Near zero-field microwave-free magnetometry with ensembles of nitrogen-vacancy centers in diamond

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We study cross-relaxation features near zero magnetic field with ensembles of nitrogen-vacancy (NV) centers in diamond and examine their properties in samples with a range of 0.9–16.0 ppm of NV concentrations. The observed NV-NV cross-relaxation features between differently oriented NV centers in high $(\gtrsim 0.9 \text{ ppm})$ -NV-density samples hold promise for a variety of magnetometry applications where microwave fields (or any bias field) disturb the system under study. We theoretically determine the values of the bias magnetic fields corresponding to cross relaxations between different axes and experimentally validate them. The behavior of zero-field cross-relaxation features as a function of temperature is also investigated.

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I. INTRODUCTION

Nitrogen-vacancy (NV) centers in diamond are used in applications such as magnetic field [\[1\]](#page-6-0), electric field [\[2\]](#page-6-0), and temperature sensors [\[3\]](#page-6-0) over a wide range of environmental conditions, e.g., pressure and temperature [\[4,5\]](#page-6-0). In most applications as magnetometers, the magnetic field is determined by using optically detected magnetic resonance (ODMR) [\[6\]](#page-6-0). In this measurement protocol, the diamond is illuminated with green laser light and a microwave field of tunable frequency is applied to measure the energy separation between the magnetically sensitive spin-1 ground-state levels to obtain the magnetic field value. For measuring weak magnetic fields where Zeeman shifts of sublevels may be nonlinear in field [\[1\]](#page-6-0), this method usually requires a bias field to lift the degeneracy between the $m_s = \pm 1$ sublevels. However, the use of microwave and external bias magnetic fields may disrupt the system of interest in some applications. To overcome this limitation, different strategies have emerged. Recently, microwave-free magnetometry [\[7–9\]](#page-6-0), as well as vector magnetometry [\[10\]](#page-6-0) based on the level anticrossing in the triplet ground state at 102.4 mT, have been demonstrated. Zero-field magnetometry was realized for both ensemble and single NV centers by using circularly polarized

microwave fields to individually address transitions to the $m_s = +1$ or $m_s = -1$ states [\[11,12\]](#page-6-0). Still, due to the high external magnetic field or the application of microwave fields, these techniques may be problematic for studying systems where both external magnetic field and the microwaves might disturb the system. Examples of such systems are high- T_c superconductors $(T_c \text{ stands for the superconducting transition})$ temperature) [\[13\]](#page-6-0), zero- to ultralow-field nuclear magnetic resonance (ZULF NMR) [\[14\]](#page-6-0), biological samples, and various magnetic materials [\[15,16\]](#page-6-0).

Recently, ODMR experiments with an additional radiofrequency field were used to study features occurring in fluorescence measurements at zero and low fields [\[17–19\]](#page-6-0). In addition, microwave-free magnetometry at low field was proposed. The technique probes the position of the cross-relaxation resonances [\[20–22\]](#page-6-0) and allows for vector magnetometry [\[23,](#page-6-0)[24\]](#page-7-0). This new magnetometry technique therefore overcomes the limitations of microwave-based protocols.

Motivated by the desire to improve the sensitivity of near zero-field magnetometry, in this work, we perform a detailed study of the cross-relaxation features with respect to the parameters that may affect the contrast and width of the feature. These include the orientation of the magnetic field with respect to the crystal axes, NV density (Sec. [IV A\)](#page-2-0), and the sample temperature (Sec. [IV B\)](#page-2-0). We found that a boost in sensitivity can be achieved by applying a transverse bias

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field; therefore, we study the cross relaxations under transverse fields up to ≈ 2.0 mT as a function of the azimuthal angle (Sec. [IV C\)](#page-4-0). We numerically predict and experimentally verify the observed cross-relaxation patterns. Conclusions and outlook are given in Sec. [IV D.](#page-5-0)

