High-throughput calculations of antiferromagnets hosting anomalous transport phenomena

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We develop a high-throughput computational scheme based on cluster multipole theory to identify new functional antiferromagnets (AFMs). This approach is applied to 228 magnetic compounds listed in the AtomWork-Adv database, known for their elevated Néel temperatures. We conduct systematic investigations of both stable and metastable magnetic configurations of these materials. Our findings reveal that 34 of these compounds exhibit AFM structures with zero propagation vectors and magnetic symmetries identical to conventional ferromagnets, rendering them potentially invaluable for spintronics applications. By cross-referencing our predictions with the existing MAGNDATA database and published literature, we verify the reliability of our findings for 26 out of 28 compounds with partially or fully elucidated magnetic structures in the experiments. These results not only affirm the reliability of our scheme but also point to its potential for broader applicability in the ongoing quest for the discovery of functional magnets.

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I. INTRODUCTION

In computer organization, the importance of memory hierarchy and non–von Neumann architectures has been increasingly recognized, particularly from the perspective of optimizing computational speed and power consumption. This entails the development of various devices optimized for diverse purposes, and innovative material designs are sought after in the field of materials science. Spintronics is a prominent example which has emerged as a viable option by offering devices that complement or even replace semiconductor-based devices.

More recently, spintronics utilizing antiferromagnets (AFMs) has gained significant attention since they offer distinct advantages over conventional ferromagnets (FMs). These benefits include the absence of stray field, fast response, and robustness against magnetic field noise [\[1–4\]](#page-9-0). However, the detection and control of magnetic structures that maintain time-reversal symmetry (TRS) present challenges, and thus, AFMs breaking TRS are particularly desirable for device applications. The examples include magnetic toroidal orders $[5-7]$ and altermagnets $[8-11]$, a third class of magnets with zero net magnetization and alternating spin splitting in momentum space. These materials hold promising potential for future applications relying on their controllability via electric currents and the spin splitter effects, respectively.

Among these compounds, AFMs with magnetic symmetries identical to those of conventional FMs are particularly valuable for integration into existing FM-based spintronics devices. These *FM-like AFMs*, as we term them in this paper, feature a small canting moment in the presence of spin-orbit coupling. Their AFM domains can be detected as the sign of anomalous transverse transport and manipulated using magnetic fields. A notable example is Mn_3X ($X = Sn$ and Ge) [\[12–15\]](#page-9-0), where recent studies have reported magnetization switching via electric current and tunneling magnetoresistance effects [\[16–20\]](#page-9-0), thereby opening an era of AFM-based spintronics. However, for practical implementation, numerous considerations such as fabrication procedures, operational temperature ranges, resistance to oxidation, and basic performance metrics intersect in a complex manner. Consequently, the exploration of functional AFMs continues to be a critical focus for advancing AFM-based spintronics. Indeed, highthroughput calculations for magnetic materials have been vigorously pursued in recent years [\[21–23\]](#page-9-0). Many of them have focused on specific groups of materials, such as Heusler compounds and two-dimensional materials, and have yet to conduct magnetic symmetry analysis related to the functionality of the AFMs. Moreover, systematic calculations including noncollinear magnetic structures are still challenging, which is required to find the prototype FM-like AFM Mn_3Sn .

In this paper, we performed high-throughput calculations in exploring potential AFMs for spintronics applications. Note that our present scheme considers not only collinear but also noncollinear magnetic structures, which is in clear

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contrast to the previous studies. Here, we utilize the cluster multipole (CMP) method and spin density functional theory (SDFT) calculations to predict stable magnetic structures from input crystal structures [\[24–27\]](#page-9-0). For material prescreening, we consulted the AtomWork-Adv database [\[28\]](#page-9-0), where AFMs known with specified Néel temperature are listed. Subsequent application of the $\text{CMP} + \text{SDFT}$ methodology on selected candidates allowed us to systematically investigate the most stable and metastable AFM configurations. From the energy comparison and the magnetic space group analysis, we identified 8 metallic and 26 insulating FM-like AFMs as among the most stable magnetic structures. Notably, our findings corroborate the efficacy of our computational approach, as they include several known FM-like AFMs such as Mn₃Ir, Mn₃Sn, and Mn₃SnN. While most identified magnetic structures of FM-like AFMs have already been established in experiments, we discovered that MnPtAl and Fe[NCN] are promising candidates for FM-like AFMs, whose magnetic structures are not completely determined by experiments. Furthermore, we proposed a range of metastable FM-like AFMs that could potentially be realized through efforts like chemical doping or synthesis optimization. Regarding the effects of electronic correlation, we also performed an analysis using S DFT + *U* calculations. While we did not discover any new promising FM-like AFM materials, there was considerable overlap between the two sets of calculations. This suggests that the correction from the Hubbard U is not significant, and thus, our scheme including metastable states might be enough to ensure that no potential FM-like AFMs are missed. Our results affirm the effectiveness of our methodology in identifying functional AFMs, even extending to metastable configurations. Future work encompassing a broader spectrum of crystals and magnetic structures with finite propagation vectors could reveal an extensive array of functional AFM compounds.

II. METHODS AND WORKFLOW

We used the $\text{CMP} + \text{SDFT}$ method to identify functional AFMs [\[26\]](#page-9-0). The specific workflow adopted in this paper is outlined as follows: Initially, we selected input crystal structures for analysis from the AtomWork-Adv database. Secondly, magnetic structures were generated for each crystal using the CMP method to serve as initial inputs for SDFT calculations. These calculations were then executed, and their outputs were subjected to magnetic symmetry analysis for further scrutiny. Below, we briefly summarize each part of the workflow.

