# Possible spin Jahn-Teller material: Ordered pseudobrookite FeTi<sub>2</sub>O<sub>5</sub>

Hao-Hang Xu,<sup>1</sup> Jian Liu,<sup>3</sup> L. L. Tao,<sup>1</sup> Xian-Jie Wang,<sup>1,\*</sup> Sergey V. Streltsov<sup>(a)</sup>,<sup>2,†</sup> and Yu Sui<sup>(b)</sup>,<sup>3,‡</sup>

<sup>1</sup>School of Physics, Harbin Institute of Technology, Harbin 150001, China

<sup>2</sup>Institute of Metal Physics, S. Kovalevskoy Street 18, 620990 Ekaterinburg, Russia

<sup>3</sup>Laboratory for Space Environment and Physical Sciences, Harbin Institute of Technology, Harbin 150001, China

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We investigated spin-lattice coupling in orthorhombic pseudobrookite  $\text{FeTi}_2\text{O}_5$  single crystal with highly ordered  $\text{Fe}^{2+}/\text{Ti}^{4+}$  occupation, which consists of quasi-one-dimensional (1D) S = 2 chains running along the *a* axis. Both the magnetization and specific heat measurements confirm that the antiferromagnetic phase transition of  $\text{FeTi}_2\text{O}_5$  occurs at  $T_N = 42$  K. The structural distortions were also observed around  $T_N$  in the thermal expansion  $\Delta L/L(T)$  data. Moreover, the magnetic field was found to strongly affect the thermal expansion both along chains and in the perpendicular direction clearly signaling a substantial magnetoelastic coupling, which was recently proposed to be the origin of a rare spin Jahn-Teller effect, when frustration is lifted via additional lattice distortions. Experimentally observed change in the thermal conductivity slope around  $T_N$  is usually associated with the orbital ordering, but density functional theory (DFT)+*U* calculations do not detect modification of the orbital structure across the transition. However, the first-principles calculation results confirm that  $\text{FeTi}_2\text{O}_5$  is a quasi-1D magnet with a ratio of frustrating interchain to intrachain exchanges J'/J = 0.03 and a substantial single-ion anisotropy (A = 4 K) of easy-axis type making this material interesting for studying quantum criticality in transverse magnetic fields.

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## I. INTRODUCTION

The Jahn-Teller (JT) effect is a spontaneous structural distortion that lifts the orbital degeneracy of the *d* electron, resulting in the orbital ordering and causing various fascinating phenomena; e.g., it can affect magnetic structure [1] and lead to the orbital-selective Mott transition [2] or the reduction of effective dimensionality [3]. In analogy to the JT effect, Yamashita and Ueda proposed the spin JT effect, when the spin degeneracy in geometrical frustration spin systems is released by the structural distortion through the spin-lattice coupling [4]. While this mechanism was initially proposed for ZnV<sub>2</sub>O<sub>4</sub> and MgV<sub>2</sub>O<sub>4</sub>, it was later also applied to other spinels [5–7].

The orthorhombic pseudobrookite  $\text{CoTi}_2\text{O}_5$  was recently proposed by Kirschner *et al.* as another candidate for spin JT effect [8]. It was suggested that the triangular geometrical frustration exists in the orthorhombic pseudobrookite  $\text{CoTi}_2\text{O}_5$  and an unexpected long-range antiferromagnetic ordering of  $\text{Co}^{2+}$  at  $T_N \sim 26$  K is due to an additional structural distortion induced by the spin-lattice coupling through the spin JT effect [8]. Combining the x-ray diffraction measurements on polycrystalline samples with the density functional theory calculations, Lang *et al.* demonstrated that the pseudobrookite FeTi<sub>2</sub>O<sub>5</sub>, so the triangular geometrical frustration also exists in FeTi<sub>2</sub>O<sub>5</sub>, as shown in Fig. 1(a), and a structural distortion is also expected in FeTi<sub>2</sub>O<sub>5</sub> [9], but no direct experimental evidence was found. This is not surprising since distortions related to lowering of the crystal structure due to the spin JT effect are expected to be extremely small and are unlikely to be measured by neutron or x-ray diffraction techniques. This remains the situation in multiferroics, where electric polarization is measurable, but corresponding distortions often remain experimentally elusive. In addition, compounds with octahedrally coordinated Fe<sup>2+</sup> could also exhibit various interesting physical properties due to the orbital ordering of  $Fe^{2+}$ . For instance, the orbital ordering of Fe<sup>2+</sup> accompanied by a structural distortion in perovskite KFeF<sub>3</sub> opens a band gap in the electronic band structure, leading to a metal-insulator transition [10]. Moreover, there is an interplay between charge, spin, and lattice degrees of freedom in the famous Fe<sub>3</sub>O<sub>4</sub>, which results in the formation of trimerons and Verwey transition [11]. Therefore, it is interesting to study coupling between all these degrees of freedom in FeTi<sub>2</sub>O<sub>5</sub> as well.

