

**Strain-tunable half-metallicity in  $VSe_2/Sc_2CO_2$  van der Waals heterostructures**Lingling Song<sup>1,\*</sup>, Runlong Ye<sup>1</sup>, Chen Su<sup>1</sup>, Canglong Wei<sup>1</sup>, Dongdong Chen,<sup>1</sup>  
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(Received 6 December 2023; revised 22 February 2024; accepted 23 February 2024; published 12 March 2024)

The quest for advancing the development of next-generation nanospintronic devices has propelled extensive research into the realization and control of half-metallicity in 2D materials. Here, the multiferroic  $VSe_2/Sc_2CO_2$  vdW heterostructures are theoretically investigated by using density functional theory to search for half-metallicity. Our theoretical exploration reveals that the  $VSe_2$  layer showcases a unique capability to transit between semiconducting and half-metallic behavior by precisely manipulating the ferroelectric polarization states of the  $Sc_2CO_2$  layer. We further delve into the diverse electronic properties of the  $VSe_2$  layer within the heterostructure, employing uniaxial tensile strain engineering to investigate its behavior in both the semiconductor and half-metallic states. In the semiconductor state, this electronic property of the  $VSe_2$  layer remains unchanged with strain. In contrast, in the half-metallic state, the  $VSe_2$  layer undergoes a fascinating modulation, transiting from the spin-down half-metal to the metal and then to the spin-up half-metal as the strain increases from 0% to 6%. This intriguing phenomenon is elucidated by the intricate rearrangement of the inner V atomic orbitals in response to strain.

DOI: [10.1103/PhysRevB.109.094105](https://doi.org/10.1103/PhysRevB.109.094105)**I. INTRODUCTION**

Half-metallicity exhibits an exceptional feature, which demonstrates a metallic behavior in one spin channel and an insulating behavior in the other, leading to great potential in spintronics [1–6]. Since the initial discovery of NiMnSb Heusler alloys [4], half-metallicity have been observed in a range of other materials, like double perovskite [7], metallic oxide [8], metal-doped diluted magnetic semiconductor [9,10], etc. Especially, the widespread emergence of many two-dimensional (2D) materials has promoted the investigation and application of half-metallicity within the realm of 2D spintronics, such as graphene [11,12], black phosphorus [13], carbon nitride [14,15], MXene [16–18], transition-metal dichalcogenides (TMDs) [19,20]. In particular, the 2H- $VSe_2$  crystal as one of the classical TMDs has been observed to exhibit a robust ferromagnetic (FM) order that remains stable even above room temperature [21]. Extensive experiments have successfully synthesized monolayer 1T- $VSe_2$ , and it has been found that infrared radiation can induce a phase transformation from 1T to 2H in  $VSe_2$  samples [22]. This suggests that 2H- $VSe_2$  is a promising spintronics material. Nevertheless,  $VSe_2$  is inherently a magnetic semiconductor rather than a half-metal, which causes significant difficulty for direct application as half-metallic devices.

There are many effective strategies to achieve and potentially control half-metallicity in 2D materials, like vertical integration [23], substituted doping [24], adsorption [25], and strain tuning [26,27]. Among them, by combining different 2D materials in a single stack, forming van der Waals (vdW) heterostructure [28,29], offers unparalleled platforms for discovering new physics, which are not found in a single 2D material. Especially, the integrating vdW heterostructure by single-component 2D TMDs and ferroelectric materials is a very novel pathway to produce half-metallic states. When  $VSe_2$  comes into contact with ferroelectric materials, the transition between the half-metallic and semiconducting states in  $VSe_2$  layer is achieved by the ferroelectric polarization reversal of the ferroelectric material [30,31]. More recently, it has been demonstrated that Janus 2H- $VSeTe$  can be modulated from spin-up half-metal to spin-down half-metal as the biaxial strain varies from  $-13\%$  to  $10\%$  [32]. Recent research has revealed that applying tensile or compressive strain within the range of  $-6\%$  to  $6\%$  can transform the monolayer  $CrS_2$  in the 1T' phase into a spin-up or spin-down half-metal [33]. Such tunable half-metallic property about spin polarization is critical for spintronic applications.

One of the conventional approaches for altering the spin polarization orientation involves the introduction of an external magnetic field, which is not easy to operate at the nanoscale. Research shows that the spin-polarization direction of half-metal is invertible in  $MnPSe_3$  as a bipolar magnetic semiconductor (BMS) when the doping type changes from electron to hole doping [34]. However, in practical applications, achieving precise control over carrier concentration in

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2D materials is a significant challenge. Instead of relying on external electrical or magnetic fields, strain engineering in TMDs offers an effective and convenient approach to manipulate the spin polarization of 2D magnetic materials.

In this paper, we propose a 2D multiferroic heterostructure by stacking of a VSe<sub>2</sub> monolayer over a ferroelectric Sc<sub>2</sub>CO<sub>2</sub> monolayer, which is chosen for its inherent out-of-plane ferroelectric polarization and its favorable lattice compatibility with the VSe<sub>2</sub> monolayer. The electronic properties of multiferroic VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> vdW heterostructures are systematically investigated by using density functional theory (DFT). We find that altering the ferroelectric polarization of Sc<sub>2</sub>CO<sub>2</sub> enables flexible tuning of the electronic band structure of VSe<sub>2</sub>, transiting it between semiconductor and half-metal. It is further shown that the uniaxial tensile strains along the along the *x* axis can induce a transition from spin-down half-metal to metal to spin-down half-metal in VSe<sub>2</sub> layer of VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P ↑ heterostructure. These results provide valuable insights into control for 2D materials and its immense potential for applications in advanced electronics and spintronics.

