsymbol{\Omega}_{\text{ex}} + \boldsymbol{\Omega}_{\text{so}}(\boldsymbol{\tau})] \times \boldsymbol{s}), \tag{3}$$

where  $\mathbf{\Omega}'_{so}(s)$  is obtained from  $\mathcal{H}_{so}$  by  $\mathbf{\tau}\mathbf{\Omega}'_{so}(s) = s\mathbf{\Omega}_{so}(\mathbf{\tau})$ and  $\hbar\mathbf{\Omega}_{ex} = \mathbf{\Delta}$ . For  $\Omega_{so} \leq \Omega_{ex}$ , this model captures the spin resonance at  $\hbar\omega \approx \Delta$ .  $E_{\omega}$  induces the dynamics of  $\mathbf{\tau}$ , which triggers the *s* precession due to spin-pseudospin coupling [44], as depicted in Fig. 2. For  $\Omega_{ex}\tau_p \gg 1$ , the intersubband spin-light coupling results in a resonant absorption peak, as discussed below.

We provide our framework for *n*-doped graphene with U = 0; the case of  $U \neq 0$  is given in [51] (see also Refs. [52,53] therein). The dynamics of two-level systems, including the lattice pseudospin, can be modeled using the classical precession equation for the quantum average of the operator, consisting of the corresponding Pauli matrices [54,55]. Ignoring SOC, Eq. (2) describes the free pseudospin oscillations with  $\Omega_k$  and, when subjected to an external oscillating field



FIG. 2. EDSR of a Dirac electron driven by coupled spinpseudospin dynamics. An incident THz radiation (yellow) with electric field  $E_{\omega}$  is absorbed creating a pseudospin component,  $\delta \tau_{\omega}$ , which precesses in the pseudospin field,  $\Omega_k$ , exerting a torque on a spin due to SOC (depicted by the orange arrow). Therefore, a spin component,  $\delta s_{\omega}$ , precesses  $\perp$  to the spin splitting  $\Delta$ , which is along the equilibrium spin  $s^0$ .

 $\Omega_{\text{int},\omega}e^{-i\omega t}$ , captures the resonance at  $\omega \approx \Omega_k$ , related to quantum pseudospin-flip transitions. An electron from the *K* valley with  $\boldsymbol{k}$  has a static pseudospin  $\tau^0 = \hat{\boldsymbol{k}}/2$ , parallel to  $\Omega_k = 2v_F \boldsymbol{k}$ . Applying  $\Omega_{\text{int}}(t)$  generates the torque  $\Omega_{\text{int}}(t) \times \tau^0 \propto \hat{\boldsymbol{k}} \times \boldsymbol{A}(t)$ , which, following Eq. (2), triggers the pseudospin rotation around  $\Omega_k$ . With  $\boldsymbol{A}(t) = 2 \operatorname{Re}[\boldsymbol{A}_{\omega}e^{-i\omega t}]$ , the linear response  $\delta \tau_{\omega} = \delta \tau_z \hat{\boldsymbol{z}} + \delta \tau_{\varphi} \hat{\boldsymbol{\varphi}}$  is perpendicular to  $\Omega_k$ 

$$\delta \tau_{z,\varphi}(\omega) = \frac{\alpha_{z,\varphi} \mathcal{T}}{\Omega_k^2 - \omega^2}, \quad \mathcal{T} = e \frac{v_F}{\hbar c} [\mathbf{A}_\omega \times \hat{\mathbf{k}}]_z, \qquad (4)$$

where  $\alpha_{z,\varphi} = (-i\omega, \Omega_k)$ . Poles in  $\delta \tau_{z,\varphi}(\omega)$  at  $\omega = \Omega_k$  give the pseudospin resonance, i.e., the interband transitions leading to the universal absorption  $\alpha_0 = \pi e^2/\hbar c$ . To obtain the interband absorption  $\alpha = (\alpha_0/2)[\Theta(\hbar\omega - 2\mu + \Delta) + \Theta(\hbar\omega - 2\mu - \Delta)]$ ,  $\Theta$  being the Heaviside function, one further needs to calculate the real part of the conductivity by summing  $2v_F \delta \tau_{\varphi}(\omega + i0)\hat{\varphi}_x$  over all quantum numbers with the equilibrium distribution function [51].