There are two main structural units in the pseudobrookite  $FeTi_2O_5$ :  $Fe^{2+}O_6$  and  $Ti^{4+}O_6$  octahedrons. Like in many other pseudobrookites [12,13], the cations order-disorder also occurs in  $FeTi_2O_5$  (*Cmcm* space group) due to the existence of the inequivalent  $M1O_6$  and  $M2O_6$  octahedrons, where M represents the  $Fe^{2+}/Ti^{4+}$  ions. For the highly ordered  $FeTi_2O_5$ ,  $Fe^{2+}$  (r = 0.76 Å) and  $Ti^{4+}$  (r = 0.68 Å) will occupy the larger  $M1O_6$  octahedron and the smaller  $M2O_6$  octahedron, respectively. However, since the 3d shell of  $Ti^{4+}$  ions is completely unoccupied, the unusual magnetic and structural properties of this material are believed to be related to Fe 3d electrons [9]. Therefore, there will be no magnetic frustration in  $FeTi_2O_5$  once the vertices of the triangle in Fig. 1(a) are occupied by nonmagnetic  $Ti^{4+}$ . Since the frustration is

<sup>\*</sup>wangxianjie@hit.edu.cn

<sup>&</sup>lt;sup>†</sup>streltsov.s@gmail.com

<sup>\*</sup>suiyu@hit.edu.cn



FIG. 1. (a) The schematic diagram of the geometrical frustration in  $\text{FeTi}_2\text{O}_5$ , in which only  $\text{Fe}^{2+}$  (the green ball) and the corner-shared  $\text{O}^{2-}$  (the red ball) were shown. Fe chains run along the *a* axis. The dashed line shows the triangular geometric frustration in  $\text{FeTi}_2\text{O}_5$ . (b) The Rietveld refinement results of  $\text{FeTi}_2\text{O}_5$ .

necessary for the spin JT effect, highly ordered Fe<sup>2+</sup>/Ti<sup>4+</sup> occupancy is needed for investigating the spin JT effect in FeTi<sub>2</sub>O<sub>5</sub>. On the other hand, for the completely ordered FeTi<sub>2</sub>O<sub>5</sub>, the distance between adjacent Fe<sup>2+</sup> along the *b* and *c* directions is much larger than that along the *a* axis (a = 3.740.98 Å, b = 9.7609 Å, c = 10.0914 Å) [9], so the one-dimensional (1D) S = 2 chains of Fe<sup>2+</sup> are formed along the *a* axis. The appearance of the 1D spin chain can result in various fascinating phenomena, e.g., Bose-Einstein condensation, formation of quantum spin-liquid states, and the Haldane phase [14–16], making FeTi<sub>2</sub>O<sub>5</sub> attractive for studying also from this perspective.

In this paper, using the floating zone method, the  $FeTi_2O_5$  single crystal with highly ordered  $Fe^{2+}/Ti^{4+}$  occupation was successfully grown. Through thermal expansion and magnetostriction measurements, we found that the magnetoelastic coupling exists in  $FeTi_2O_5$ .

## **II. EXPERIMENTAL AND CALCULATION DETAILS**

A FeTi<sub>2</sub>O<sub>5</sub> single crystal was grown by the optical floating zone technique in an image furnace with two ellipsoidal mirrors (IR Image Furnace G3, Quantum Design Japan). The crystal was grown in pure Ar atmosphere with a growth rate of 1 mm/h. MgTi<sub>2</sub>O<sub>5</sub> single crystal was also prepared under the same condition in order to estimate the lattice specific heat of FeTi<sub>2</sub>O<sub>5</sub>. The phase purity was identified by x-ray diffraction (XRD) (Aeris, Cu  $K\alpha_1$  radiation) and x-ray Laue back diffraction was used to confirm the quality of the crystal and determine the crystal principal axes (the Laue picture can be seen in the Supplemental Material [17]). The magnetic susceptibility and magnetization measurements were performed by using a commercial superconducting quantum interference device magnetometer (MPMS3). The measurement of specific heat C(T) was performed by a physical property measurement system (PPMS) (DynaCool-14 T). Both thermal expansion  $\Delta L/L_0(T)$  and magnetostriction  $\Delta L/L_0(H)$  were performed

in the PPMS by using an AH 2550A capacitance dilatometer that was calibrated with 99.999% pure Cu and Al rods. The thermal conductivity  $\kappa(T)$  was measured in the PPMS with the "one heater, two thermometers" method.

We used density functional theory calculations as realized in the VASP package [18] with generalized gradient approximation (GGA) and the exchange-correlation potential in Perdew-Burke-Ernzerhof (PBE) form [19] to study the electronic and magnetic properties of FeTi<sub>2</sub>O<sub>5</sub>. The correlation effects were taken into account by the GGA + *U* approach [20] with  $U-J_H = 4 \text{ eV}$  for Fe and  $U-J_H = 2.5 \text{ eV}$ , close to typical values of Hubbard repulsion (*U*) and intra-atomic exchange used in the literature [21,22]. All calculations were performed for the  $9 \times 9 \times 5$  mesh of the Brillouin zone; the convergence criterion was set to  $10^{-5} \text{ eV}$ , while the cutoff energy was chosen to be 500 eV. The following Wigner-Seitz radii were chosen for calculations of atomic charges and magnetic moments:  $R_{\text{Fe}} = 1.302 \text{ Å}$ ,  $R_{\text{Ti}} = 1.323 \text{ Å}$ , and  $R_{\text{O}} = 0.82 \text{ Å}$ .

