

Spin-switching energy gap in a compensated NdFeO<sub>3</sub> ferrimagnetI. Fita<sup>1,\*</sup>, R. Puzniak<sup>1</sup>, E. E. Zubov<sup>2</sup>, R. Diduszko<sup>1</sup> and A. Wisniewski<sup>1</sup><sup>1</sup>*Institute of Physics, Polish Academy of Sciences, Aleja Lotnikow 32/46, PL-02668 Warsaw, Poland*<sup>2</sup>*Kyiv Academic University, 36 Acad. Vernadsky Blvd., UA-03142 Kyiv, Ukraine*

(Received 12 June 2023; revised 27 November 2023; accepted 4 January 2024; published 5 February 2024)

Spontaneous and field-dependent spin switching (magnetization reversal) has been studied in the compensated ferrimagnet NdFeO<sub>3</sub>. The spin switching temperature  $T_{sw}$  monotonically approaches the compensation temperature  $T_{comp}$  with an increase in the applied magnetic field above  $T_{comp} \approx 9$  K. However, below  $T_{comp}$ , a sharp drop in  $T_{sw}$  towards low temperatures and a simultaneous increase in the magnetization jump  $\Delta M$  at  $T_{sw}$  were found. The discontinuity in  $T_{sw}$  leads to two different  $T_{sw}$ - $H$  phase lines shifted in opposite directions in temperature on the  $T$ - $H$  plane. These lines are described by two different spin switching energies. The same splitting in the switching energy of  $600 \text{ emu g}^{-1} \text{ Oe}$  follows directly from the magnetization jump data, and also coincides with the difference in unidirectional anisotropy energies for positive and negative exchange bias, both found near  $T_{comp}$ . This indicates that the split spin switching energy, responsible for the anomaly in the  $T$ - $H$  diagram in NdFeO<sub>3</sub>, arises from the coexistence of two different exchange biases of opposite signs.

DOI: [10.1103/PhysRevB.109.054404](https://doi.org/10.1103/PhysRevB.109.054404)

Orthoferrite NdFeO<sub>3</sub> is a compensated ferrimagnet [1–4], which exhibits the exotic phenomenon of negative magnetization and associated magnetization reversal due to fast spin switching between two coexisting states with negative and positive magnetization. Such remarkable properties have potential applications in the development of fast switching and magnetic storage devices. Therefore, an important question is what is the nature of the spin switching, what factors can influence the fast magnetization reversal, and what stimulus can cause it.

The magnetic compensation in NdFeO<sub>3</sub> occurs due to antiferromagnetic (AFM) exchange interaction between Nd<sup>3+</sup> and Fe<sup>3+</sup> spins, which polarizes the Nd<sup>3+</sup> spins opposite to the weak ferromagnetic (FM) moment, arising from canted AFM order of Fe spins below  $T_N = 690$  K [5] due to the antisymmetric Dzyaloshinskii-Moriya (DM) exchange interaction. The polarized paramagnetic moment of Nd spins increases with decreasing temperature, while the weak FM moment of the canted spins of Fe remains unchanging; therefore, two opposite moments annul each other at the compensation temperature  $T_{comp}$  of about 9 K. When an external magnetic field is applied, the metastable states with negative magnetization appear near  $T_{comp}$ , and the spontaneous or field-induced spin switching to the equilibrium state occurs as soon as the change in the Zeeman energy upon switching overcomes the anisotropy energy barrier [6]. Similar compensated spin structures and switching between them were found in  $RMO_3$  orthorhombic magnetic perovskites ( $R$  = rare earth elements,  $M$  = Fe, Cr, Mn) [7–13]. However, in contrast to NdFeO<sub>3</sub>, where the Nd ions remain in a paramagnetic state up to 1 K [2], in the isostructural ferrimagnet NdMnO<sub>3</sub> another type of magnetic compensation is observed, namely, two opposite FM

components of the ordered sublattices Mn and Nd compensate each other at the ordering temperature of Nd equal to 15 K, which is accompanied by strong structural distortions due to magnetostructural coupling due to Jahn-Teller nature of Mn ions [14,15].

The anisotropic  $R$ -Fe exchange induces in orthoferrites the Fe spin reorientation (SR), leading to the weak FM moment rotation from the  $c$  axis to the  $a$  axis. Temperature of the reorientation,  $T_{SR}$ , varies in a wide range because the  $R$ -Fe interaction differs significantly in various compounds. In both Nd and Er orthoferrites, the transition occurs at  $T_{SR} \approx 100$  K [16,17], and in SmFeO<sub>3</sub> at  $T_{SR} \approx 480$  K [7].

It has been found that spin switching in compensated Er, Nd, and Sm orthoferrites can be exchange-biased, as evidenced by the hysteresis loops  $M$  vs  $H$  [18–21]. The exchange bias (EB) field arises and increases when approaching  $T_{comp}$  and changes sign when crossing  $T_{comp}$ . The EB sign may be changed as well by varying the field cooling (FC) protocol, depending on whether  $T_{comp}$  is reached with a decrease or increase in temperature. Recently, it was found that the EB in ErFeO<sub>3</sub> also manifests itself in the temperature shift of the hysteresis loops  $M$  vs  $T$  [21]. This leads to the remarkable feature that the switching temperature  $T_{sw}$  depends on EB, and the  $T_{sw}$ - $H$  line, which limits the region of metastable states in  $T$ - $H$  phase diagram, shifts to the left or right in temperature, depending on whether EB is positive or negative, respectively. This behavior is explained by the fact that the unidirectional EB anisotropy contributes to the energy barrier for spin switching and, therefore, increases or decreases the switching energy and  $T_{sw}$  depending on the sign of the EB.

In the present work, we found that the  $T_{sw}$ - $H$  line below  $T_{comp}$  in a compensated NdFeO<sub>3</sub> ferrimagnet with a low  $T_{comp}$  is not continuous and monotonic, as is observed in ErFeO<sub>3</sub>, but has a discontinuity. There are two different  $T_{sw}$ - $H$  phase lines shifted in opposite directions in temperature on the  $T$ - $H$

