

Electrically controllable topological magnetism in multiferroic antiferromagnetic PbVO_3 Yonglong Ga,^{1,2,4,*} Dongxing Yu,^{1,5,*} Yong Li,^{3,*} Jiawei Jiang,² Liming Wang,¹ Peng Li,¹
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(Received 25 May 2023; accepted 9 January 2024; published 5 February 2024)

We propose to realize the nonvolatile four-state antiferromagnetic (AFM) skyrmions in multiferroic oxide system with underlying asymmetry. Subsequently, through strain-mediated magnetic phase engineering, we find that AFM skyrmions can be obtained in bulk PbVO_3 . Moreover, we also explore possible existence of AFM skyrmions in the $\text{SrTiO}_3/\text{PbVO}_3$ ($\text{PbTiO}_3/\text{PbVO}_3$) heterostructures via *ab initio* calculations, where AFM skyrmions can still survive. Eventually, we realize four-state AFM skyrmions ($\mathbf{P}\uparrow, \mathbf{L}\downarrow$), ($\mathbf{P}\uparrow, \mathbf{L}\uparrow$), ($\mathbf{P}\downarrow, \mathbf{L}\downarrow$), and ($\mathbf{P}\downarrow, \mathbf{L}\uparrow$) with different chirality induced by polarization ($\mathbf{P}$) switching and polarity arising from magnetization ($\mathbf{L}$) reversal in multiferroic PbVO_3 . In this letter, we provide an avenue toward electric-field control of AFM skyrmions in multiferroic oxides and offer perspectives for designing AFM skyrmion-based spintronic devices.

DOI: [10.1103/PhysRevB.109.L060402](https://doi.org/10.1103/PhysRevB.109.L060402)

Introduction. The search for intrinsic multiferroic compounds that can realize electrically switchable topological magnetism has been an intensive topic in spintronics [1–6]. Both space-inversion asymmetry and time-reversal symmetry breaking in multiferroics can induce fourfold degenerate chiral states, which can provide a pathway toward multi-bit memory and logic devices [7–10]. More recently, chiral spin configurations, e.g., chiral domain walls [11], magnetic skyrmions [12,13], and bimerons [14,15], which are stabilized by the Dzyaloshinskii-Moriya interaction (DMI) in noncentrosymmetric magnets with spin-orbit coupling (SOC) [16–18], are of great interest as ideal information carriers for future spintronic applications [1,19–24]. Experimental reports have revealed that topologically protected spin textures can be observed in multiple magnetic systems, such as B20 [13,25,26], ferromagnet (FM)/heavy metal (HM) thin films [27–30], Heusler compounds [31,32], and multiferroics [33,34]. Among these, multiferroic materials combining ferroelectricity and magnetism provide the opportunity to obtain four states from the perspective of symmetry [8,9,35], which enable the possibility of manipulating the chirality and polarity of topological magnetic states. Previously, vibrant research has shown that electrically switchable four FM skyrmions can be realized in multiferroic thin films [36,37]. Recently, many efforts have demonstrated that chiral domain walls and even skyrmions can be realized in FM multiferroic materials or

FM-based multiferroic heterostructures [34,38–43]. In contrast, FM chiral textures can be tuned by external magnetic field, and antiferromagnetic (AFM) chiral spin textures are insensitive to magnetic field due to intrinsic lack of net magnetization. Realizing the effective manipulation and detection of spins stored in AFM materials is difficult based on common magnetic detectors [44,45]. Otherwise, electric-field control of AFM skyrmions is rarely reported. Excitingly, experimental progress has revealed that spins in AFM thin films can be manipulated by means of alternative internal field [46–48]. Additionally, it has been shown that AFM textures can be realized in multiferroic materials [33,49–51], and transformation between skyrmion and bimeron has recently been reported by controlling temperature or magnetic field [14,52]. Inspired by the experiments on strain-engineering magnetic parameters and magnetic orderings [23,53–56], we propose to realize colorful magnetic states via strain and electric-field control of chirality and polarity of tunable AFM textures in multiferroic materials.

In this letter, we propose the concept of switchable DMI and AFM skyrmions in type-I multiferroic oxide. Using first-principles calculations, we first present a theoretical study of magnetic parameters of PbVO_3 under continuous strain. The results of our simulations of an effective spin model with exchange parameters from *ab initio* calculations in PbVO_3 suggest that this material can host AFM skyrmions under different strain conditions [57,58]. Specifically, in contrast with vortex-antivortex pairs with relatively weaker in-plane magnetic anisotropy (IMA), the enhancement of compressive strain tends to form bimerons, while skyrmions can be stabilized under larger tensile strain. At last, using atomistic