## **III. RESULTS AND DISCUSSION**

## A. X-ray diffraction and magnetic susceptibility

To identify the degree of the ordering of  $Fe^{2+}/Ti^{4+}$  in  $FeTi_2O_5$ , the powder XRD was measured and Rietveld refinement was performed to identify the degree of the ordering of  $Fe^{2+}/Ti^{4+}$  in  $FeTi_2O_5$ , as shown in Fig. 1(b). The refined lattice parameters for room temperature are  $a = 3.740 \, 14(2)$  Å,  $b = 9.763 \, 75(6)$  Å, and  $c = 10.084 \, 96(7)$  Å, as listed in Table I, consistent with the results reported before [9]. From the refinement results, we can also get the information of the  $Fe^{2+}/Ti^{4+}$  disorder parameter X in  $FeTi_2O_5$ , which is defined as the atomic concentration of  $Ti^{4+}$  in TM1 sites [23]. For the grown  $FeTi_2O_5$  single crystal, X is only 0.12, which is smaller than 0.14 for the well-studied pseudobrookite  $MgTi_2O_5$  ceramics with highly ordered  $Mg^{2+}/Ti^{4+}$  occupation [23]. Therefore, in our  $FeTi_2O_5$  single crystal, most of

TABLE I. Refined crystal structure parameters of FeTi<sub>2</sub>O<sub>5</sub>.

Cell parameters					
Space gro	oup: Cmcm				
<i>a</i> , <i>b</i> , <i>c</i> (Å): 3.740 14(2), 9.763 75(6), 10.084 96(7) Atomic fractional coordinates					
Fe1	4c	0	0.1916	0.2500	0.8885
Ti1	4c	0	0.1916	0.2500	0.1115
Fe2	8f	0	0.1343	0.5666	0.0558
Ti2	8f	0	0.1343	0.5666	0.9442
01	4c	0	0.7810	0.2500	1.0000
O2	8f	0	0.0450	0.1130	1.0000
03	8 <i>f</i>	0	0.3150	0.0610	1.0000

the  $Fe^{2+}$  occupy the *M*1 sites, forming the  $Fe^{2+}$  chain along the *a* axis.

The temperature dependence of magnetic susceptibilities of FeTi<sub>2</sub>O<sub>5</sub> single crystal along different axes is displayed in Fig. 2. The rapid decrease at  $T_N = 42$  K in the  $\chi(T)$  curve along the *b* axis of FeTi<sub>2</sub>O<sub>5</sub> corresponds to the long-range antiferromagnetic ordering of Fe<sup>2+</sup>, consistent with the previous report [9], while the susceptibilities along the *a* axis and the *c* axis turn to increase with decreasing temperature below  $T_N$ . The anisotropic behavior of  $\chi(T)$  curves suggests that the *b* axis is the easy axis in FeTi<sub>2</sub>O<sub>5</sub>. When applying different magnetic fields along the *b* axis of FeTi<sub>2</sub>O<sub>5</sub>, as shown in Fig. 2(b),  $T_N$  decreases with increasing the field and the rapid drop in the magnetic susceptibility tends to disappear. The temperature dependence of the magnetic susceptibility of FeTi<sub>2</sub>O<sub>5</sub> above 90 K was fitted by the Padé approximation following Ref. [24]. The fitting yields nearest neighbor exchange interaction  $J_{NN} \sim 22$  K if the Heisenberg model is defined as

$$H_{\text{Heis}} = \sum_{i>j} J_{ij} S_i S_j, \qquad (1)$$

and the g factors along different axes are  $g_a \sim 2.24$ ,  $g_b \sim 2.20$ , and  $g_c \sim 2.30$ , which is in accordance with the small difference in the susceptibilities for three different directions at 300 K. As shown in Fig. 2(c), by fitting the  $1/\chi$ -T curve of FeTi<sub>2</sub>O<sub>5</sub> with the Curie-Weiss law from 200 to 300 K, the effective magnetic moments along the *a*, *b*, and *c* axes were obtained as  $5.96 \mu_B$ ,  $5.59 \mu_B$ , and  $6.35 \mu_B$ , respectively,



FIG. 2. The magnetic measurements of FeTi<sub>2</sub>O<sub>5</sub> single crystal along different axes. (a)  $\chi$ -*T*. The inset presents the broad peak along the *b* axis in enlarged form. (b) Low-temperature susceptibilities at different fields along the *b* axis. (c)  $1/\chi$ -*T*. (d) *M*(*H*) curves.



FIG. 3. (a), (b) The thermal expansion of  $\text{FeTi}_2O_5$  single crystal along the *a* axis and *b* axis. The insets show the thermal expansion coefficient  $\alpha$  of  $\text{FeTi}_2O_5$ . (c) The magnetostriction of  $\text{FeTi}_2O_5$  single crystal along the *a* axis at different temperatures. (d) The magnetostriction of  $\text{FeTi}_2O_5$  single crystal along the *b* axis below  $T_N$ .

which are much larger than the spin-only value of  $4.90 \,\mu_B$  for the Fe<sup>2+</sup> with S = 2, indicating that there is an orbital contribution to the magnetic moment in FeTi<sub>2</sub>O<sub>5</sub>.

