## **Unconventional periodicities of the Little-Parks effect observed in a topological superconductor**

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(Received 22 December 2020; revised 23 November 2021; accepted 4 January 2024; published 26 February 2024)

In superconductors, the condensation of Cooper pairs gives rise to fluxoid quantization in discrete units of  $\Phi_0 = hc/2e$ . The denominator of 2*e* is the signature of electron pairing, which is evidenced by a number of macroscopic quantum phenomena, such as the Little-Parks effect and the Josephson effect, where the critical temperature or the critical current oscillates with the periodicity of  $\Phi_0$ . Here we report the observation of Little-Parks oscillation periodicities of  $2\Phi_0$ ,  $3\Phi_0$ , and  $4\Phi_0$ , besides the conventional  $\Phi_0$ , in mesoscopic rings of epitaxial  $\beta - Bi_2Pd$ , a topological superconductor. These unexpected findings suggest new physics to account for the observed quantizations.

DOI: [10.1103/PhysRevB.109.L060504](https://doi.org/10.1103/PhysRevB.109.L060504)

The most distinctive feature of superconductivity is the presence of the complex-valued many-particle wave function that sustains phase coherence over macroscopic distances. One of its experimental manifestations is the fluxoid quantization in a superconducting ring. The single-value nature of the wave function dictates a universal phase change of  $2\pi$  for any closed path around the ring. As a result, the fluxoid  $\Phi'$  can only take on quantized values in integer steps of  $\Phi_0 = hc/e^*$ , where *h* is the Planck constant, *c* is the speed of light, and *e*<sup>∗</sup> is the effective charge. As a key evidence of electron pairing, *e*<sup>∗</sup> is found to be 2*e* of the Cooper pairs [\[1\]](#page-5-0). The quantization unit of  $\Phi_0$ , or the  $2\pi$  periodicity, has been confirmed by numerous experiments including magnetometry [\[2,3\]](#page-5-0), the Little-Parks effect [\[4\]](#page-5-0), and the Josephson effect/quantum interference experiments [\[5,6\]](#page-5-0).

The Little-Parks effect concerns the quantum oscillation of the superconducting critical temperature,  $T_c$ , as a function of the applied magnetic flux threading through the enclosed area of a superconducting ring, reflecting the periodic oscillation of the free energy. The  $T_c$  oscillation is experimentally observed by measuring the magnetoresistance of the ring at temperatures just below  $T_c$ . The first experiment by Little and Parks in superconducting tin rings [\[4\]](#page-5-0), which formally establishes integer fluxoid quantization [\[7\]](#page-5-0), demonstrates two distinctive hallmarks: (i) the resistance oscillates only with a single period of  $\Phi_0$ , and (ii) the minima of resistance occur when the applied flux is  $\Phi = n\Phi_0$ , where *n* is an integer. These key features reprise in all singlet superconductors (SCs) including *s*-wave SCs [\[8,9\]](#page-5-0) and *d*-wave SCs [\[10–12\]](#page-5-0), in both singlecrystalline and polycrystalline forms. For the unconventional

superconductor  $Sr<sub>2</sub>RuO<sub>4</sub>$ , the integer quantization also holds up well [\[13\]](#page-5-0), unless a large additional in-plane magnetic field is applied [\[14–16\]](#page-5-0).

Unlike the commonly observed even-parity spin-singlet pairing, in a topological superconductor with spin-triplet pairing, the gap function has odd parity and experiences a sign change upon inversion. This crucial sign change can facilitate a  $\pi$  phase shift at crystalline grain boundaries as first predicted theoretically [\[17\]](#page-5-0), giving rise to half-integer fluxoid quantization  $\Phi' = (n + 1/2)\Phi_0$ . The manifestation in the Little-Parks effect is that resistance minima appear at half-integer quanta instead, breaking Hallmark (ii). This halfquantum fluxoid (HQF) was recently reported in polycrystalline  $\beta - Bi_2Pd$  [\[18\]](#page-5-0), an intrinsic topological superconductor [\[19–22\]](#page-5-0). The Little-Parks oscillation of the polycrystalline  $\beta - Bi_2Pd$ , despite the HQF, remains exactly  $2\pi$  periodic, leaving Hallmark (i) intact.