A. Input crystal structures

Although the $\text{CMP} + \text{SDFT}$ method could accommodate any crystal structure, computational limitation needs a more selective approach to input. For this paper, we confined our analysis to structures cataloged in the AtomWork-Adv database [\[28\]](#page-9-0), provided by the National Institute for Materials Science, for several reasons. First, the database contains abundant materials whose Néel temperatures T_N are established, enabling a targeted focus on high- T_N materials, which is crucial for spintronics applications. Secondly, it includes

both AFMs with established magnetic structures and those where only a Néel transition has been indicated. This makes the database invaluable both for predicting AFMs and as a benchmark for our method.

In practice, we adhere to the following three criteria in selecting crystal structures for analysis: (1) a Néel temperature exceeding 273 K, (2) a unit cell containing between 2 and 24 magnetic atoms, and (3) the absence of disorder or partially occupied sites. Conditions (1) and (2) are related to the limitation of the computational source, as mentioned above. Note that, for the same reason, we consider magnetic structures with zero propagation vector, and thus, the structures with a single magnetic atom in the unit cell do not support AFM states. Since AFMs with finite propagation vectors are commonly observed in experiments, it is anticipated that, in the future, this issue will be addressed combining the CMP method and the downfolding techniques to derive the classical spin models, such as the local force method [\[29–31\]](#page-9-0). Condition (3) is required due to the lack of reliable methods for handling disorder or partial occupancy, such as the coherent potential approximation. While lifting this restriction could be valuable, especially given that chemical substitution is a key strategy for material optimization, we defer this issue to future research. Another point overlooked in this scheme is the impact of finite temperature effects because they cannot be handled in the SDFT calculations. To deal with these effects, we would need to use methods that require more computing cost, such as the disordered local moment method [\[32\]](#page-9-0). Alternatively, we can combine our current scheme with a mapping method to the classical spin models. This approach allows us to conduct spin-wave analysis, akin to crystal structure optimization that considers the finite temperature effects by including the phonon contributions [\[33\]](#page-10-0).

B. Input magnetic structures

In addition to the crystal structures, magnetic structures are required as inputs for SDFT calculations. For this purpose, we employ the CMP expansion method, as outlined in Refs. [\[25,27\]](#page-9-0). This method produces an orthonormal and complete basis set in a 3*N*-dimensional vector space, where *N* represents the number of magnetic atoms considered for the expansion. This basis set can represent any magnetic structure that arises in a given crystal, as it is classified by multipole degrees of freedom and the irreducible representations of the point group symmetry. Notably, as detailed in Ref. [\[26\]](#page-9-0), this basis set effectively represents magnetic structures observed in nature. In fact, >90% of magnetic structures cataloged in the MAGNDATA database $[34,35]$ can be expressed by linear combinations of up to three CMP basis elements. Thus, in this paper, we focus on magnetic structures that can be represented by linear combinations of up to three CMP basis components. For computational feasibility, we adhere to two conditions for these structures: First, as in Ref. [\[26\]](#page-9-0), we limit ourselves to linear combinations of CMP bases that belong to the same multipole rank and irreducible representation. Second, we exclude magnetic structures where equivalent atoms (in terms of Wyckoff positions) have different sizes of local moments. Such configurations are often computationally unstable due to the need for spontaneous symmetry breaking in the charge

density distribution. While such input magnetic structures can give rise to more plausible AFM structures through the selfconsistent iteration, we choose to simplify our model by not considering this possibility.

C. SDFT calculations

For a given input of crystal and magnetic structure, we perform SDFT calculations to obtain the total energies. We use the ATOMATE package for the management of workflow of the high-throughput calculation [\[36\]](#page-10-0), which internally utilizes PYMATGEN, CUSTODIAN, and FIREWORKS libraries [\[37,38\]](#page-10-0). For the electronic structure calculations, we use VASP [\[39\]](#page-10-0). Here, we employ the exchange-correlation functional proposed by Perdew, Burke, and Ernzerhof [\[40\]](#page-10-0), and pseudopotentials with the projector augmented-wave basis [\[41,42\]](#page-10-0). The spin-orbit coupling effect is also considered. The other key setting of the VASP inputs are given as follows: ENCUT = $1.5 \times$ (the highest ENMAX in the POTCAR file), EDIFF = 10^{-5} , SIGMA = 0.05, $LASPH = True$, $AMIX = 0.1$, $AMIX_MAG = 0.4$, $BMIX = 0.0001$, BMIX_MAG = 0.0001 , PREC = Accurate, and NELM = 400. We use the Γ -centered **k** grid generated by the PYMATGEN code with the grid density $= 4000/(number of atoms in the$ unit cell). For the unconverged cases, we try additional calculations with the change guided by the default setting in the CUSTODIAN code. In the case for $SDFT + U$ calculations, we set $U = 3$ eV for all 3*d* transition metal elements and 0 eV for the other elements. The other settings are the same as the SDFT calculations.

In this paper, we deal with all transition elements as magnetic and the other elements as nonmagnetic. Owing to this definition, we treat the rare-earth elements as nonmagnetic although they show magnetic orders in most cases. This is because we consider only materials with high $T_N > 273$ K in this paper, and thus, almost all materials include transition metal elements, as shown in Sec. III A. Even in compounds containing both types of elements, it is a reasonable assumption that only transition metal elements exhibit substantial magnetic moments at elevated temperatures, as commonly seen in rareearth and transition metal oxides. Accordingly, we employ open-core pseudopotentials for rare-earth elements through the calculations.