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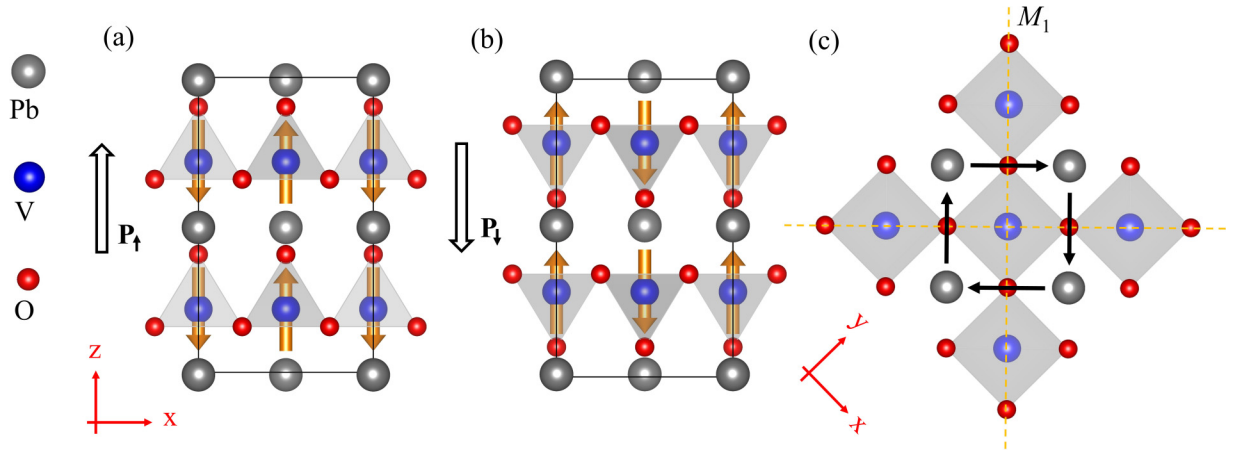


FIG. 1. (a) and (b) Ferroelectric $P4mm$ phase of $PbVO_3$ with opposite polarizations, in which orange arrows are atomic magnetic moment and spin orientation. (c) Dyzaloshinskii-Moriya interaction (DMI) vectors (black arrows) between nearest-neighbor (NN) V atoms and M_1 indicate the mirror operations (orange dotted lines).

spin dynamics (ASD) simulations, four-state AFM skyrmions states ($\mathbf{P}\uparrow, \mathbf{L}\downarrow$), ($\mathbf{P}\uparrow, \mathbf{L}\uparrow$), ($\mathbf{P}\downarrow, \mathbf{L}\downarrow$), and ($\mathbf{P}\downarrow, \mathbf{L}\uparrow$) with different chirality and polarity are realized in multiferroic $PbVO_3$, where $\mathbf{P}$ and $\mathbf{L}$ represent the electric polarization and staggered magnetization $\mathbf{L} = (\mathbf{S}_i - \mathbf{S}_j)/2$ of FM sublattice pairs of AFM skyrmions ($\mathbf{S}_i$ and $\mathbf{S}_j$ are the nearest-neighbor (NN) spin pairs in skyrmion core [59]), respectively.

Concept. The energy dispersion $E_\sigma(\mathbf{k})$ of a given spin state is closely related to the symmetry of the system (σ and $\mathbf{k}$ indicate the spin up or down and wave vector). For a nonmagnetic paraelectric phase, it follows $E_\uparrow(\mathbf{k}) = E_\downarrow(-\mathbf{k})$ or $E_\downarrow(\mathbf{k}) = E_\uparrow(-\mathbf{k})$ arising from time-reversal symmetry (T) and $E_\uparrow(\mathbf{k}) = E_\uparrow(-\mathbf{k})$ or $E_\downarrow(\mathbf{k}) = E_\downarrow(-\mathbf{k})$ arising from inversion symmetry (I). Here, I is broken in a ferroelectric nonmagnetic system, SOC effect will induce so-called spin splitting at opposite wave vector $\mathbf{k}$ and $-\mathbf{k}$ points [$E_\uparrow(\mathbf{k}) \neq E_\uparrow(-\mathbf{k})$; $E_\downarrow(\mathbf{k}) \neq E_\downarrow(-\mathbf{k})$]. Instead, in a paraelectric FM system, the exchange field will lift degeneracy of energy dispersion [$E_\uparrow(\mathbf{k}) \neq E_\downarrow(-\mathbf{k})$ or $E_\downarrow(\mathbf{k}) \neq E_\uparrow(-\mathbf{k})$] due to the absence of T . The full breaking of I and T provides a sufficient condition to induce colorful spin textures. Strikingly, multiferroics simultaneously coexisting with ferroelectric and magnetic order can result in both I and T breaking, and thereby, four nondegenerate spin states will be induced. Electric-field control of ferroelectric polarization further can induce the full reversal of spin states [60–62]. The DMI effect is considered in multiferroics, where clockwise (CW) and anti-CW (ACW) chirality spin textures can be realized at opposite polarizations under certain conditions, respectively [36,37,63]. We put forward the concept in an AFM system, in which we have introduced four switchable AFM skyrmions ($\mathbf{P}\uparrow, \mathbf{L}\downarrow$), ($\mathbf{P}\uparrow, \mathbf{L}\uparrow$), ($\mathbf{P}\downarrow, \mathbf{L}\downarrow$), and ($\mathbf{P}\downarrow, \mathbf{L}\uparrow$), as is shown in Fig. S1 in the Supplemental Material [64]. More specifically, we focus on AFM multiferroic $PbVO_3$ that can realize AFM skyrmions, discussed in detail below.