\*Corresponding author: ifita@ifpan.edu.pl

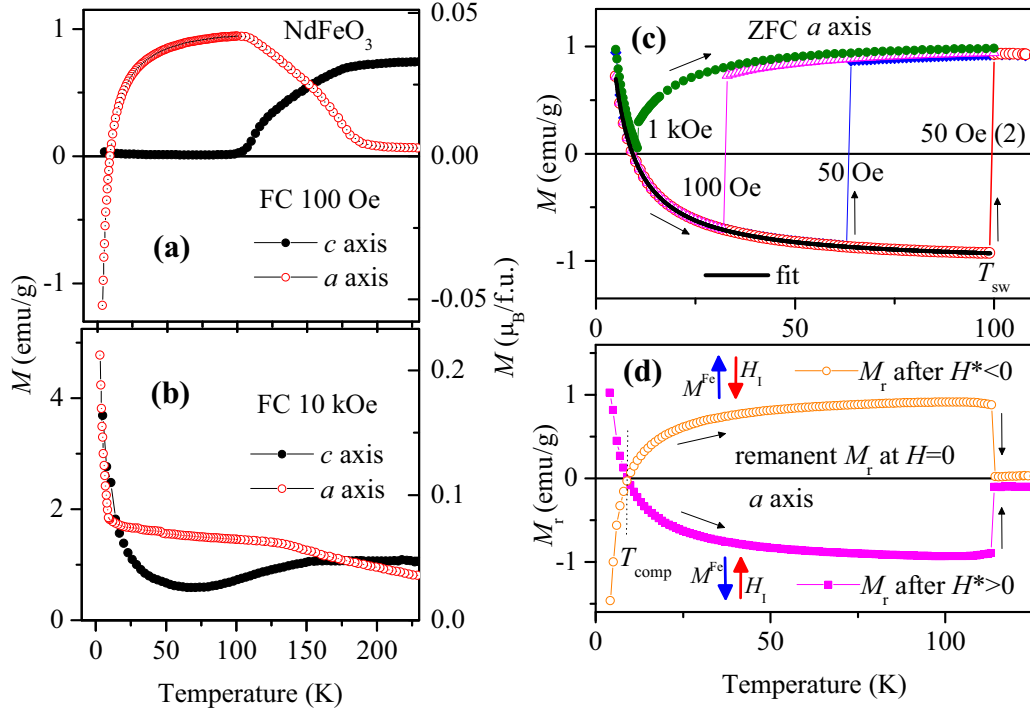


FIG. 1. Temperature dependences of the field-cooled (FC) magnetization of NdFeO<sub>3</sub> single crystal measured along the *a* and *c* axes upon cooling in fields of (a) 100 Oe and (b) 10 kOe. *M* vs *T* curves measured upon warming for the *a* axis: (c) in different magnetic fields applied after ZFC; (d) in zero field  $H = 0$ , which represent two opposite remanent single-domain magnetization  $M_r$ , created by a short-term application of a field  $H^* = +5$  and  $-5$  kOe at 4 K with two mutually opposite orientations of the FM moment  $M^{\text{Fe}}$  and internal field  $H_i$ . Curve (2) in (c) shows an increase in the switching temperature  $T_{\text{sw}}$  after a short-term application of a field  $H^* > 500$  Oe at 4 K and solid line in (c) represent fit with Eq. (1).

plane, described by two different spin switching energies. This difference of the switching energy turned out to be equal to the difference between the energies of the unidirectional anisotropy for positive and negative EB, both measured near  $T_{\text{comp}}$ . This proves that the split spin switching energy and the anomalous  $T_{\text{sw}}-H$  dependence in NdFeO<sub>3</sub> arise due to the coexistence of two different exchange biases of opposite signs.

Magnetization measurements were performed on a flux-grown NdFeO<sub>3</sub> single crystal with a size of  $\sim 2$  mm and a mass of 55 mg, which was previously used in the studies of spin switching and exchange bias [3], in the temperature range 3–230 K and in magnetic field up to 15 kOe using a PAR (Model 4500) vibrating sample magnetometer. The *c* axis was identified with x-ray diffraction, and the correct orientation of the *a* and *c* axes along the magnetic field in the magnetometer was established based on the known strong magnetic anisotropy and spontaneous reorientation of the weak FM moment in NdFeO<sub>3</sub> [1,4]. Namely, the single crystal was rotated in a small field  $H = 100$  Oe and the direction along which the magnetization *M* reached its maximum value at temperatures above the spin reorientation  $T_{\text{SR}}$  was taken as the direction of the *c* axis, the direction along which *M* showed its maximum value below  $T_{\text{SR}}$  was established as the *a* axis. A crystal oriented in this way shows rotation of the FM moment from the *c* axis to the *a* axis between temperatures of 185 and 100 K [see Fig. 1(a)]. The magnetization along the *c* axis is 0.74 emu/g at 220 K and along the *a* axis it reaches 0.93 emu/g at 100 K, which agrees well with recent studies [1,4]. Note that

each time before starting magnetization measurements in the FC or zero field cooling (ZFC) modes, in order to eliminate or reduce the influence of the previous magnetic history, the sample was demagnetized at 230 K by stepwise reducing the magnetic field to zero with a change in its sign. Curves *M* vs *T* recorded in a weak field, shown in Fig. 1(a), demonstrate that the FM moment directed along the *a* axis below 100 K is completely compensated at  $T_{\text{comp}} = 9.2$  K, and below  $T_{\text{comp}}$  a negative FM moment opposite to the applied field arises due to strong magnetic anisotropy. On the contrary, an applied field of 10 kOe strongly suppresses the anisotropy, so both spin reorientation and magnetic compensation are weakly expressed and below 15 K the magnetization along both axes is practically the same [see Fig. 1(b)]. Curves *M* vs *T*, presented in Fig. 1(c), were measured for the *a* axis when heated in various magnetic fields applied at 4 K after ZFC. They show a negative value of *M* and a sharp change in *M* to positive values at temperatures  $T_{\text{sw}}$ , that are much higher than  $T_{\text{comp}}$  at a low field, while  $T_{\text{sw}}$  approaches  $T_{\text{comp}}$  with increasing field. It was also found that the temperature  $T_{\text{sw}}$  measured at 50 Oe increases significantly if a field  $H^*$  exceeding 500 Oe is applied briefly (for 1 min) at a temperature of 4 K before the measurements. A very similar increase in  $T_{\text{sw}}$ , which occurs after a short-term application of a strong magnetic field at low temperature, was observed in the ErFeO<sub>3</sub> ferrimagnet, and was explained by the field-induced increase in the spin-switching energy barrier [21]. Dependences of the remanent magnetization on temperature, shown in Fig. 1(d), measured at  $H = 0$  after a short-term application of a field  $H^* = +5$

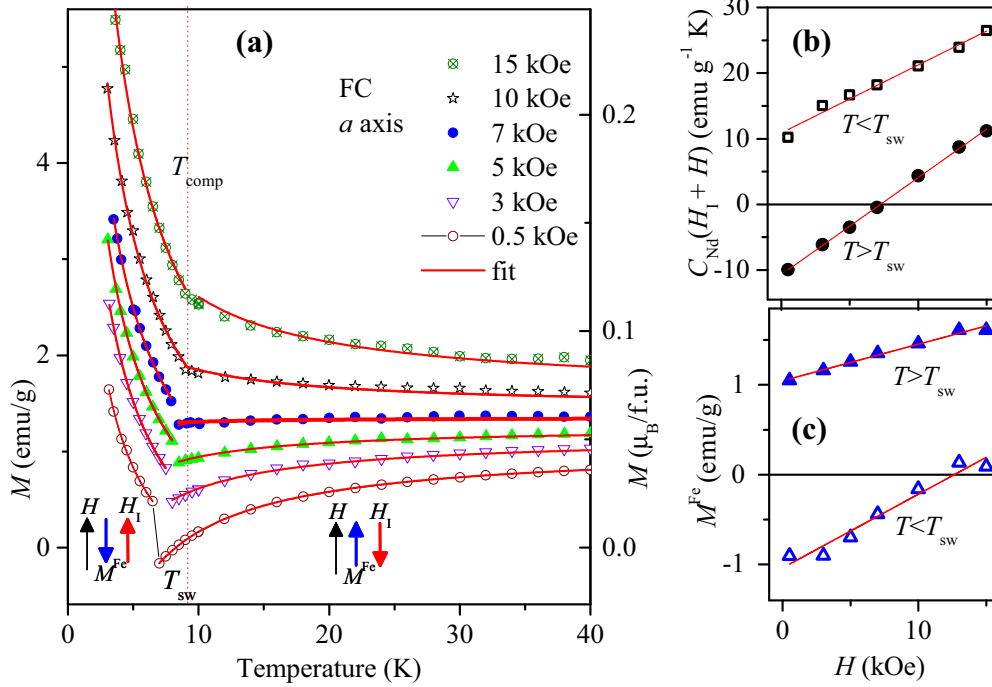


FIG. 2. (a) FC magnetization of NdFeO<sub>3</sub> as a function of temperature, measured upon cooling in various magnetic fields applied along the *a* axis. Two opposite orientations of the FM moment  $M^{\text{Fe}}$  and the internal field  $H_1$  are shown above and below the spin switching temperature  $T_{\text{sw}}$ . Lines in (a) represent fit with Eq. (1) with two fitting parameters,  $C_{\text{Nd}}(H_1 + H)$  and  $M^{\text{Fe}}$ , shown in (b) and (c) as a function of field  $H$ , and the lines in (b) and (c) represent the linear fit.

and  $-5$  kOe at 4 K, exhibit two opposite single-domain FM magnetizations with mutually opposite orientations of the FM moment  $M^{\text{Fe}}$ . Internal field  $H_1$  is indicated, which exist up to 114 K and disappear only above 114 K, when spin reorientation already begins (the FM moment deviates from the *a* axis) and, consequently, a multidomain state arises. Both curves intersect at  $M = 0$  exactly at  $T_{\text{comp}} = 9.2$  K and their values of  $M_r$  are almost identical in absolute value above  $T_{\text{comp}}$ , while the unexpected nonzero value of  $M$  in the multidomain state for the curve with  $H^* = +5$  kOe appears due to the nonzero field  $H = -2$  Oe instead of the required  $H = 0$ , which was caused by imperfect stabilization of the magnetic field in this case. Overall, the mirror image of the  $M_r$  vs  $T$  curves well confirms the existence of a strong Fe-Nd AFM interaction, which controls the magnetization in NdFeO<sub>3</sub> through the internal field  $H_1$ .

