Letter

Superconductivity at carrier density 10^{17} cm^{-3} in quasi-one-dimensional $Li_{0.9}Mo_6O_{17}$

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Quasi-one-dimensional systems, having tendencies toward density-wave order in competition with superconductive pairing in their ground states, may give rise to unconventional superconductivity, a central theme in condensed matter physics. Partial density-wave gapping of electronic bands at the Fermi surface in such systems can yield superconductivity at very low carrier density that challenges Bardeen-Cooper-Schrieffer (BCS) theory since the pairing energy scale may approach or exceed the Fermi energy and render screening of the Coulomb interaction ineffective. Here we present low-T magnetotransport measurements on the quasi-one-dimensional conductor $Li_{0.9}Mo_6O_{17}$ showing the metallic state from which superconductivity emerges ($T_c \simeq 2$ K) to possess among the lowest known carrier densities, $\sim 10^{17}$ cm^{-3}, and a ratio of T_c to Fermi temperature within the BCS–Bose-Einstein-condensation crossover regime. A semimetallic state caused by a density-wave-induced Fermi surface reconstruction with highly anisotropic electron and hole pockets is implied. The degree of interpocket nesting appears to determine whether the extreme low-density ground state is superconducting or undergoes additional Fermi surface gapping.

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Electron pairing in the Bardeen-Cooper-Schrieffer (BCS) theory of superconductivity, arising from weak attractive interactions in a degenerate fermionic system, results in a superconducting transition temperature that is typically orders of magnitude smaller than the Fermi temperature, $T_c/T_F \sim 10^{-4}$. In the opposite limit of a Bose-Einstein condensate (BEC), strongly coupled fermions (composite bosons) condense into a coherent quantum state, and typically $T_c/T_F \gtrsim 0.1$ [1]. A small number of materials having $T_c/T_F \sim 0.04$–0.1 within the BCS-BEC crossover regime include high-T_c cuprates and heavy-fermion and Fe-based compounds, superconductors believed to involve spin-mediated pairing [2–4].

Quasi-one-dimensional (q1D) electron systems may harbor unconventional superconductivity within the BCS-BEC crossover regime when partial density-wave gapping of electronic bands at the Fermi surface (FS), induced by competing density-wave order, yields a metallic state with very small Fermi energy. $Li_{0.9}Mo_6O_{17}$ (lithium purple bronze, LiPB) is a transition metal oxide with q1D electronic properties. Its resistivity is metallic at high T, exhibits a minimum at 15 K $\lesssim T_{\min} \lesssim 30$ K, and rises below $T_{\min}$ to the superconducting transition at $T_c \simeq 2$ K [5–7]. The metallic phase at $T \geqslant T_{\min}$ exhibits features [8,9] of a Tomonaga-Luttinger liquid (TLL) [10] with spin-charge separation [11–13]. The mechanisms for the upturn in the resistivity at $T < T_{\min}$ and superconductivity remain a mystery in spite of substantial experimental efforts over decades. The superconducting state is three dimensional with highly anisotropic upper critical fields (H_{c2}) consistent with its normal-state electrical anisotropy [7]. For field applied along the q1D chains, H_{c2} substantially exceeds the Pauli paramagnetic limit, motivating the proposal [7] that LiPB is a triplet superconductor [14–18].

The LiPB band structure, studied extensively via photoemission [19] and computation [11,19–22], consistently reveals two q1D, nearly degenerate electron bands crossing the Fermi energy, derived from d_{xy} orbital overlap along the zigzag Mo-O chains (crystallographic b axis). Superconductivity requires a dimensionality increase, for which the resistivity minimum is presumed to be the signature. Potential explanations include charge- or spin-density-wave (CDW or SDW) formation, a structural change [23,24], and a recent proposal involving the ordering of long-lived excitons [25,26]. Experiments rule out CDW [23,27,28] and SDW [29] order (though the latter less convincingly), and good agreement between the local-density approximation band structure and photoemission [19] for the bands near E_F is compelling evidence against the occurrence of a TLL fluctuation-induced suppression of dimensional crossover [30].

