Possible spin Jahn-Teller material: Ordered pseudobrookite FeTi₂O₅

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We investigated spin-lattice coupling in orthorhombic pseudobrookite $FeTi₂O₅$ single crystal with highly ordered Fe²⁺/Ti⁴⁺ occupation, which consists of quasi-one-dimensional (1D) $S = 2$ chains running along the *a* axis. Both the magnetization and specific heat measurements confirm that the antiferromagnetic phase transition of FeTi₂O₅ occurs at $T_N = 42$ K. The structural distortions were also observed around T_N in the thermal expansion $\Delta L/L(T)$ data. Moreover, the magnetic field was found to strongly affect the thermal expansion both along chains and in the perpendicular direction clearly signaling a substantial magnetoelastic coupling, which was recently proposed to be the origin of a rare spin Jahn-Teller effect, when frustration is lifted via additional lattice distortions. Experimentally observed change in the thermal conductivity slope around T_N is usually associated with the orbital ordering, but density functional theory (DFT)+*U* calculations do not detect modification of the orbital structure across the transition. However, the first-principles calculation results confirm that FeTi₂O₅ is a quasi-1D magnet with a ratio of frustrating interchain to intrachain exchanges $J'/J = 0.03$ and a substantial single-ion anisotropy $(A = 4K)$ of easy-axis type making this material interesting for studying quantum criticality in transverse magnetic fields.

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I. INTRODUCTION

The Jahn-Teller (JT) effect is a spontaneous structural distortion that lifts the orbital degeneracy of the *d* electron, resulting in the orbital ordering and causing various fascinating phenomena; e.g., it can affect magnetic structure [\[1\]](#page-6-0) and lead to the orbital-selective Mott transition [\[2\]](#page-6-0) or the reduction of effective dimensionality [\[3\]](#page-6-0). In analogy to the JT effect, Yamashita and Ueda proposed the spin JT effect, when the spin degeneracy in geometrical frustration spin systems is released by the structural distortion through the spin-lattice coupling [\[4\]](#page-6-0). While this mechanism was initially proposed for ZnV_2O_4 and MgV_2O_4 , it was later also applied to other spinels $[5-7]$.

The orthorhombic pseudobrookite $CoTi₂O₅$ was recently proposed by Kirschner *et al.* as another candidate for spin JT effect [\[8\]](#page-6-0). It was suggested that the triangular geometrical frustration exists in the orthorhombic pseudobrookite CoTi_2O_5 and an unexpected long-range antiferromagnetic ordering of Co^{2+} at $T_N \sim 26$ K is due to an additional structural distortion induced by the spin-lattice coupling through the spin JT effect [\[8\]](#page-6-0). Combining the x-ray diffraction measurements on polycrystalline samples with the density functional theory calculations, Lang *et al.* demonstrated that the pseudobrookite $FeTi₂O₅$ has the same crystal and magnetic structures as $CoTi₂O₅$, so the triangular geometrical frustration also exists in FeT₁₂O₅, as shown in Fig. [1\(a\),](#page-1-0) and a structural distortion is also expected in FeTi₂O₅ [\[9\]](#page-6-0), but no direct experimental evidence was found. This is not surprising since distortions related to lowering of the crystal structure due to the spin JT effect are expected to be extremely small and are unlikely to be measured by neutron or x-ray diffraction techniques. This remains the situation in multiferroics, where electric polarization is measurable, but corresponding distortions often remain experimentally elusive. In addition, compounds with octahedrally coordinated $Fe²⁺$ could also exhibit various interesting physical properties due to the orbital ordering of Fe^{2+} . For instance, the orbital ordering of $Fe²⁺$ accompanied by a structural distortion in perovskite $KFeF₃$ opens a band gap in the electronic band structure, leading to a metal-insulator transition [\[10\]](#page-6-0). Moreover, there is an interplay between charge, spin, and lattice degrees of freedom in the famous $Fe₃O₄$, which results in the formation of trimerons and Verwey transition $[11]$. Therefore, it is interesting to study coupling between all these degrees of freedom in $FeTi₂O₅$ as well.