The phenomenon of magnetic compensation in NdFeO<sub>3</sub> can be satisfactorily described using a simple model, which has been well confirmed for compensated orthoferrites and orthochromites [3,12,21,22]. The model takes into account the weak FM moment  $M^{\text{Fe}}$  due to the canted AFM ordered spins of Fe and the opposite moment of paramagnetic Nd<sup>3+</sup> spins induced by the AFM interaction between Fe<sup>3+</sup> and Nd<sup>3+</sup> spins, so that the total magnetization in an external field  $H$  is expressed as

$$M = M^{\text{Fe}} + C_{\text{Nd}}(H_1 + H)/(T - \theta), \quad (1)$$

where  $C_{\text{Nd}} = Ng^2\mu_B^2J(J+1)/3k_B$  is the Curie constant, which is equal to  $6.5 \text{ emu K g}^{-1} \text{ kOe}^{-1}$  in the case of free Nd<sup>3+</sup> ions with the ground multiplet  $^4I_{9/2}$  ( $L = 6, S = 3/2, J = 9/2$ ) and  $g = 8/11$ ,  $H_1$  is the internal effective ex-

change field resulting from the Fe-Nd AFM interaction, which induces a paramagnetic moment of Nd spins directed against the  $M^{\text{Fe}}$  magnetization [it should be noted that the  $H_1$  field actually reflects the canted AFM structure of Fe spins and therefore indirectly depends on the antisymmetric DM exchange interaction between Fe spins, so that the  $H_1$  is expected to be zero if there is no DM interaction and in consequence no FM moment  $M^{\text{Fe}}$ ], and  $\theta$  is the Weiss temperature, linked to the AFM interaction between Nd<sup>3+</sup> spins. It should be noted that  $M^{\text{Fe}}$  is close to saturation far from the Néel temperature  $T_N = 690$  K, since it is considered to follow the Brillouin function  $B_{S=5/2}(T)$  for spin  $S = 5/2$  and can be considered as independent of temperature below 100 K. Equation (1) was fitted to the dependences of  $M$  on  $T$  measured during heating upon warming in a weak field of 50 Oe (see the line in Fig. 1(c) for which the best fitting parameters are:  $M^{\text{Fe}} = -1.03 \text{ emu/g}$ ,  $C_{\text{Nd}}H_1 = 10.8 \text{ emu K/g}$ , and  $\theta = -1.2$  K), as well as during cooling in various fields  $H$  applied along the *a* axis, as shown in Fig. 2(a). These FC curves exhibit the jump in  $M$  below  $T_{\text{comp}}$  at  $T_{\text{sw}}$  at which the mutually opposite magnetization  $M^{\text{Fe}}$  and the internal field  $H_1$  change their direction with respect to the external field  $H$ , so that the fields  $H_1$  and  $H$  are opposite at  $T > T_{\text{sw}}$  and parallel at  $T < T_{\text{sw}}$  [see Fig. 2(a)]. It is clearly seen that above  $T_{\text{sw}}$ , the magnetization increases with decreasing  $T$  at high  $H$  and decreases in low  $H$ , while for  $H = 7$  kOe it remains practically constant [see bold line in Fig. 2(a)]. This means, according to Eq. (1), that the fields  $H$  and  $H_1$  are opposite and compete, and the external field of 7 kOe completely compensates the internal field  $H_1$ , therefore,  $H_1 \approx -7$  kOe. Since for each field  $H$  there are two opposite spin configurations, the fitting was carried

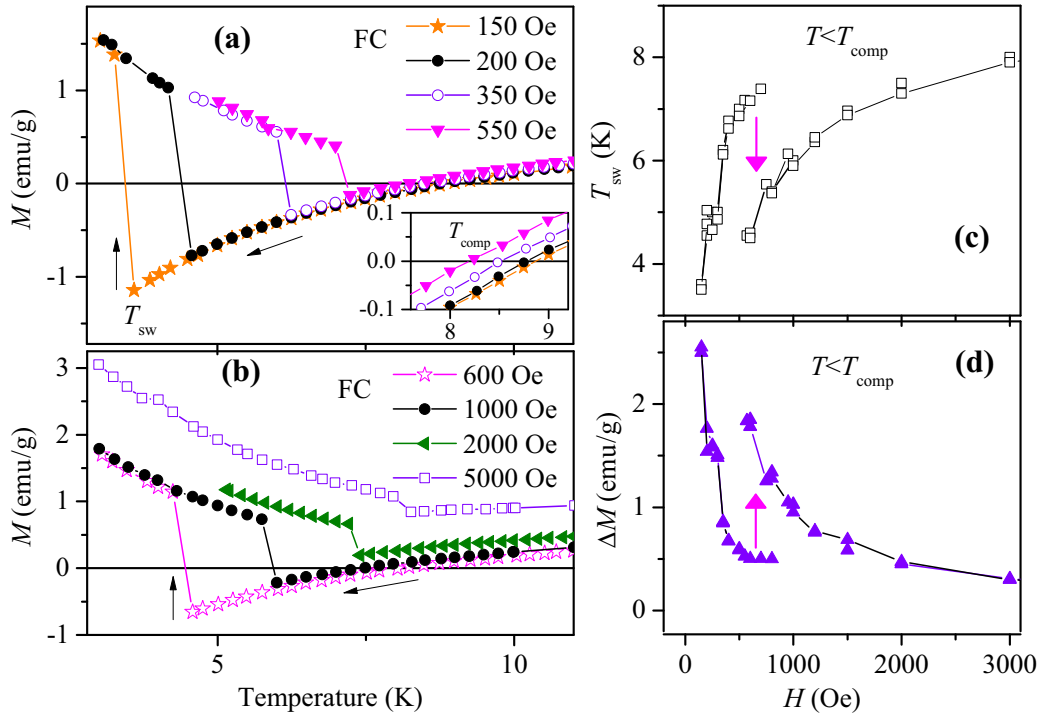


FIG. 3. (a), (b) Field-cooled  $M$  vs  $T$  curves at several fields  $H$  along the  $a$  axis show a monotonic increase in the switching temperature  $T_{sw}$  with increasing  $H$  and an unexpected drop in  $T_{sw}$  by 2.5 K as  $H$  changes from 550 to 600 Oe. Inset in (a) shows the decrease in temperature  $T_{comp}$ , at which  $M = 0$ , with increasing  $H$ . (c), (d) Field dependences of the temperature  $T_{sw}$  (c) and the magnetization jump  $\Delta M$  at  $T_{sw}$  (d), demonstrating a sharp drop in  $T_{sw}$  and a simultaneous increase in  $\Delta M$  (marked by arrows) in the range of 600–800 Oe.