D. Analysis of outputs

Finally, we analyze the total energies and magnetic structures for each material from the SDFT solutions. Here, we regard a material to be AFM when the output magnetic structures satisfy

$$
\frac{\left\| \sum_{i} \mathbf{m}_{i}^{\text{out}} \right\|}{\sum_{i} \left\| \mathbf{m}_{i}^{\text{out}} \right\|} < 0.05,\tag{1}
$$

where $\mathbf{m}_i^{\text{out}}$ denotes the magnetic moment of the *i* site. Then we identify potential FM-like AFMs by analyzing their magnetic point group symmetries using the SPINSPG package [\[43\]](#page-10-0), built upon SPGLIB [\[44\]](#page-10-0). Note that a small canting moment is generally induced in the presence of spin-orbit coupling if their magnetic point groups are identical to conventional FMs [\[45\]](#page-10-0). However, anomalous Hall transport is allowed regardless of the existence of net magnetization. In this analysis, we use

the input magnetic structures, rather than the outputs, since the self-consistent calculation could break the crystal symmetry due to numerical errors. Instead, we only adopt results where the overlap between the input and output magnetic structures satisfies

> $\overline{}$ $\overline{}$ $\overline{}$ \mid

$$
\frac{\sum_{i} \mathbf{m}_{i}^{\text{in}} \cdot \mathbf{m}_{i}^{\text{out}}}{\sqrt{\sum_{i} \|\mathbf{m}_{i}^{\text{out}}\| \sum_{i} \|\mathbf{m}_{i}^{\text{in}}\|}} \Big| > 0.99. \tag{2}
$$

Note that not only the most stable but also the metastable magnetic structures are considered in the analysis since they are potentially accessible through experimental techniques such as synthesis optimization, chemical doping, and deviceimposed strain. Here, we define the most stable structures as those with a relative energy per magnetic atom ΔE < 0.1 meV, reflecting the numerical accuracy of our highthroughput calculations. Structures with 0.1 meV $\langle \Delta E \rangle$ 20 meV are classified as metastable, which approximates the energy scale of the Néel temperatures under consideration.

III. RESULTS AND DISCUSSION

A. Investigated materials

After applying the selection criteria, 231 material candidates remain for consideration. As anticipated, the vast majority of these materials include 3*d* transition metal elements due to their high Néel temperatures. Indeed, only three exceptions, GeS ($T_N = 455 \text{ K}$) [46], GdI₂ ($T_N = 313 \text{ K}$) [\[47\]](#page-10-0), and hcp-Gd $(T_N = 293 \text{ K})$, are listed in AtomWork-Adv. However, recent literature suggests that GeS may have AFM-like behavior induced by transition metal impurities [\[46\]](#page-10-0), and GdI₂ is FM with a Curie temperature $T_c = 276 \text{ K}$ [\[48,49\]](#page-10-0). Additionally, it is known that hcp-Gd shows FM at the highest transition temperature. Thus, these three materials are simply excluded from subsequent calculations. A mere two substances, BaRuO₃ ($T_N = 430 \text{ K}$) and Sr₂MgReO₆ ($T_N =$ 320 K), are found to contain only 4*d* and 5*d* transition metals as magnetic atoms, respectively. As a result, our following calculations include 226 materials with 3*d*, one with 4*d*, and one with 5*d* transition metal magnetic materials, which are listed in the Appendix.

In the selected materials, Mn is the most prevalent among 3*d* transition metals, appearing 100 times. It is followed by Fe with 76 occurrences, Co with 22, Cr with 11, and Ni appearing 10 times. This distribution aligns well with the tendency of Mn and Fe to adopt high-spin configurations in oxide environments, where ions of 3*d* transition metals typically have valence states of $2+$ or $3+$. Such configurations often lead to strong exchange interactions and high Néel temperatures. It is worth noting that compounds containing Co as well as Fe are renowned for their high Curie temperatures, especially in the context of permanent magnets [\[50\]](#page-10-0). However, in our analysis of AFMs, Co appears only $\sim \frac{1}{4}$ as frequently as Mn. This is likely due to the AFM nature of 3*d* transition metals located to the left of Mn compared with the FM nature of those to the right of Fe [\[51\]](#page-10-0). Therefore, when searching for AFM materials with high Néel temperatures, focusing on Mn-based compounds proves to be the most effective strategy.

In our dataset of 228 materials, several share identical crystal structure prototypes. To understand the structural types more likely to exhibit high Néel temperatures, we performed a prototype analysis. In this paper, two conditions define an equivalence relation for classifying these prototypes: (1) the space group number and (2) the set of atom counts in the unit cell, although exact matching at the Wyckoff positions is not required.

The results are summarized as follows. The most frequently occurring crystal prototype is the $ThCr₂Si₂$ structure with space group $G_{SG} = 14/mmm$, appearing 35 times. Most of them are $R M n_2 S i_2$ and $R M n_2 G e_2$ (R 's are rare-earth elements), and unfortunately, FM-like AFM structures with zero propagation vector are hardly realized in this prototype. The second most common is the HfFe₆Ge₆ structure with G_{SG} = *P*6/*mmm*, appearing 27 times. This structure has been the subject of intense recent study due to its unique properties related to the kagome net of the Fe layer. The third most common is the orthorhombic perovskite $ABO₃$, appearing 18 times, followed by the CeCo₄B, tetragonal CeFeSi, and $HfFe_6Sn_4Ge_2$ structures, each appearing 8 times. The orthorhombic TiNiSi appears 7 times and the NiAs structure 6 times. Among these frequently appearing prototypes, only the $HfFe₆Ge₆$ and $HfFe_6Sn_4Ge_2$ structures can host noncollinear AFMs based on our CMP + SDFT analysis. This suggests that high- T_N , zero-propagation vector, and noncollinear FM-like AFMs are rarely realized in nature. Therefore, collinear AFMs breaking TRS, such as altermagnets, would play a significant role in future spintronics applications. In the following, we will see that the NiAs structure and its derivatives are such promising crystal structures in the search for FM-like AFMs.