There are two main structural units in the pseudobrookite FeTi₂O₅: Fe²⁺O₆ and Ti⁴⁺O₆ octahedrons. Like in many other pseudobrookites [\[12,13\]](#page-7-0), the cations order-disorder also occurs in FeTi₂O₅ (*Cmcm* space group) due to the existence of the inequivalent $M1O_6$ and $M2O_6$ octahedrons, where M represents the Fe²⁺/Ti⁴⁺ ions. For the highly ordered FeTi₂O₅, Fe^{2+} ($r = 0.76 \text{ Å}$) and Ti^{4+} ($r = 0.68 \text{ Å}$) will occupy the larger $M1O_6$ octahedron and the smaller $M2O_6$ octahedron, respectively. However, since the $3d$ shell of Ti^{4+} ions is completely unoccupied, the unusual magnetic and structural properties of this material are believed to be related to Fe 3*d* electrons [\[9\]](#page-6-0). Therefore, there will be no magnetic frustration in FeTi₂O₅ once the vertices of the triangle in Fig. $1(a)$ are occupied by nonmagnetic Ti^{4+} . Since the frustration is

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FIG. 1. (a) The schematic diagram of the geometrical frustration in FeTi₂O₅, in which only Fe²⁺ (the green ball) and the corner-shared O^{2-} (the red ball) were shown. Fe chains run along the *a* axis. The dashed line shows the triangular geometric frustration in FeTi₂O₅. (b) The Rietveld refinement results of $FeTi₂O₅$.

necessary for the spin JT effect, highly ordered Fe^{2+}/Ti^{4+} occupancy is needed for investigating the spin JT effect in $FeTi₂O₅$. On the other hand, for the completely ordered FeTi₂O₅, the distance between adjacent Fe²⁺ along the *b* and *c* directions is much larger than that along the *a* axis $(a = 3.74098 \text{ Å}, b = 9.7609 \text{ Å}, c = 10.0914 \text{ Å}$ [\[9\]](#page-6-0), so the one-dimensional (1D) $S = 2$ chains of Fe²⁺ are formed along the *a* axis. The appearance of the 1D spin chain can result in various fascinating phenomena, e.g., Bose-Einstein condensation, formation of quantum spin-liquid states, and the Haldane phase $[14–16]$, making FeTi₂O₅ attractive for studying also from this perspective.

In this paper, using the floating zone method, the $FeTi₂O₅$ single crystal with highly ordered Fe^{2+}/Ti^{4+} occupation was successfully grown. Through thermal expansion and magnetostriction measurements, we found that the magnetoelastic coupling exists in $FeTi₂O₅$.

II. EXPERIMENTAL AND CALCULATION DETAILS

A FeT_i₂O₅ single crystal was grown by the optical floating zone technique in an image furnace with two ellipsoidal mirrors (IR Image Furnace G3, Quantum Design Japan). The crystal was grown in pure Ar atmosphere with a growth rate of 1 mm/h. $MgTi₂O₅$ single crystal was also prepared under the same condition in order to estimate the lattice specific heat of $FeTi₂O₅$. The phase purity was identified by x-ray diffraction (XRD) (Aeris, Cu $K\alpha_1$ radiation) and x-ray Laue back diffraction was used to confirm the quality of the crystal and determine the crystal principal axes (the Laue picture can be seen in the Supplemental Material [\[17\]](#page-7-0)). The magnetic susceptibility and magnetization measurements were performed by using a commercial superconducting quantum interference device magnetometer (MPMS3). The measurement of specific heat*C*(*T*) was performed by a physical property measurement system (PPMS) (DynaCool-14 T). Both thermal expansion $\Delta L/L_0(T)$ and magnetostriction $\Delta L/L_0(H)$ were performed

in the PPMS by using an AH 2550A capacitance dilatometer that was calibrated with 99.999% pure Cu and Al rods. The thermal conductivity $\kappa(T)$ was measured in the PPMS with the "one heater, two thermometers" method.