out for two temperature intervals above and below  $T_{sw}$ . Solid lines in Fig. 2(a) are the best fit with Eq. (1) with two fitting parameters,  $C_{Nd}(H_1 + H)$  and  $M^{Fe}$ , which vary linearly with the field  $H$  [see Figs. 2(b) and 2(c)]; the value  $\theta = -1.2$  K was fixed at fitting. Fit clearly shows that the magnetization  $M^{Fe}$  and the exchange field  $H_1$  are always mutually opposite and change sign/direction at the switching temperature  $T_{sw}$ . The  $C_{Nd}(H_1 + H)$  vs  $H$  line for  $T > T_{sw}$  in Fig. 2(b) crosses zero giving the internal field  $H_1 = -7.3$  kOe. The line slope corresponds to Curie constant  $C_{Nd} = 1.48$  emu K  $g^{-1}$  kOe $^{-1}$ , which is much smaller than the value of 6.5 emu K  $g^{-1}$  kOe $^{-1}$  calculated for free Nd ions, but practically coincides with the value calculated for a completely isolated ground-state Kramers doublet with effective spin 1/2 and  $g = 2$ . It was also obtained that at  $H = 0$ , the canted FM moment  $M^{Fe} = 1.04$  emu/g is almost the same in value and has different signs above and below  $T_{sw}$ , and the value of  $M^{Fe}$  increases linearly with the field  $H$  when it is directed along  $H$  (the canting angle of Fe spins increases with increasing  $H$ ) and decreases when it is directed against it [see Fig. 2(c)]. It should be noted that the values  $H_1 = -7.3$  kOe and  $M^{Fe} = 1.04$  emu/g obtained here are in good agreement with the internal effective field  $H_{eff} = -7.7$  kOe and the canting angle  $\alpha = 8.5$  mrad (which corresponds to  $M^{Fe} = gS\mu_B \sin\alpha = 0.96$  emu/g for  $S = 5/2$ ,  $g = 2$ ), determined already by Treves for NdFeO $_3$  [5], so the above fit is a good test of magnetic properties of the studied NdFeO $_3$  sample. We also note that qualitatively the same dependence on magnetic field of the magnetization and fitting parameters shown in Fig. 2 were recently observed in compensated ErFeO $_3$  ferrimagnet [21]. Moreover, as the applied field  $H$  increases, the switching temperature  $T_{sw}$  approaches  $T_{comp}$  and

the magnetization jump  $\Delta M$  at  $T_{sw}$  collapses [see Figs. 1(c) and 2(a)], similarly to what was observed in ErFeO $_3$  [21] and GdCrO $_3$  [12]. However, unlike ErFeO $_3$  and GdCrO $_3$  crystals, NdFeO $_3$  surprisingly showed an anomalous discontinuous dependence of  $T_{sw}$  on  $H$  below  $T_{comp}$ , namely: with an increase in the cooling field  $H$ , the switching temperature  $T_{sw}$  normally increases, approaching  $T_{comp}$ , over the entire range of fields, but unexpectedly drops by 2.5 K when changing  $H$  from 550 to 600 Oe [see Figs. 3(a) and 3(b)]. Interestingly, when  $T_{sw}$  jumps towards a lower temperature, the magnetization jump  $\Delta M$ , which occurs at  $T_{sw}$ , simultaneously sharply increases. This unusual behavior was repeated in several series of measurements, and the values of  $T_{sw}$  and  $\Delta M$  as functions of the field  $H$  are shown in Figs. 3(c) and 3(d). They show a sharp drop in  $T_{sw}$  and a simultaneous increase in  $\Delta M$  between 600 and 800 Oe, and also show that in the temperature range from 4.5 to 7.5 K, spin switching with the same temperature  $T_{sw}$  can occur with two different applied fields. It should be noted that, despite the discontinuity of  $T_{sw}$ , the  $\Delta M$  value corresponds exactly to the temperature, which may indicate that the observed behavior is inherent in NdFeO $_3$  and is not associated with any parasitic magnetic inclusions. In order to prove this assumption, we further analyzed the  $\Delta M$  vs  $T$  dependence within the model, and we get Eq. (1). When the magnetization direction is reversed, the magnetization jump is  $\Delta M = 2M$ , therefore, according to Eq. (1), the change in  $M$  at  $T_{sw}$ , which occurs above  $T_{comp}$ , is  $\Delta M = 2M^{Fe} - 2C_{Nd}H_1/(T_{sw} - \theta)$ , and  $\Delta M = -2M^{Fe} + 2C_{Nd}H_1/(T_{sw} - \theta)$  when the spin switching occurs below  $T_{comp}$ . Figure 4(a) shows the  $\Delta M$  vs  $T_{sw}$  dependence, where the jump  $\Delta M$  is determined directly from the  $M$  vs  $T$  curves, as well as the best fits for parameters  $M^{Fe} =$

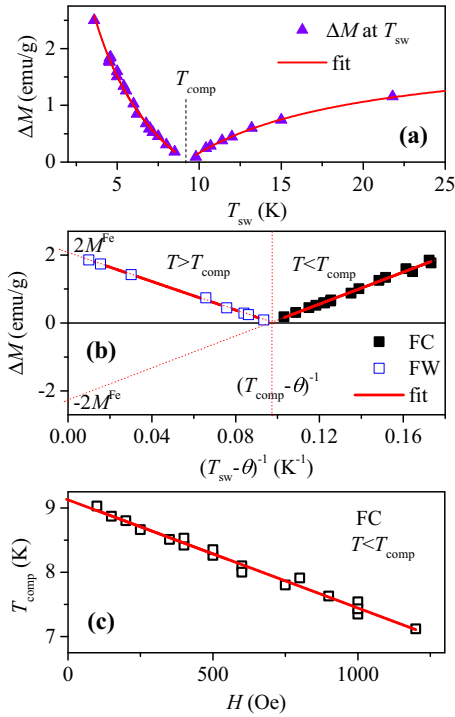


FIG. 4. (a) Dependence of the magnetization jump  $\Delta M$  on the switching temperature  $T_{sw}$ . The lines represent fits by the equation  $\Delta M = 2M^{Fe} - 2C_{Nd}H_I/(T_{sw} - \theta)$  for two variable parameters, setting  $\theta = -1.2$  K. (b) The jump  $\Delta M$  at  $T_{sw}$ , taken as a function of  $(T_{sw} - \theta)^{-1}$  with  $\theta = -1.2$  K below and above  $T_{comp}$ , and the lines present linear approximation. (c) Decreasing compensation temperature  $T_{comp}$  with increasing cooling field  $H$  and line is linear fit.

$-1.08$  emu/g,  $C_{Nd}H_I = 11.4$  emu  $g^{-1}$  K, and  $\theta = -1.2$  K, which are close to the values obtained from the above  $M$  vs  $T$  fit. In Fig. 4(b) the same data  $\Delta M$  are taken as a function of  $(T_{sw} - \theta)^{-1}$ , and the lines, which represent linear approximation, intersect at  $(T_{comp} - \theta)^{-1} = 0.097$   $K^{-1}$ , maintaining  $T_{comp} = 9.15$  K and  $\theta = -1.2$  K, and  $\Delta M = 0$  at  $T_{comp}$ . In addition, the compensation temperature calculated with the above parameters as  $T_{comp} = -C_{Nd}H_I/M^{Fe} + \theta = 9.35$  K is very close to the measured value. The fact that the magnetization jump  $\Delta M$  is a smooth function of  $T_{sw}$  and is well described by Eq. (1), despite the anomalous discontinuity in  $T_{sw}$  and  $\Delta M$  with a change in the magnetic field, unambiguously indicates that the spin switching is a true reversal of mutually opposite magnetization  $M^{Fe}$  and induced paramagnetic moment of  $Nd^{3+}$  spins. This conclusion is also supported by the linear decrease in  $T_{comp}$  with the FC field  $H$ , which is also observed for the region of  $H$  where discontinuities  $T_{sw}$  and  $\Delta M$  are pronounced [see Fig. 4(c) and inset of Fig. 3(a)]. Here, a linear fit gives  $T_{comp}(H = 0) = 9.13$  K and slope  $C_{Nd}/M^{Fe} = -0.00168$  K/Oe, which corresponds to the Curie constant  $C_{Nd} = 1.55$  emu K  $g^{-1}$  kOe $^{-1}$  in the case  $M^{Fe} = -1.08$  emu/g, which agrees well with what was found above from another fit.