II. NV-CENTER GROUND STATE

The fluorescence rate is reduced due to the T_1 relaxation between bright and dark states. The coupling mediated by dipolar coupling leads to faster T_1 relaxation and such coupling is enhanced when NV states of different axes are degenerate [\[21\]](#page-6-0). In the following, we are studying the Hamiltonian to determine at what external fields this might be observable and compare it to the experiment. The NV ground state in the presence of an external magnetic field can be described by the Hamiltonian

$$
H = D\left(S_z^2 - \frac{1}{3}\vec{S}^2\right) + E\left(S_x^2 - S_y^2\right) + g_s \mu_B \vec{B} \cdot \vec{S},\qquad(1)
$$

where $D = 2.87$ GHz is the axial and *E* is the transverse zero-field-splitting (ZFS) parameters, \vec{B} is the magnetic field, and \vec{S} is the electronic spin with components S_x , S_y , and S_z . The electron *g* factor is $g_s = 2.003$ [\[25\]](#page-7-0) and μ_B is the Bohr magneton. The Larmor frequency of the NV center is $\Omega =$ magneton. The Larmor frequency of the NV center is $\Omega = \frac{g_2 \mu_B}{\hbar} B$. Here, the *z* axis is chosen along the NV axis. The spin operators S_x , S_y , S_z can be written as

 Δ

$$
\begin{pmatrix} 0 & \frac{1}{\sqrt{2}} & 0 \\ \frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \\ 0 & \frac{1}{\sqrt{2}} & 0 \end{pmatrix}, \begin{pmatrix} 0 & \frac{-i}{\sqrt{2}} & 0 \\ \frac{i}{\sqrt{2}} & 0 & \frac{-i}{\sqrt{2}} \\ 0 & \frac{1}{\sqrt{2}} & 0 \end{pmatrix}, \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}.
$$
 (2)

A unit vector with an angle of β to the *z* axis can be written as

$$
\vec{n} = (\cos \phi \sin \beta, \sin \beta \sin \phi, \cos \beta), \tag{3}
$$

where ϕ is the azimuthal angle. Then Eq. (1) can be written as

$$
H = \begin{pmatrix} D + \Omega \cos \beta & \frac{e^{-i\phi} \Omega \sin \beta}{\sqrt{2}} & E \\ \frac{e^{i\phi} \Omega \sin \beta}{\sqrt{2}} & 0 & \frac{e^{-i\phi} \Omega \sin \beta}{\sqrt{2}} \\ E & \frac{e^{i\phi} \Omega \sin \beta}{\sqrt{2}} & D - \Omega \cos \beta \end{pmatrix}.
$$
 (4)

A schematic of the energy levels obtained by diagonalization of the Hamiltonian (4) is shown in Fig. 1. The ground state $|g\rangle$ is split by the dipole-dipole interaction described by the parameter *D*, lifting the degeneracy between the $m_s = \pm 1$ and m_s = 0 sublevels. Application of a magnetic field along the NV axis further lifts the $m_s = \pm 1$ degeneracy level by $2\gamma_e B_{\text{NV}}$ above the $m_s = -1$ when B_{NV} is applied.

Consider the following four possible crystallographic axes of diamond lattice for NV centers: [111], [1 $\overline{11}$], [$\overline{11}$], and $[\overline{111}]$. In the diamond samples used in this work, the NV centers are uniformly distributed over the possible orientations. Since NVs of all orientations have equal ground-state splitting, the transition energies of all orientations cross at $\vec{B} = 0$. When the splittings of orientationally inequivalent NV centers match, a cross-relaxation feature occurs and we observe a decrease in fluorescence. A recently developed model [\[26\]](#page-7-0) suggests that local energy relaxation occurs when a randomly distributed portion of NV centers rapidly incoherently

FIG. 1. (a) Energy-level diagram of the NV center in the presence of magnetic field. (b) Energy separation (transition energy) between the ground $m_s = 0$ and ± 1 states for all four crystallographic axes as a function of B_z when a 2 mT transverse field is applied along \hat{x} . Blue stars are the positions where the crossings happen between transition energies for different NV orientations. Fifteen transition-energy crossings between different orientations are expected in total.

depolarizes. Through dipolar interactions, these spins can depolarize the entire ensemble at zero field. It was also observed that there is a significant contribution of local electric fields and the interaction between identically and differently oriented NVs on depolarization at zero field for high-density samples [\[27\]](#page-7-0).