The field dependence of the magnetization of FeTi<sub>2</sub>O<sub>5</sub> presented in Fig. 2(d) also confirmed the existence of the orbital contribution. Indeed, M(H) curves along the *a* and *c* axes of FeTi<sub>2</sub>O<sub>5</sub> deviate from linearity at substantial fields and do not saturate even at about 100 kOe, suggesting a strong magnetic anisotropy due to unquenched orbital moment and substantial spin-orbit coupling. As mentioned above, the 1D chains of  $Fe^{2+}$  will be formed along the *a* axis in  $FeTi_2O_5$ with highly ordered Fe<sup>2+</sup>/Ti<sup>4+</sup> occupation. This quasi-onedimensionality is manifested by the broad peak at around 75 K in the  $\chi(T)$  curve, as shown in the inset of Fig. 2(a). Although the  $Fe^{2+}$  chains exist in  $FeTi_2O_5$ , the magnetic structure of  $FeTi_2O_5$  is three-dimensional (3D). This is also consistent with the high Néel temperature in FeTi<sub>2</sub>O<sub>5</sub> ( $T_N \sim 42$  K) which suggests a large interchain exchange interaction in FeTi<sub>2</sub>O<sub>5</sub>. However, care should be taken in this respect, since in some low-dimensional materials the ordering temperature is largely suppressed by the logarithm of the ratio of intra- and interchain exchanges [25].

The large interchain exchange interaction in the FeTi<sub>2</sub>O<sub>5</sub> having a triangular motif as shown in Fig. 1(a) can result in a geometrical frustration being antiferromagnetic. The frustration index commonly estimated as  $|\theta_{CW}|/T_N$  varies from 2.9 to 5.0 for FeTi<sub>2</sub>O<sub>5</sub> because the fitted Weiss temperature  $\theta_{CW}$  differs along different axes. Lang *et al.* proposed that the long-range antiferromagnetic ordering in FeTi<sub>2</sub>O<sub>5</sub> appears if the frustration is released by the spin Jahn-Teller effect [9], but no structural distortion has been detected so far.

## B. Thermal expansion, specific heat, and thermal conductivity

We measured the temperature dependence of thermal expansion  $(\Delta L/L_{80 \text{ K}})$  of FeTi<sub>2</sub>O<sub>5</sub> single crystal along different axes, where the value of  $\Delta L/L_{80 \text{ K}}$  was normalized as [L(T)-L(80 K)]/L(80 K), as shown in Figs. 3(a) and 3(b). As the temperature decreases, the *a* axis of FeTi<sub>2</sub>O<sub>5</sub> shows positive thermal expansion behavior with two anomalies around  $T_N$  at 41 and 43 K, respectively, while the negative thermal expansion appears along the *b* axis, and the slope of the  $\Delta L/L_{80 \text{ K}}$  curve along the *b* axis also changes around  $T_N$ . This anomaly is easier to see from the thermal expansion coefficient  $\alpha(T) = d[\Delta L(T)/L_{80 \text{ K}}]/dT$  plot shown in the insets



FIG. 4. (a) The specific heat of  $FeTi_2O_5$  under different magnetic fields. (b) The magnetic specific heat and change of magnetic entropy of  $FeTi_2O_5$ .

of Figs. 3(a) and 3(b). We also performed the magnetostriction measurement to confirm the existence of the spin-lattice coupling in FeTi<sub>2</sub>O<sub>5</sub>. As shown in Figs. 3(c) and 3(d), the negative and positive magnetostriction effects appear clearly below  $T_N$  along the *a* and *b* axes, respectively, indicating that there is an obvious spin-lattice coupling in FeTi<sub>2</sub>O<sub>5</sub>. This magnetostriction can soften the phonons and induce lattice distortions in FeTi<sub>2</sub>O<sub>5</sub> at  $T_N$ . A similar effect has been reported for some transition-metal oxides, e.g., for Fe<sub>3</sub>(PO<sub>4</sub>)O<sub>3</sub> [26] and Bi<sub>2</sub>Fe<sub>4</sub>O<sub>9</sub> [22,27]. With decreasing the temperature, the magnitude of magnetostriction of FeTi<sub>2</sub>O<sub>5</sub> increases, as shown in Fig. 3(c), indicating the enhancement of spin-lattice coupling at low temperature.

The temperature dependence of the specific heat of  $FeTi_2O_5$  single crystal was shown in Fig. 4(a). A peak can be seen at  $T_N = 42$  K in the C(T) curve, corresponding to the antiferromagnetic ordering of  $FeTi_2O_5$  [9]. As the temperature decreases, a shoulder-type peak appears in the C(T) curve at 41 K. These two peaks are consistent with two anomalies in thermal expansion along the *a* axis. This double-peak behavior in C(T) may correspond to two domains of comparable volume. It is tempting to ascribe this effect to two magnetic domains, characterized by propagation vectors  $\mathbf{k}_1 = (\frac{1}{2}, \frac{1}{2}, 0)$ and  $\mathbf{k}_2 = (-\frac{1}{2}, \frac{1}{2}, 0)$  [8]. These two phases are degenerate and tiny distortions can lift this degeneracy through the spin JT effect, resulting in the formation of several domains. However, one cannot rule out a simpler scenario, when domains appear due to different degrees of stoichiometry, which comes from the mutual substitution of Fe<sup>2+</sup> and Ti<sup>4+</sup>. This slightly nonuniform distribution of Fe<sup>2+</sup> and Ti<sup>4+</sup> can cause local strains, stabilizing one or another magnetic phases. Finally, the peak at  $T_N = 42$  K can be associated with the long-range antiferromagnetic ordering, and the peak at 41 K comes from the structural distortion induced by the magnetostriction phenomenon, which is commonly seen in antiferromagnetic oxides below the Néel temperature, e.g., CoO, etc. [28].