Figure 5 shows  $T$ - $H$  diagram with the switching temperatures  $T_{sw}$  of  $NdFeO_3$  at various field  $H$  applied along the  $a$  axis, determined from the  $M$  vs  $T$  curves obtained in the FC mode below  $T_{comp}$  and in ZFC mode above  $T_{comp}$ . The lines

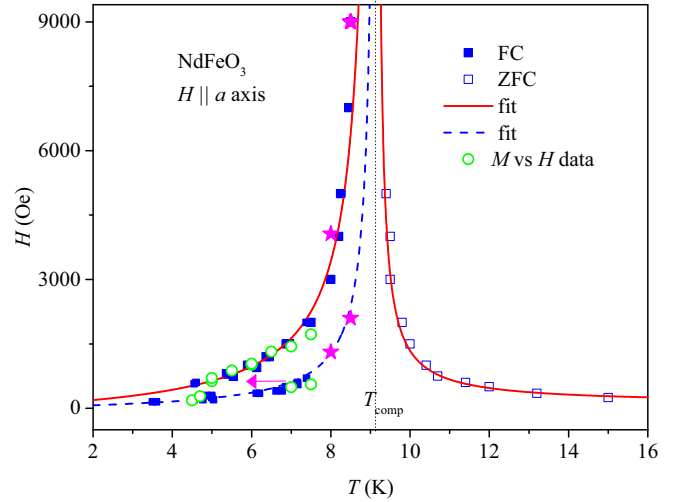


FIG. 5. The spin switching temperature  $T_{sw}$  of  $NdFeO_3$  as a function of the magnetic field  $H$ , determined from the  $M$  vs  $T$  curves in the FC mode below  $T_{comp}$  and in ZFC mode above  $T_{comp}$ . The switching fields  $H_{sw}$ , determined from the  $M$  vs  $H$  curves (circles) and from the EB data at  $T = 8$  and  $8.5$  K (asterisks) are also indicated. The lines represent fits with Eq. (2) for the variable parameter  $\Delta E_Z/2M^{Fe}$ . The arrow shows a sharp drop in  $T_{sw}$  as  $H$  increases in the range of 600–800 Oe.

$T_{sw}$ - $H_{sw}$  are the boundaries between a metastable state with negative magnetization (at lower  $H$ ) and an equilibrium magnetic state (at higher  $H$ ). Near  $T_{comp}$ , where the magnetization is very low, the metastable phase propagates into the region of strong magnetic fields. The  $T_{sw}$ - $H_{sw}$  line above  $T_{comp}$  is very similar to that recently observed for  $ErFeO_3$  orthoferrites with  $T_{comp} = 45$  K [21]. In contrast to  $ErFeO_3$ , the anomalous discontinuity in  $T_{sw}$ , leading to a double switching field  $H_{sw}$  at the same  $T_{sw}$ , appears below  $T_{comp}$  in  $NdFeO_3$ . We then analyze the  $T_{sw}$  vs  $H$  dependence since an understanding of the nature of spin switching will help us to understand the reason for the puzzling jump in  $T_{sw}$  below  $T_{comp}$ . The spontaneous spin switching is actually a first-order phase transition from a metastable state with the negative magnetization (in this spin configuration the Zeeman energy  $E_Z = -MH$  is maximal) to an equilibrium state with positive magnetization and minimum energy  $E_Z$ . Consequently, the system must spend the energy required for magnetization reversal by  $180^\circ$  around the  $a$  axis in order to overcome the anisotropy energy  $E_a$ . This energy is equal to the drop in the Zeeman energy  $\Delta E_Z$  at  $T_{sw}$ . Therefore, spin switching occurs at that temperature at which the modulus of negative magnetization becomes large enough for  $\Delta E_Z$  to reach the energy barrier  $E_a$ . This explains why the temperature  $T_{sw}$  is far from  $T_{comp}$  at applied small  $H$ , and close to  $T_{comp}$  at large  $H$ . According to Eq. (1), the decrease in the Zeeman energy at spin switching is equal to  $\Delta E_Z = \Delta MH = 2[M^{Fe} - C_{Nd}H_I/(T_{sw} - \theta)]H$ , and taking into account that  $T_{comp} = (C_{Nd}H_I/M^{Fe}) + \theta$ , the switching field  $H_{sw}$  as a function of temperature can be expressed as follows:

$$H_{sw} = -(\Delta E_Z/2M^{Fe})(T - \theta)/(T - T_{comp}). \quad (2)$$

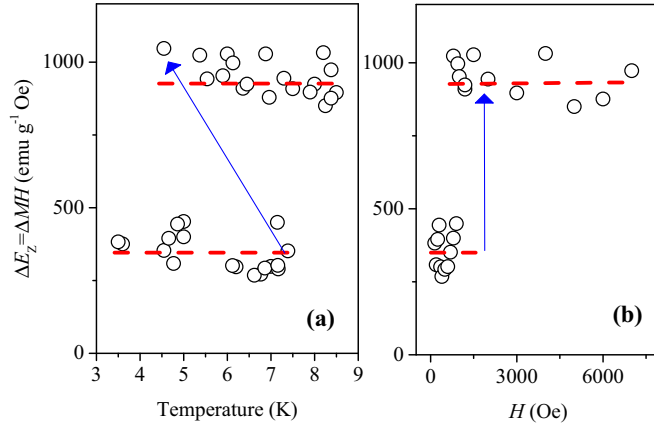


FIG. 6. Spin switching energy  $\Delta E_z$ , calculated as  $\Delta MH$  at  $T_{\text{sw}}$  directly from the  $M$  vs  $T$  curves, as a function of (a) temperature and (b) applied magnetic field  $H$ . There is a gap in the switching energy at low and high  $H$ , and the arrow shows a jump in  $\Delta E_z$  as  $H$  increases. The dashed lines show the values of  $\Delta E_z = 345$  and  $925$   $\text{emu g}^{-1} \text{Oe}$ , obtained as a result of fitting the  $T_{\text{sw}}-H_{\text{sw}}$  line according to Eq. (2), shown in Fig. 5 for low and high fields  $H$ , respectively.

This equation was previously successfully used to describe the field dependence of the switching temperature  $T_{\text{sw}}$  in compensated ferrimagnets  $\text{ErFeO}_3$  [21] and  $\text{GdCrO}_3$  [12]. The lines in Fig. 5 represent fits with Eq. (2) for the variable parameter  $\Delta E_z/2M^{\text{Fe}}$  while maintaining constant values  $T_{\text{comp}} = 9.15$  K and  $\theta = -1.2$  K. The best fitting value for the line above  $T_{\text{comp}}$ ,  $\Delta E_z/2M^{\text{Fe}} = 102$  Oe was obtained, from which we estimate the spin switching energy  $\Delta E_z = 220$   $\text{emu g}^{-1} \text{Oe}$ , taking into account the canted FM moment  $M^{\text{Fe}} = 1.08$   $\text{emu/g}$  as determined above. The data obtained below  $T_{\text{comp}}$  at temperatures below and above the  $T_{\text{sw}}$  jump were analyzed separately due to the  $T_{\text{sw}}$  discontinuity. The solid  $T_{\text{sw}}-H_{\text{sw}}$  line for higher values of  $H$  shows the best fitting parameter  $\Delta E_z/2M^{\text{Fe}} = 428$  Oe, which corresponds to the switching energy  $\Delta E_z = 925$   $\text{emu g}^{-1} \text{Oe}$ . The dashed line represents the best fit obtained for the low-field switching data, calculated and extrapolated closer to  $T_{\text{comp}}$  with  $\Delta E_z/2M^{\text{Fe}} = 160$  Oe, which corresponds to an energy of  $\Delta E_z = 345$   $\text{emu g}^{-1} \text{Oe}$ . The huge difference in the switching energy  $\Delta E_z$  obtained for different regions of fields explains the discontinuity in the  $T_{\text{sw}}-H_{\text{sw}}$  line and its shift away from the  $T_{\text{comp}}$ . It turns out that an applied field FC above 600–800 Oe causes an increase in the energy barrier for spin switching, and therefore spontaneous magnetization reversal occurs at a lower temperature, when the Zeeman energy  $-MH$  is large enough to overcome the increased barrier. On the other hand, the appearance of a gap in  $\Delta E_z$  is also clearly seen from the data of the magnetization jump  $\Delta M$  measured directly at  $T_{\text{sw}}$ , regardless of the model used. Fig. 6 shows the spin switching energy  $\Delta E_z$ , calculated as  $\Delta MH$  at  $T_{\text{sw}}$  directly from the  $M$  vs  $T$  curves, as a function of temperature and applied FC field  $H$ . The  $\Delta MH$  data demonstrate two well-separated energy levels below  $T_{\text{comp}}$ , which are almost identical to those obtained from the analysis of  $T_{\text{sw}}$  vs  $H$ , see red dashed lines in Fig. 6(a). This fact may indicate that the model used correctly describes the spin switching phenomena. In addition, the dependence