## II. COMPUTATIONAL METHODS

The geometrical optimizations and the spin-resolved electronic structure calculations were performed with the Vienna *Ab initio* Simulation Package (VASP) [35], within the generalized gradient approximation (GGA) in the parametrization of Perdew-Burke-Ernzerhof (PBE) [36]. The interactions between valence electrons and ionic cores were described with the projector augmented wave (PAW) method [37]. A kinetic energy cutoff of 500 eV was set for the plane wave basis set. Moreover, to eliminate interactions between two neighboring vdW heterostructures, a vacuum region of around 20 Å was used along the direction perpendicular to the 2D layers. Geometrical structures were relaxed with the residual force less than 0.02 eV/Å, and the total energies were converged to 10<sup>-6</sup> eV. The integration over the Brillouin zone was carried out using 13×7×1 Monkhorst-Pack k-point grid for the rectangular supercell. In addition, the semiempirical correction scheme of Grimme, DFT-D2 [38], was applied to treat the vdW weak interaction for all stacking configurations. A dipole correction was implemented to mitigate the influence of the vacuum electric field. Considering that the localized V-3*d* orbitals have a significant effect on the electronic structure of the heterostructure, the GGA+*U* method is also employed for the magnetic calculations. Based on recent research on VSe<sub>2</sub>, the on-site Coulomb energy *U* and exchange parameter *J* were assigned values of 2 eV and 0.84 eV, respectively [39–41].

## III. RESULTS AND DISCUSSION

Figures 1(a) and 1(b) depict the top and side views of the monolayer structures of 2H-VSe<sub>2</sub> and Sc<sub>2</sub>CO<sub>2</sub>, respectively, revealing their honeycomb-like structure akin to graphene. Specially, we note that a lower-energy structure made of trimers of carbon atoms has been proposed for Sc<sub>2</sub>CO<sub>2</sub> [42], which suggests that the ferroelectric phase [43] is not the most stable structure. However, since the energy barrier between these two phases reaches 0.445 eV per primitive cell, the

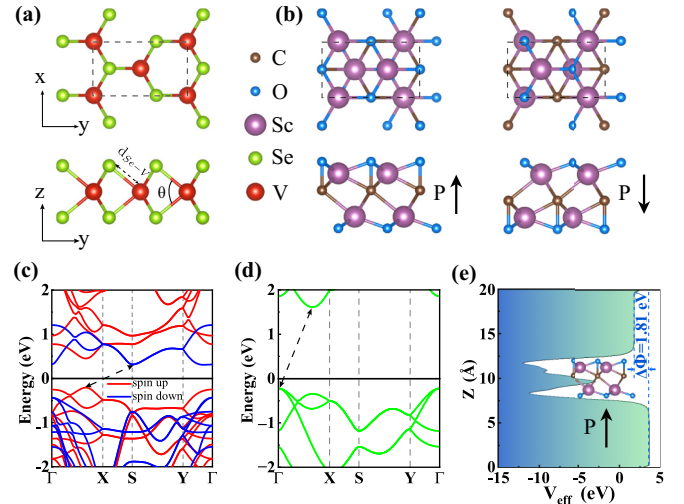


FIG. 1. The top and side views of the 2D structure of monolayer 2H-VSe<sub>2</sub> (a) and monolayer Sc<sub>2</sub>CO<sub>2</sub> (b), respectively. The unit cell is denoted by a rectangle drawn with solid grey lines. All structures have undergone complete optimization. Band structure of monolayer 2H-VSe<sub>2</sub> (c) and monolayer Sc<sub>2</sub>CO<sub>2</sub> (d). The Fermi level is set to zero. (e) The effective potentials ( $V_{\text{eff}}$ ) along the vertical *z* direction to the monolayer Sc<sub>2</sub>CO<sub>2</sub>, in which  $\Delta\Phi$  represent potential difference.

ferroelectric phase is practically attainable and can be used for constructing ferroelectric tunnel junctions [42]. After the appropriate structural relaxation, the in-plane lattice constants of the VSe<sub>2</sub> monolayer are determined to be  $a_1 = 3.34$  Å and  $b_1 = 5.79$  Å. The corresponding lattice constants for the Sc<sub>2</sub>CO<sub>2</sub> monolayer are found to be  $a_2 = 3.44$  Å and  $b_2 = 5.95$  Å. These values are consistent with findings that have been reported [2,30,44]. The 2D vdW VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> multiferroic heterostructure is achieved by vertically stacking monolayer VSe<sub>2</sub> and Sc<sub>2</sub>CO<sub>2</sub>. The lattice mismatch, referred to as  $\eta$ , is calculated using the formula  $\eta = \frac{a_2 - a_1}{0.5(a_1 + a_2)} \times 100\%$ . In this case, the calculated lattice mismatch is found to be less than 3%, which falls within the acceptable range for the fabrication of vdW heterostructures.

For the electronic properties, Figs. 1(c) and 1(d) present the band structures of freestanding 2H-VSe<sub>2</sub> monolayer and Sc<sub>2</sub>CO<sub>2</sub> monolayer, respectively. Obviously, the 2H-VSe<sub>2</sub> monolayer is a BMS with a band gap of 0.52 eV. Specifically, the valence band maximum (VBM) originates from the spin-up channel, while the conduction band minimum (CBM) in the spin-down channel is below the CBM in the spin-up channel. This observation is in agreement with prior research [45,46]. Sc<sub>2</sub>CO<sub>2</sub> exhibits nonmagnetic insulator behavior with a band gap of 1.84 eV. Additionally, monolayer Sc<sub>2</sub>CO<sub>2</sub> has been theoretically proposed as an out-of-plane polarized material, and the intrinsic dipole introduces an electrostatic potential difference  $\Delta\Phi = 1.81$  eV between the two surfaces of Sc<sub>2</sub>CO<sub>2</sub>, as shown in Fig. 1(e). Thus, there are two dynamically stable ferroelectric states in Sc<sub>2</sub>CO<sub>2</sub>, and the polarized state is denoted as P ↑ or P ↓, as shown in Fig. 1(b).