C. FM-like AFMs as the most stable structures

Table [I](#page-4-0) shows the FM-like AFMs identified as the most stable magnetic structures in the $\text{CMP} + \text{SDFT}$ method. The 34 materials are listed, where 8 are metals and 26 are insulators, although SDFT calculations sometimes fail to reproduce metallicity due to the approximate treatment of the electronic correlation effects. For 16 of these 34 AFMs, the magnetic structures are already established and listed in the MAGN-DATA database, as indicated in Table [I.](#page-4-0) Only two compounds, LaFeO₃ ht₁ and Nd₂NiO₃ rt, exhibit AFM structures with finite propagation vectors, which are beyond the scope of this paper. However, for 13 out of the remaining 14 compounds, MAGNDATA features at least one magnetic structure that aligns with one of the most stable AFMs determined in our calculations. The sole exception is $La₂NiO₄$ lt, a collinear AFM structure with the magnetic moments aligned parallel to the a axis. In our CMP $+$ SDFT calculations, the closest initial guess has finite components along both the *a* and *c* axes. After self-consistent calculations, this leads to an AFM structure oriented along the *c* axis. Since this structure is different from the one listed in MAGNDATA only in the direction of the magnetic moments, it could potentially be realized by some efforts including a chemical doping. It should be noted that, although FeF₃ rt and LaCrO₃ ht₁ are identified as conventional AFMs in MAGNDATA, these are also reproduced in our calculations as nearly degenerate states.

Even in cases where magnetic structures are not listed in the MAGNDATA database, there are experimental studies providing direct and indirect evidence for their magnetic structures in most cases. After examining the existing literature, it appears that the magnetic structures of Fe[NCN] and MnPtAl are not fully established in the experiments, in which our results offer predictive insights into the potential FM-like AFM structures. A brief discussion of these compounds is presented below.

1. Orthorhombic R**FeO**₃

The orthorhombic perovskites $RFeO₃$, where $R = Pr$, Eu, Y, Er, Tm, Yb, and Gd, are identified as potential FM-like AFMs yet remain unlisted in MAGNDATA. However, these materials are well studied, particularly for their ferroelectric and multiferroic properties. They generally exhibit two types of magnetic transitions. The first type initially forms a G_z -type AFM structure with $G_{\text{MSG}} = Pn'ma'$, followed by a spin-reorientation transition to a G_y -type AFM with $G_{\text{MSG}} =$ $Pn'm'a$. Compounds in this category include $R = Pr$ [\[52–54\]](#page-10-0), Er [\[55–57\]](#page-10-0), Tm [\[58,59\]](#page-10-0), and Yb [\[60–62\]](#page-10-0). The second type undergoes a single magnetic transition to the G_z -type AFM, as in the cases of $R = Y$ [\[63,64\]](#page-10-0), Eu [\[65,66\]](#page-10-0), and Gd [\[65\]](#page-10-0). This fact shows that the two AFM structures are energetically so close that they can interchange with a small energy scale of the temperature effects, and our SDFT calculations correctly capture this feature. Note that, although these AFM states often possess a weak FM component due to the Dzyaloshinskii-Moriya interaction, which is not accounted for in our initial structures, it appears during the self-consistent calculation. As these compounds are insulators, magneto-optical effects are anticipated for their AFM structures, and these have already been observed experimentally $[67,68]$. Note that TlFeO₃ is also indicated to be an FM-like AFM in our calculations. While the specifics of its magnetic structure are likely not well documented, its crystal structure and systematic variations in T_N lead us to expect properties like those of $RFeO₃$ [\[69\]](#page-10-0).

2. **Sr2Fe2O5**

The compound $Sr_2Fe_2O_5$ with space group $G_{SG} = Ima2$ is a brownmillerite oxide. Neutron diffraction experiments suggested that its magnetic structure is consistent with $G_{\text{MSG}} =$ *Im*['] a ['] 2 [\[70,71\]](#page-10-0); however, this result is in contradiction with our computational prediction of the FM-like AFM with $G_{\text{MSG}} = Im'a2'$. The discrepancy arises because our initial guess does not include the experimentally suggested *G*-type AFM structure. The complexity lies in the fact that such a structure demands a linear combination of nonequivalent Fe moments, which belong to different irreducible representations of the point group. To capture such AFM configurations, it will be necessary to expand the search area by relaxing the present constraints.

*3. A***Fe[MoO4]2**

Here, $AFe[MoO₄]₂$, where $A = K$ and Na, are layered molybdates known for their ferroelastic transition from a high-temperature trigonal phase with $G_{SG} = P\overline{3}c1$ to a lowtemperature monoclinic phase with $G_{SG} = C2/c$ [\[72\]](#page-10-0). The frustrated triangular Fe net has prompted interest in their

TABLE I. Summary of FM-like AFMs identified as the most stable magnetic structures found by CMP+SDFT calculations. Substance names follow the notation of Atomwork-Adv database, where polymorphisms are distinguished by the characters following the formula. G_{SG} represents the space group in standard setting and may not be identical to MAGNDATA/Atomwork-Adv in certain cases. $G_{\rm{MSG}}$ represents the magnetic space group of the FM-like AFMs. For systems meeting the criterion $\Delta E < 0.1$ meV, all corresponding G_{MSG} symbols are listed. The Met./Ins. column signifies whether the system is metallic (M) or insulating (I), based on the calculations. A note is added when a system is metallic in calculations but insulating in experimental data $(*M)$. T_N is the experimental Néel temperature, given in Atomwork-Adv. In the MAGNDATA column, $q = 0$ and $q \neq 0$ indicate that a magnetic structure with zero and finite propagation vectors is listed in MAGNDATA, respectively. The compounds with [∗]1 −∗ 4 indicate that no identical material is listed, but chemically substituted materials with the same crystal structure are found. Specifically, *1 refers to La_{0.5}Sr_{0.5}FeO_{2.5}F_{0.5}, *2 to La_{0.33}Sr_{0.67}FeO₃, *3 to Ho_xBi_{1−*x*}FeO₃ (*x* = 0.15, 0.20), and *4 to $Ho_xBi_{1-x}FeO_3$ ($x = 0.05, 0.10, 0.15, 0.20$). The conv. AFM column specifies whether there is a conventional AFM structure also meets the criterion $\Delta E < 0.1$ meV. An asterisk (*) indicates that a conventional AFM is indicated in the experiments. The Consistency column employs two symbols to denote the following: \times represent that a $q = 0$ structure is reported in the experiments, but our method fails to reproduce it as the most stable states; an asterisk (*) indicates that a $q \neq 0$ structure is reported in the experiments, which is beyond the reach of our method. All other entries imply that the magnetic structures have either been partially or fully corroborated by the experiments and are also reproduced by our method.