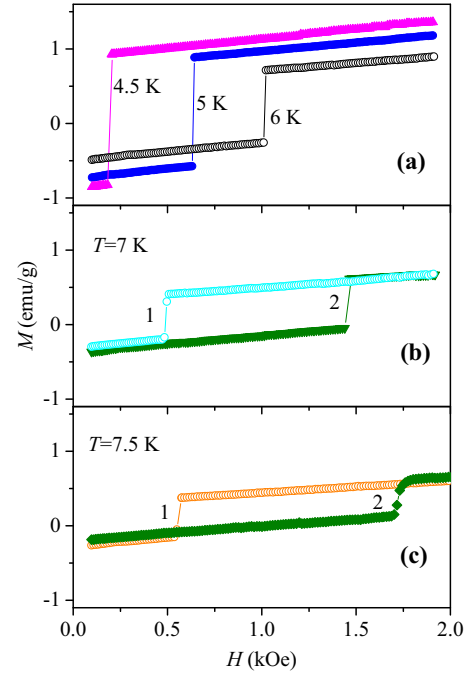


FIG. 7.  $M$  vs  $H$  curves measured along the  $a$  axis at several temperatures below  $T_{\text{comp}}$  after the same FC procedure in a field of 100 Oe. Two different spin switching fields  $H_{\text{sw}}$  can be detected in repeated cycles at temperatures of 7 and 7.5 K, see curves 1 and 2 in (b) and (c).

of  $\Delta MH$  on  $H$  in Fig. 6(b) clearly shows the field-induced transition from low to high switching energy.

The temperature range between 4.5 and 7.5 K, which exhibits a mysterious splitting of temperature  $T_{\text{sw}}$  and switching energy  $\Delta E_z$ , was further investigated using magnetization curves  $M$  vs  $H$  measured at different constant temperatures  $T$ , presented in Fig. 7. Each magnetization curve began after performing the same FC procedure in a field of 100 Oe from 230 K to a given  $T$ . The  $M$  vs  $H$  curves show a sharp jump in magnetization at spin switching fields  $H_{\text{sw}}$ , which are shown as open circles in the  $T-H$  diagram, see Fig. 5. It appears that the obtained points practically coincide with those determined from the  $M$  vs  $T$  curves, namely, they are located either on the lower or upper lines  $T_{\text{sw}}-H_{\text{sw}}$ , which are described with different switching energies  $\Delta E_z$ . Interestingly, at temperatures of 7 and 7.5 K, spin switching can be detected simultaneously in both the lower and upper  $H_{\text{sw}}$  fields [see Figs. 7(b) and 7(c)], i.e., a jump in the  $H_{\text{sw}}$  field is observed, very similar to a temperature jump at fields of about 800 Oe, see Fig. 5. In this case, the gap in switching energy  $\Delta E_z$ , calculated as the product  $\Delta M \Delta H_{\text{sw}}$ , also corresponds well to that shown in Fig. 6.

To elucidate the nature of the field-induced transition to states with a high spin-switching energy, which leads to a shift of the  $T_{\text{sw}}-H_{\text{sw}}$  line to low  $T$  and high  $H$ , we consider possible contributions to the crystal magnetic anisotropy energy  $E_a$ , which is actually an energy barrier for spin-switching. Previously, it was shown for a compensated ferrimagnet such as  $\text{ErFeO}_3$  that, the position of the spin switching line in the  $T-H$  plane depends on both the magnitude and the type of

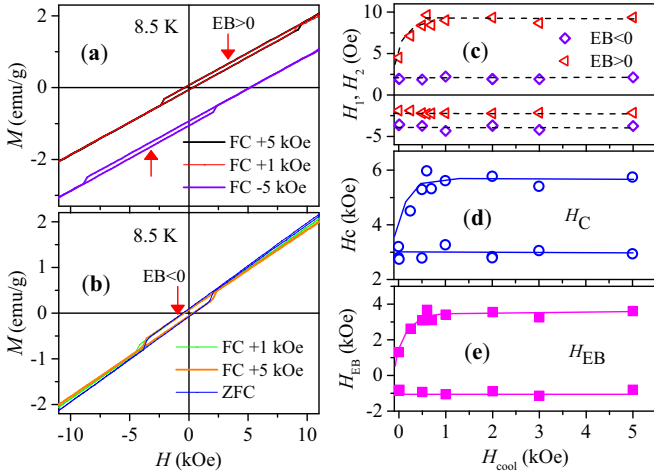


FIG. 8. (a), (b) NdFeO<sub>3</sub> magnetization hysteresis loops measured at  $T = 8.5$  K, in the field range from 15 kOe to  $-15$  kOe along the  $a$  axis, and at various cooling fields (the loop for FC  $-5$  kOe is shifted down by 1 emu/g for clarity). Loops randomly show either positive (a) or negative (b) EB field  $H_{EB}$ , marked by arrows. (c), (d), (e) For each FC field higher than 800 Oe, two different pairs of switching fields, negative  $H_1$  and positive  $H_2$ , are observed, corresponding to two different values of the field  $H_{EB}$  and to two average coercive fields  $H_C$  (the cases  $EB > 0$  and  $EB < 0$ ).

magnetic anisotropy [21]. In the case of conventional uniaxial magnetic anisotropy  $K$ , which provides the same energy barrier for both spin up and down switching, it turns out that the asteroidlike lines  $T_{sw}-H_{sw}$  on the  $T-H$  plane limit the region of metastable states (see Fig. 7 in Ref. [21]). This region collapses to the point ( $T = T_{comp}$ ,  $H = 0$ ) when the anisotropy  $K$  decreases to zero. In the case when the unidirectional anisotropy  $U$ , which arises due to the exchange bias effect, is added to the uniaxial anisotropy  $K$ , the energy barrier for spin switching in one direction of the easy axis increases to a value of  $K + U$ , and in the opposite direction decreases to  $K - U$ , since the sign of anisotropy  $U$  depends on direction. Consequently, positive anisotropy  $U$  shifts the  $T_{sw}-H_{sw}$  line further from  $T_{comp}$ , and negative anisotropy brings this line closer to  $T_{comp}$ . Therefore, it can be assumed that the EB effect, which is known to exist in NdFeO<sub>3</sub> near  $T_{comp}$  [3], is the cause of the field-induced increase in the spin switching energy and the shift of the  $T_{sw}-H_{sw}$  line. Recall that a positive EB (shift of the magnetization hysteresis loop towards field cooling) induced by applied  $H_{cool} = 15$  kOe was observed earlier in NdFeO<sub>3</sub> below  $T_{comp}$  [3]. To elucidate this issue, we studied in detail the EB in NdFeO<sub>3</sub> in the vicinity of  $T_{comp}$  at various fields FC. Figures 8(a) and 8(b) shows several typical magnetization hysteresis loops between fields of 15 kOe and  $-15$  kOe obtained with different FC modes at  $T = 8.5$  K. Surprisingly, the loop measured in the ZFC mode exhibits a negative EB with field  $H_{EB} \approx -1000$  Oe, while loops obtained with various  $H_{cool}$  from 1 to 5 kOe show randomly either a positive shift  $H_{EB} \approx +3500$  Oe, or negative shift  $H_{EB} \approx -1000$  Oe. Also, change of the sign of the field  $H_{cool}$  symmetrically changes the direction of the loop shift, confirming the occurrence of the positive EB. It turns out that