Results and discussion. Like perovskite ferroelectrics, e.g., $BaTiO_3$ and $PbTiO_3$, bulk $PbVO_3$ displays the polar crystal structure with the $P4mm$ space group, which has been synthesized in experiments [58,65]. The top and side views of $PbVO_3$ crystal structure are presented in Figs. 1(a)–1(c), in which the orange arrows represent the magnetic orderings of

the bulk phase. In our calculations, lattice constants are fixed to experimental values $a = b = 3.800 \text{ \AA}$ and $c = 4.670 \text{ \AA}$. The ground states of $PbVO_3$ are calculated by considering four types of magnetic orderings (FM and A-, C-, and G-type AFM), as shown in Figs. S2(b)–S2(e) in the Supplemental Material [64]. The calculations show that the C-type AFM (Fig. S2(a) in the Supplemental Material [64]) is the ground state, which is consistent with experiment [65]. Furthermore, to explore the magnetic properties of studied systems, we adopt the following spin Hamiltonian:

$$H = - \sum_{\langle i,j \rangle} \mathbf{D}_{ij} \cdot (\mathbf{S}_i \times \mathbf{S}_j) - J_1 \sum_{\langle i,j \rangle} (\mathbf{S}_i \cdot \mathbf{S}_j) - J_2 \sum_{\langle i,j \rangle} (\mathbf{S}_i \cdot \mathbf{S}_j) - J_3 \sum_{\langle i,j \rangle} (\mathbf{S}_i \cdot \mathbf{S}_j) - K \sum_i (S_i^z)^2,$$

where J_1 , J_2 , and J_3 are the intralayer NN, next-NN (NNN), and interlayer exchange coupling constants, respectively. Here, K and $\mathbf{D}_{ij}$ represent the magnetic anisotropy and DMI, respectively. ASD is used to explore the final chiral states by solving the Landau-Lifshitz-Gilbert equation, and magnetic parameters J , K , and D per magnetic atom are obtained by using DFT calculations. The computational details are given in the Supplemental Material [64].

First, we discuss the significant parameter D arising from the I breaking of the studied system. Bulk $PbVO_3$ has mirror operations M_1 passing through the NN V elements and vertical to the xy plane. According to the Moriya symmetry rules, there will be a DMI vector perpendicular to the NN magnetic atoms [see Fig. 1(c)] [17]. Additionally, one can see that the dominant energy contribution ΔE_{SOC} for the isotropic DMI vector stems from scattering of the heavy Pb element with strong SOC, as displayed in Fig. 2(b), like FM/HM interfaces [30,66,67], in which ΔE_{SOC} is mainly contributed by heavy $5d$ metal elements of the interfacial location. This is consistent with the Fert-Lévy mechanism of DMI [67,68]. In addition, Figs. 2(a) and S3 in the Supplemental Material [64] display the calculated spin-spiral energy $E(q)$ and DMI energy $\Delta E_{DMI}(q)$ as a function of spin-spiral length q in the interval of q from $-\frac{\sqrt{2}}{2}(\frac{2\pi}{a})$ to $+\frac{\sqrt{2}}{2}(\frac{2\pi}{a})$ along the high-symmetry