Let us concentrate on the ground $m_s = \pm 1$ states. Only $m_s =$ ± 1 states are taken into account since these are the states for which the transition energies to $m_s = 0$ intersect/cross at zero field. The ground-state splitting for transition energies of different axes differs when a transverse field is present. As a result, there are multiple crossings between the transition energies at various values of B_z . The magnitude of the transverse field and the azimuth angle ϕ affect the positions of crossings. When the field is scanned along [111] in the presence of 2 mT of transverse field along \hat{x} (this direction is defined so that one of the carbons associated with the NV center is in the *x*-*z* plane), the transition energies behave as shown in Fig. $1(b)$ for ground ± 1 states for all possible NV axes. There are 15 transition-energy crossings; however, some of them occur exactly at the same B_z such that only five cross-relaxation features are expected. Note that for the calculations shown in Fig. 1 (for 2 mT of transverse field), we neglected the

FIG. 2. Schematic diagram of experimental setup.

parameter E , while, in general, up to six crossing positions can be observed when the [111] axis of the diamond is aligned with the *z* axis of the setup.

III. EXPERIMENTAL SETUP

To study the cross-relaxation features, we use a home-built wide-field fluorescence microscope (Fig. 2), where a laser (Toptica iBeam smart) with the output wavelength of 515 nm is employed. The diamond is mounted on a rotational mount and the laser beam is reflected via a dichroic mirror. The beam is then focused into the diamond using a microscope objective (Olympus PLN Plan Achromat 10x Microscope Objective, 0.25 NA, 10.6 mm WD). The NV-center fluorescence is collected using the same objective, passing the dichroic mirror and a long-pass filter to remove the green reflection of the laser light from the diamond. The fluorescence is detected with a photodiode (APD120A/M - Si Avalanche Photodetector, 400–1000 nm). Electromagnetic coils are used to apply a magnetic field in three different directions.

IV. RESULTS

A. Characterization of zero-field cross-relaxation feature

We explored the properties of the cross-relaxation feature at zero field in different diamond samples with varying NV density. During these experiments, neither microwave nor radio-frequency fields were applied. We only observed the cross-relaxation feature at the zero field in diamonds with NV density $\gtrsim 0.9$ ppm. Moreover, the linewidth and contrast

FIG. 3. Zero fields features recorded on two different diamond samples while the magnetic field is along \hat{z} . For sample S2 (16 ppm NV density), the full width at half maximum (FWHM) and the contrast are 1.42(3) mT and 3.95(4)%, respectively. For sample 1970608-29 (3.8 ppm NV density), these are 0.78(4) mT and 1.79(5)%.

of the zero-field cross-relaxation feature depends on the NVcenter density. In the examples in Fig. 3, both linewidth and contrast increase with NV-center density. The contrast of the feature also depends on the laser intensity. Table I summarizes the characteristics of the observed zero-field cross-relaxation feature in different samples. Characterization of the zero-field cross-relaxation feature was performed with a laser spot diameter of 50 µm. For the bulk NVs, the optimum contrast is observed at different values of laser intensity for each sample. Higher laser intensity is used in the case of thin-film NV samples because the signal-to-noise ratio for such samples is low at reduced power and the contrast increases with laser intensity. The NV density of the sumi_300 kev sample is estimated based on a comparative NV fluorescence measurement with respect to the 2170612-13 sample. The linewidth and contrast are slightly position dependent because of the variation of NV density over the sample. The lowest (i.e., most favorable) ratio of linewidth and contrast is observed for the 3.7 ppm-NV-concentration bulk sample ("George").

B. Temperature dependence of zero-field cross-relaxation feature

We observed that the sample temperature affects the contrast of the zero-field cross-relaxation feature. The

TABLE I. Characterization of the zero-field cross-relaxation feature in different diamond samples where B_z is along the cut surface. Here, γ and *C* are the linewidth and contrast, respectively. The samples with * in their names are thin-layer samples.

Diamond name	Cut	(N) Density (ppm)	NV density (ppm)	Laser intensity (mW)	ν (mT)	Optimum $C(\%)$	γ (mT)/C (%)
Super diamond	111	\sim 3	0.9		0.12	0.04	3.00
George	100	\sim 13	3.7	5.93	0.20	0.91	0.21
1970608-29	111		3.8	2.98	0.78	2.85	0.27
S ₂	111	~< 100	16.0	20.2	1.42	4.01	0.35
sumi 300 keV^*	110	\sim 150	14.0	37.00	1.42	1.21	1.17
2170612-13*	100	\sim 14	4.5	37.00	0.17	0.29	0.59

FIG. 4. Temperature dependence of the zero-field cross-relaxation feature. (a) Zero-field cross-relaxation feature at selected temperatures for sample S2. The zero-field cross-relaxation feature becomes observable at \approx 5 K. (b), (c) Linewidth and contrast dependence on temperature for sample S2 and 1970608-29. The features are Lorentzian fitted with 95% confidence interval for each temperature to extract the linewidth and contrast.

temperature dependence was investigated on two samples cut along (111), with the results shown in Fig. 4.