for every FC field greater than 800 Oe, there are two different pairs of switching fields, negative  $H_1$  and positive  $H_2$ , [see Fig. 8(c)], corresponding to two different values of the field  $H_{EB} = (H_2 - H_1)/2$  [Fig. 8(e)] and to two average coercive fields  $H_C = (H_2 + H_1)/2$  [Fig. 8(d)]. The difference  $\Delta H_{EB}$  in two different states is 4.5 kOe, and the field  $H_C$  is about 5.7 kOe in the case of positive EB and  $H_C \approx 3$  kOe in the case of  $EB < 0$ . It is noteworthy that the FC field of 800 Oe splits both the exchange bias and the coercive field, and also the same magnitude of the cooling field causes sharp jumps in both  $T_{sw}$ ,  $\Delta M$ , and the spin switching energy [see Figs. 3 and 6], which indicates a common origin of these phenomena. The coexistence of positive and negative exchange bias may reflect the existence of two very different spin-switching energies  $\Delta E_Z$  [see Fig. 6], which are associated with two different magnetic states and describe the lower and upper phase lines  $T_{sw}-H_{sw}$  below  $T_{comp}$  [see Fig. 5]. This is well confirmed by the coincidence of the positive switching fields  $H_2$ , determined from the magnetization hysteresis loops, with the upper line  $T_{sw}-H_{sw}$  in the case of a positive EB and with the lower line in the case of a negative EB [see fields  $H_2$  at 8 and 8.5 K marked with asterisks in Fig. 5]. Indeed, if the positive/negative EB is associated to the upper/lower  $T_{sw}-H_{sw}$  line shown in Fig. 5, one can distinguish between the two separated levels of spin-switching energies shown in Fig. 6 as follows:  $\Delta E_{Z1} = K + U_{pos} = 925 \text{ emu g}^{-1} \text{ Oe}$  and  $\Delta E_{Z2} = K + U_{neg} = 345 \text{ emu g}^{-1} \text{ Oe}$ , where  $K$  is the uniaxial anisotropy constant,  $U_{pos}$ , and  $U_{neg}$  are unidirectional anisotropy energies in the cases of positive and negative EB. It follows that the gap in the spin switching energy is equal to the difference in the anisotropy energies  $U$ :  $\Delta E_{Z1} - \Delta E_{Z2} = U_{pos} - U_{neg} = 580 \text{ emu g}^{-1} \text{ Oe}$ . Interestingly, the same result follows directly from the EB hysteresis loops data: considering that  $U = \Delta M H_{EB}$  and at  $T = 8.5$  K  $\Delta M = 0.13 \text{ emu/g}$ , and  $H_{EB}$  takes values of 3500 Oe or  $-1000$  Oe (see Fig. 8), we calculate  $U_{pos} = 455 \text{ emu g}^{-1} \text{ Oe}$  and  $U_{neg} = -130 \text{ emu g}^{-1} \text{ Oe}$ , so the difference  $U_{pos} - U_{neg} = 585 \text{ emu g}^{-1} \text{ Oe}$  represents the gap in the spin switching energy. In addition, from the relationship  $\Delta E_{Z1} + \Delta E_{Z2} = 2K + U_{pos} + U_{neg} = 1270 \text{ emu g}^{-1} \text{ Oe}$ , we estimate the uniaxial anisotropy constant  $K = 472 \text{ emu g}^{-1} \text{ Oe}$ . The above estimates, made on the basis of experimental data obtained by various methods, convincingly indicate that the spin switching energy gap in NdFeO<sub>3</sub> arises due to the coexistence of positive and negative EB. However, the nature of the EB field fluctuations between the two opposite values remains unclear. It can be assumed that the magnetization vector of the ferrimagnetic system has two local energy minima, separated from each other by an energy barrier and the studied system can quantum-mechanically tunnel between these metastable magnetic states [23]. A good example for such a phenomenon is tunneling of the magnetic moment of a single-domain ferromagnetic particle between the energy minima created by the magnetic anisotropy [24]. As shown above, NdFeO<sub>3</sub> exhibits quantum behavior at low temperatures, which is reflected in the effective spin 1/2 for Nd<sup>3+</sup> due to the well isolated Kramers doublet in the ground state. It is important to note that the zero-field Zeeman splitting of the ground doublet, caused mainly by the Nd-Fe exchange field, is of about 7 K [2,25]. Therefore, it can be expected that at lower temperatures the upper level of the ground doublet will be less filled,

which leads to an increase in the density of states of the lower level. An external magnetic field applied in the FC regime can change the effective Zeeman splitting and, consequently, varies the populations of both levels of the ground doublet. Moreover, the FC field in the temperatures above the switching temperature  $T_{sw}$  is opposite to the exchange field, so that the doublet splitting effectively decreases, while below  $T_{sw}$  it is directed along the exchange field and the splitting increases. This competition between external and internal fields strongly affects the metastable magnetic state, characterized by negative magnetization and known to be responsible for the positive EB effect in compensated orthoferrites [3,21], while the negative EB is associated with the equilibrium magnetic state. Here, we note that in conventional bilayer FM-AFM systems, the positive EB appears in the case of AFM interaction between layers [26]. The complex interplay of the above effects can push the magnetic system towards one of the two local energy minima through the energy barrier between them during the FC process, resulting in a positive or negative EB effect. However, to elucidate the true reason for the coexistence of opposite EB effects and the appearance of a gap in the spin switching energy in NdFeO<sub>3</sub>, further studies are required. In particular, one way, expanding the temperature range of magnetic measurements to higher temperatures up to 690 K, in order to be able to start measurements from the paramagnetic state [27], can provide useful information and shed light on the mysterious nature of EB in NdFeO<sub>3</sub>.

It should also be noted that the observed anomalous discontinuity in the  $T_{sw}$ - $H$  phase line may be of interest in connection with very recent discovery of the possibility of toroidal ordering in NdFeO<sub>3</sub> obtained in neutron diffraction experiments [28]. It has been suggested [29] that Nd ions

possess Dirac multipoles, both magnetic and polar, which are permitted in the monoclinic space group found in NdFeO<sub>3</sub> instead of the usual orthorhombic one [28], so this compound is unique, providing strong correlations between anapole and orbital degrees of freedom.

In conclusion, it was found that in the compensated NdFeO<sub>3</sub> ferrimagnet, the magnetization  $M$ , the spin switching temperature  $T_{sw}$ , and the magnetization jump  $\Delta H$  at  $T_{sw}$  are well described within a simple compensation model that includes the competition of the FM moment from the canted spins of Fe and the effective interaction field Nd-Fe, as was found earlier in compensated ErFeO<sub>3</sub> and GdCrO<sub>3</sub>. However, in contrast to these ferrimagnets, below  $T_{comp}$  in NdFeO<sub>3</sub> there is an anomalous discontinuity in the dependence of  $T_{sw}$  on the cooling field  $H$ , which actually leads to two different  $T_{sw}$ - $H$  phase lines shifted in opposite directions in temperature, which are described by two different spin-switching energies. In an agreement, the same discontinuity of about 600 emu g<sup>-1</sup> Oe in the switching energy in low and high fields was determined directly from the data on the magnetization jump  $\Delta M$  at  $T_{sw}$ . On the other hand, this switching energy difference turned out to be equal to the difference between the energies of the unidirectional anisotropy for positive and negative EB, both measured near  $T_{comp}$ . This convincingly indicates that the split spin switching energy and the anomalous  $T_{sw}$ - $H$  dependence in NdFeO<sub>3</sub> arise below  $T_{comp}$  due to the coexistence of two different exchange biases of opposite signs.

The authors are grateful to Prof. G. Gorodetsky and Dr. V. Markovich for providing NdFeO<sub>3</sub> crystals.