We used density functional theory calculations as realized in the VASP package [\[18\]](#page-7-0) with generalized gradient approximation (GGA) and the exchange-correlation potential in Perdew-Burke-Ernzerhof (PBE) form [\[19\]](#page-7-0) to study the electronic and magnetic properties of $FeTi₂O₅$. The correlation effects were taken into account by the $GGA + U$ approach [\[20\]](#page-7-0) with $U-J_H = 4$ eV for Fe and $U-J_H = 2.5$ eV, close to typical values of Hubbard repulsion (*U*) and intra-atomic exchange used in the literature $[21,22]$. All calculations were performed for the $9 \times 9 \times 5$ mesh of the Brillouin zone; the convergence criterion was set to 10^{-5} eV, while the cutoff energy was chosen to be 500 eV. The following Wigner-Seitz radii were chosen for calculations of atomic charges and magnetic moments: $R_{\text{Fe}} = 1.302 \text{ Å}$, $R_{\text{Ti}} = 1.323 \text{ Å}$, and $R_{\rm O} = 0.82$ Å.

III. RESULTS AND DISCUSSION

A. X-ray diffraction and magnetic susceptibility

To identify the degree of the ordering of Fe^{2+}/Ti^{4+} in $FeTi₂O₅$, the powder XRD was measured and Rietveld refinement was performed to identify the degree of the ordering of Fe^{2+}/Ti^{4+} in FeTi₂O₅, as shown in Fig. 1(b). The refined lattice parameters for room temperature are $a = 3.74014(2)$ Å, $b = 9.76375(6)$ Å, and $c = 10.08496(7)$ Å, as listed in Table [I,](#page-2-0) consistent with the results reported before [\[9\]](#page-6-0). From the refinement results, we can also get the information of the Fe²⁺/Ti⁴⁺ disorder parameter *X* in FeTi₂O₅, which is defined as the atomic concentration of Ti^{4+} in *TM*1 sites [\[23\]](#page-7-0). For the grown FeT₁₂O₅ single crystal, *X* is only 0.12, which is smaller than 0.14 for the well-studied pseudobrookite MgTi₂O₅ ceramics with highly ordered Mg²⁺/Ti⁴⁺ occupation $[23]$. Therefore, in our FeTi₂O₅ single crystal, most of

TABLE I. Refined crystal structure parameters of $FeTi₂O₅$.

Cell parameters Space group: Cmcm a, b, c (Å): 3.740 14(2), 9.763 75(6), 10.084 96(7) Atomic fractional coordinates											
						Atom	Site	\overline{a}	h	\mathcal{C}	Occ.
						Fe1	4c	0	0.1916	0.2500	0.8885
						Ti1	4c	0	0.1916	0.2500	0.1115
Fe ₂	8 f	0	0.1343	0.5666	0.0558						
Ti2	8f	0	0.1343	0.5666	0.9442						
O ₁	4c	0	0.7810	0.2500	1.0000						
O ₂	8 f	0	0.0450	0.1130	1.0000						
O ₃	8 f	0	0.3150	0.0610	1.0000						

the Fe²⁺ occupy the *M*1 sites, forming the Fe²⁺ chain along the *a* axis.

The temperature dependence of magnetic susceptibilities of $FeTi₂O₅$ single crystal along different axes is displayed in Fig. 2. The rapid decrease at $T_N = 42$ K in the $\chi(T)$ curve along the *b* axis of $FeTi₂O₅$ corresponds to the long-range

antiferromagnetic ordering of Fe^{2+} , consistent with the previous report [\[9\]](#page-6-0), while the susceptibilities along the *a* axis and the *c* axis turn to increase with decreasing temperature below T_N . The anisotropic behavior of $\chi(T)$ curves suggests that the *b* axis is the easy axis in $FeTi₂O₅$. When applying different magnetic fields along the *b* axis of $FeTi₂O₅$, as shown in Fig. $2(b)$, T_N decreases with increasing the field and the rapid drop in the magnetic susceptibility tends to disappear. The temperature dependence of the magnetic susceptibility of $FeTi₂O₅$ above 90 K was fitted by the Padé approximation following Ref. [\[24\]](#page-7-0). The fitting yields nearest neighbor exchange interaction J_{NN} ~ 22 K if the Heisenberg model is defined as

$$
H_{\text{Heis}} = \sum_{i>j} J_{ij} S_i S_j, \qquad (1)
$$

and the *g* factors along different axes are $g_a \sim 2.24$, $g_b \sim$ 2.20, and $g_c \sim 2.30$, which is in accordance with the small difference in the susceptibilities for three different directions at 300 K. As shown in Fig. $2(c)$, by fitting the $1/\chi$ -*T* curve of FeTi₂O₅ with the Curie-Weiss law from 200 to 300 K, the effective magnetic moments along the *a*, *b*, and *c* axes were obtained as 5.96 μ_B , 5.59 μ_B , and 6.35 μ_B , respectively,