Magnetic contribution to the specific heat  $C_m(T)$  of FeTi<sub>2</sub>O<sub>5</sub> can be obtained by subtracting the lattice specific

heat  $C_p(T)$  from the total specific heat of FeTi<sub>2</sub>O<sub>5</sub>. The  $C_p$  of the FeTi<sub>2</sub>O<sub>5</sub> single crystal was estimated from the  $C_p$  of the nonmagnetic MgTi<sub>2</sub>O<sub>5</sub> single crystal by using the formula  $C_m(T)$ FeTi<sub>2</sub>O<sub>5</sub> =  $\sqrt{M_{\text{FeTi}_2O_5}/M_{\text{MgTi}_2O_5}}C_p(T)_{\text{MgTi}_2O_5}$ , in which  $M_{\text{FeTi}_2O_5}$  and  $M_{\text{MgTi}_2O_5}$  represent the relative molecular masses of FeTi<sub>2</sub>O<sub>5</sub> and MgTi<sub>2</sub>O<sub>5</sub>, respectively. The magnetic entropy change of FeTi<sub>2</sub>O<sub>5</sub> calculated from  $\Delta S = \int_{T_1}^{T_2} \frac{C_m}{T} dT$  is 6.41 J mol<sup>-1</sup> K<sup>-1</sup> at  $T_N$ , which is about 48% of  $R \ln(2 \times 2 + 1) \approx 13.37$  J mol<sup>-1</sup> K<sup>-1</sup> (R is the gas constant) expected for S = 2 and close to the value of  $R \ln 2 \approx 5.76$ . The difference between the calculated and the expected value of  $\Delta S$  may come from two reasons: (i) the magnetic entropy is released far above  $T_N$  by the short-range magnetic ordering in the 1D Fe<sup>2+</sup> spin chains and (ii) due to the spin JT effect.

As an exclusively sensitive probe for the itinerant excitations [29], the thermal conductivity of FeTi<sub>2</sub>O<sub>5</sub> single crystal was also measured to further investigate the source of the structural distortions in FeTi<sub>2</sub>O<sub>5</sub>. In Fig. 5, the thermal conductivity of FeTi<sub>2</sub>O<sub>5</sub> increases monotonically with decreasing temperature and suddenly enhances around  $T_N$ , which is more pronounced in the  $1/\kappa(T)$  curve, and a cusp occurs at  $T_N$ . When applying the magnetic field of 120 kOe, the  $\kappa$  of  $FeTi_2O_5$  below  $T_N$  was apparently suppressed. The change of the slope of  $1/\kappa$  is commonly seen in the spinel oxides with orbital degrees of freedom and is explained as the result of the orbital ordering [30,31]. Therefore, one may expect that this change in the  $1/\kappa(T)$  curve of FeTi<sub>2</sub>O<sub>5</sub> also stems from the orbital ordering of  $Fe^{2+}$ , which leads to the anomaly in temperature dependence of  $\Delta L/L_{80 \text{ K}}$ , but this hypothesis must be verified by other methods, e.g., x-ray spectroscopy, while our density functional theory (DFT) calculations do not detect any changes in the orbital occupations; see next section. Therefore, this slope change may imply the appearance of spin JT in FeTi<sub>2</sub>O<sub>5</sub>. Another possibility for the slope changing in  $\kappa(T)$  is that the phonons are transferred more efficiently in the ordered phase. Since FeTi<sub>2</sub>O<sub>5</sub> is a quasi-1D antiferromagnet with S = 2, a spin gap is expected to open in its magnetic excitation spectrum. Therefore, the increase of  $\kappa$ 



FIG. 5. The thermal conductivity of FeTi<sub>2</sub>O<sub>5</sub> single crystal along the *a* axis under different magnetic fields. (a)  $\kappa$ -*T*, (b)  $1/\kappa$ -*T*. The dashed line in the  $1/\kappa$ -*T* at zero field is used to show the change in the slope.

below  $T_N$  may also result from the weakening of the scattering of phonons by magnons. A similar effect has been observed in some quasi-1D antiferromagnets, e.g., NaV<sub>2</sub>O<sub>5</sub> [32]. The low-temperature peak in the  $\kappa$ -*T* curve of FeTi<sub>2</sub>O<sub>5</sub> around 30 K is commonly seen in solids, resulting from phonon-phonon scattering [33].

### C. First-principles calculations

To check possible modifications of the orbital structure in FeTi<sub>2</sub>O<sub>5</sub> and study exchange interaction, we performed GGA and GGA + U calculations. It has to be mentioned that Fe resides in 4c positions in the *Cmcm* space group [9], which corresponds to the  $C_{2v}$  point group. The degeneracy of 3d orbitals is completely lifted in this case. Indeed, results of the Wannier function projection of the nonmagnetic GGA Hamiltonian using the WANNIER90 code [34] for the experimental crystal structure measured for room temperature [9] presented in Fig. 6(a) confirm general symmetry arguments. Thus there is no orbital degeneracy to be lifted. The lowest in energy is the xz orbital (in the global coordinate system), which is shown in Fig. 6(b). In the high-spin  $d^6$  configuration of Fe<sup>2+</sup> a single electron with spin minority must occupy this orbital,



FIG. 6. (a) Crystal-field splitting of the Fe 3d shell as obtained by the Wannier function projection of nonmagnetic GGA calculations. (b) The lowest in energy xz orbital (in the global coordinate system) in GGA nonmagnetic calculations; Fe ions are shown by red, while O is shown by violet balls.

and the next in energy orbital is split by 210 meV. Such a large crystal-field splitting agrees with strong distortions of FeO<sub>6</sub> octahedra and disfavors any redistribution of electrons, which is needed for any nontrivial orbital ordering below  $T_N$ . Weak distortions due to the spin JT are not expected to strongly affect electronic level structure.