magnetic properties, and indeed, the multiferroic AFM structures along with electronic polarization for $R = Rb$ have been intensively discussed recently [\[73,74\]](#page-10-0). For the $R = K$ case, coexistence of spin spiral and commensurate AFM structures has been reported, both with finite propagation vectors [\[75\]](#page-10-0), although T_N reported in Ref. [\[75\]](#page-10-0) is 2.5 K, considerably lower than 653 K in Ref. [\[76\]](#page-10-0) referred in AtomWork-Adv. In the Na variant, experimental data on magnetic structures seems to be lacking, but a theoretical investigation suggested a *G*-type AFM with finite propagation vectors as the most stable state [\[77\]](#page-10-0), which our current calculations cannot capture.

4. **FeSht**₂

Here, FeS is characterized as a *p*-type narrow-gap semiconductor and undergoes a structural transition from a high-temperature hexagonal phase (FeS ht₂) with G_{SG} = $P6_3/mmc$ to a low-temperature trigonal phase with G_{SG} =

 $P\bar{6}2c$ [\[78\]](#page-10-0). Although AtomWork-Adv lists an additional phase, FeS ht₁ with $G_{SG} = P6_3mc$, we have chosen to exclude it from consideration in this paper since it includes the distortion accompanied by the Néel transition [\[79\]](#page-10-0). In both highand low-temperature phases, FeS manifests collinear AFM order. Within each Fe layer, the local moments align FM, while they stack AFM along the *c* axis. Additionally, a spin reorientation transition, commonly referred to as the Morin transition, occurs in the low-temperature phase [\[80,81\]](#page-10-0). In this transition, the local moments reorient from being normal to parallel with respect to the *c* axis. The easy-plane AFM structure aligns with the calculated $Cm'c'm$ phase. This phase holds the potential for exhibiting anomalous transport phenomena, a claim recently substantiated through experimental work [\[82\]](#page-10-0).

5. **Fe3BO6**

Here, $Fe₃BO₆$ is an insulator that exhibits a collinear AFM structure with a minor FM component. Like orthoferrites, *RFeO₃*, this compound undergoes a spin reorientation transition between two distinct AFM configurations [\[83,84\]](#page-10-0). In the high-temperature phase, the magnetic moments align AFM along the *c* axis, while two nonequivalent Fe moments within the same c plane couple FM $[85]$. This magnetic structure matches the $G_{\text{MSG}} = Pnm'a'$ configuration listed in Table [I.](#page-4-0) It is anticipated to exhibit anomalous magneto-optical effects, which is in alignment with experimental findings [\[86\]](#page-10-0).

$6.$ **Mn₃SnN</sub>** *and* $AgMn_3N$

Here, Mn_3SnN and $AgMn_3N$ belong to a family of cubic antiperovskite nitrides. This family typically features two types of magnetic structures within the kagome (111) plane: two 120◦ triangular spin textures that are rotated by 90◦ relative to each other [\[87\]](#page-10-0). These configurations are referred to as the Γ_{4g} and Γ_{5g} structures, whose magnetic symmetries are $G_{\text{MSG}} = R\bar{3}m'$ and $R\bar{3}m$, respectively. Although the energy levels of these two states are close due to a result of the sixfold symmetry of magnetic anisotropy and the small spin-orbit couplings, only the Γ_{4g} state exhibits the anomalous Hall effect attributed to nonzero Berry curvature, which has been experimentally observed in Mn_3SnN thin films [\[88,89\]](#page-10-0). More precisely, $AgMn_3N$ initially exhibits the Γ_{5g} structure before transitioning to a mixed phase of $\Gamma_{4g} + \Gamma_{5g}$ states. Conversely, Mn3SnN starts with the mixed state and later transitions to a more complex phase characterized by finite propagation vectors [\[87\]](#page-10-0). Note that our calculations focus solely on states with zero propagation vector and exclude mixed states with different irreducible representations, and thus, an exact match with experimental observations cannot be achieved. Nevertheless, both the Γ_{4g} and Γ_{5g} states are identified as one of the ground state magnetic structures in AgMn₃N, and Γ_{4g} as the ground state and Γ_{5g} as the metastable state in Mn₃SnN. Although accurately estimating the stability of these structures is challenging due to minor differences in energy scales, these results indicate that our scheme reliably finds potentially useful magnetic structures. Note that the magnetic structures and anomalous Hall effects of this Mn3*X*N group have been the subject of intensive theoretical investigation in recent years [\[90](#page-10-0)[,91\]](#page-11-0).

FIG. 1. Magnetic configurations of (a) $G_{\text{MSG}} = Cm'c'm$ structure of Fe[NCN], (b) $G_{\text{MSG}} = Cm'c'm$ structure, and (c) $G_{\text{MSG}} = Cmcm$ structure of MnPtAl.