Here we report comprehensive magnetotransport measurements within the most conducting bc plane (field along a) at $T \gtrsim 0.4$ K for both superconducting (SC) and nonsuperconducting (non-SC) LiPB crystals, revealing extremely low carrier densities ($n \sim 10^{17}$ cm^{-3}) throughout the range $T \leqslant 100$ K and a rich multicarrier physics. The mobile carrier densities are among the lowest known for any superconductor [31,32], placing superconductivity of LiPB in a regime at the border between BCS and BEC. A density-wave-induced semimetallic reconstruction of the FS composed of highly anisotropic electron and hole pockets is implicated at $T \gg T_{\min}$ for both sets of samples. Competition for the ground state

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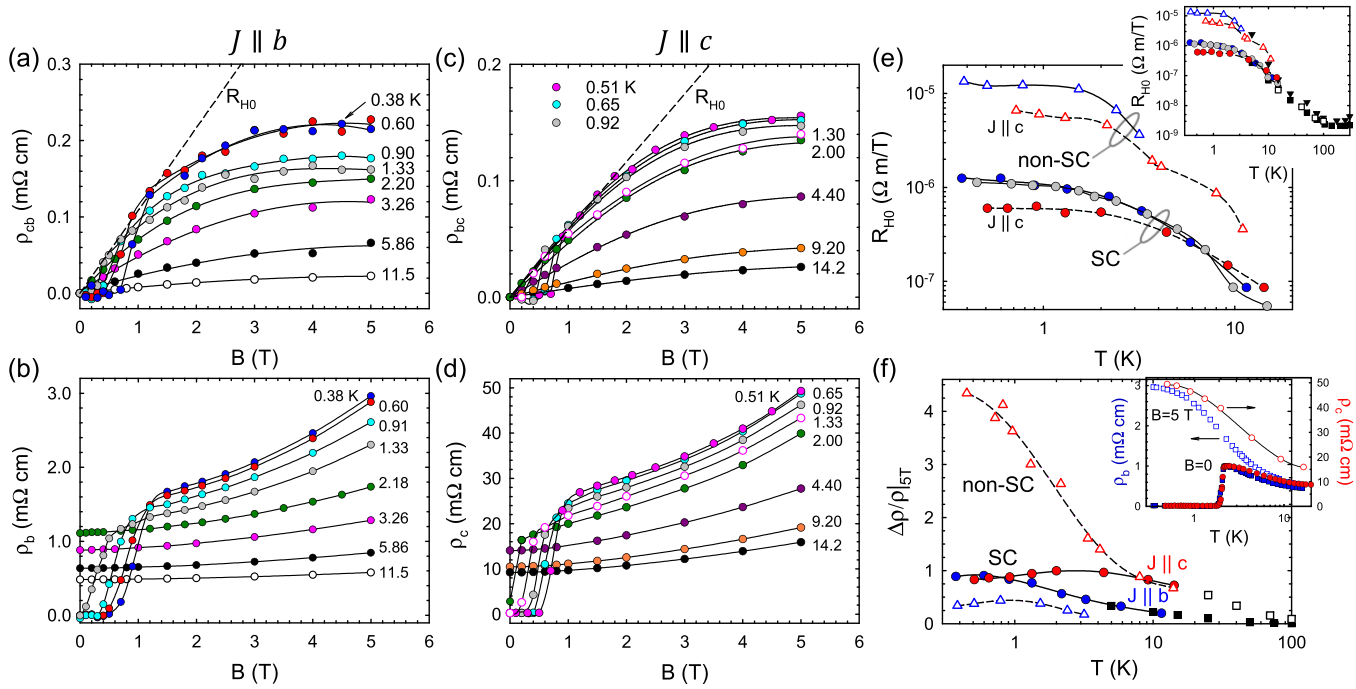

FIG. 1. (a)–(d) Hall and longitudinal resistivities for two orientations of the current flow **J** in superconducting crystals. Dashed lines in (a) and (c) are the initial slopes, $R_{H0} \equiv d\rho_{xy}/dB|_{B\to 0}$, at low T. (e) R_{H0} vs T for all crystals (SC, filled symbols; non-SC, open symbols). The inset compares data from the main panel with data at higher T for crystals from Refs. [35,36] with current parallel to b (filled squares and inverted triangles) and parallel to c (open squares). (f) Longitudinal magnetoresistance at $B = 5$ T vs T for all crystals. The inset shows $\rho_b(T)$ (squares, left ordinate) and $\rho_c(T)$ (circles, right ordinate) at $B = 0, 5$ T. Solid and dashed curves are guides for the eye.