To illustrate the spin-pseudospin dynamics, we consider surface inversion asymmetry and the relevant Bychkov-Rashba SOC [56,57]

$$\mathcal{H}_{\rm so} = 2\lambda_{\rm so}(\xi\,\tau_x s_y - \tau_y s_x),\tag{5}$$

where the SOC strength  $\lambda_{so} \leq \Delta$  [3,4,22]. For the spin dynamics, in the lowest order of  $\lambda_{so}/\mu$ , we account for  $\mathcal{H}_{so}$  only in Eq. (3). The oscillating pseudospin,  $\delta \tau(t) = 2 \operatorname{Re}[e^{-i\omega t} \delta \tau_{\omega}]$ , induced by  $E_{\omega}$ , then contributes to  $\hbar \Omega_{so}(t) = 2\lambda_{so}[\hat{z} \times \delta \tau(t)]$  and exerts a torque on *s* (Fig. 2). For the outof-plane geometry,  $s^0 \parallel \Delta \parallel \hat{z}$ , the resonant spin component in Eq. (3) linear in  $\lambda_{so}$ ,  $\delta s_{\omega} = \delta s_k \hat{k} + \delta s_{\omega} \hat{\varphi}$ , is given by

$$\delta s_{k,\varphi}(\omega) = s^0 \beta_{k,\varphi} \frac{2\hbar^{-1} \lambda_{so} \Omega_k \mathcal{T}}{\left(\Omega_{ex}^2 - \omega^2\right) \left(\Omega_k^2 - \omega^2\right)},\tag{6}$$

where  $\beta_{k,\varphi} = (\Omega_{ex}, -i\omega)$  and  $s^0 = \pm 1/2$  is the initial spin state. A pole at  $\hbar\omega = \Delta$  corresponds to intersubband

spin-flip transitions. This resonance contributes to the absorption, which can be calculated from Eq. (6) in the rotating frame [48] by collecting the spin response from all electrons with different quantum numbers [51].

We can complement this analysis by evaluating, quantum mechanically, the EDSR-induced absorption. The matrix element  $M_{\uparrow\downarrow}$  of the direct intersubband spin-flip transition from  $(+\downarrow)$  to  $(+\uparrow)$  states (see Fig. 1) is found from the second-order perturbation theory

$$M_{\uparrow\downarrow} = \frac{\mathcal{V}_{(+\uparrow;-\uparrow)}\mathcal{H}_{(-\uparrow;+\downarrow)}^{\rm so}}{\varepsilon_{k,\downarrow}^{+} - \varepsilon_{k,\uparrow}^{-}} + \frac{\mathcal{H}_{(+\uparrow;-\downarrow)}^{\rm so}\mathcal{V}_{(-\downarrow;+\downarrow)}}{\varepsilon_{k,\downarrow}^{+} + \hbar\omega - \varepsilon_{k,\downarrow}^{-}}, \qquad (7)$$

where  $\varepsilon_{k,s}^{\pm} = \pm v_F \hbar k + s\Delta$  and  $\mathcal{V} = \hbar \Omega_{\text{int},\omega} \cdot \tau$ . The spingeneration rate is given by Fermi's golden rule

$$W_s = \frac{2\pi}{\hbar} \sum_k 2|M_{\uparrow\downarrow}|^2 (f_k^{\uparrow} - f_k^{\downarrow}) \mathcal{L}(\hbar\omega), \qquad (8)$$

where  $f_k^{\uparrow,\downarrow}$  is the Fermi-Dirac function of  $(\uparrow,\downarrow)$  electrons in the conduction band, the factor 2 accounts for (K, K') valleys, and the frequency broadening  $\mathcal{L}(\hbar\omega) = (\gamma/\pi)/[(\hbar\omega - \Delta)^2 + \gamma^2]$  is given by the Lorentzian with the spin-flip dephasing rate,  $\gamma$ . We express  $W_s = \alpha_{\rm sf}(\omega)(I/\hbar\omega)$  in terms of the radiation intensity, I, and the absorption coefficient,  $\alpha_{\rm sf}(\omega)$ , which at zero temperature is  $\alpha_{\rm sf} = \pi \gamma \alpha_{\rm sf}^{\rm max} \mathcal{L}(\hbar\omega)$ with

$$\alpha_{\rm sf}^{\rm max} = \alpha_0 b \frac{\lambda_{\rm so}^2}{4\Delta\pi\gamma} \bigg[ \ln\left(\frac{\mu+\Delta}{\mu-\Delta}\right) + \frac{\Delta^3/2\mu}{(\mu^2-\Delta^2)} \bigg], \qquad (9)$$

where  $b \sim 1$  is a prefactor determined by the directions of  $\Delta$ ,  $E_{\omega}$ . The same expression for  $\alpha_{sf}(\omega)$  can be obtained using the Kubo formula for the optical conductivity by including SOC in the velocity matrix elements [51].