7. **Fe[NCN]**

Here, Fe[NCN] is recognized as a potent electrode material in Li- and Na-ion batteries [\[92\]](#page-11-0). It crystallizes in a hexagonal lattice with space group $G_{SG} = P6_3/mmc$ at room temperature, featuring Fe²⁺ planes interconnected by linear NCN^{2−} chains. While AFM coupling of Fe atoms has been suggested in prior studies [\[93,94\]](#page-11-0), the exact magnetic structure seems to remain undetermined. Our results, whose magnetic structure is shown in Fig. $1(a)$, indicate that exploring the magnetooptical properties of this material could be quite interesting.

8. **MnPtAl**

Here, MnPtAl is an intermetallic compound with a $Ni₂$ Intype structure, sharing the same crystal arrangement as MnPtGa, known to host a Néel-type skyrmion phase [\[95\]](#page-11-0). Neutron studies suggested that the Mn moments in MnPtAl align FM within the plane and AFM along the *c* axis [\[96\]](#page-11-0). These magnetic moments are perpendicular to the *c* axis, which is in agreement with the $G_{\text{MSG}} = Cm'c'm$ phase predicted in our calculations, shown in Fig. $1(b)$. It is worth noting that, like FeS with the NiAs structure, the in-plane direction of the magnetic moments is critically important; a 30◦ rotation of each spin can transform the FM-like AFM into a conventional AFM, shown in Fig. $1(c)$. Thus, the experimental determination of the local moment directions as well as the observation of anomalous Hall effects is important, although our calculations indicated that the in-plane magnetic anisotropy is not very weak, as no conventional AFM states are found as the nearly degenerate states [\[97\]](#page-11-0).

9. **SrMnO3 4H rt**

Here, $SrMnO₃$ 4H rt is a distorted hexagonal perovskite with $G_{SG} = C222_1$ and is found to have a magnetic structure identical to the $G_{\text{MSG}} = C22'2'_1$ in our calculations. This is consistent with neutron diffraction studies that describe the AFM ordering along the c axis both within the $Mn₂O₉$ dimers and between the corner-sharing $MnO₆$ octahedra, with spins

TABLE II. List of FM-like AFMs identified as metastable magnetic structures found by $\text{CMP}+\text{SDFT}$ calculations. ΔE is the relative energy to the ground state per one magnetic atom of the FM-like AFM structure. The other notations carry the same meaning as in the Table [I.](#page-4-0)

parallel to the *a* axis [\[98,99\]](#page-11-0). Note that a 90° rotated AFM structure also falls under the category of FM-like AFM unlike FeS, Fe[NCN], and MnPtAl structures.

D. FM-like AFMs as the metastable structures

An advantage of the CMP method lies in its ability to systematically assess the magnetic structures with energies of metastable states. Table II outlines FM-like AFM materials that we identified as metastable states; these are characterized by $\Delta E < 20$ meV. Table II shows seven such metastable magnetic structures, with experimental data for three of these materials available in MAGNDATA. Thanks to their small ΔE , we expect that it is possible to realize them given the experimental tunability, finite temperature effects, and the limitation of the accuracy of SDFT. For instance, $Fe₂O₃$ hem exhibits a collinear AFM and undergoes a Morin transition, altering the direction of magnetic moments from in-plane at high temperatures to out-of-plane at low temperatures [\[100\]](#page-11-0). These transitions respectively align well with the $C2'/c'$ and $P\bar{1}$ states in Table II. MnTe rt, which adopts the NiAs structure, serves as another such example. This compound has been reported to exhibit an AFM state with magnetic moments aligned parallel to the $[1\bar{1}00]$ direction, representing a conventional AFM structure [\[101\]](#page-11-0). However, recent research has suggested that strain induced by epitaxial lattice mismatch with a substrate alters the in-plane magnetic anisotropy. Specifically, this leads the magnetic moments to align parallel to the [1120] direction, corresponding to the $Cm'c'm$ state listed in Table II [\[102\]](#page-11-0). In fact, this structure has been the subject of recent study as a typical example of an altermagnet [\[103\]](#page-11-0). These observations demonstrate the effectiveness of our approach in identifying metastable structures.

For the other candidates, we confirmed that the experimental structures do not correspond to FM-like AFMs listed in Table II. Here, we briefly comment on them. CrSb belongs to the NiAs structure and shows staggered AFM along the *c* axis, whose magnetic moments are aligned parallel to the *c* axis [$104,105$]. The *Cm'c'm* structure in Table II is obtained by rotating spins of it to the in-plane. MnSn₃C is known to show complex spin configurations consisting of AFM and AM components with finite propagation vectors, as suggested in Ref. [\[106\]](#page-11-0). Our results show that $R\overline{3}m'$ structure, which is the same as $MnSn₃N$, also lies as a low-energy state. $Ca₂FeMnO₅$ orth₁ is known to show *G*-type AFM structure, whose magnetic moment is parallel to the *c* axis [\[107\]](#page-11-0). Our *Pnm'a'* and $Pn'm'a$ structures correspond to the same AFM structure with the moments perpendicular to the *c* axis like $Ca₂Fe₂O₅$ [\[108\]](#page-11-0). CrSb₂ is known to show collinear AFM structure with a finite propagation vector [\[109\]](#page-11-0), which cannot be accessible in our current scheme. FeSe hp_1 is known to show both AFM and FM-like behavior, depending on temperature and amount of self-intercalation of Se [\[110\]](#page-11-0). Since the origin of the AFM nature of FeSb has not been made clear yet, we may have a chance to realize an FM-like AFM state in hexagonal FeSe.