appears to be controlled by the degree of interpocket nesting, leading to further density-wave gapping (non-SC samples) or superconductivity. This nesting is manifested in the strong scattering and localization of in-chain hole and interchain electron states on the reconstructed FS at $T \gtrsim T_{\min}$. A sharp suppression of this scattering in SC samples at $T \lesssim T_{\min}$ signals delocalization of these states and emergence of quasi-two-dimensional transport within each of the pockets as a precursor to superconductive pairing.

Figures 1(a)–1(d) show the field-dependent Hall and longitudinal resistivities for two orientations of the electric current flow ($\mathbf{J}\|b$ and $\mathbf{J}\|c$) in SC crystals at various T. Similar data for the non-SC crystals are presented in the Supplemental Material [33] (Fig. S1). Superconducting transitions are evident at low fields for temperatures $T < T_c$ [see also the inset of Fig. 1(e)]; the inferred upper critical fields and range of values for $T_{\min}$ [$\sim$18 K ($\sim$30 K) for the SC (non-SC) specimens] agree with those of prior studies [5–7] (Fig. S2 [33]).

Substantial nonlinearities of the Hall resistivities with field (especially at the lowest T) suggest the presence of charge carriers with opposing signs. The initial slopes, $R_{H0} \equiv d\rho_{xy}/dB|_{B\to 0}$ [Fig. 1(e)] yield $T \to 0$ values $R_{H0} \simeq 10^{-6}$ (10^{-5}) Ω m/T for SC (non-SC) samples, corresponding to approximate carrier densities, $n = 1/(R_{H0}e) \simeq 6 \times 10^{18}$ (6×10^{17}) cm^{-3}. However, the data are more aptly described by an anisotropic, two-carrier model, for which $R_{H0} = (n_h\mu_h^2 - n_e\mu_e^2)e/[\sigma_b(0)\sigma_c(0)]$ (where $\sigma_b(0)$ and $\sigma_c(0)$ are the zero-field conductivities) as discussed further below.

The thermoelectric coefficients tell a similar story of extremely low carrier density. The field dependencies of the Nernst signal, $N_{yx} = E_y/|\nabla T_x|$, and thermopower, $S_x = E_x/\nabla T_x$ ($x, y = b, c$), for the SC crystals are shown in Figs. 2(a)–2(d). Note the different vertical scales (millivolts versus microvolts) for N_{cb} (heat current $\mathbf{J}_q\|b$) and N_{bc} ($\mathbf{J}_q\|c$): extreme anisotropy, $N_{cb} \simeq 300N_{bc}$, is observed. Sharp maxima in the low-field Nernst signals for $T < T_c$ (especially for N_{cb}) near the midpoints of the SC transitions are attributed to a flux-flow Nernst effect [34]. Very similar results for N_{cb} were found for a second SC crystal (Fig. S3 [33]). Possible contaminating signals associated with the Righi-Leduc (thermal Hall) effect are negligible for both orientations (Fig. S4 [33]). In comparison to the Nernst signal, the thermopower is more isotropic, with a stronger field dependence evident for S_c. Though the in-chain thermopower S_b is positive, it is decidedly electronlike at $T \gtrsim 30$ K: linear in T with negative slope, resulting in negative values at $T \gtrsim 300$ K [35–37].