 $\alpha_{\rm sf}^{\rm max}$  from Eq. (9) has an anomalous and counterintuitive polarization structure encoded in *b*, reflecting the role of both the pseudospin dynamics and SOC field symmetry for EDSR. Instead of directly interacting with  $E_{\omega}$ , a *K*-valley electron spin interacts with a SOC field,  $\hbar \Omega_{\rm so}(t) = -2\lambda_{\rm so}\delta \tau_{\varphi}(t)\hat{k}$  linearly polarized, irrespective of  $E_{\omega}$ . For a gapless spectrum, this results in the suppressed EDSR sensitivity to the  $E_{\omega}$ polarization: for  $\Delta \parallel \hat{z}$ ,  $\alpha_{\rm sf}$  is the same for both circular polarizations with b = 1, while, in the case of the in-plane  $\Delta$ orientation, b = 3/4 and b = 1/4, for  $E \parallel \Delta$  and  $E \perp \Delta$ , respectively.

However, for massive Dirac electrons with  $\mu \leq 2U$  the EDSR at  $\mathbf{\Delta} \parallel \hat{z}$  and  $\Delta > 0$  is induced preferably for  $\sigma^+$ polarization, as shown in Fig. 3 for  $\alpha_{sf}^-/\alpha_{sf}^+$ . In contrast to Eq. (4), at  $pv_F \ll U$  the vector  $\boldsymbol{\tau}^0 \parallel \hat{\boldsymbol{z}}$  and  $\delta \boldsymbol{\tau}_{\omega}$  lies within the electron motion plane, implying  $\mathbf{\Omega}_{so}(t) \propto \lambda_{so}[\hat{\mathbf{z}} \times \hat{\boldsymbol{\rho}}_{\sigma}(t)]$ follows  $\hat{\rho}_{\sigma}(t)$ , with the unit vector rotating counter- or clockwise depending on  $\sigma$ . Hence the spin resonance for  $\delta s_{\omega}$ obeys the ordinary polarization rules, i.e., at  $\Omega_{\text{ex}} \parallel \hat{z}$ , the EDSR absorption is active only for  $\sigma^+$  in both valleys. As  $\mu$ departs from the conduction band bottom,  $\Omega_k$  and  $\tau^0$  gradually tilt onto the plane, which suppresses the polarization sensitivity of the EDSR approaching the result b = 1 for the linear spectrum at  $\mu \gg U$ ; see Fig. 3. This behavior also contrasts the valley-dependent circular dichroism for the interband spin-conserving absorption [58–60], i.e., the fundamental absorption in the K(K') valley occurs for  $\sigma^+(\sigma^-)$ . A



FIG. 3. Ratio of the EDSR absorption for two circular polarizations of  $E_{\omega}$  as a function of the Fermi energy. The parameters are  $\Delta = 5 \text{ meV}, \lambda_{so} = 1.2 \text{ meV}, \text{ and } U = 3.5 \text{ meV}.$ 

more accurate analysis [51] shows that at  $\mu \leq U$  the EDSR does inherit a finite valley dependence with slightly different absorptions of  $\sigma^+$  light in *K* and *K'* valleys.

At smaller frequencies ~GHz,  $\omega \tau_p \lesssim 1$ , there is a change in the mechanism for the EDSR resonance from Eqs. (2) and (3) to the current-induced spin resonance [37,47]. Here, a spin torque acting on a 2DEG equilibrium spin density  $S^0 = \Delta/2\pi v_F^2 \hbar^2$  stems from an effective Larmor frequency  $\Omega_{so}^{D}(t) = (\lambda_{so}/\hbar v_F)[\hat{z} \times v(t)]$ , determined by the Drude velocity  $v(t) = 2 \operatorname{Re}[v_{\omega}e^{-i\omega t}]$  with  $v_{\omega} = eE_{\omega}\tau(v_F/p_F)/(1 - i\omega\tau)$ . One can qualitatively analyze the emerging nonequilibrium spin density,  $S_{\omega}$ , based on the Bloch spin-resonance equation

$$-i\omega S_{\omega} + T_2^{-1} S_{\omega} = [\mathbf{\Omega}_{\text{ex}} \times S_{\omega}] + [\mathbf{\Omega}_{\text{so},\omega}^{\text{D}} \times S^0].$$
(10)

Since  $\Omega_{so,\omega}^{D} \propto [\hat{z} \times E_{\omega}]$ , the resonant absorption for  $\Delta \parallel \hat{z}$ will be active only for one circular polarization. For the inplane geometry, the absorption only takes place when  $E \parallel \Delta$ , since the torque is absent as  $\Omega_{so,\omega}^{D} \parallel S^{0}$  for  $E \perp \Delta$ . In the intermediate regime,  $\omega \tau_{p} \sim 1$ , both resonance mechanisms (intraband and intersubband) should be considered on equal footing.