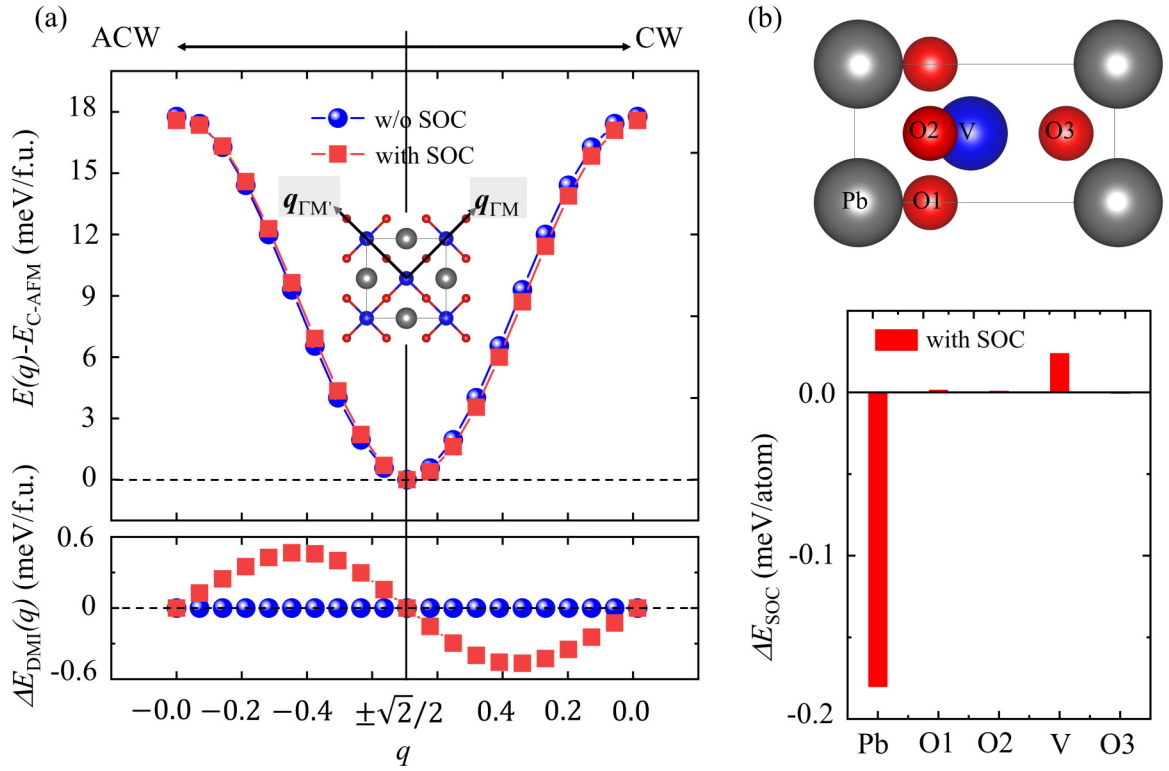


FIG. 2. (a) Spin spiral energy $E(q)$ (upper panel) and Dzyaloshinskii-Moriya interaction (DMI) energy $\Delta E_{\text{DMI}}(q)$ (lower panel) as functions of spin spiral length q for PbVO_3 , in which E_{AFM} represents the energy of the antiferromagnetic (AFM) state at $q = \pm \frac{\sqrt{2}}{2}$. Red and blue points are calculated with and without (w/o) spin-orbit coupling (SOC), respectively. (b) Atom-resolved SOC energy ΔE_{SOC} at $q = \pm \frac{\sqrt{2}}{20}$, where one can clearly see that the energy source of SOC is dominated by the Pb atom.