Like the Hall resistivity, significant nonlinearity of the Nernst signals (particularly at low T) suggests competing electron and hole contributions. For comparison with the estimates from R_{H0}, we compute carrier densities from the $B = 5$ T, $T \to 0$ limiting values for ν/T ($\nu = N/B$) and S/T indicated by the dashed lines in Figs. 2(e) and 2(f). For a broad spectrum of correlated and low-dimensional metals it has been shown [38] that these quantities scale well with carrier mobility μ and Fermi temperature T_F as prescribed by the free-electron, Boltzmann theory expressions for carrier diffusion, $\nu/T = (\pi^2/3)(k_B/e)(\mu/T_F)$ and $S/T = (\pi^2/3)(k_B/e)(1/T_F)$. Using $\mu = 0.2$ T^{-1} (determined from the analysis below) and averaging values for the two experimental orientations, $\nu/T \simeq 15$ μV/(T K^2)

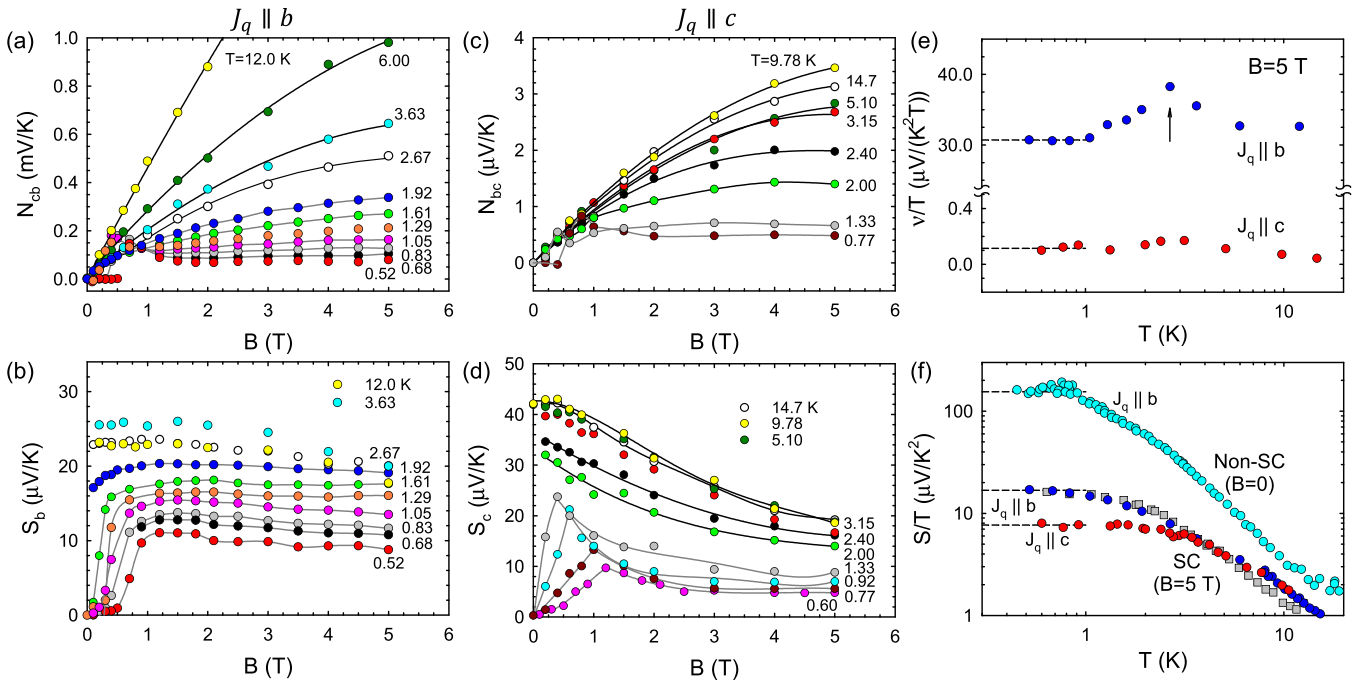

FIG. 2. (a)–(d) Nernst signal and thermopower for two orientations of the heat current $\mathbf{J}_q$ in superconducting crystals. Solid curves are guides for the eye. (e) and (f) T dependence of ν/T (e) and S/T (f). The vertical arrow in (e) marks a "kink" in ν/T near $T \simeq 3$ K (see text and Supplemental Material). The squares in (f) are from a second superconducting b-axis specimen.

($S/T \simeq 12\ \mu\text{V/K}^2$), we find $T_F \simeq 19$ K (23 K). The free-electron relation $E_F = k_B T_F = (\hbar^2/2m)(3\pi^2 n)^{2/3}$ thus implies $n \approx 3.5 \times 10^{17}\ \text{cm}^{-3}$.