E. FM-like AFMs in SDFT+*U* **calculations**

Finally, we comment on the results with the SDFT $+ U$ calculations. As widely recognized, strong electronic correlation effects play a critical role in many magnetic materials, especially in oxides, and these effects are not sufficiently captured by standard SDFT. Therefore, we explored the impact of the correlation effects on magnetic structures by performing S DFT + *U* calculations. According to the systematic calculations, we found that, while the inclusion of the Hubbard *U*

TABLE III. Summary of FM-like AFMs identified as the most stable magnetic structures newly found by CMP + SDFT+*U* calculations. The notations carry the same meaning as in Table [I.](#page-4-0) Note that CrSb and MnTe rt are listed in TABLE II.

Substance	$G_{\rm SG}$	$G_{\rm{MSG}}$	Met./Ins.	T_N (K)	MAGNDATA	conv. AFM	consistency
CrSb	$P6_3/mmc$	Cm'c'm	*M	711	$\mathbf{q}=0$	N _o	
Mn ₂ As	P4/nmm	P4/nm'm'	M	582	$q \neq 0$	No	\ast
$Sr_2Co_2O_5$	Ima ₂	Ima'2'	M	535	$q \neq 0$	No	\ast
Fe ₂ As	P4/nmm	Pmm'n', Cmm'a'	M	353	$q \neq 0$	N ₀	\ast
FeGe rt	$P2_13$	$P2'_{1}2'_{1}2_{1}$	M	310	$q \neq 0$	Yes	\ast
MnTe rt	$P6_3/mmc$	Cm'c'm		309	$q=0$	Yes	
NiS ht	$P6_3/mmc$	Cm'c'm		304	$\overline{}$	$*Yes$	

TABLE IV. List of FM-like AFMs identified as metastable magnetic structures newly found by CMP + SDFT+*U* calculations. The notations carry the same meaning as in the Table [II.](#page-6-0) Note that FeS ht₂, Fe[NCN], MnPtAl, and AgMn₃N are listed in Table [I.](#page-4-0)

Substance	G_SG	$G_{\rm{MSG}}$	ΔE (meV)	Met./Ins.	T_N (K)	MAGNDATA
FeS $ht2$	$P6_3/mmc$	Cm'c'm	0.9		599	
Fe[NCN]	$P6_3/mmc$	Cm'c'm	2.4		345	
MnNiGe rt	Pnma	Pnm'a'	1.3	М	336	
$Ba_2Y_2Co_4O_{11}$ rt	Pmmm	Pm'm'm	14.5	М	291	
MnPtAl	$P6_3/mmc$	Cm'c'm	2.5	М	290	
$AgMn_3N$	$Pm\bar{3}m$	$R\bar{3}m'$	0.1	М	281	

TABLE V. List of materials considered in this paper. Remarks for Formula, G_{SG} , and T_N (K) are the same as in Table [I.](#page-4-0)

Formula	G_{SG}	T_N (K)	Formula	G_{SG}	T_N (K)	Formula	G_{SG}	T_N (K)
TIFeO ₃	Pnma	560	Mn_3Sn	$P6_3/mmc$	411	NiS ht	$P6_3/mmc$	304
NdMnSiH	P4/nmm	560	$DyMn_6Sn_4Ge_2$	P6/mmm	411	BaCuLuFeO ₅	P _{4mm}	303
ErFe ₆ Sn ₆	Cmcm	560	TbMnSi rt	Pnma	410	SmCo ₂ P ₂	I4/mmm	302
$HoFe_6Sn_6$ orth	<i>Immm</i>	559	$Ca2MnFeO5$ orth ₁	Pnma	407	BaY_2NiO5	<i>Immm</i>	300
$DyFe6Sn6rt_orth_1$	Cmcm	559	HoCo ₄ B	P6/mmm	404	$La_3Mn_4Sn_4$	<i>Immm</i>	300
$GdFe_6Sn_6$	Cmcm	554	FeGe ht_1	P6/mmm	404	BaNd Mn_2O_6 ht	P4/mmm	300
CuMn ₃ As ₂	Pnma	550	GdTiSi orth	P4/nmm	400	HoMn ₂ Ge ₂	I4/mmm	300
Mn ht ₂ stab	I4/mmm	540	LaMn ₂ Ge ₂	I4/mmm	398	BaMn ₃ O ₆	C2/m	295
DyFeO ₃	Pnma	540	$ScMn_6Sn_4Ge_2$	P6/mmm	397	CuTb ₂ O ₄	I4/mmm	295
$Ca2ReFeO6$ lt	$P2_1/c$	540	$DyMn_6Sn_6$	P6/mmm	395	$LaCrO3$ rt	Pnma	291
$Sr_2Co_2O_5$	Ima ₂	535	Mn_3SnN	$Pm\bar{3}m$	395	$Ba2Y2Co4O11$ rt	Pmmm	291
GdFeO ₃	Pnma	530	Mn_3B_4	Immm	394	MnPtAl	$P6_3/mmc$	290
NiO ht	$Fm\bar{3}m$	526	CeMn ₂ Ge ₂	I4/mmm	393	ErMn ₂ Ge ₂	I4/mmm	290
$Ba_4Fe_9O_{14}[OH]_6$	C2/m	520	$Cr2 As$ rt	P4/nmm	393	$Ba2Dy2Co4O11$ ht	Pmmm	290
$YbMn_2Si_2$	I4/mmm	520	$H_0Mn_6Sn_4Ge_2$	P6/mmm	391	SrMnO ₃ 4H	$P6_3/mmc$	290
$LuMn_6Ge_6$	P6/mmm	518	MnRhSi	Pnma	389	CoO ht	$Fm\overline{3}m$	289
Ho_6Fe_{23}	$Fm\bar{3}m$	515	$ScMn_6Sn_6$	P6/mmm	388	CoO rt	I4/mmm	289
HoCo ₃ Ga ₂	P6/mmm	514	ErCo ₄ B	P6/mmm	387	TbTiSi	P4/nmm	287
TiFe ₆ Ge ₆	P6/mmm	513	GdMnGe	Pnma	382	CeCo ₄ B	P6/mmm	287
TbMnGe	Pnma	510	$FeSn2$ rt	I4/mcm	381	TbTiGe rt	P4/nmm	287
$TbCo3$ ht	$R\bar{3}m$	509	$Sr2Mn2O5$ orth ₁	Pbam	380	CrN lt	Pmmn	285
$TbMn_2Si_2$	I4/mmm	509	MnCoSi rt	Pnma	380	CrN rt	$Fm\overline{3}m$	283
ZrFe ₆ Ge ₆	P6/mmm	509	$Sr_3Fe_2Cl_2O_4$	I4/mmm	378	$AgMn_3N$	$Pm\bar{3}m$	281
Fe ₃ BO ₆	Pnma	508	CeMn ₂ Si ₂	I4/mmm	378	SrMnO ₃ 4Hrt	$C222_1$	280
LuMn ₂ Ge ₂	I4/mmm	508	NdMn ₂ Si ₂	I4/mmm	377	$TmMn_6Sn_6$	P6/mmm	280
$DyMn_2Si_2$	I4/mmm	506	$HoMn_6Sn_6$	P6/mmm	376	Fe ₂ RuSi	$Fm\overline{3}m$	280
GdCo ₄ B	P6/mmm	505	$LuMn_6Sn_6$	P6/mmm	373	$TiFe2$ rt	$P6_3/mmc$	278
$TmMn_2Si_2$	I4/mmm	498	V_2WO_6	$P4_2/mnm$	370	NiBiO ₃	$P\bar{1}$	278
DyFe ₆ Ge ₆	Cmcm	497	$PrMn_2Si_2$	I4/mmm	369	CuHo ₂ O ₄ hp	I4/mmm	278
$Fe2O3$ orth	Pna2 ₁	495	$BaTbMn2O6$ rt	$P2_1/m$	367	CrSb ₂	Pnnm	275
$Sr3Cu2Fe2Se2O5$	I4/mmm	490	FeSn	P6/mmm	367	YFe ₂ Si ₂	I4/mmm	275