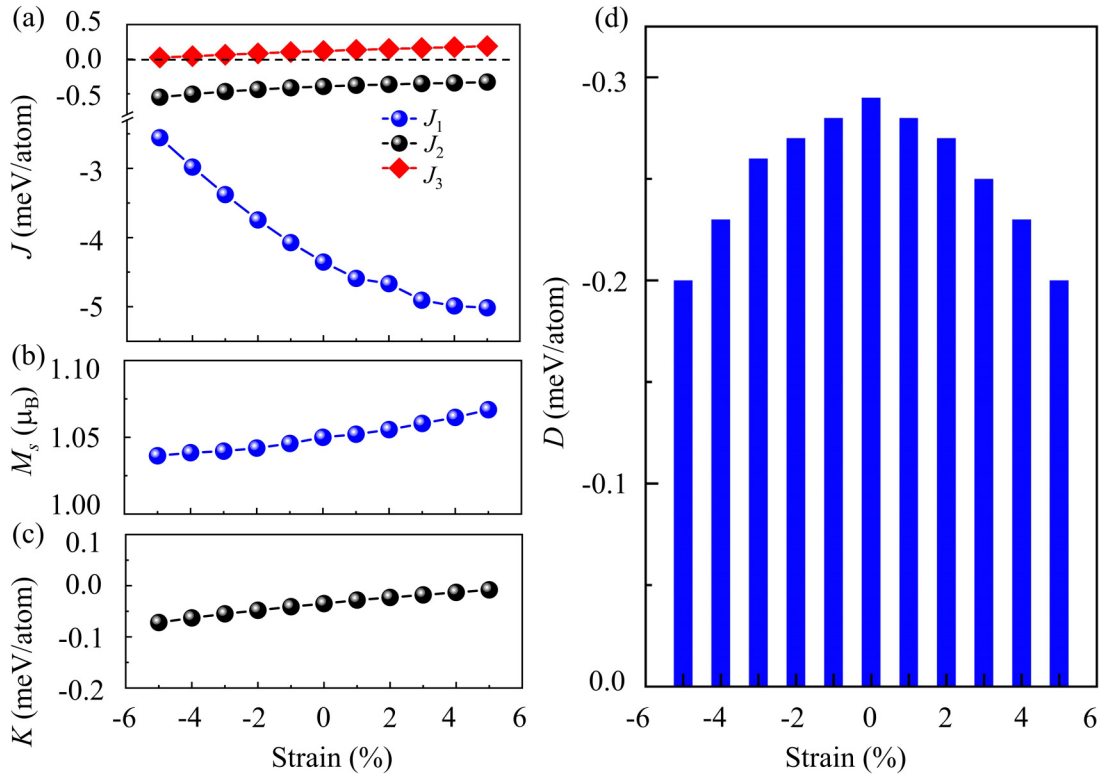


FIG. 3. The calculated (a) in-plane nearest-neighbor (NN), next-NN (NNN), and interlayer exchange coupling parameters J_1 , J_2 , and J_3 , (b) magnetic moment M_s , (c) magnetic anisotropy K and Dzyaloshinskii-Moriya interaction (DMI) parameters D per V atom as functions of strain in multiferroic PbVO_3 .

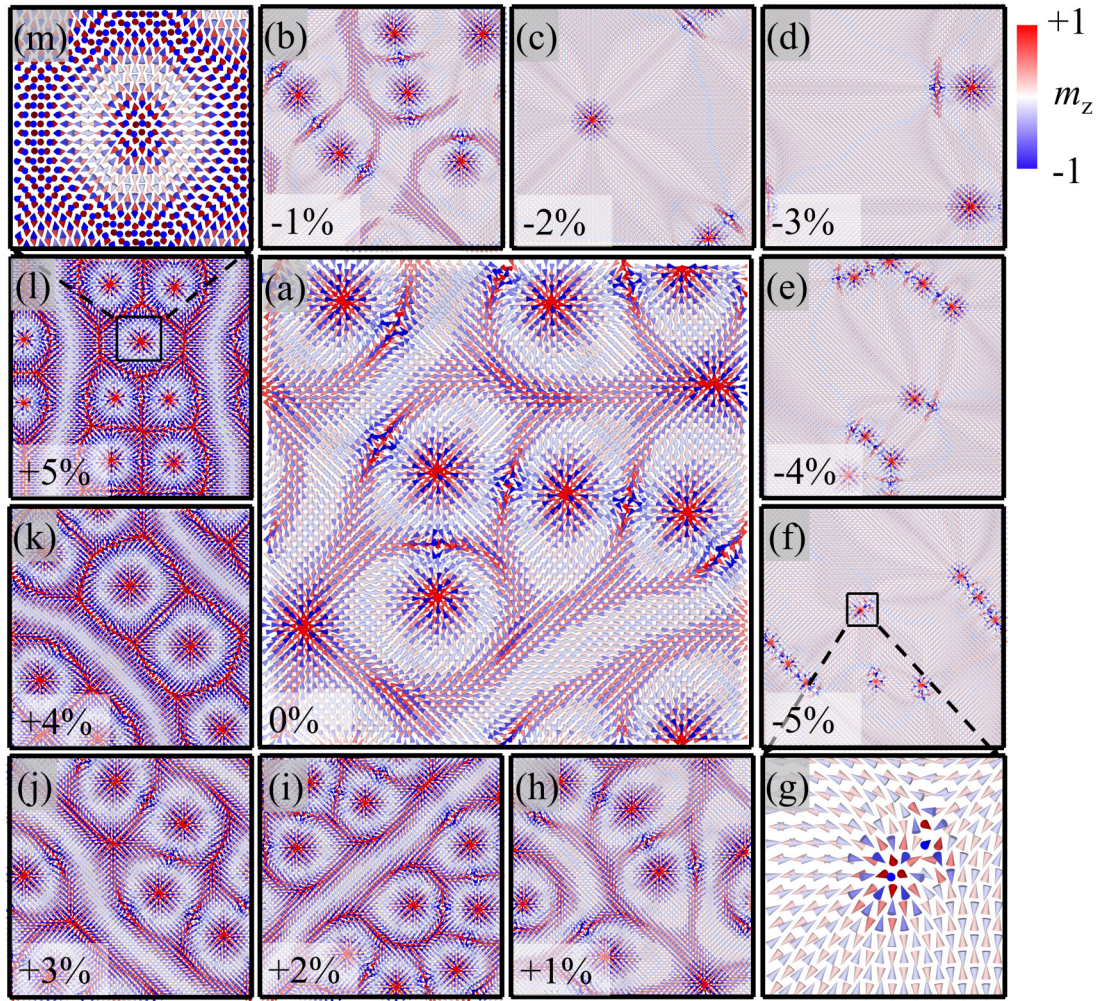


FIG. 4. (a)–(m) The evolution of spin textures with different strain varying from -5% to $+5\%$. A complete transformation process of antiferromagnetic (AFM) skyrmion, vortex-antivortex pairs, and AFM bimeron as a function of strain in multiferroic PbVO_3 .