There are several effects that are of note. The zero-field signal is apparent at 5 K, which represents the lowest temperature achievable within our setup. However, this feature exhibits a significantly diminished contrast below ≈ 20 K. The contrast increases with temperature and then declines above ≈ 250 K, retaining a sizable value at room temperature [Fig. 4(b)]. The highest contrast is observed in the range of 180–200 K. The linewidth is roughly constant over the entire temperature range [Fig. 4(c)]. The high-temperature behavior is likely due to the increase of the longitudinal relaxation rate with temperature.

In order to understand the observed temperature dependence of the contrast of the zero-field cross-relaxation feature at cryogenic temperatures, we need to identify the factors affecting the contrast. To do so, we first study the energylevel structure of coupled NV centers; see Fig. 5(a). When hyperfine, strain, and electric-field-induced splittings of the spin states are neglected, the energy levels of a many-NV system fall into branches with a ladderlike structure, where the spacing of the steps is equal to the zero-field splitting (ZFS) parameter *D*. It is important to note the degeneracy of the branches. The lowest-lying $|0, 0, 0\rangle$ state is nondegenerate, even for NV centers of different orientations. The higherlying states are, however, degenerate and include mixed |0

FIG. 5. (a) Energy levels of three coupled NV centers and (b) temperature dependence of the lifetime of the ${}^{1}E$ NV shelving state [\[28,29\]](#page-7-0).

and $|\pm 1\rangle$ states; see Fig. $5(a)$ illustrating this for three NV centers. When all NV centers are completely polarized to $|0\rangle$, the many-spin system populates the nondegenerate (lowest-energy) state. Spin-relaxation effects may connect the lower-lying state with higher-lying states; however, such processes are suppressed by the large value of the ZFS compared to the typical strength of dipole-dipole interactions.

Drop of the NV polarization, i.e., population of the higherlying energy states, enables spin flip flop among the NV centers. However, the averaged probability of finding the NV centers in $|0\rangle$ does not change even in this case. Dipolar spin relaxation alone cannot account for the zero-field crossrelaxation feature.

To understand depolarization in a dense NV ensemble, we need to utilize the concept of spin fluctuators, as explained in Ref. [\[26\]](#page-7-0). Spin fluctuators are NV centers with a short-lived ground-state electron spin, through which a polarized, dipolar coupled NV bath can dissipate its energy faster than through the conventional spin-lattice relaxation. At nonzero magnetic field, only NV centers and fluctuators along the same axes couple. At zero magnetic field, however, all NV centers couple to each other, which increases the effective density of the NV centers and the spin-fluctuator bath. In turn, this gives rise to the zero-field cross-relaxation feature. The contrast of the zero-field cross-relaxation feature thus depends on the density of the NV centers, as well as the ratio of the short-lived spin fluctuators and the "normal" long-lived NV centers. Since the former is not temperature but sample dependent, the latter is a possible temperature-dependent factor.

As discussed in Ref. [\[26\]](#page-7-0), spin fluctuators can be close NV centers of different charge states, where electron (charge) tunneling between the centers can shorten the spin-state lifetime in the ground state of the negatively charged NV center. Therefore, the fluctuator per normal NV center ratio and, correspondingly, the contrast of the zero-field cross-relaxation feature depend on the $NV(-)/NV(0)$ ratio (see Supplemental Material [\[30\]](#page-7-0)), which is temperature, excitation power, and sample dependent. Considering the applied 515 nm excitation, which is energetic enough to ionize the NV center from the ${}^{1}E$ shelving state (see, for example, Ref. [\[31\]](#page-7-0)), we attribute the temperature dependence of the contrast to the temperature dependence of the lifetime of the ${}^{1}E$ electronic state of the NV center. The ${}^{1}E$ electronic state couples to the

FIG. 6. Simulation (upper row) and experimental measurement (lower row) of the cross-relaxation features in the presence of a transverse field of 2 mT. (a) Simulation and (b) measurement of the transition energy difference between the *ms* = +1 and −1 states for all four NV axes. Here, B_z is along [111] and the azimuthal angle of the transverse field is ϕ . (c), (d) Varying the transverse field and B_z at an angle of 5°. (e), (f) Transition energy difference between the $m_s = +1$ and -1 states when B_z is along [100] at varying angles when 16 mT of transverse field is applied.