We report in this Letter the experimental observation of multiple non- $2\pi$  periodicities in the Little-Parks effect of epitaxial  $\beta - Bi_2Pd$  ring devices. Although no HQF is observed in epitaxial  $\beta - Bi_2Pd$  samples, an expected outcome due to the absence of crystalline grain boundaries, it is evident that the quantization oscillation is never purely  $\Phi_0$  periodic. The decisive yet unexpected departure from Hallmark (i), a fundamental feature of fluxoid quantization, indicates exciting new physics. The underlying mechanism invites future theoretical deliberations.

We prepare 70-nm-thick epitaxial  $\beta - Bi_2Pd/SrTiO_3(001)$ and  $\beta - Bi_2Pd/MgO(001)$  thin films by magnetron sputtering. The as-grown films exhibit  $T_c$  of about 3.5 K. The thin films are subsequently patterned into submicron mesoscopic ring devices by electron-beam lithography. The Little-Parks experiment setup is depicted in Fig.  $1(b)$ . The ring device, shown in scanning electron microscopic image, is  $800 \times$ 800 nm in size, marked by the scale bar. The length of the side is measured between the midpoints of the opposite sides of the square. We have prepared seven different designs with various ring sizes and geometries, as shown in Figs.  $1(b)$  and  $1(c)$ . This helps us to reliably determine the  $\Phi_0$ -corresponding

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FIG. 1. Experimental setup. (a) Relation between the effective charge and the quantization periodicity. (b) A scanning electron microscope image of a representative  $800 \times 800$  nm ring device. (c) Scanning electron microscopic images of various ring device designs. The scale bars mark the length of the side of the square devices or the diameter of the round device. (d) Temperature regime of the Little-Parks effect with respect to the superconducting phase transition, indicated by the blue- and red-shaded areas in the normalized resistance vs temperature curves for ring devices of polycrystalline  $β - Bi<sub>2</sub>Pd/Si$  [\[18\]](#page-5-0) and epitaxial  $β - Bi<sub>2</sub>Pd/SrTiO<sub>3</sub>(001)$  (ring type-IV, Device A), respectively. (e) Resistance vs temperature curves for Device B (type-I,  $\beta - Bi_2Pd/MgO$ ) and Device C (type-VI,  $\beta - Bi_2Pd/SrTiO_3$ ). (f) Upper panel: The raw data observed in Device A at 2.7 K. The dashed line indicates the aperiodic background. Lower panel: The Little-Parks oscillation obtained after subtracting the background.

oscillation period in term of magnetic field. The Little-Parks effect is observed when the ring device is placed at a fixed temperature within the superconducting transition regime, where the variation of the  $T_c$  manifests as oscillations of the electrical resistance  $[4]$ . In Fig.  $1(d)$ , we compare a representative epitaxial ring of  $\beta - Bi_2Pd/SrTiO_3$  (Device A, Type-IV design) to our previous results from a polycrystalline ring of  $\beta - Bi_2Pd/Si$  [\[18\]](#page-5-0) with the same ring design, where the color shades indicate the temperature windows in which the Little-Parks effect was observed. Evidently, the Little-Parks regimes are located at virtually identical transition stages. The  $T_c$  transition behaves similarly for all the ring designs that we have examined. Figure  $1(e)$  compares the smallest design (Device B) and the largest design (Device C), where they only differ in the absolute values of resistance, dictated by the device line widths. In general, the Little-Parks effect is observed in the temperature window between 2 and 3 K. Above 3.2 K, no oscillations can be observed in magnetoresistance. A representative experimental result, the resistance of Device A as a function of the applied field, is presented in Fig. 1(f). Oscillatory features are observed on top of a roughly parabolic-shaped background. The aperiodic background is commonly observed in Little-Parks experiments, and presumably originates from field misalignment and finite device line width  $[8,23,24]$ , which can be approximated by a polynomial fitting (dashed line) and subsequently removed. The LittleParks oscillation  $\Delta R - H$  is revealed after subtracting the background from the raw data, as shown in Fig. 1(f).