- 
- [1] S. J. Yuan, W. Ren, F. Hong, Y. B. Wang, J. C. Zhang, L. Bellaiche, S. X. Cao, and G. Cao, Spin switching and magnetization reversal in single-crystal NdFeO<sub>3</sub>, *Phys. Rev. B* **87**, 184405 (2013).
- [2] J. Bartolome, E. Palacios, M. D. Kuz'min, F. Bartolome, I. Sosnowska, R. Przeniosło, R. Sonntag, and M. M. Lukina, Single-crystal neutron diffraction study of Nd magnetic ordering in NdFeO<sub>3</sub> at low temperature, *Phys. Rev. B* **55**, 11432 (1997).
- [3] I. Fita, A. Wisniewski, R. Puzniak, E. E. Zubov, V. Markovich, and G. Gorodetsky, Common exchange-biased spin switching mechanism in orthoferrites, *Phys. Rev. B* **98**, 094421 (2018).
- [4] M. H. Mohammed, Zh. Cheng, S. X. Cao, and J. Horvat, Magnetization reversal on different time-scales for ErFeO<sub>3</sub> and NdFeO<sub>3</sub> single crystals, *Phys. Chem. Chem. Phys.* **23**, 5415 (2021).
- [5] D. Treves, Studies on orthoferrites at the Weizmann Institute of Science, *J. Appl. Phys.* **36**, 1033 (1965).
- [6] A. Kumar and S. M. Yusuf, The phenomenon of negative magnetization and its implications, *Phys. Rep.* **556**, 1 (2015).
- [7] S. Cao, H. Zhao, B. Kang, J. Zhang, and W. Ren, Temperature induced spin switching in SmFeO<sub>3</sub> single crystal, *Sci. Rep.* **4**, 5960 (2014).
- [8] J.-H. Lee, Y. K. Jeong, J. H. Park, M.-A. Oak, H. M. Jang, J. Y. Son, and J. F. Scott, Spin-canting-induced improper ferroelectricity and spontaneous magnetization reversal in SmFeO<sub>3</sub>, *Phys. Rev. Lett.* **107**, 117201 (2011).
- [9] J. A. de Jong, A. V. Kimel, R. V. Pisarev, A. Kirilyuk, and Th. Rasing, Laser-induced ultrafast spin dynamics in ErFeO<sub>3</sub>, *Phys. Rev. B* **84**, 104421 (2011).
- [10] J.-S. Jung, A. Iyama, H. Nakamura, M. Mizumaki, N. Kawamura, Y. Wakabayashi, and T. Kimura, Magnetocapacitive effects in the Néel  $N$ -type ferrimagnet SmMnO<sub>3</sub>, *Phys. Rev. B* **82**, 212403 (2010).
- [11] R. Huang, S. Cao, W. Ren, S. Zhan, B. Kang, and J. Zhang, Large rotating field entropy change in ErFeO<sub>3</sub> single crystal with angular distribution contribution, *Appl. Phys. Lett.* **103**, 162412 (2013).
- [12] I. Fita, R. Puzniak, A. Wisniewski, and V. Markovich, Spin switching and unusual exchange bias in the single-crystalline GdCrO<sub>3</sub> compensated ferrimagnet, *Phys. Rev. B* **100**, 144426 (2019); I. Fita, R. Puzniak, and A. Wisniewski, Pressure-tuned spin switching in compensated GdCrO<sub>3</sub> ferrimagnet, *ibid.* **103**, 054423 (2021).
- [13] Y. Cao, S. Cao, W. Ren, Z. Feng, S. Yuan, B. Kang, B. Lu, and J. Zhang, Magnetization switching of rare earth orthochromite CeCrO<sub>3</sub>, *Appl. Phys. Lett.* **104**, 232405 (2014).



- [14] A. Kumar, S. M. Yusuf, and C. Ritter, Nd-ordering-driven Mn spin reorientation and magnetization reversal in the magnetostructurally coupled compound  $\text{NdMnO}_3$ , *Phys. Rev. B* **96**, 014427 (2017).
- [15] Ankita Singh, A. Jain, Avijeet Ray, B. Padmanabhan, Ruchika Yadav, Vivian Nassif, Sajid Husain, S. M. Yusuf, T. Maitra, and V. K. Malik, Spin reorientation in  $\text{NdFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ : Neutron scattering and *ab initio* study, *Phys. Rev. B* **96**, 144420 (2017).
- [16] W. Sławiński, R. Przeniosło, I. Sosnowska, and E. Suard, Spin reorientation and structural changes in  $\text{NdFeO}_3$ , *J. Phys.: Condens. Matter* **17**, 4605 (2005).
- [17] Ya. B. Bazaliy, L. T. Tsybal, G. N. Kakazei, A. I. Izotov, and P. E. Wigen, Spin-reorientation in  $\text{ErFeO}_3$ : Zero-field transitions, three-dimensional phase diagram, and anisotropy of erbium magnetism, *Phys. Rev. B* **69**, 104429 (2004).
- [18] I. Fita, A. Wisniewski, R. Puzniak, V. Markovich, and G. Gorodetsky, Exchange-bias reversal in magnetically compensated  $\text{ErFeO}_3$  single crystal, *Phys. Rev. B* **93**, 184432 (2016).
- [19] X. Wang, S. Gao, X. Yan, Q. Li, J. Zhang, Y. Long, K. Ruan, and X. Li, Giant spontaneous exchange bias obtained by tuning magnetic compensation in samarium ferrite single crystals, *Phys. Chem. Chem. Phys.* **20**, 3687 (2018).
- [20] S. L. Ding, M. Z. Xue, Z. Y. Liang, Z. Liu, R. B. Li, S. X. Cao, Y. B. Sun, J. J. Zhao, W. Y. Yang, and J. B. Yang, Spin switching temperature modulated by the magnetic field and spontaneous exchange bias effect in single crystal  $\text{SmFeO}_3$ , *J. Phys.: Condens. Matter* **31**, 435801 (2019).
- [21] I. Fita, R. Puzniak, E. E. Zubov, P. Iwanowski, and A. Wisniewski, Temperature-driven spin switching and exchange bias in the  $\text{ErFeO}_3$  ferrimagnet, *Phys. Rev. B* **105**, 094424 (2022).
- [22] A. H. Cooke, D. M. Martin, and M. R. Wells, Magnetic interactions in gadolinium orthochromite,  $\text{GdCrO}_3$ , *J. Phys. C* **7**, 3133 (1974).
- [23] E. M. Chudnovsky, Macroscopic quantum tunneling of the magnetic moment (invited), *J. Appl. Phys.* **73**, 6697 (1993).
- [24] E. M. Chudnovsky and L. Gunther, Quantum tunneling of magnetization in small ferromagnetic particles, *Phys. Rev. Lett.* **60**, 661 (1988).
- [25] M. Loewenhaupt, I. Sosnowska, and B. Frick, Spin-reorientation in  $\text{NdFeO}_3$  and the magnetic excitation spectrum of Nd, *J. Phys. Colloques* **49**, C8-921 (1988).
- [26] J. Nogues, D. Lederman, T. J. Moran, and Ivan K. Schuller, Positive exchange bias in  $\text{FeF}_2 - \text{Fe}$  bilayers, *Phys. Rev. Lett.* **76**, 4624 (1996).
- [27] T. Shalini, P. Vijayakumar, and J. Kumar, Studies on structural and magnetic properties of  $\text{NdFeO}_3$  single crystals grown by optical floating zone technique, *Bull. Mater. Sci.* **43**, 285 (2020).
- [28] P. Fabrykiewicz, R. Przeniosło, and I. Sosnowska, Magnetic, electric and toroidal polarization modes describing the physical properties of crystals.  $\text{NdFeO}_3$  case, *Acta. Crystallogr. A* **79** 80 (2023).
- [29] S. W. Lovesey, Orthoferrite with a hidden lanthanide magnetic motif:  $\text{NdFeO}_3$ , *Phys. Rev. B* **107**, 214426 (2023); see also: S. W. Lovesey, T. Chatterji, A. Stunalt, D. D. Khalyavin, and G. van der Laan, Direct observation of anapoles by neutron diffraction, *Phys. Rev. Lett.* **122**, 047203 (2019).