FIG. 2. The magnetic measurements of FeTi₂O₅ single crystal along different axes. (a) χ -T. The inset presents the broad peak along the *b* axis in enlarged form. (b) Low-temperature susceptibilities at different fields along the *b* axis. (c) $1/\chi$ -*T*. (d) *M*(*H*) curves.

FIG. 3. (a), (b) The thermal expansion of FeTi₂O₅ single crystal along the *a* axis and *b* axis. The insets show the thermal expansion coefficient α of FeTi₂O₅. (c) The magnetostriction of FeTi₂O₅ single crystal along the *a* axis at different temperatures. (d) The magnetostriction of FeTi₂O₅ single crystal along the *b* axis below T_N .

which are much larger than the spin-only value of $4.90 \mu_B$ for the Fe²⁺ with $S = 2$, indicating that there is an orbital contribution to the magnetic moment in $FeTi₂O₅$.

The field dependence of the magnetization of $FeTi₂O₅$ presented in Fig. [2\(d\)](#page-2-0) also confirmed the existence of the orbital contribution. Indeed, *M*(*H*) curves along the *a* and *c* axes of $FeTi₂O₅$ deviate from linearity at substantial fields and do not saturate even at about 100 kOe, suggesting a strong magnetic anisotropy due to unquenched orbital moment and substantial spin-orbit coupling. As mentioned above, the 1D chains of Fe²⁺ will be formed along the *a* axis in FeTi₂O₅ with highly ordered Fe^{2+}/Ti^{4+} occupation. This quasi-onedimensionality is manifested by the broad peak at around 75 K in the $\chi(T)$ curve, as shown in the inset of Fig. [2\(a\).](#page-2-0) Although the Fe²⁺ chains exist in FeTi₂O₅, the magnetic structure of $FeTi₂O₅$ is three-dimensional (3D). This is also consistent with the high Néel temperature in FeTi₂O₅ ($T_N \sim 42$ K) which suggests a large interchain exchange interaction in $FeTi₂O₅$. However, care should be taken in this respect, since in some low-dimensional materials the ordering temperature is largely suppressed by the logarithm of the ratio of intra- and interchain exchanges [\[25\]](#page-7-0).

The large interchain exchange interaction in the $FeTi₂O₅$ having a triangular motif as shown in Fig. $1(a)$ can result in a geometrical frustration being antiferromagnetic. The frustration index commonly estimated as $|\theta_{\rm CW}|/T_N$ varies from 2.9 to 5.0 for $FeTi₂O₅$ because the fitted Weiss temperature $\theta_{\rm CW}$ differs along different axes. Lang *et al.* proposed that the long-range antiferromagnetic ordering in $FeTi₂O₅$ appears if the frustration is released by the spin Jahn-Teller effect [\[9\]](#page-6-0), but no structural distortion has been detected so far.

B. Thermal expansion, specific heat, and thermal conductivity

We measured the temperature dependence of thermal expansion $(\Delta L/L_{80 \text{ K}})$ of FeTi₂O₅ single crystal along different axes, where the value of $\Delta L / L_{80 \text{ K}}$ was normalized as $[L(T)-L(80 \text{ K})]/L(80 \text{ K})$, as shown in Figs. 3(a) and 3(b). As the temperature decreases, the *a* axis of $FeTi₂O₅$ shows positive thermal expansion behavior with two anomalies around T_N at 41 and 43 K, respectively, while the negative thermal expansion appears along the *b* axis, and the slope of the $\Delta L/L_{80\,\text{K}}$ curve along the *b* axis also changes around T_N . This anomaly is easier to see from the thermal expansion coefficient $\alpha(T) = d[\Delta L(T)/L_{80 \text{ K}}]/dT$ plot shown in the insets