higher-lying ${}^{1}A_1$ state through the pseudo-Jahn-Teller effect and to the even higher-lying E' state through the dynamics Jahn-Teller effect [\[28\]](#page-7-0). The first excited vibronic level can be found at 16 meV above the lowest vibronic level of the ${}^{1}E$ state, which gives rise to the characteristic temperature dependence that is depicted, for example, for the lifetime of ${}^{1}E$ in Fig. [5\(b\).](#page-3-0) Boltzmann occupation of the excited vibronic levels significantly increases beyond 20 K, which, on one hand, shortens the lifetime of the ${}^{1}E$ state [see Fig. [5\(b\)\]](#page-3-0), and on the other hand, increases the photoionization rate from the ${}^{1}E$ state towards the conduction band. We attribute the onset of the zero-field contrast at around 20 K to the increasing ionization rate due to the thermal occupation of the vibronic excited energy levels of the ${}^{1}E$ state (e.g., such an effect is discussed for silicon carbide divacancy centers in Ref. [\[32\]](#page-7-0)), whereas the shortening of the ${}^{1}E$ lifetime, i.e., intersystem crossing towards the ground state of $NV(-)$, will compete with this photoionization process at elevated temperatures. Quantitative simulation of the contrast requires additional information on the dynamics of the spin fluctuators, which is the subject of further investigations.

From the study of temperature dependence and the above discussion, we conclude that the $\text{NV}(-)/\text{NV}(0)$ ratio governs the temperature dependence of the zero-field cross-relaxation feature contrast. Sensitive dependence of this parameter on excitation power and wavelength gives pathways to engineer the contrast of the zero-field cross-relaxation feature without the need for microwave excitations.

C. NV-NV cross relaxation in the presence of a transverse field

This section describes calculations and experimentally measured additional cross-relaxation features observed when B_z is along [111] (and [100] later on) when applying 2 mT (1.6 mT for [100]) transverse field.

Figure $6(a)$ shows a density plot of the simulated contrast based on the numerically evaluated transition frequency differences as a function of B_z along [111] and the azimuthal angle of the transverse magnetic field (2 mT). Here, we assume that the cross-relaxation features have a Lorentzian line shape. The parameters of the Lorentzian function are adjusted to reflect the measured data. There are multiple crossings between the transition energies for differently oriented NVs at different values of B_z . The position of the crossings and the overlap between the transition energies depend on ϕ when the diamond is rotated around \hat{z} with a transverse field present. When B_z is along [111] [Fig. $6(a)$], for every multiple of 60◦, starting at 30◦, transitions for NVs along two of three nonaligned crystallographic axes overlap each another. These are the orientations where the crossings between the transition energies at the three values of B_z occur. Also, two out of three inequivalent transition energies successively cross each other at $B_z = 0$ for every multiple of 60°, starting from 0°. For each of these values of ϕ , crossings occur at five distinct values of B_z ; Fig. [1\(b\)](#page-1-0) shows one of those cases when $\phi = 0^\circ$.

Figure $6(b)$ shows experimentally measured crossrelaxation patterns between NVs oriented along different axes. For every multiple of $60°$, starting from $30°$, there is an overlap of three separate cross-relaxation features at −1.4 mT and $+1.4$ mT and of two separate features at $+0.7$ mT and −0.7 mT. As a result, cross-relaxation features are observed at only three values of B_z at these angles. For multiples of 60[°], starting from 0° , there is an overlap of two separate features at $B_z = 0$ so that five crossings are observed at these angles. There are always six cross-relaxation values of B_z for the rest of the angles, but these values depend on the angle ϕ . The observed cross-relaxation features when we apply a transverse field have narrower linewidth than the zero transverse-field cross-relaxation feature, which can be attributed to the effect of electric field, strain, and additional cross-relaxation chan-

FIG. 7. Dominant central cross-relaxation feature observed while applying 1.6 mT of transverse field at an azimuthal angle of ≈90°. The FWHM and the contrast for this feature are 0.20(2) mT and 1.85(10)%, respectively.

nels in the sample. We also note the different widths of the lines in the figure. This is related to the difference in the derivatives of the crossing transition energies as a function of *Bz*. Note, also, that one can estimate the direction of the magnetic field from the positions of the crossings, which is useful for vector magnetometry applications [\[24\]](#page-7-0).