The period of the Little-Parks oscillation is dictated by the area of the ring with respect to the value of  $\Phi_0 \approx 20.7$  Gauss- $\mu$ m<sup>2</sup>. For the ring size of 800 × 800 nm as demonstrated in Fig.  $1(b)$ , the expected  $\Phi_0$  period for two-electron pairing is 32.3 Oe. Experimentally observed oscillation periods closely agree with the expected values. An example of a polycrystalline niobium ring manifesting a uniform oscillation period of 30.2 Oe is presented in Fig.  $2(a)$ . Indeed, both hallmarks of the ordinary Little-Parks effect as a result of the integer fluxoid quantization are on display in this classical example of an *s*-wave SC: a unified period of the oscillation by  $\Phi_0$  and a series of resistance minima at  $n\Phi_0$ . On the other hand, in polycrystalline  $\beta - Bi_2Pd$  rings, as we have reported earlier, the Little-Parks oscillation can exhibit HQF of  $(n + \frac{1}{2})\Phi_0$  as a result of the anisotropic triplet pairing state [\[18\]](#page-5-0). One such example is demonstrated in Fig.  $2(b)$ , where the resistance minima appear at half-integer quanta, distinctively different from the case of integer-fluxoid quantization in Nb. Nevertheless, the Little-Parks effect with HQF is still strictly  $2\pi$ periodic. In the right panels of Figs.  $2(a)$  and  $2(b)$ , the Little-Parks oscillation is converted to the frequency domain by Fourier transform analysis. In both cases, the spectral weight occurs only at the period of  $\Phi_0$ , indicating the exclusive  $2\pi$ periodicity.

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FIG. 2. Little-Parks effect in Nb, polycrystalline, and epitaxial  $\beta - Bi_2Pd$  rings. Left: The Little-Parks effect of (a) polycrystalline Nb, (b) polycrystalline, and (c) epitaxial  $\beta - Bi_2Pd$  (Device A) rings. Right: The fast Fourier transform (FFT) spectra of the Little-Parks oscillations. The yellow triangle marks where to expect the peak for the  $2\pi$  periodicity. The experimental data shown in (a)–(c) are collected at 5.7 K for Nb, 2.6 K for polycrystalline  $\beta - Bi_2Pd$ , and 2.7 K for epitaxial  $\beta - Bi_2Pd/SrTiO_3(001)$  (Device A), respectively. The Little-Parks oscillations of polycrystalline Nb and  $\beta - Bi_2Pd$  [(a) and (b)] are reproduced from Ref. [\[18\]](#page-5-0).

The HQF originates from a  $\pi$  phase shift added to the superconducting wave function across certain crystalline grain boundaries [\[17\]](#page-5-0). In the absence of grain boundaries, such  $\pi$  phase shifts and hence HQF should not occur in epitaxial superconducting rings, irrespective of the gap parity, and none has been observed in epitaxial rings of  $\beta - Bi_2Pd$ . As an example, the Little-Parks effect observed in Device A [Figs.  $1(f)$  and  $2(c)$ ] shows no signs of HQF. Indeed, HQF is *completely* absent in the total of 30 epitaxial ring samples that we have measured. Striking features emerge, however, when one examines the periods of the Little-Parks oscillations in epitaxial samples. In Fig.  $2(c)$ , the same data of  $\Delta R$  oscillation in Device A from Figs.  $1(f)$  are plotted as a function of  $\Phi/\Phi_0$ , where the  $\Phi_0$  period is determined to correspond to 33.5 Oe of the applied field, consistent with the expected value of 32.3 Oe. The resistance minima of Device A are separated roughly by  $2\Phi_0$  with  $4\pi$  periodicity, instead of  $\Phi_0$ as in both Figs.  $2(a)$  and  $2(b)$ . Deviations in the positions of

the minima from the exact even-integer quanta are indicative of the mixture of longer periodicities. The Fourier transform analysis shows a dominating spectral peak at  $2\Phi_0$ , indicating the  $4\pi$  periodicity. Smaller contributions can also be found at  $3\Phi_0$  and  $4\Phi_0$ . In contrast, the spectral weight of the conventional  $2\pi$  periodicity is negligible at  $\Phi_0$ . The presence of the  $2\pi$ -periodic fluxoid quantization can only be hinted at by the kinklike feature in the  $\Delta R - \Phi$  curve near ±3  $\Phi_0$ . In the Fourier spectrum, the spectral weight of the  $2\pi$ -periodic component can be recovered after removing the spectral noise (Figs. S3 and S4; see the Supplemental Material for further details [\[25\]](#page-5-0)).