FIG. 4. (a) The specific heat of $Feri₂O₅$ under different magnetic fields. (b) The magnetic specific heat and change of magnetic entropy of $FeTi₂O₅$.

of Figs. $3(a)$ and $3(b)$. We also performed the magnetostriction measurement to confirm the existence of the spin-lattice coupling in FeTi₂O₅. As shown in Figs. $3(c)$ and $3(d)$, the negative and positive magnetostriction effects appear clearly below T_N along the *a* and *b* axes, respectively, indicating that there is an obvious spin-lattice coupling in $FeTi₂O₅$. This magnetostriction can soften the phonons and induce lattice distortions in FeTi₂O₅ at T_N . A similar effect has been reported for some transition-metal oxides, e.g., for $Fe₃(PO₄)O₃$ [26] and $Bi₂Fe₄O₉$ [$22,27$]. With decreasing the temperature, the magnitude of magnetostriction of $FeTi₂O₅$ increases, as shown in Fig. $3(c)$, indicating the enhancement of spin-lattice coupling at low temperature.

The temperature dependence of the specific heat of $FeTi₂O₅$ single crystal was shown in Fig. 4(a). A peak can be seen at $T_N = 42$ K in the $C(T)$ curve, corresponding to the antiferromagnetic ordering of $FeTi₂O₅$ [\[9\]](#page-6-0). As the temperature decreases, a shoulder-type peak appears in the $C(T)$ curve at 41 K. These two peaks are consistent with two anomalies in thermal expansion along the *a* axis. This double-peak behavior in $C(T)$ may correspond to two domains of comparable volume. It is tempting to ascribe this effect to two magnetic domains, characterized by propagation vectors $\mathbf{k}_1 = (\frac{1}{2}, \frac{1}{2}, 0)$ and $\mathbf{k}_2 = (-\frac{1}{2}, \frac{1}{2}, 0)$ [\[8\]](#page-6-0). These two phases are degenerate and tiny distortions can lift this degeneracy through the spin JT effect, resulting in the formation of several domains. However, one cannot rule out a simpler scenario, when domains appear due to different degrees of stoichiometry, which comes from the mutual substitution of Fe^{2+} and Ti^{4+} . This slightly nonuniform distribution of Fe^{2+} and Ti^{4+} can cause local strains, stabilizing one or another magnetic phases. Finally, the peak at $T_N = 42$ K can be associated with the long-range antiferromagnetic ordering, and the peak at 41 K comes from the structural distortion induced by the magnetostriction phenomenon, which is commonly seen in antiferromagnetic oxides below the Néel temperature, e.g., CoO, etc. [\[28\]](#page-7-0).

Magnetic contribution to the specific heat $C_m(T)$ of $FeTi₂O₅$ can be obtained by subtracting the lattice specific heat $C_p(T)$ from the total specific heat of FeTi₂O₅. The C_p of the FeTi₂O₅ single crystal was estimated from the C_p of the nonmagnetic $MgTi₂O₅$ single crystal by using the formula $C_m(T)$ FeTi₂O₅ = $\sqrt{M_{\text{FeTi}_2O_5}}/M_{\text{MgTi}_2O_5}C_p(T)_{\text{MgTi}_2O_5}$, in which $M_{\text{FeTi}_2\text{O}_5}$ and $M_{\text{MgTi}_2\text{O}_5}$ represent the relative molecular masses of FeTi₂O₅ and MgTi₂O₅, respectively. The magnetic entropy change of FeTi₂O₅ calculated from $\Delta S =$ magnetic entropy change of FeTi₂O₅ calculated from $\Delta S = \int_{T_1}^{T_2} \frac{C_m}{T} dT$ is 6.41 J mol⁻¹ K⁻¹ at *T_N*, which is about 48% of $R \ln(2 \times 2 + 1) \approx 13.37 \text{ J} \text{ mol}^{-1} \text{ K}^{-1}$ (*R* is the gas constant) expected for $S = 2$ and close to the value of $R \ln 2 \approx 5.76$. The difference between the calculated and the expected value of ΔS may come from two reasons: (i) the magnetic entropy is released far above T_N by the short-range magnetic ordering in the 1D Fe²⁺ spin chains and (ii) due to the spin JT effect.