When B_z is scanned for each value of the transverse field, the splitting of the cross-relaxation features linearly depends upon the transverse field, i.e., all of these cross-relaxation features are magnetically sensitive. (An exception is crossings occurring at $B_z = 0$ for certain values of the azimuthal angle.) Figures $6(c)$ and $6(d)$ shows the simulated and experimentally measured cross-relaxation features for $\phi \approx 5^{\circ}$ angle. It shows the linear dependence on the transverse magnetic field. A limitation of these extra cross-relaxation features (other than the cross-relaxation feature at zero longitudinal field) for magnetometry applications requiring operation near zero field is that application of a 0.5–1.0 mT transverse field is necessary to clearly resolve these features.

Similarly, in the case of B_z along [100] [Fig. [6\(e\)\]](#page-4-0), due to the crystal symmetry, transverse fields are equal for two groups of NVs that have pairs of transition energies crossing each other at $B_z = 0$ for every multiple of 90°, starting at 0°. Since these two pairs of transition energies intersect at $B_7 = 0$, there is just one crossing between the transition energies at $B_z = 0$. Figure 7 shows the dominant single cross-relaxation feature at one of such angles, $\approx 90^\circ$. At this angle, the contrast is larger than that of the zero-transverse-field cross-relaxation feature of the same sample ("George"). Other small features are still observed, likely because of a small misalignment with respect to the transverse field. Additionally, two out of every four transition energies successively overlap at every multiple of 45◦, resulting in crossings at three different values of *Bz*. Figure $6(e)$ shows the density plot of transition-frequency differences as a function of B_z along [100] and the azimuthal angle of the transverse magnetic field at 1.6 mT. Figure $6(f)$ shows the experimentally measured cross-relaxation features. Since the transition energies for each angle cross at $B_z = 0$,

a cross-relaxation feature is always visible at the zero field. There are five cross-relaxation positions for the remaining angles. In our setup, while rotating the diamond, there is a slight translation. Therefore, if we compare the experimentally measured data in Fig. $6(f)$ with the calculations in Fig. $6(e)$, we see a slight displacement of the features, which, however, does not obscure the overall good agreement.

The cross-relaxation features in the presence of a transverse field are measured on diamond sample "S2" for [111] and on sample "George" for [100] (see Table [I\)](#page-2-0).

The photon shot-noise limited sensitivity is approximated as $\eta \approx \sqrt{2}\Delta B/C/\sqrt{I_0}$, where $\Delta B = 1.2$ mT is the linewidth and $C = 3.0\%$ is the contrast for the zero-field crossrelaxation feature of the S2 sample. The photon-detection rate $I_0 = 2.4 \times 10^{13}$ /s. For these values, the estimated photon shot-noise limited sensitivity is around $2.7nT/\sqrt{Hz}$, while the measured sensitivity, as detailed in the Supplemental Material [\[30\]](#page-7-0), is approximately 110 nT/\sqrt{Hz} , exhibiting a relatively consistent noise floor across frequencies. This observation suggests that the performance is limited not by shot noise, but rather by other sources of noise such as laser noise, ambient magnetic noise, etc. Enhancements in sensitivity can be attained through the optimization of light power and the augmentation of light-collection efficiency [\[33,34\]](#page-7-0). This sensitivity is sufficient for applications such as studying superconducting vortices and magnetic properties of magnetic materials [\[13,15\]](#page-6-0).

D. Conclusion

We have investigated the zero-field cross-relaxation feature with respect to the NV density and the axis of sample cut. The NV density influences both the linewidth and the contrast of this feature. The temperature dependence of the zero-field cross-relaxation feature was studied. The feature is more prominent above 20 K. The contrast increases with temperature and gradually decreases from about 250 K [\(4\)](#page-3-0). In the presence of a transverse field, various cross-relaxation features are detected due to the dipolar interaction between differently oriented NVs providing depolarization channels. The number and location of cross-relaxation features are determined by the orientation of the magnetic field with respect to the crystal axes, azimuthal angle, and the strength of the transverse field. These cross-relaxation features follow a specific pattern (well reproduced by our theoretical calculations) when the azimuthal angle is changed with respect to the transverse field. These features have a narrower linewidth than the zero-field cross-relaxation feature. Moreover, higher contrast is observed at certain angles where there is only one decay channel available to depolarize.

These results will be used in scalar- and vectormagnetometry applications, forming the basis of a practical near zero-field microwave-free or even all-optical technique.

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