Evidently, the dominating non- $2\pi$  periodicities of the Little-Parks oscillations in Device A shatter Hallmark (i). It bears profound implications as the conventional wisdom expects the exclusively  $2\pi$ -periodic fluxoid quantization universally for all superconducting loops, regardless of their single-crystalline/polycrystalline nature or any details of the

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FIG. 3. The non-2π periodicities. (a) The Little-Parks oscillations and (b) the Fourier transform analyses of Device B, a type-I ring device of epitaxial  $\beta - Bi_2Pd/MgO(001)$ , plotted to the  $\Phi_0$  period of 116 Oe (102 Oe expected from the design geometry). The yellow triangle marks the position of the  $2\pi$  periodicity. (c)–(f) The (c),(e) Little-Parks effect and (d),(f) Fourier transform spectra of Devices C and D, respectively. Device C is a type-VI ring device of  $\beta - Bi_2Pd/SrTiO_3(001)$  which expects a  $\Phi_0$  period of 25.5 Oe. (c) and (d) are plotted to the observed  $\Phi_0$ period of 27.6 Oe. Device D is a type-III ring device of  $\beta - Bi_2Pd/SrTiO_3(001)$  with expected  $\Phi_0$  period of 57.4 Oe. (e) and (f) are plotted to the observed  $\Phi_0$  period of 60.0 Oe.

particular device, such as size, shape, presence of defects, etc. We have surveyed a total of 30 epitaxial  $\beta - Bi_2Pd$  rings and, in stark contrast, not a single ring exclusively displays the  $2\pi$ periodicity. Non- $2\pi$  periodicities are always observed. Multiple periodicities may coexist, with noticeable variations in the amplitudes among samples. Figure  $3(a)$  shows the Little-Parks effect observed in Device B, a 450-nm-size ring (type-I) fabricated using an epitaxial  $\beta - Bi_2Pd/MgO$  thin film. Above 3 K, a superposition of  $2\pi$  and  $4\pi$  periodicities is observed.

Below 3 K, a prominent  $3\Phi_0$ -periodic component emerges, indicating  $6\pi$  periodicity. The presence of  $2\pi$ ,  $4\pi$ , and  $6\pi$ periodicities can be confirmed by the Fourier transform analysis as shown in Fig.  $3(b)$ , unambiguously demonstrating the simultaneous presence of multiple periodicities. Figures  $3(c)$ and  $3(d)$  showcase an example of  $6\pi$  dominance, observed in Device C, a 900-nm-size ring (type-VI) of epitaxial  $\beta$  –  $Bi<sub>2</sub>Pd/SrTiO<sub>3</sub>$ . The prevailing  $6\pi$  periodicity is unequivocally demonstrated in both the  $\Delta R - \Phi$  curves [Fig. 3(c)] and



FIG. 4. Summary of observed periodicities. (a) Determination of the  $\Phi_0$  period. Squares:  $\Phi_0$  periods of 11 polycrystalline  $\beta - Bi_2Pd/Si$ ring devices [\[18\]](#page-5-0). Triangles:  $Φ_0$  periods of six polycrystalline α-BiPd/SrTiO<sub>3</sub> ring devices [\[26\]](#page-5-0). Circles:  $Φ_0$  periods of epitaxial  $β - Bi_2Pd$ rings, Devices A–D (this work). The curves present a calculated correct  $\Phi_0$  period and two other erroneously calculated periods. Yellow:  $\Phi_0$ period,  $H_{2\pi} = \frac{\Phi_0}{\mu_0 L^2}$ . Green:  $2\Phi_0$  period,  $H_{2\Phi_0} = \frac{hc}{e\mu_0 L^2}$ . Blue:  $\frac{1}{2}\Phi_0$  period,  $H_{\frac{1}{2}\phi_0} = \frac{hc}{4e\mu_0 L^2}$ . (b) The graph summarizes the occurrence of different periodicities observed from a total number of 30 ring devices made of 70-nm-thick  $\beta - Bi_2Pd$  thin films epitaxially grown on SrTiO<sub>3</sub>(001) and MgO(001) substrates with various device design geometries.