The direct GGA + U calculations confirm that correlation effects do not change the situation and indeed a single electron with spin minority occupies the xz orbital, making this orbital doubly occupied and inactive in the exchange interaction along the chain. Moreover, we also performed optimization of the crystal structure and calculations taking into account experimental modifications of lattice parameters according to our thermal expansion measurements (expand along the a axis and shrink in the b direction). None of them show changes in the orbital structure.

Figure 7 shows the density of state plots in the case of GGA + U calculation with spins in the chain ordered antiferromagnetically. One can see that the bottom of the conduction band is formed by completely empty Ti 3d states, while the top of the valence band is formed by Fe 3d spin-minority states [narrow bands just below the Fermi level have xz character; the corresponding orbital is shown in Fig. 6(b)]. The band gap is ~1.7 eV.

Finally, we calculated the exchange interaction parameter for the Heisenberg model (1) using the method of four configurations [35]. The intrachain exchange was found to be J = 17.7 K. This agrees with the fitting of magnetic susceptibility by the Padé approximation of the 1D Heisenberg model as explained above. The diagonal interchain exchange (for simplicity we do not differentiate between such exchanges in the *ab* and *ac* planes) was calculated to be J' = 0.6 K.

In addition, GGA + U + SOC (SOC stands for the spinorbit coupling) calculations reveal that spins are directed along the *b* axis with orbital momentum ~ 0.1  $\mu_{\rm B}$ . This fully agrees with our magnetization measurements (see Sec. III A). The single-ion anisotropy modeled by  $H_{\rm SIA} = \sum_i A(S_i^z)^2$  was found to be A = 4 K from the total energy GGA + U + SOC



FIG. 7. Total and partial densities of states (DOS) as obtained in GGA + U calculations for the magnetic configuration, where spins in the same chain are AFM ordered. For O 2p, Fe 3d, and Ti 3d two spin projections are shown by positive DOS for spin majority and negative DOS for spin minority. The Fermi level is set to zero.

calculations of four configurations: when one of the spins is directed along b, -b, a, or -a, while all other spins are along the c axis.

Thus we see that FeTi<sub>2</sub>O<sub>5</sub> exhibits Ising-like behavior and can be an example of a quasi-1D Ising antiferromagnet with spin S = 2. Indeed, the ratio of intra- to interchain exchanges  $J/J' \sim 30$  and  $A/J' \sim 7$ . This model has highly unusual properties in the presence of the transverse magnetic field. There can be a quantum critical behavior (as the field increases) together with the exotic  $E_8$  excitations. This is now one of the hot subjects in the physics of low-dimensional magnetic systems and material realizations of these phenomena, e.g., in 1D ferromagnetic CoNb<sub>2</sub>O<sub>6</sub> [36–38] or antiferromagnetic BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub> [39–41] are under active studying. However, interest in the Ising model in the transverse field is not restricted by materials with S = 1/2, since the field induces tunneling processes between states in a double-well potential characterized by different spin projections and these are not necessarily only the states with  $S_z = 1/2$  [42].

## **IV. CONCLUSION**

The pseudobrookite FeTi<sub>2</sub>O<sub>5</sub> single crystal with highly ordered Fe<sup>2+</sup>/Ti<sup>4+</sup> occupation was grown under pure Ar atmosphere. Magnetostriction measurements clearly demonstrate the appearance of the magnetoelastic coupling, which is consistent with the previously proposed spin Jahn-Teller scenario of lifting degeneracy in this highly frustrated system due to coupling with a crystal lattice and stabilizing a long-range magnetic order [9]. While tiny distortions associated with the spin Jahn-Teller effect are unluckily to be measured by diffraction techniques, our experiments reveal the existence of magnetoelastic coupling in FeTi<sub>2</sub>O<sub>5</sub> and *ab initio* calculations rule out another mechanism of symmetry lowering due to orbital degrees of freedom. In addition, density functional theory calculations unravel a substantial easy-axis anisotropy putting this material in the class of the quasi-1D Ising model, which agrees with the field dependence of magnetization. Exotic properties of Ising systems in the transverse magnetic fields together with a strong magnetoelastic coupling make FeTi<sub>2</sub>O<sub>5</sub> a unique object interesting for further detailed investigation.