Γ - M direction via performing the qSO method [69–71]. Not surprisingly, when SOC is neglected, calculated $E(q)$ and $\Delta E_{\text{DMI}}(q)$ with $+q$ and $-q$ are degenerated [see the blue solid circles of Fig. 2(a)]. Once SOC is considered, energy dispersion $E(q)$ shows asymmetric behavior arising from DMI [see the red solid square of Fig. 2(a)]. Then from the linear fit of $\Delta E_{\text{DMI}}(q)$ near the M point, the DMI parameters can be extracted by taking the slope of dispersion in the vicinity of the AFM ground state. It is worth noting that the real-space spin-spiral method further confirms the reliability of our results [67]; details are in the Supplemental Material [64]. Otherwise, notice that the magnetic anisotropy of bulk PbVO_3 is very small, which is the consequence of Kramers degeneracy for the odd-electron systems, as depicted in previous reports [72,73]. We also estimate the in-plane NN, NNN, and interlayer exchange constants J_1 , J_2 , and J_3 . Calculated results indicate that the magnitudes of J_1 are much larger than J_2 and J_3 , as shown in Fig. 3(a). Otherwise, J_1 and J_2 are AFM coupling, which indicates the possibility of in-plane spin frustration [74–76]. Figure S4 in the Supplemental Material [64] further displays the ratio of J_2/J_1 as a function of strain; we can see that J_2/J_1 evidently decreases as the strain rises from -5% to $+5\%$. Finally, we perform ASD simulations to explore the

possibility of topological magnetism from the above magnetic parameters. Clearly, one can see that vortex-antivortex pairs will emerge [Fig. 4(a)] due to the weak IMA. Once the IMA is increased (decreased), bimerons (skyrmions) can be realized in this multiferroic oxide, and detailed discussion follows.

Transformation of AFM skyrmions-AFM vortex and antivortex pairs-AFM bimerons. With the help of ASD simulations, AFM spin textures in real space corresponding to different strains are displayed as shown in Fig. 4. In the strain ranging from 0 to -5% , one can see that topological spin texture evolves from vortex-antivortex pairs to isolated bimerons and further transforms into a bimeron chain. For the initial state, we can understand that the loops of vortices and antivortices arise from the result of interplay between exchange coupling and DMI within weak IMA, which is consistent with previous results, e.g., $\text{In}_2\text{Se}_3/\text{La}_2\text{Cl}_2$ ($K = -0.06$ meV) and Janus $\text{MnBi}_2\text{Se}_2\text{Te}_2$ ($K = 0.006$ meV) [77,78]. Next, we find that IMA can effectively improve with the compressive strain varying from 0 to -5% and the ratio of D/J_1 remains roughly constant (see Fig. S16 in the Supplemental Material [64]), where the chiral spin texture can evolve from vortex-antivortex pairs to bimerons and further transform into a bimeron chain. The above results are like $\text{In}_2\text{Se}_3/\text{La}_2\text{Cl}_2$,