the Fourier transform spectra [Fig.  $3(d)$ ]. At 2.5 K, a weak high-pitch oscillation with the period of  $\frac{1}{2}\Phi_0$  emerges. The spectral weight of this  $\pi$  periodicity, however, is not immediately recognizable from the Fourier transform spectra due to the small oscillation amplitude. Nevertheless, the  $\pi$ -periodic contribution to the Fourier spectra could be distinguished following the analysis presented in Sec. IV and Fig. S6 of the Supplemental Material [\[25\]](#page-5-0). Dominating  $8\pi$  periodicity at all temperatures can be observed in Device D, a 600-nm-size ring (type-III) of epitaxial  $\beta - Bi_2Pd/SrTiO_3$ . Prominent peaks corresponding to the  $8\pi$  periodicity are evident in the Fourier transform spectra shown in Fig. [3\(f\).](#page-3-0) A smaller  $2\pi$ -periodic component can also be observed at the lower temperatures such as 2.4 and 2.6 K.

A spikelike feature may emerge at the zero magnetic field in the  $\Delta R - \Phi$  curves. Such feature can be seen in Device D [2.9 K of Fig.  $3(e)$ ] and Device A [Fig.  $2(c)$ ]. It only appears at higher temperatures, above 2.7 K. Its sharp decay at finite magnetic field and the nonrepeating nature suggests that the spike is unrelated to the Little-Parks effect and not indicative of any periodicities. Further discussions about its likely origin can be found in the Supplemental Material (Sec. VI) [\[25\]](#page-5-0).

The observation of non- $2\pi$  periodicities in epitaxial  $\beta$  – Bi<sub>2</sub>Pd rings came as a surprise, to which there is no comprehensive explanation readily available. It is pertinent to first discuss what the observed effect is *not*. The unconventional non- $2\pi$  periodicities are not the result of a spurious determination of the  $\Phi_0$  period. We have examined seven ring designs with various sizes and aspect ratios. The fluxoid quantization period in term of magnetic field can be calculated as  $H_{2\pi}$  =  $\frac{\Phi_0}{\mu_0 A} = \frac{hc}{2\epsilon \mu_0 L^2}$ , where  $\overline{A} = L^2$  is the effective area of the ring device, and *L* is the side length of a square ring measured between the middle points of the arms. In every ring device, we find the observed  $\Phi_0$  period in good agreement with the expected values calculated from the design geometry. The result can also be compared with the  $\Phi_0$  periods determined from our previous studies employing polycrystalline rings devices

[\[18,26\]](#page-5-0), where only the conventional  $2\pi$  periodicity is present. The comparison to the expected period and among experiments is presented in Fig.  $4(a)$ . All experimental data show excellent agreement with the calculated  $\Phi_0$  period  $(H_{2\pi})$ . We also plot two other curves if we erroneously determined the  $\Phi_0$  period to be two times, with  $H_{2\Phi_0} = \frac{hc}{e\mu_0 L^2}$  (green curve), or half of the correctly determined  $\Phi_0$ , with  $H_{\frac{1}{2}\Phi_0} = \frac{hc}{4e\mu_0 L^2}$ (blue curve). It is evident that all the experimental data are located at the  $\Phi_0$  curve without exceptions. We have correctly identified the  $\Phi_0$  period. This also reaffirms that the non- $2\pi$ periodicities are not the result of any particular device geometries. At any rate, the non- $2\pi$  periodicities differ from the conventional  $2\pi$  periodicity by at least a factor of 2, which is too large to be discounted by flux focusing or uncertainties in calculating the effective loop area. Nor can these potential artifacts account for the coexistence of multiple periodicities repeatedly observed in epitaxial  $\beta - Bi_2Pd$  ring devices.