In the vertical VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> multiferroic heterostructure, the ferromagnetic VSe<sub>2</sub> can combine with the P ↑ (P ↓) state of the ferroelectric Sc<sub>2</sub>CO<sub>2</sub>, resulting in the formation of a

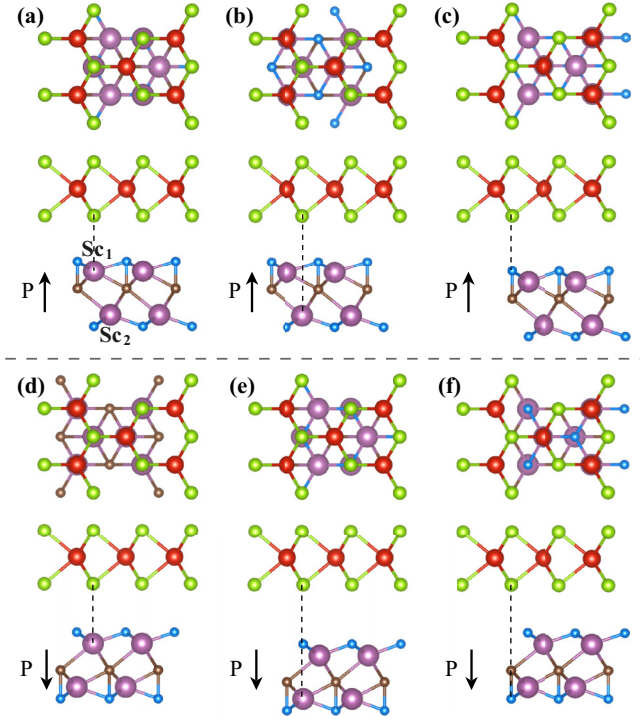


FIG. 2. [(a)–(f)]  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  vdW heterostructures featuring diverse stacking configurations under different polarization states. For A, B, and C stacking configurations, the  $P \uparrow$  and the  $P \downarrow$  states are shown in (a)–(c) and (d)–(f), respectively.

heterostructure of  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  ( $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$ ). For the  $\text{Sc}_2\text{CO}_2$   $P \uparrow$  heterostructure, three different stacking configurations, denoted as A, B, and C are considered [see Figs. 2(a)–2(c)]. The three configurations are detailed as follows: in the  $z$  direction, the Sc atoms from  $\text{Sc}_2\text{CO}_2$  in the upper layer are defined as  $\text{Sc}_1$ , and those in the lower layer are defined as  $\text{Sc}_2$ . For the A configuration, the Se atoms in  $\text{VSe}_2$  monolayer are directly above the  $\text{Sc}_1$  atoms in the unit cell. For the B configuration, the Se atoms are directly above the  $\text{Sc}_2$  atoms. For the C configuration, the Se atoms sit on the top of the vertical C-O bonds. Similarly, for the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$  heterostructure, three additional stacking configurations are shown in Figs. 2(d)–2(f).

In order to check the stability of the heterostructures, the binding energy  $E_b$  of the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  vdW heterostructure is calculated using the formula  $E_b = (E_{\text{VSe}_2/\text{Sc}_2\text{CO}_2} - E_{\text{VSe}_2} - E_{\text{Sc}_2\text{CO}_2})/S$ , where  $E_{\text{VSe}_2/\text{Sc}_2\text{CO}_2}$ ,  $E_{\text{VSe}_2}$  and  $E_{\text{Sc}_2\text{CO}_2}$  are the energy of the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  heterostructure,  $\text{VSe}_2$  and  $\text{Sc}_2\text{CO}_2$  monolayer, respectively, and  $S$  is the in-plane surface area of the considered heterostructure. The optimal interlayer distance is the one that falls within the appropriate range for achieving the minimum binding energy. Based on first-principle calculations, the binding energy  $E_b$  and the respective optimal interlayer distance  $d$  of the combined systems for all stacking configurations are listed in Table I. Negative  $E_b$  values and smaller  $d$  values indicate the energetic stability and strong physical interactions between  $\text{VSe}_2$  and  $\text{Sc}_2\text{CO}_2$  monolayer. The most stable structure for  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  is A configuration, while the most stable structure for  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$  is C configuration, and the

TABLE I. Interface binding energies ( $E_b$ ) and interlayer distance ( $d$ ) of different stacking modes for  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  heterostructures.

Configuration	$\text{VSe}_2/\text{Sc}_2\text{CO}_2 \uparrow$		$\text{VSe}_2/\text{Sc}_2\text{CO}_2 \downarrow$	
	$E_b$ (meV/Å <sup>2</sup> )	$d$ (Å)	$E_b$ (meV/Å <sup>2</sup> )	$d$ (Å)
A	−169.70	2.72	−152.19	3.50
B	−164.24	2.75	−152.59	2.87
C	−163.85	2.75	−154.15	2.85

top and side views of corresponding structures are shown in Figs. 4(a) and 4(b) (see below). Thus, we focus on the two most stable  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  heterostructures as the main research objects in the following calculation.