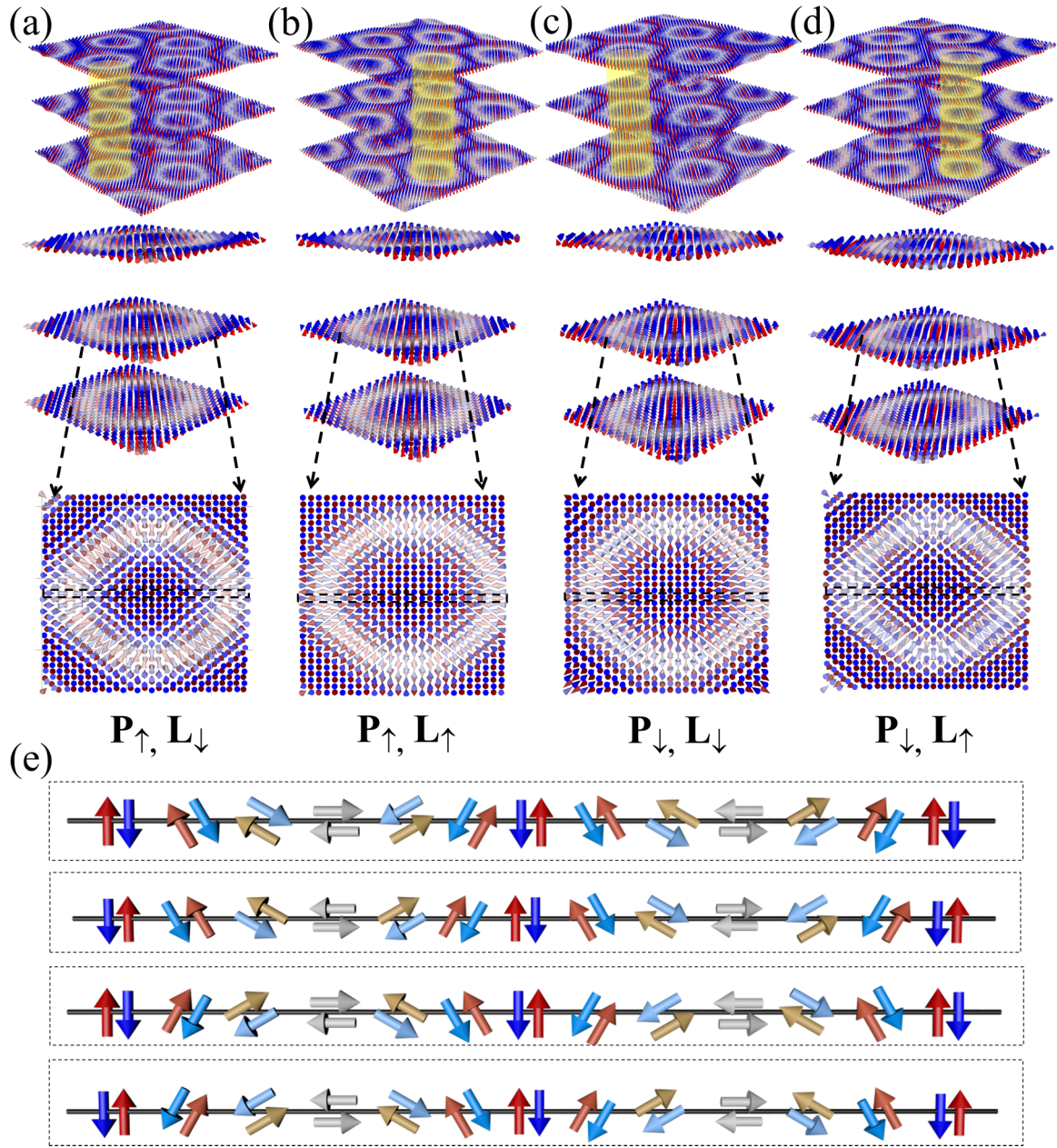


FIG. 5. (a)–(d) The realization of four-state antiferromagnetic (AFM) skyrmions ($\mathbf{P}_\uparrow, \mathbf{L}_\downarrow$), ($\mathbf{P}_\uparrow, \mathbf{L}_\uparrow$), ($\mathbf{P}_\downarrow, \mathbf{L}_\downarrow$), and ($\mathbf{P}_\downarrow, \mathbf{L}_\uparrow$) with different chirality and polarity. Here, $\mathbf{P}$ and $\mathbf{L}$ represent the electric polarization and staggered magnetization $\mathbf{L} = (\mathbf{S}_i - \mathbf{S}_j)/2$ of ferromagnetic sublattice pairs of AFM skyrmion ($\mathbf{S}_i$ and $\mathbf{S}_j$ are the nearest-neighboring spins), respectively. (e) Cycloidal spin spirals with AFM short-range orders corresponding to above four-state skyrmions propagate with wave vector $\mathbf{q}$ along the x direction.

where the increasing easy-plane anisotropy will result in the transformation between vortex-antivortex pairs and bimerons. Meanwhile, we can find the existence of isolated merons with the increase of IMA [Fig. 4(c)]. Such spin textures with a half-quantized skyrmion number $Q = \frac{1}{2}$ have also been reported in chiral magnets with easy-plane anisotropy [79,80]. Additionally, we calculate the topological distribution of PbVO_3 in strain varying from 0 to -5% . The Q of meron and antimeron are all $-\frac{1}{2}$, and the Q of an isolate bimeron composed of them is -1 , as shown in Fig. S6 in the Supplemental Material [64].

Meanwhile, we find that the formation of Néel skyrmions can appear under strain varying from 0 to $+5\%$. Figures 4(h)–

4(l) represent the skyrmion textures gradually emerging when the IMA is decreased to a relatively lower value [see Fig. 3(c)]. Meanwhile, in the zoomed AFM skyrmion, as shown in Fig. 4(m), two FM sublattices with opposite topological charges Q can be observed. This will lead to the AFM skyrmion moving parallel to the applied current direction without showing the skyrmion Hall effect [81–83]. As shown in Fig. S6 in the Supplemental Material [64], one can see that the skyrmion numbers under $+5\%$ tensile strain are equal to -5 , which is consistent with the results from calculation of the topological charge. In addition, the influence of temperature effects on the magnetic structure is further considered, and the details are described in the Supplemental Material [64].