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- J. B. Goodenough, Theory of the role of covalence in the perovskite-type manganites [La, *M*(II)]MnO<sub>3</sub>, Phys. Rev. **100**, 564 (1955).
- [2] M. Neupane, P. Richard, Z.-H. Pan, Y.-M. Xu, R. Jin, D. Mandrus, X. Dai, Z. Fang, Z. Wang, and H. Ding, Observation of a novel orbital selective Mott transition in Ca<sub>1.8</sub>Sr<sub>0.2</sub>RuO<sub>4</sub>, Phys. Rev. Lett. **103**, 097001 (2009).
- [3] D. I. Khomskii and S. V. Streltsov, Orbital effects in solids: Basics, recent progress, and opportunities, Chem. Rev. 121, 2992 (2021).
- [4] Y. Yamashita and K. Ueda, Spin-driven Jahn-Teller distortion in a pyrochlore system, Phys. Rev. Lett. 85, 4960 (2000).
- [5] S. Kondo, C. Urano, Y. Kurihara, M. Nohara, and H. Takagi, From the geometrically frustrated antiferromagnets ZnV<sub>2</sub>O<sub>4</sub> and ZnCr<sub>2</sub>O<sub>4</sub> to the heavy-mass Fermi liquid LiV<sub>2</sub>O<sub>4</sub>, J. Phys. Soc. Jpn. **69**(Suppl. B), 139 (2000).

- [6] Y. Kino and B. Lüthi, Magnetic and elastic properties of zincchromite, Solid State Commun. 9, 805 (1971).
- [7] V. Tsurkan, H.-A. Nidda, J. Deisenhofer, P. Lunkenheimer, and A. Loidl, On the complexity of spinels: Magnetic, electronic, and polar ground states, Phys. Rep. 926, 1 (2021).
- [8] F. K. K. Kirschner, R. D. Johnson, F. Lang, D. D. Khalyavin, P. Manuel, T. Lancaster, D. Prabhakaran, and S. J. Blundell, Spin Jahn-Teller antiferromagnetism in CoTi<sub>2</sub>O<sub>5</sub>, Phys. Rev. B 99, 064403 (2019).
- [9] F. Lang, L. Jowitt, D. Prabhakaran, R. D. Johnson, and S. J. Blundell, FeTi<sub>2</sub>O<sub>5</sub>: A spin Jahn-Teller transition enhanced by cation substitution, Phys. Rev. B 100, 094401 (2019).
- [10] J. Varignon, M. Bibes, and A. Zunger, Origins versus fingerprints of the Jahn-Teller effect in *d*-electron *ABX*<sub>3</sub> perovskites, Phys. Rev. Res. 1, 033131 (2019).

- [11] M. S. Senn, J. P. Wright, and J. P. Attfield, Charge order and three-site distortions in the Verwey structure of magnetite, Nature (London) 481, 173 (2012).
- [12] Y. Suzuki and Y. Shinoda, Magnesium dititanate ( $MgTi_2O_5$ ) with pseudobrookite structure: a review, Sci. Technol. Adv. Mater. **12**, 034301 (2011).
- [13] Y. Ohya, Y. Kawauchi, and T. Ban, Cation distribution of pseudobrookite-type titanates and their phase stability, J. Ceram. Soc. Jpn. 125, 695 (2017).
- [14] V. Zapf, M. Jaime, and C. D. Batista, Bose-Einstein condensation in quantum magnets, Rev. Mod. Phys. 86, 563 (2014).
- [15] L. Clark and A. H. Abdeldaim, Quantum spin liquids from a materials perspective, Annu. Rev. Mater. Res. 51, 495 (2021).
- [16] O. V. Maksimova, S. V. Streltsov, and A. N. Vasiliev, Long range ordered, dimerized, large-*D* and Haldane phases in spin 1 chain compounds, Crit. Rev. Solid State Mater. Sci. 46, 371 (2021).
- [17] See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevB.109.184430 for Laue picture of FeTi<sub>2</sub>O<sub>5</sub> single crystal.
- [18] G. Kresse and J. Furthmüller, Efficient iterative schemes for *ab initio* total-energy calculations using a plane-wave basis set, Phys. Rev. B 54, 11169 (1996).
- [19] J. P. Perdew, K. Burke, and M. Ernzerhof, Generalized gradient approximation made simple, Phys. Rev. Lett. 77, 3865 (1996).
- [20] S. L. Dudarev, G. A. Botton, S. Y. Savrasov, C. J. Humphreys, and A. P. Sutton, Electron-energy-loss spectra and the structural stability of nickel oxide: An LSDA + U study, Phys. Rev. B 57, 1505 (1998).
- [21] S. V. Streltsov, O. A. Popova, and D. I. Khomskii, Comment on "Sodium pyroxene NaTiSi<sub>2</sub>O<sub>6</sub>: Possible Haldane spin-1 chain system, Phys. Rev. Lett. **96**, 249701 (2006).
- [22] Z. V. Pchelkina and S. V. Streltsov, *Ab initio* investigation of the exchange interactions in Bi<sub>2</sub>Fe<sub>4</sub>O<sub>9</sub>: The Cairo pentagonal lattice compound, Phys. Rev. B 88, 054424 (2013).
- [23] M. He, B. Winkler, J. D. Bauer, L. Bayarjargal, J. Ruiz-Fuertes, I. Alencar, W. Morgenroth, K. Refson, and V. Milman, Lattice dynamics and Mg/Ti order in orthorhombic pseudobrookitetype MgTi<sub>2</sub>O<sub>5</sub>, J. Alloys Compd. 699, 16 (2017).
- [24] J. M. Law, H. Benner, and R. K. Kremer, Padé approximations for the magnetic susceptibilities of Heisenberg antiferromagnetic spin chains for various spin values, J. Phys.: Condens. Matter 25, 065601 (2013).
- [25] A. A. Katanin, A. A. Katanin, and V. Y. Irkhin, Magnetic order and spin fluctuations in low-dimensional insulating systems, Phys.-Usp. 50, 613 (2007).
- [26] A. Pal, C. H. Huang, T. W. Yen, P. H. Lee, Y. H. Chang, C. H. Yeh, T. W. Kuo, A. Tiwari, D. C. Kakarla, S. M. Huang *et al.*, Spin-induced strongly correlated magnetodielectricity, magnetostriction effect, and spin-phonon coupling in helical magnet Fe<sub>3</sub>(PO<sub>4</sub>)O<sub>3</sub>, Phys. Rev. B **106**, 094404 (2022).
- [27] I. K. Jeong and N. Hur, Local structural distortion induced by antiferromagnetic ordering in Bi<sub>2</sub>Fe<sub>4</sub>O<sub>9</sub> studied using neutron total scattering analysis, J. Korean Phys. Soc. 69, 75 (2016).