Besides, three possible magnetic configurations including the FM, stripe-antiferromagnetic (AFM), and zigzag-AFM are considered within the  $2 \times \sqrt{3} \times 1$  supercell as depicted in Figs. 3(a)–3(c). The relative energies ( $\Delta E_m = E_{\text{AFM}} - E_{\text{FM}}$ ) of the FM, stripe-AFM, and zigzag-AFM structures, are shown in Table II. By GGA/PBE calculations, the energy difference between the AFM and FM ground states is always positive, suggesting that the FM ground state is more stable in the proposed  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  heterostructures for both the polarization states.

Now, the calculated projected band structures of the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  and  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$  heterostructures are displayed in Figs. 4(c) and 4(d). After constructing vdW heterostructures, the  $\text{VSe}_2$  layer still exhibits a significant spin polarization in its projected bands, while the spin-up and spin-down projected bands of the  $\text{Sc}_2\text{CO}_2$  layer are nearly degenerate in energy. In the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  case, the electronic states originating from the  $\text{VSe}_2$  layer are energetically downshifted and cross the Fermi level compared to those of the free standing  $\text{VSe}_2$  monolayer. Conversely, the electronic states originating from the  $\text{Sc}_2\text{CO}_2$  layer are energetically upshifted and cross the Fermi level compared to those of the free standing  $\text{Sc}_2\text{CO}_2$  monolayer. Consequently,  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  exhibits metallic properties, specifically with a half-metallic characteristic in the  $\text{VSe}_2$  layer and a metallic property in the  $\text{Sc}_2\text{CO}_2$  layer. Interestingly, the electronic structures of the heterostructure almost show the superposition of the electronic states of the  $\text{VSe}_2$  and  $\text{Sc}_2\text{CO}_2$  monolayer in the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$  case, a common band

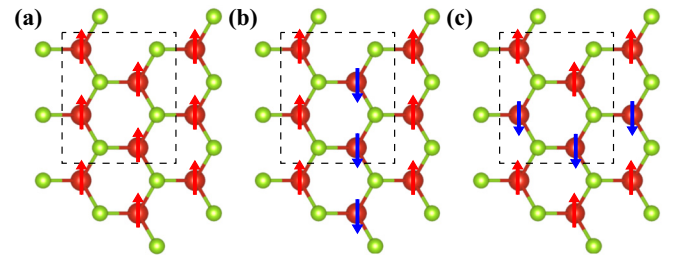


FIG. 3. Different magnetic couplings between V atoms in the  $\text{VSe}_2$  monolayer and the proposed  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  heterostructures. The red and blue arrows represent the spin-up and spin-down directions of V atoms, respectively. (a) The FM, and the two AFM configurations: (b) stripe-AFM, (c) zigzag-AFM.

TABLE II. The energy difference per primitive cell ( $\Delta E_m$ ) between FM and AFM order in the the monolayer  $\text{VSe}_2$  and  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  heterostructures. A zero value of  $\Delta E_m$  represents the magnetic ground state.

Magnetic configuration		FM	stripe-AFM	zigzag-AFM
$\Delta E_m$ (meV)	monolayer $\text{VSe}_2$	0.0	106.0	108.9
	$\text{VSe}_2/\text{Sc}_2\text{CO}_2 \uparrow$	0.0	65.7	123.9
	$\text{VSe}_2/\text{Sc}_2\text{CO}_2 \downarrow$	0.0	103.2	106.9

gap is retained and the heterostructure exhibits semiconductor behavior. In short, the  $\text{VSe}_2$  transforms from a semiconductor to a half-metal together with the switching from the  $P \downarrow$  to the  $P \uparrow$  state in the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  system. Given the metallic nature of the  $P \uparrow$  vdW heterostructure, it is believed that manipulating the polarization direction of the ferroelectric layer becomes challenging due to screening effects from free electrons. Thus, this would ruin the functionality of the ferroelectric layer. However, such a situation is only limited to bulk ferroelectric metals. Cobden *et al.* proposed that a thin enough polar metal can be sufficiently penetrated by an electric field to have its polarity switched [47] and confirmed it experimentally with a ferroelectric bilayer  $\text{WTe}_2$ . A later experimental work by Chen *et al.* also confirms this conclusion [48]. These pioneering studies demonstrate the possibility of manipulating the polarization direction of 2D ferroelectric metals with an electrical field.

The observed switching behavior can be attributed to the different charge transfer across the interfaces of the  $\text{VSe}_2$  and  $\text{Sc}_2\text{CO}_2$  contacts, when the ferroelectric polarization is switched between the  $P \uparrow$  and  $P \downarrow$  states. The presence of different vacuum levels on the two surfaces of the ferroelectric  $\text{Sc}_2\text{CO}_2$  layer results in the existence of two distinct work functions [49]. For two insulators stacked together, charge transfer occurs only when the CBM of one material falls below the VBM of the other material, resulting from the relative shift in the energy bands of the two materials [50]. Exploring the  $\text{Sc}_2\text{CO}_2$  monolayer in different polarization states when

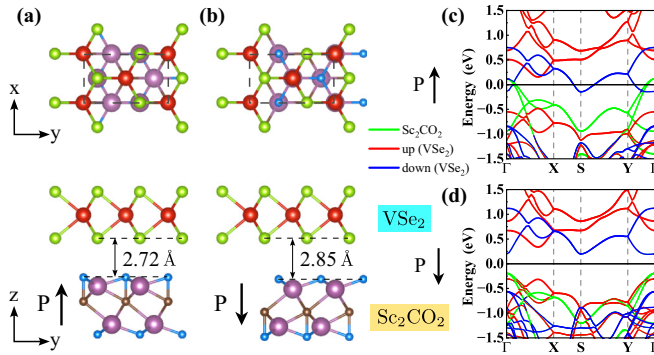


FIG. 4. (a) and (b) are the top and side views of A configuration of  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  vdW heterostructures and C configuration of  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$  vdW heterostructures, respectively. Spin-resolved projected band structure of (c) A configuration of  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  vdW heterostructure and (d) C configuration of  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$  vdW heterostructure. The Fermi level is set to zero.