We can also rule out the Aharonov-Bohm effect, which is on the scale of  $e^2/h$  in terms of conductance [\[27,28\]](#page-5-0). The observed Little-Parks effect, converted to magnetoconductance oscillations, can be two to three orders of magnitude greater in amplitude (see Sec. VII of the Supplemental Material [\[25\]](#page-5-0)). Multiple flux jumps have been reported in conventional *s*wave SCs when  $T \ll T_c$  [\[29,30\]](#page-5-0). It is well understood that they do not occur in the resistive state in the vicinity of  $T_c$ where the Little-Parks effect is observed [\[30\]](#page-5-0), and therefore can be ruled out as alternative interpretations for our results (see Sec. VIII of the Supplemental Material [\[25\]](#page-5-0)).

The 30 epitaxial ring devices studied in this work allow us to summarize the statistical representativeness of the observed periodicities by counting their numbers of occurrences in the histogram presented in Fig.  $4(b)$ . Each device could offer multiple counts, matching the number of periodicities observed therein. While the conventional  $2\pi$  periodicity is still observed in most devices, there is not a single epitaxial ring that exclusively displays the  $2\pi$  periodicity. The occurrence <span id="page-5-0"></span>of the  $4\pi$ ,  $6\pi$ , and  $8\pi$  periodicities are only slightly less. On the other hand, the  $\pi$  periodicity is far less frequent than the other non- $2\pi$  periodicities, only observed in about one-tenth of the devices. Apart from the four representative devices presented in Figs. [2](#page-2-0) and [3,](#page-3-0) we include more examples for each of the non- $2\pi$  periodicities in the Supplemental Material (Figs. S7–S9) [25]. It is evident that devices exhibit different combinations of periodicities of  $\pi$ ,  $2\pi$ ,  $4\pi$ ,  $6\pi$ , and  $8\pi$ . For a particular epitaxial ring device, the predominate periodicity is  $2\pi$  and  $4\pi$ .

The superconducting Cooper pairs bear the effective charge of  $2e$ , which defines the value of  $\Phi_0$  and hence the  $2\pi$  periodicity. Applying the same argument, the non- $2\pi$  periodicities would imply quasiparticles with effective charges being a fraction of 2*e*. The  $4\pi$ ,  $6\pi$ , and  $8\pi$  periodicities would correspond to  $e^*$  being  $e, \frac{2}{3}e,$  and  $\frac{1}{2}e$ , respectively. In topological superconductors, it has been proposed that the fractional Josephson effect could give rise to  $4\pi$  periodicity [31[–34\]](#page-6-0), which is actively explored by numerous experiments [\[35–37\]](#page-6-0).  $8\pi$  periodicity has also been proposed in the presence of strong interactions [\[38–40\]](#page-6-0). The theoretical discussions of unusual periodicities are often conducted in the context of the Josephson current-phase relation. One may expect the Little-Parks effect to demonstrate the same oscillation

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period as the Josephson effect. After all, the  $T_c$  oscillation and the *Ic* oscillation would eventually reflect the same oscillation of the free energy. We have conducted a theoretical analysis that shows, based on a one-dimensional (1D)-Kitaevchain model discussed in the Supplemental Material [25], that indeed the  $4\pi$  periodicity could be projected to the Little-Parks effect when it is expected for the fractional Josephson effect.

In summary, we have discovered non- $2\pi$  periodicities of the Little-Parks effect in epitaxial rings of  $\beta - Bi_2Pd$ , a topological superconductor with triplet pairing. The conventional, exclusively  $2\pi$ -periodic Little-Parks oscillation never manifests in epitaxial  $\beta - Bi_2Pd$ , as would be expected for any other superconductors. Even for  $\beta - Bi_2Pd$ , the unconventional periodicities occur only in epitaxial and not in polycrystalline samples. Having excluded trivial causes, the experimental findings call for new mechanisms to account for the unexpected quantizations.

This work was supported by the U.S. Department of Energy, Basic Energy Science, Award No. DE-SC0009390. The electron-beam lithography was conducted at the University of Delaware Nanofabrication Facility (UDNF). We thank K. Lister for assistance in the nanofabrication processes.

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