More specifically, we summarize the diagrams of magnetic textures of one and three layers as a function of strain in Figs. 4 and S5 in the Supplemental Material [64], respectively. Clearly, a complete evolution of skyrmion to vortex and antivortex pairs to bimeron spin textures is shown. In contrast, authors of previous works have reported on transition of topological magnetism by controlling temperature or magnetic field [14,84]. However, an ideal transition between an AFM skyrmion and an AFM bimeron has not been reported. Our results present an interesting transition between an AFM skyrmion and an AFM bimeron, which is helpful for us to design AFM-skyrmion-based memory devices.

In addition, it has been unveiled that strain-dependent magnetic textures can be obtained by an epitaxial substrate in ultrathin oxides [38,56,85,86]. To demonstrate strain-engineered AFM skyrmions in similar heterostructures, we construct ultrathin $\text{PbVO}_3/\text{BaTiO}_3$ and $\text{PbVO}_3/\text{SrTiO}_3$ heterostructures (Fig. S21 in the Supplemental Material [64]). We find that AFM skyrmions can still be realized in ultrathin heterostructures through using ASD simulations, as shown in Fig. S22 in the Supplemental Material [64]. These results sufficiently prove the existence of AFM skyrmions in PbVO_3 . Additionally, the multiferroic structure, which has opposite DMI chirality, provides the possibility of manipulating the chirality of topological magnetic states by electric field. As shown in Fig. S12 in the Supplemental Material [64], we have investigated the ferroelectric switching pathway by using the climbing-image nudged elastic band (CI-NEB) method [87], where the ferroelectric phase corresponding to polarization down $\mathbf{P}\downarrow$ first converts into a transition state and moves further from the transition state back to the ferroelectric phase with opposite polarization up $\mathbf{P}\uparrow$. With the reversal of polarization in multiferroic PbVO_3 by an out-of-plane electric field, the chirality of DMI can be switched. Meanwhile, we perform ASD for ferroelectric phases ($\mathbf{P}\uparrow$ and $\mathbf{P}\downarrow$) and calculate the

numerical energy of these states; one can clearly see that the total energy of AFM skyrmions for ferroelectric phases are basically the same (see Fig. S13 in the Supplemental Material [64]). Like previous reports on multiferroic CrN and $\text{Co}(\text{MoS}_2)_2$ [36,37,88], we relax from a random state [or FM and C- and G-type AFM, and spin-spiral states (see Figs. S14 and S15 in the Supplemental Material [64])] to obtain four-state AFM skyrmions ($\mathbf{P}\uparrow, \mathbf{L}\downarrow$), ($\mathbf{P}\uparrow, \mathbf{L}\uparrow$), ($\mathbf{P}\downarrow, \mathbf{L}\downarrow$), and ($\mathbf{P}\downarrow, \mathbf{L}\uparrow$) with different chirality and polarity via applying 5% tensile strain in bulk PbVO_3 (see Fig. 5). Our findings provide a platform to investigate electric-field control chirality and polarity of AFM skyrmions, which is useful for potential application of future devices.

Conclusions. In conclusion, we propose that the chirality and polarity of AFM skyrmions can be controlled in multiferroic oxides. Using first-principles calculations and ASD simulations, we unveil the process of phase transformation of AFM bimerons, AFM vortex-antivortex pairs, and AFM skyrmions in PbVO_3 . Moreover, we demonstrate that AFM skyrmions can be realized in multiferroic PbVO_3 and even its ultrathin heterostructures based on strain-mediated phase engineering. Finally, we show that four-state AFM skyrmions, i.e., ($\mathbf{P}\uparrow, \mathbf{L}\downarrow$), ($\mathbf{P}\uparrow, \mathbf{L}\uparrow$), ($\mathbf{P}\downarrow, \mathbf{L}\downarrow$), and ($\mathbf{P}\downarrow, \mathbf{L}\uparrow$) with different chirality and polarity, can be realized in PbVO_3 via external electric field. Our results provide a highly promising approach to control the AFM topological spin textures in multiferroic compounds.

Acknowledgments. This letter was supported by the “Pioneer” and “Leading Goose” R&D Program of Zhejiang Province (Grant No. 2022C01053), the National Key Research and Development Program of China (Grants No. 2022YFA1405100 and No. 2022YFA1403601), the National Natural Science Foundation of China (Grants No. 12174405 and No. 12204497), Ningbo Key Scientific and Technological Project (Grant No. 2021000215).

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