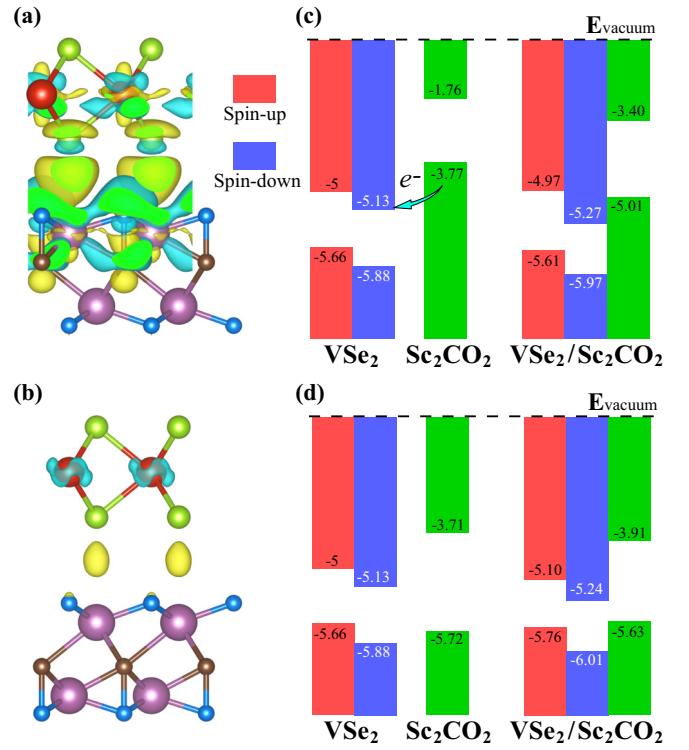


FIG. 5. The three-dimensional isosurface of the electron density difference of the multiferoic system with  $P \uparrow$  (a) and  $P \downarrow$  (b) states, respectively, where the yellow and blue areas represent electron accumulation and depletion, respectively. Band alignments for  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$  with ferroelectric polarization of  $P \uparrow$  (c) and  $P \downarrow$  (d), respectively, of isolated layers (left panel) and that after forming heterostructure (right panel). The energies are displayed in the unit of eV.

forming vdW heterostructures, as depicted in Figs. 5(a)–5(d), reveals distinctive charge transfer characteristics. When  $\text{VSe}_2$  is combined with  $\text{Sc}_2\text{CO}_2$   $P \uparrow$ , a notable charge transfer occurs as the VBM of  $\text{Sc}_2\text{CO}_2$  becomes energetically higher than the spin-down CBM of  $\text{VSe}_2$ . The electrons in the VBM of  $\text{Sc}_2\text{CO}_2$  are sufficiently energetic to transit to the CBM of  $\text{VSe}_2$ . As shown in the 3D isosurface of the electron density difference of  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \uparrow$  heterostructure in Fig. 5(a), numerous electrons accumulate around the  $\text{VSe}_2$  layer. Following our computations, the Bader charge analysis indicates a charge transfer of  $0.11 e$  per cell during the formation of the heterostructure. As the spin-down CBM is lower than the spin-up CBM, electrons from  $\text{Sc}_2\text{CO}_2$  predominantly migrate to the spin-down CBM of  $\text{VSe}_2$ . Due to the restricted quantity of electrons introduced into  $\text{VSe}_2$  layer, almost no electrons occupy the spin-up CBM, resulting the spin-up CBM still above the Fermi level. As a result, the  $\text{VSe}_2$  layer demonstrates half-metallic characteristics, as demonstrated in Fig. 5(c). In contrast, in the  $\text{VSe}_2/\text{Sc}_2\text{CO}_2$   $P \downarrow$  case, the VBM of  $\text{Sc}_2\text{CO}_2$  is not higher than the CBM of  $\text{VSe}_2$ , as depicted in Fig. 5(d). The built-in electric field caused by the difference in work function [50], with a vector pointing from  $\text{Sc}_2\text{CO}_2$  layer to  $\text{VSe}_2$  layer, induces a displacement of the energy bands in opposite directions for two materials. However, since no charge transfer occurs between two materials shown in Fig. 5(b), such

TABLE III. Binding energies ( $E_b$ ) in of the heterostructures in the P  $\uparrow$  and P  $\downarrow$  states under tensile strain from 0% to 6%.

Strain (%)		0	1	2	3	4	5	6
$E_b$ (meV/ $\text{\AA}^2$ )	VSe <sub>2</sub> /Sc <sub>2</sub> CO <sub>2</sub> $\uparrow$	-169.7	-167.4	-165.2	-163.1	-161.3	-159.9	-158.8
	VSe <sub>2</sub> /Sc <sub>2</sub> CO <sub>2</sub> $\downarrow$	-156.7	-154.1	-151.1	-147.8	-144.3	-140.6	-136.8

effect is still insufficient to close the common band gap in the VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\downarrow$  heterostructure.