- [28] S. Greenwald, The antiferromagnetic structure deformations in CoO and MnTe, Acta Crystallogr. 6, 396 (1953).
- [29] M. Yamashita, M. Akazawa, M. Shimozawa, T. Shibauchi, Y. Matsuda, H. Ishikawa, T. Yajima, Z. Hiroi, M. Oda, H. Yoshida *et al.*, Thermal-transport studies of kagomé antiferromagnets, J. Phys.: Condens. Matter **32**, 074001 (2020).
- [30] Y. Ishitsuka, T. Ishikawa, R. Koborinai, T. Omura, and T. Katsufuji, Comparative studies of the thermal conductivity of spinel oxides with orbital degrees of freedom, Phys. Rev. B 90, 224411 (2014).
- [31] T. Omura, T. Ishikawa, Y. Ishitsuka, and T. Katsufuji, Orbital fluctuations in spinel  $Mn(V_{1-x}Al_x)_2O_4$  studied by thermal conductivity measurements, Phys. Rev. B **86**, 054436 (2012).
- [32] M. Markina, A. Vasiliev, J. Mueller, M. Lang, K. Kordonis, T. Lorenz, M. Isobe, and Y. Ueda, Thermal properties of NaV<sub>2</sub>O<sub>5</sub>, J. Magn. Magn. Mater. **258–259**, 398 (2003).
- [33] B. Ramachandran, K. K. Wu, Y. K. Kuo, and M. S. Ramachandra Rao, Phonon thermal transport and phonon-magnon coupling in polycrystalline BiFeO<sub>3</sub> systems, J. Phys. D: Appl. Phys. 48, 115301 (2015).
- [34] G. Pizzi, V. Vitale, R. Arita, S. Blgel, F. Freimuth, G. Granton, M. Gibertini, D. Gresch, C. Johnson, and T. Koretsune, WAN-NIER90 as a community code: new features and applications, J. Phys.: Condens. Matter 32, 165902 (2020).
- [35] H. Xiang, E. Kan, S.-H. Wei, M.-H. Whangbo, and X. Gong, Predicting the spin-lattice order of frustrated systems from first principles, Phys. Rev. B 84, 224429 (2011).
- [36] R. Coldea, D. A. Tennant, E. M. Wheeler, E. Wawrzynska, D. Prabhakaran, M. Telling, K. Habicht, P. Smeibidl, and K. Kiefer, Quantum criticality in an Ising chain: Experimental evidence for emergent E<sub>8</sub> symmetry, Science **327**, 177 (2010).
- [37] M. Fava, R. Coldea, and S. A. Parameswaran, Glide symmetry breaking and Ising criticality in the quasi-1D Magnet CoNb<sub>2</sub>O<sub>6</sub>, Proc. Natl. Acad. Sci. USA 117, 25219 (2020).
- [38] C. M. Morris, N. Desai, J. Viirok, D. Hvonen, U. Nagel, T. Rõõm, J. W. Krizan, R. J. Cava, T. M. McQueen, S. M. Koohpayeh *et al.*, Duality and domain wall dynamics in a twisted Kitaev chain, Nat. Phys. **17**, 832 (2021).
- [39] Q. Faure, S. Takayoshi, S. Petit, V. Simonet, S. Raymond, L.-P. Regnault, M. Boehm, J. S. White, M. Månsson, C. Rüegg *et al.*, Topological quantum phase transition in the Ising-like antiferromagnetic spin chain BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub>, Nat. Phys. 14, 716 (2018).
- [40] S. K. Niesen, G. Kolland, M. Seher, O. Breunig, M. Valldor, M. Braden, B. Grenier, and T. Lorenz, Magnetic phase diagrams, domain switching, and quantum phase transition of the quasi-one-dimensional Ising-like antiferromagnet BaCo<sub>2</sub>V<sub>2</sub>O<sub>8</sub>, Phys. Rev. B 87, 224413 (2013).
- [41] X. Wang, K. Puzniak, K. Schmalzl, C. Balz, M. Matsuda, A. Okutani, M. Hagiwara, J. Ma, J. Wu, and B. Lake, Spin dynamics of the *E*<sub>8</sub> particles, arXiv:2308.00249.
- [42] S. Suzuki, J.-i. Inoue, and B. K. Chakrabarti, *Quantum Ising Phases and Transitions in Transverse Ising Models*, Lecture Notes in Physics (Springer, Berlin, Heidelberg, 2013), Vol. 862.