As an exclusively sensitive probe for the itinerant excitations $[29]$, the thermal conductivity of FeTi₂O₅ single crystal was also measured to further investigate the source of the structural distortions in FeTi₂O₅. In Fig. [5,](#page-5-0) the thermal conductivity of $FeTi₂O₅$ increases monotonically with decreasing temperature and suddenly enhances around T_N , which is more pronounced in the $1/\kappa(T)$ curve, and a cusp occurs at T_N . When applying the magnetic field of 120 kOe, the κ of $FeTi₂O₅$ below T_N was apparently suppressed. The change of the slope of $1/\kappa$ is commonly seen in the spinel oxides with orbital degrees of freedom and is explained as the result of the orbital ordering [\[30,31\]](#page-7-0). Therefore, one may expect that this change in the $1/\kappa(T)$ curve of FeTi₂O₅ also stems from the orbital ordering of Fe^{2+} , which leads to the anomaly in temperature dependence of $\Delta L / L_{80 \text{ K}}$, but this hypothesis must be verified by other methods, e.g., x-ray spectroscopy, while our density functional theory (DFT) calculations do not detect any changes in the orbital occupations; see next section. Therefore, this slope change may imply the appearance of spin JT in FeTi₂O₅. Another possibility for the slope changing in $\kappa(T)$ is that the phonons are transferred more efficiently in the ordered phase. Since $FeTi₂O₅$ is a quasi-1D antiferromagnet with $S = 2$, a spin gap is expected to open in its magnetic excitation spectrum. Therefore, the increase of κ

FIG. 5. The thermal conductivity of FeTi2O5 single crystal along the *a* axis under different magnetic fields. (a) κ-*T*, (b) 1/κ-*T*. The dashed line in the $1/\kappa$ -*T* at zero field is used to show the change in the slope.

below T_N may also result from the weakening of the scattering of phonons by magnons. A similar effect has been observed in some quasi-1D antiferromagnets, e.g., NaV_2O_5 [\[32\]](#page-7-0). The low-temperature peak in the κ -*T* curve of FeTi₂O₅ around 30 K is commonly seen in solids, resulting from phonon-phonon scattering [\[33\]](#page-7-0).

C. First-principles calculations

To check possible modifications of the orbital structure in $FeTi₂O₅$ and study exchange interaction, we performed GGA and $GGA + U$ calculations. It has to be mentioned that Fe resides in 4*c* positions in the *Cmcm* space group [\[9\]](#page-6-0), which corresponds to the C_{2v} point group. The degeneracy of 3*d* orbitals is completely lifted in this case. Indeed, results of the Wannier function projection of the nonmagnetic GGA Hamiltonian using the WANNIER90 code [\[34\]](#page-7-0) for the experimental crystal structure measured for room temperature [\[9\]](#page-6-0) presented in Fig. $6(a)$ confirm general symmetry arguments. Thus there is no orbital degeneracy to be lifted. The lowest in energy is the *xz* orbital (in the global coordinate system), which is shown in Fig. $6(b)$. In the high-spin d^6 configuration of Fe²⁺ a single electron with spin minority must occupy this orbital,

FIG. 6. (a) Crystal-field splitting of the Fe 3*d* shell as obtained by the Wannier function projection of nonmagnetic GGA calculations. (b) The lowest in energy *xz* orbital (in the global coordinate system) in GGA nonmagnetic calculations; Fe ions are shown by red, while O is shown by violet balls.

and the next in energy orbital is split by 210 meV. Such a large crystal-field splitting agrees with strong distortions of $FeO₆$ octahedra and disfavors any redistribution of electrons, which is needed for any nontrivial orbital ordering below T_N . Weak distortions due to the spin JT are not expected to strongly affect electronic level structure.

The direct $GGA + U$ calculations confirm that correlation effects do not change the situation and indeed a single electron with spin minority occupies the *xz* orbital, making this orbital doubly occupied and inactive in the exchange interaction along the chain. Moreover, we also performed optimization of the crystal structure and calculations taking into account experimental modifications of lattice parameters according to our thermal expansion measurements (expand along the *a* axis and shrink in the *b* direction). None of them show changes in the orbital structure.