More interestingly, external factors, such as mechanical strain, can effectively and significantly modulate the electronic properties of 2D materials [27,51]. Therefore, we systematically investigate the evolution of the electronic properties of the heterostructure by in-plane uniaxial tensile strain  $\varepsilon$  along the  $x$  axis. For strain  $\varepsilon$ , it can be defined as  $\varepsilon = (a - a_1)/a_1 \times 100\%$ , where  $a$  represents the equilibrium lattice constant with strain application. The binding energy  $E_b$  of the VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> vdW heterostructure in the P  $\uparrow$  and P  $\downarrow$  states under strains are calculated for stability analysis. The calculated values (all negative) are presented in Table III, highlighting the energetic stability of the P  $\uparrow$  and the P  $\downarrow$  states. Figures 6(a)–6(d) and 6(f)–6(i) show the calculated projected band structures of the P  $\uparrow$  and P  $\downarrow$  heterostructures within a slight strain range from 0% to 6%, respectively. In the case of VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\downarrow$ , the semiconductor nature is well preserved as  $\varepsilon$  increases from 0% to 6%. In the case of VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\uparrow$ , the electronic properties of the Sc<sub>2</sub>CO<sub>2</sub> layer are strain insensitive, consistently demonstrating metallic properties and intrinsic spin degeneracy. In contrast, the VSe<sub>2</sub> layer exhibits more pronounced strain-dependent properties. When no strain is applied, as mentioned above, VSe<sub>2</sub> is in spin-down half-metallic states. As the strain is increased,

the energy levels of CBM for spin-up and spin-down channels undergo different changes. Specifically, for the spin-up channel, the CBM moves towards lower energy and intersects with the Fermi level at approximately 2.8% strain, after which it continues to decrease. For the spin-down channel, the CBM moves towards higher energy and just fails to approach the Fermi level at 4.7% strain, beyond which it continues to increase. Consequently, between 2.8% and 4.7% strain, the VSe<sub>2</sub> remains as a metal. When the tensile strain is higher than 4.7%, it transforms into a spin-up half-metal. The VSe<sub>2</sub> layer undergoes an interesting conversion from spin-down half-metal to metal to spin-up half-metal within the entire range from 0% to 6%. Thus, the spin polarization reversal of the 2D VSe<sub>2</sub> layer in VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\uparrow$  can be controlled by applied strain, making it very attractive for spintronics applications.

By employing strain engineering, significant modifications can be observed in the projected band structures of VSe<sub>2</sub> within two heterostructures. For more accurate description, we selected the CBM of two spin channels for VSe<sub>2</sub> as a function of strain in the VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\uparrow$  and VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\downarrow$  heterostructures, as illustrated in Figs. 6(e) and 6(j), respectively. In terms of the energy position relative to its two spin channel CBMs and the Fermi level, the two heterostructure cases are different. For the P  $\uparrow$  heterostructure,

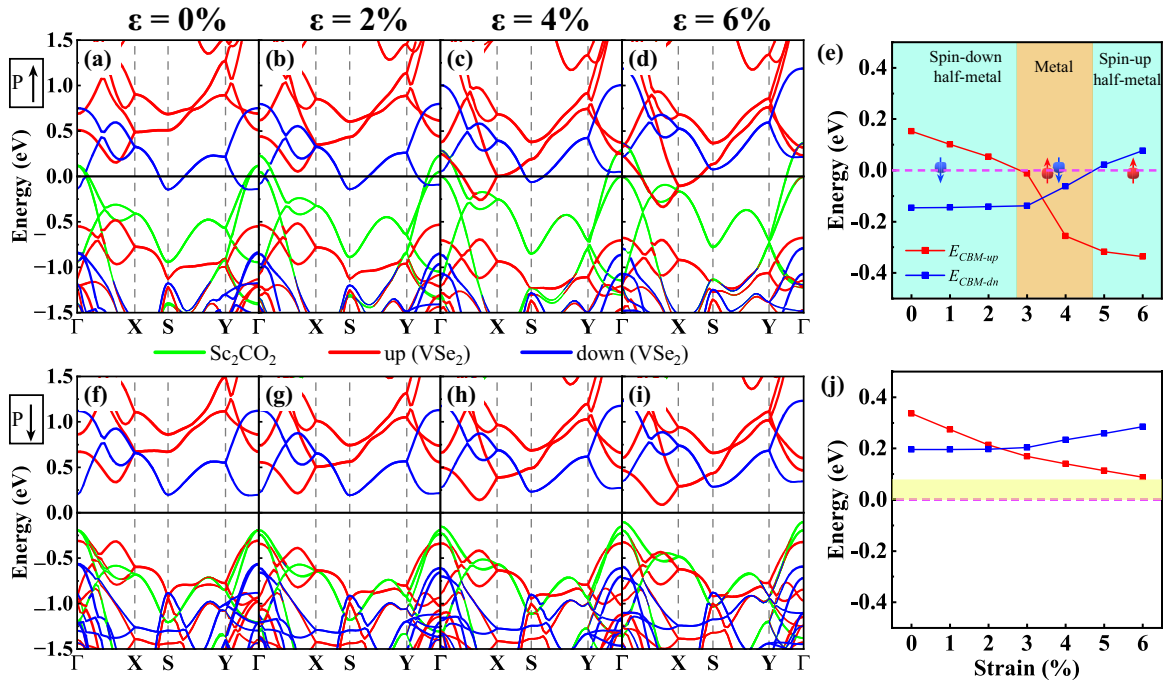


FIG. 6. Band structure of VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\uparrow$  and VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\downarrow$  at uniaxial tensile strains of (a), (f) 0%; (b), (g) 2%; (c), (h) 4%; and (d), (i) 6%. The dependence of band edges of VSe<sub>2</sub> layer in (e) the VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\uparrow$  and (j) VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P  $\downarrow$  heterostructure. The Fermi level is set to zero.