It is instructive to compare  $\alpha_{sf}^{max}$  with  $\alpha_0 \approx 2.5\%$  for graphene. For  $\mu \gtrsim 2\Delta$  (or  $\mu \gtrsim 2U$  for massive Dirac electrons with  $U > \Delta$ )  $\alpha_{sf}(\omega) \approx \alpha_0 b(\lambda_{so}^2/2\mu)\mathcal{L}(\hbar\omega)$ , with the peak value determined by  $\alpha_{sf}^{max} = \alpha_0 b\lambda_{so}^2/(2\pi\mu\gamma)$ . For  $\mu = 16 \text{ meV}$ ,  $\lambda_{so} = 0.7 \text{ meV}$ , and  $T_2 = \hbar/\gamma = 70 \text{ ps}$ , we obtain  $\alpha_{sf}^{max} \approx 0.55\alpha_0 = 1.25\%$ . We also compare the EDSRinduced  $M_{\uparrow\downarrow}$  from Eq. (7) with the matrix element of spin-flip transitions due to magnetodipole interaction,  $M_{md} = \mu_B g_e B/2$ , where  $g_e$  is the electron g factor and B is the magnetic field. With  $g_e \approx 1.99$  in graphene,  $M_{md}/M_{\uparrow\downarrow} \approx 10^{-4}$ , giving a strong SOC enhancement of the spin susceptibility compared to the ESR.

Our results for the linear spectrum and  $\alpha_{sf}^{max}(\mu)$  from Eq. (9) in Fig. 4(a) reveal an enhanced absorption when spin and pseudospin resonances approach each other at  $\mu \rightarrow \Delta$ . To analyze  $\alpha_{sf}(\omega)$  at  $\mu \approx \Delta$ , one needs to treat SOC nonperturbatively and account for spin-pseudospin correlations responsible for interband spin-flip transitions [61,62] at combined frequencies ( $\Omega_k \pm \Omega_{ex}$ ). We further identify an



FIG. 4. Evolution of the spin-pseudospin coupling-induced EDSR absorption with the Fermi energy and SOC. (a) Linear spectrum (inset); the parameters are  $\Delta = 5 \text{ meV}$ ,  $\hbar/\gamma = 70 \text{ ps}$ , with  $\gamma$  the spin-flip dephasing rate, and  $\lambda_{so} = 0.8$ , 1.4, and 2.0 meV. (b) Massive Dirac electrons (inset) for two circular polarizations, U = 3.5 meV, and  $\lambda_{so} = 1.2 \text{ meV}$ .

enhanced spin-light coupling with SOC, as  $\alpha_{sf}^{max} \propto \lambda_{so}^2/\gamma$  from Eq. (9). For  $\lambda_{so} = 2$  meV and  $\hbar/\gamma = 70$  ps,  $\alpha_{sf}^{max} > 20\%$ , an order of magnitude larger than  $\alpha_0$ .  $\alpha_{sf}^{max} \propto \lambda_{so}^2/\gamma$  is sensitive to the spin relaxation rate [37,63], which might be suppressed by  $\Delta$  [64] (implying an enhanced EDSR efficiency), while also having an inherent anisotropy in graphene-based heterostructures [65,66]. For massive Dirac electrons and different  $E_{\omega}$  polarizations,  $\alpha_{sf}^{max}(\mu)$  is shown in Fig. 4(b) [51].  $\alpha_{sf}^{max}$  maximum at  $\mu \approx U/2$  has the magnitude still larger than ESR. For both cases,  $\alpha_{sf}^{max}$  decreases at  $\mu \gg \Delta$  due to dynamic suppression of spin-pseudospin coupling; see the denominator of  $\delta \tau_{\omega}$ ,  $\delta s_{\omega}$  in Eqs. (4) and (6).