Figure [7](#page-6-0) shows the density of state plots in the case of $GGA + U$ calculation with spins in the chain ordered antiferromagnetically. One can see that the bottom of the conduction band is formed by completely empty Ti 3*d* states, while the top of the valence band is formed by Fe 3*d* spin-minority states [narrow bands just below the Fermi level have *xz* character; the corresponding orbital is shown in Fig. $6(b)$]. The band gap is \sim 1.7 eV.

Finally, we calculated the exchange interaction parameter for the Heisenberg model [\(1\)](#page-2-0) using the method of four configurations [\[35\]](#page-7-0). The intrachain exchange was found to be $J = 17.7$ K. This agrees with the fitting of magnetic susceptibility by the Padé approximation of the 1D Heisenberg model as explained above. The diagonal interchain exchange (for simplicity we do not differentiate between such exchanges in the *ab* and *ac* planes) was calculated to be $J' = 0.6$ K.

In addition, $GGA + U + SOC$ (SOC stands for the spinorbit coupling) calculations reveal that spins are directed along the *b* axis with orbital momentum $\sim 0.1 \mu_B$. This fully agrees with our magnetization measurements (see Sec. [III A\)](#page-1-0). The single-ion anisotropy modeled by $H_{\text{SIA}} = \sum_{i} A(S_i^z)^2$ was found to be $A = 4K$ from the total energy $GGA + U + SOC$

FIG. 7. Total and partial densities of states (DOS) as obtained in $GGA + U$ calculations for the magnetic configuration, where spins in the same chain are AFM ordered. For O 2*p*, Fe 3*d*, and Ti 3*d* two spin projections are shown by positive DOS for spin majority and negative DOS for spin minority. The Fermi level is set to zero.

calculations of four configurations: when one of the spins is directed along *b*, *–b*, *a*, or *–a*, while all other spins are along the *c* axis.

Thus we see that $FeTi₂O₅$ exhibits Ising-like behavior and can be an example of a quasi-1D Ising antiferromagnet with spin $S = 2$. Indeed, the ratio of intra- to interchain exchanges $J/J' \sim 30$ and $A/J' \sim 7$. This model has highly unusual properties in the presence of the transverse magnetic field. There can be a quantum critical behavior (as the field increases) together with the exotic E_8 excitations. This is now one of the hot subjects in the physics of low-dimensional magnetic systems and material realizations of these phenomena, e.g., in 1D ferromagnetic $CoNb₂O₆$ [\[36–38\]](#page-7-0) or antiferromagnetic $BaCo₂V₂O₈$ [\[39–41\]](#page-7-0) are under active studying. However, interest in the Ising model in the transverse field is not restricted

by materials with $S = 1/2$, since the field induces tunneling processes between states in a double-well potential characterized by different spin projections and these are not necessarily only the states with $S_z = 1/2$ [\[42\]](#page-7-0).

IV. CONCLUSION

The pseudobrookite $FeTi₂O₅$ single crystal with highly ordered Fe²⁺/Ti⁴⁺ occupation was grown under pure Ar atmosphere. Magnetostriction measurements clearly demonstrate the appearance of the magnetoelastic coupling, which is consistent with the previously proposed spin Jahn-Teller scenario of lifting degeneracy in this highly frustrated system due to coupling with a crystal lattice and stabilizing a long-range magnetic order [9]. While tiny distortions associated with the spin Jahn-Teller effect are unluckily to be measured by diffraction techniques, our experiments reveal the existence of magnetoelastic coupling in $FeTi₂O₅$ and *ab initio* calculations rule out another mechanism of symmetry lowering due to orbital degrees of freedom. In addition, density functional theory calculations unravel a substantial easy-axis anisotropy putting this material in the class of the quasi-1D Ising model, which agrees with the field dependence of magnetization. Exotic properties of Ising systems in the transverse magnetic fields together with a strong magnetoelastic coupling make $FeTi₂O₅$ a unique object interesting for further detailed investigation.

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