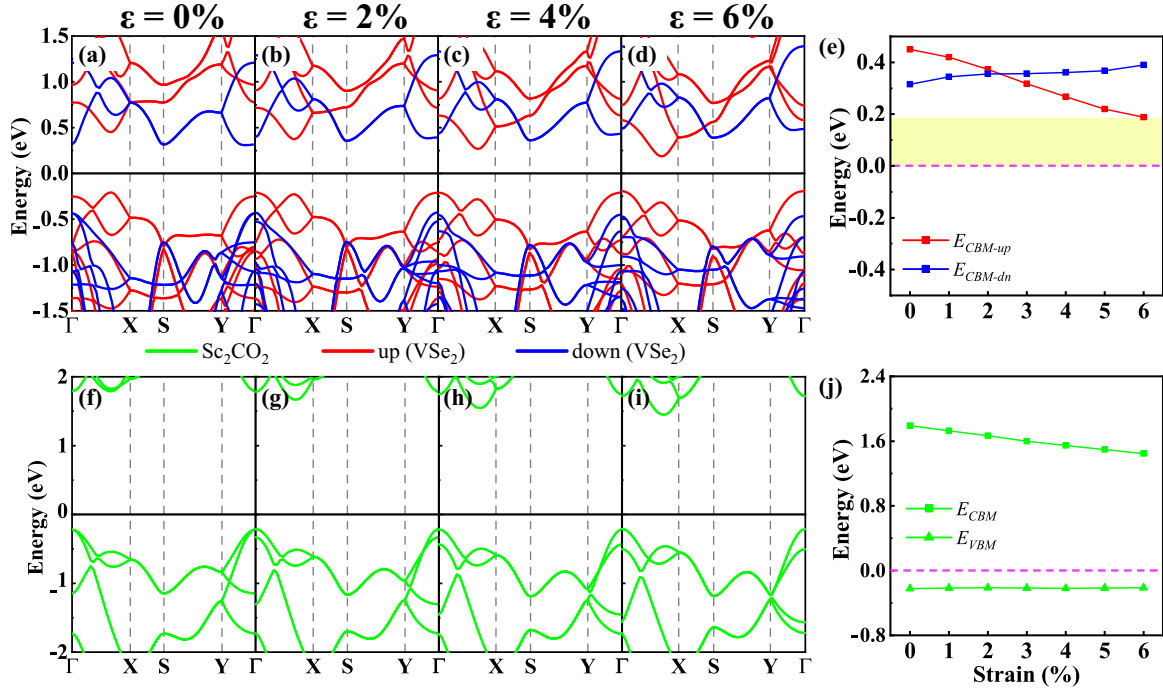


FIG. 7. Band structure of monolayer VSe<sub>2</sub> and Sc<sub>2</sub>CO<sub>2</sub> at uniaxial tensile strains of (a), (f) 0%; (b), (g) 2%; (c), (h) 4%; and (d), (i) 6%. The dependence of band edges of VSe<sub>2</sub> layer in (e) the VSe<sub>2</sub> monolayer and (j) the Sc<sub>2</sub>CO<sub>2</sub> monolayer. The Fermi level is set to zero. The red (blue) lines represent spin-up (spin-down) bands, the green lines represent Sc<sub>2</sub>CO<sub>2</sub> bands, and square (triangle) lines represent the energy position of the CBM (VBM) bands.

the CBM associated with two spin channels is located near the Fermi level. This is the reason why the VSe<sub>2</sub> layer exhibits the most diverse electronic properties when subjected to strain engineering. For the P ↓ heterostructure, the CBM associated with the two spin channels is always above the Fermi level. Furthermore, there exists a minimum energy difference of 0.088 eV between the CBM and the Fermi level. Thus, the polarization direction of Sc<sub>2</sub>CO<sub>2</sub> plays a crucial role in tuning Fermi level shifts in heterostructures. We also explore the electronic structures of the isolated monolayer VSe<sub>2</sub> and Sc<sub>2</sub>CO<sub>2</sub> under strains in Figs. 7(a)–7(d) and 7(f)–7(i), respectively. For the Sc<sub>2</sub>CO<sub>2</sub>, the material always exhibits a nonmagnetic semiconductor as the strain varies. The Fermi level in this process remains almost constant relative to the VBM location [see Fig. 7(j)]. But once it combines with VSe<sub>2</sub> to form above heterostructures, the Fermi level experiences a substantial downward shift. For the VSe<sub>2</sub>, the CBM variation behavior for two spin channels in monolayer VSe<sub>2</sub> is similar to that in VSe<sub>2</sub> layer of heterostructures under strains [see Fig. 7(e)]. The Fermi level also remains almost constant from  $\varepsilon = 0\%$  to 6%. Once it combines with Sc<sub>2</sub>CO<sub>2</sub> to form heterostructures, there is a significant increase in the Fermi level. The alterations in the band structures and band edges of monolayers of VSe<sub>2</sub> and Sc<sub>2</sub>CO<sub>2</sub> under strain, as depicted in Fig. 7(e), demonstrate that strain has a substantial impact on two spin channels CBM in VSe<sub>2</sub>. Consequently, this leads to diverse modifications in the properties of VSe<sub>2</sub>/Sc<sub>2</sub>CO<sub>2</sub> P ↑ heterostructure. It is well known that uniaxial strain can substantially change electronic structures due to structural variation. Geometrically speaking, the transition metal V atom is surrounded by six Se atoms in a triprismatic coordination,

as depicted in Fig. 8(a). Considering that 2H-VSe<sub>2</sub> possesses the  $D_{3h}$  point group symmetry, so that the  $d$  orbitals of the V atom are split into three groups at different energy levels: a nondegenerate  $a$  ( $d_{z^2}$ ) state, and two doubly degenerate  $e_1$  ( $d_{x^2-y^2}, d_{xy}$ ) and  $e_2$  ( $d_{xz}, d_{yz}$ ) states. Meanwhile,  $a$  and  $e_1$  orbitals have the lowest energy, while  $e_2$  orbitals are lying on higher-energy levels, as schematically illustrated in Fig. 8(b), which is consistent with our calculated band structure