As an alternative to spectroscopic studies, we propose the electrical detection of resonant spin generation by THz radiation [51]. This is based on interfacial spin-to-charge conversion at the graphene-ferromagnet (F) contact. With the proximity-induced  $\Delta$  in graphene and the spin-dependent interfacial properties, together with the common  $\mu$  and charge transfer, the THz absorption in graphene leads to a nonequilibrium spin polarization and the generation of an interfacial electromotive force (EMF). This scheme is an extension of the Johnson-Silsbee spin-charge coupling or spin-voltaic effect [36,67–70] applied to Dirac materials, where EMF can be detected electrically. To preserve graphene's Dirac spectrum, in addition to an insulating or metallic F with h-BN spacer [21,71], even a direct contact with a metallic F can be suitable [22]. The enhanced spin-to-charge interconversion at the graphene-F interfaces enables THz optospintronics and graphene THz detection.

We have revealed the role of coupled spin-pseudospin dynamics for the understanding of THz spin susceptibility in proximitized Dirac materials. The discovered features are universal for a wide range of vdW heterostructures: (i) graphene with proximity-induced Zeeman spin splitting by various magnetic substrates [22–25,72–80], (ii) vdW hexagonal crystals with gapped spectrum, such as silicene [81], Bi(111) [82], or puckered 2D lattice with Dirac points [83], and (iii) nonmagnetic bilayers, such as graphene/TMD [8,10,11], with valley-dependent Zeeman spin splitting due to the hybridization of graphene *p* states with TMD bands [4,8,10]. In the latter case, we predict that, for  $\mu \leq 2U$  and B = 0, the EDSR will be induced selectively for *K* or *K'*, depending on the circular polarization. Furthermore, EDSR in graphene/TMD can imprint many-body effects from collective modes of spinorbital Fermi liquids [62,84].

With challenges and experimental surprises in the understanding of Zeeman splitting [85,86], a key parameter in proximitized vdW heterostructures, EDSR studies offer a versatile probe to address this situation and to quantify other proximity-induced spin splittings. For instance, our predicted polarization structure of  $\alpha_{sf}$ , with its small- $\mu$  enhancement, has a clear difference as compared to k-linear SOC. In that case, for the spin-light coupling,  $k \rightarrow k - (e/c)A$  in the klinear Rashba Hamiltonian,  $H_{\rm R} = \lambda_{\rm R} (\mathbf{k} \times \hat{\mathbf{z}}) \mathbf{s}$ , leads to the interaction potential,  $\mathcal{V}' = e\lambda_{\rm R}(\hat{z} \times A_{\omega})s/c$ , that couples  $A_{\omega}$ directly with the electron spin, rather than with pseudospin. For the usual SOC strength,  $\lambda_R$ , the corresponding torque leads to spin-flip transitions in  $\Delta$  with an ordinary polarization structure. As a fingerprint for different contributions to spinlight coupling in proximitized Dirac materials, it is natural to analyze the polarization dependence of EDSR for different mutual orientations of  $\Delta$ ,  $E_{\omega}$ , and its  $\mu$  dependence.

The phenomenon of a coupled spin-pseudospin dynamics has a broad range of implications beyond the EDSR, as it is inherent to many other manifestations of the spin-charge conversion, such as the spin-voltaic or spin-galvanic effects [69,87], which can be strongly modified in Dirac systems and whose dynamical properties remain to be understood. Another striking example is the study of the spin-orbit torque (SOT), which is expected to enable the next generation of embedded memories using 2D materials or to integrate photonics, electronics, and spintronics [88-90]. However, the spin-pseudospin dynamics in SOT has not been explored. With the push towards ultrafast SOT [91], our analysis of the THz spin-charge conversion, provides a further motivation to consider proximitized vdW heterostuctures, both for the resonant SOT generation and for the THz spintronics beyond magnetic multilayers.

Our picture could be used to analyze nonlinear optical response of Dirac systems and the nonlinear Hall effect [92] for different topological regimes [93]. The inverse effect of spin precession on orbital dynamics can be derived from the coupled spin-pseudospin dynamics, providing an alternative treatment of the topology-sensitive Kerr effect [94,95]. The discussed picture could be also used to analyze spin-flip transitions in a Dirac system with a stronger SOC, such as graphene-TMD heterostructures [4], and be implemented in graphene quantum dots and nanoflakes to realize qubits for THz quantum computing. While SOC has been employed to realize fast qubit rotations and control with electric fields [39,42,43], EDSR has not been exploited in graphene or bilayer graphene due to their low intrinsic SOC [96].

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