TABLE V. (Continued.)

does affect the energy levels of various magnetic states, it does not significantly change their order in most materials. Indeed, we identified only seven FM-like AFMs as ground states that are not found in the SDFT calculations, as shown in Table [III.](#page-6-0) Of these, two are also identified as metastable states in the SDFT calculations. Among the remaining five materials, four have established AFM structures listed in MAGNDATA, all of which have finite propagation vectors and thus fall outside the scope of our current scheme. The last one, NiS ht with the NiAs structure, is known in experiments to be an AFM oriented along the *c* axis [\[111\]](#page-11-0). This state is indeed found in our calculations as one of the most stable magnetic structures; however, it is a conventional AFM.

The results for metastable states are shown in Table [IV.](#page-7-0) Our calculations identify six FM-like AFMs not identified as metastable states in the SDFT calculations, while four of them are already listed as the most stable magnetic structures in the SDFT calculations. The remaining two are MnNiGe rt and $Ba_2Y_2Co_4O_{11}$ rt. MnNiGe shares the same crystal structures as NbMnP, in which the anomalous Hall effect in an AFM state has been recently observed [\[112\]](#page-11-0). However, MnNiGe is known to be an AFM with a finite propagation vector, making it outside what our calculations can handle [\[113\]](#page-11-0). Similarly, $Ba_2Y_2Co_4O_{11}$, a layered perovskite, is also known to be an AFM with a finite propagation vector, again exceeding the

bounds of our current approach [\[114\]](#page-11-0). In summary, while certain materials have been recognized through the $SDFT + U$ calculations, the majority coincide with those identified in SDFT calculations, suggesting that the incorporation of *U* exerts small influence on the stability of magnetic structures, particularly when metastable states are also considered in the evaluation.

IV. CONCLUSIONS

In this paper, we have introduced a high-throughput computational framework utilizing CMP theory and SDFT calculations to systematically identify functional AFMs suitable for spintronics applications. We applied this approach to 228 magnetic compounds cataloged in the AtomWork-Adv database, renowned for their elevated Néel temperatures. Our systematic investigations yielded 34 compounds that display AFM structures with zero propagation vectors, featuring magnetic symmetries identical to conventional FMs. Among these, 9 are metallic and 25 are insulating, and our results include known FM-like AFMs such as Mn_3Sn and Mn_3SnN . Furthermore, we identified MnPtAl and Fe[NCN] as promising yet experimentally undetermined candidates for FM-like AFM materials. By cross-referencing our theoretical predictions with existing experimental data from the MAGNDATA database and published literature, we confirmed the accuracy of our findings for 26 out of the 28 compounds that have been partially or fully characterized in experiments. This validation not only attests to the reliability of our computational scheme but also hints at its broader applicability in the continuous endeavor to discover functional magnetic materials. Importantly, our method has also uncovered a range of metastable FM-like AFM structures that could be experimentally realized through techniques such as chemical doping or synthesis optimization.

In summary, we have established a solid foundation for future research that could expand the scope to include a wider variety of crystal structures and magnetic arrangements with finite propagation vectors, thereby opening avenues for the discovery of functional AFM materials

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APPENDIX: LIST OF ALL MATERIALS

This Appendix shows the summary of materials we considered in this paper. These are listed in the AtomWork-Adv database and satisfy (1) a Néel temperature exceeding 273 K, (2) a unit cell containing between 2 and 24 magnetic atoms, and (3) the absence of disorder or partially occupied sites. The results are shown in Table [V.](#page-7-0)

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