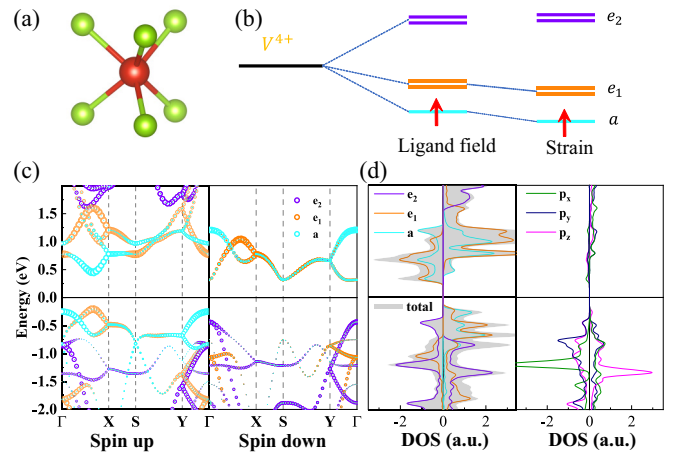


FIG. 8. (a) Structure of V<sup>4+</sup> ions at the crystallographic site of  $D_{3h}$  symmetry. (b) Schematic diagram of the evolution of V<sup>4+</sup>  $d$  orbitals splitting in monolayer VSe<sub>2</sub> under the influence of uniaxial strain. (c) Orbital resolved (left) spin-up and (right) spin-down band structures of VSe<sub>2</sub>. (d) The partial density of states (PDOS) of (left)  $d$ -resolved orbitals (right)  $p$ -resolved orbitals of VSe<sub>2</sub>.

TABLE IV. The bond length ( $d_{Se-V}$ ) and the Se-V-Se angle ( $\theta$ ) under different uniaxial strains.

Strain (%)	0	1	2	3	4	5	6
$d_{Se-V}$ (Å)	2.511	2.518	2.526	2.533	2.540	2.549	2.556
$\theta$ (°)	79.52	79.26	79.00	78.76	78.57	78.28	78.11

displayed in Fig. 8(c). To gain more physical insights into the interplay of the  $d$  orbitals, the spin-resolved partial density of states of  $VSe_2$  are shown in Fig. 8(d). The electronic states of the two spin CBMs contributed mainly from  $a$  orbital of the V atom and feebly by the  $p$  orbitals of the Se atom. The crystal field deformation surrounding the V atom can be fine-tuned by exerting external strains, and further affect the Coulomb repulsion interactions between the V atom and ligands, resulting in the rearrangement of V orbitals. The  $a$  orbital demonstrates a predilection for participating in out-of-plane bonding with the Se atom, whereas the  $e_1$  orbitals are conducive to in-plane bonding. Under tensile strain range from 0% to 6%, the Se-V bond length ( $d_{Se-V}$ ) and the Se-V-Se angle ( $\theta$ ) of the  $VSe_2$  monolayer are presented in Table IV [details are shown in Fig. 1(a)]. Structurally, as the in-plane lattice parameter is increased (under tension), the bond lengths between the V and Se atom increase and the bond angles  $\theta$  decrease. This leads to a reduction in the overlap between  $a$  and chalcogen states, our findings align with prior researches [52–54]. With increasing strain, the Se-V bond length increases, which means that the Se atoms gradually move away from the magnetic V atoms. Thus, the interaction between the V atoms and the Se atoms becomes weaker and the  $d$  orbital of the V atom becomes more localized. For  $d$  orbitals, a stronger localization results in a more pronounced exchange-enhanced spin splitting. With the decrease in  $a$ -state energy (independent of spin) being taken into consideration, the spin-up conduction band drops further, while the upshift of the spin-down conduction band due to the exchange interaction is counteracted by the downshift induced by the decrease in  $a$ -state energy, which ultimately leads to the increasing spin splitting in the conduction band.

#### IV. CONCLUSIONS

In conclusion, using first-principles calculations, we determined the structural stability and electronic properties of  $VSe_2/Sc_2CO_2$  multiferroic vdW heterostructures. Under  $Sc_2CO_2$  P  $\uparrow$ , a transition from semiconductor to half-metal observed in  $VSe_2$  layer of  $VSe_2/Sc_2CO_2$  P  $\uparrow$  heterostructure, which can be used in efficient memory devices. This transition is attributed to the presence of a built-in electric field induced by polarization and the resulting charge transfer. Besides, electronic structure calculations demonstrate that the uniaxial tensile strains along the  $x$  axis can induce a transition from spin-down half-metal ( $0\% < \varepsilon < 2.8\%$ ) to metal ( $2.8\% < \varepsilon < 4.7\%$ ) to spin-down half-metal ( $\varepsilon > 4.7\%$ ) in  $VSe_2$  layer of  $VSe_2/Sc_2CO_2$  P  $\uparrow$  heterostructure. Further analysis demonstrates that half-metals with adjustable spin polarization in  $VSe_2/Sc_2CO_2$  P  $\uparrow$  under strain mainly stems from the reduction of the spin-up CBM for the  $VSe_2$  layer. In addition, we found that strains can effectively modulate the electronic structures of the spin-up CBM through the change of the Se-V distance and Se-V-Se bond angle. This characteristic enables the manipulation of strain in various regions of  $VSe_2/Sc_2CO_2$  P  $\uparrow$  heterostructure, making it easy to switch spin conduction channels for precise control of spin current. Our paper opens a promising scheme for achieving the rational control of 2D spintronics.

#### ACKNOWLEDGMENT

We gratefully acknowledge financial support by the National Natural Science Foundation of China under Grant No. 21503061.

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