To refine our understanding of the magnetotransport, consider a two-carrier model for the bc plane, with holes and electrons (densities n_h and n_e, respectively) for each direction having different mobilities, μ_{ib}, μ_{ic} ($i = h, e$) [39]. The model has four carrier densities (holes and electrons for each direction) but is simplified because for each pair of crystals (two orientations each, SC and non-SC), we observe $\rho_{cb} \simeq \rho_{bc}$ (Figs. 1(a), 1(c), and 1(e) and Supplemental Material, Fig. S1 [33]). This isotropy of the transverse magnetoresistivities contrasts with the anisotropy of the longitudinal magnetoresistivities, $\Delta\rho(B)/\rho(0)$ [Fig. 1(f)]. In such a case, the model dictates isotropy of hole and electron densities [39]. Switching to the equivalent and simpler conductivity expressions, the field dependencies of the coefficients are then given by

$$\sigma_b = \sigma_{hbb} + \sigma_{ebb} = \frac{n_h e\mu_{hb}}{(1+\mu_h^2 B^2)} + \frac{n_e e\mu_{eb}}{(1+\mu_e^2 B^2)},$$

$$\sigma_c = \sigma_{hcc} + \sigma_{ecc} = \frac{n_h e\mu_{hc}}{(1+\mu_h^2 B^2)} + \frac{n_e e\mu_{ec}}{(1+\mu_e^2 B^2)},$$

$$\sigma_{bc} = \sigma_{cb} = \sigma_{hbc} + \sigma_{ebc} = \frac{n_h e\mu_h^2 B}{(1+\mu_h^2 B^2)} - \frac{n_e e\mu_e^2 B}{(1+\mu_e^2 B^2)},$$

where $\mu_h = \sqrt{\mu_{hb}\mu_{hc}}$ and $\mu_e = \sqrt{\mu_{eb}\mu_{ec}}$ are effective mobilities governing the field dependencies. Examples of the simultaneous fitting to these equations at various temperatures and the computed partial conductivities are presented in Figs. S5–S7 [33]. The fitted values of the carrier densities and mobilities as functions of T are shown in Fig. 3. The analysis was extended to higher T for SC crystals using data from prior work [35,36] in the range $25\ \text{K} \leqslant T \leqslant 100$ K [open and filled squares in the inset of Fig. 1(e) and in Fig. 1(f)], where the magnetoresistance and Hall resistivity are quadratic and linear, respectively, in applied fields $B \leqslant 5$ T, consistent with prior studies [6,7,40,41]. The same model parameters were employed to fit the field-dependent thermoelectric coefficients (Eqs. (S1)–(S3) and Figs. S8 and S9 [33]) to extract partial coefficients for holes and electrons. The "kink" in the ν/T curve [arrow in Fig. 2(e)] is found to arise from competition between Nernst terms (carrier diffusion and the product of Hall conductivity and thermopower) with opposite sign (Eq. (S2) and Fig. S9 [33]).

A central outcome of the analysis is that, consistent with the measured $R_{H0}(T)$ for multiple specimens and orientations [inset of Fig. 1(e)], the carrier densities for both SC and non-SC crystals [Fig. 3(a)] are comparable at $T \gtrsim 10$ K, with $n_e \sim 3.5 n_h \simeq 10^{17}\ \text{cm}^{-3}$ in the former. Thus LiPB is partially compensated, with extremely low carrier densities throughout the entire T range. This result is not in conflict with established TLL physics at higher T for LiPB since TLL characteristics are independent of carrier density [42]. The single-band expression $n = 1/(R_{H0}e)$ at 100 K yields $n \sim 3 \times 10^{21}\ \text{cm}^{-3}$, a substantial overestimate of the actual value, and coincidentally comparable to, though opposite in sign, that expected from the band structure and chemical valence, 1.9 e/unit cell [13,35]. The rise in R_{H0} by more than two orders of magnitude from $T \sim 100$ K to $T \sim 10$ K [35,40,41,43] is almost entirely attributable to an increase in the effective carrier mobilities [dashed curves, Fig. 3(b)] [44].

The small density (or T_F) is incompatible with the large Fermi wave number $k_F \simeq \pi/(2b)$ determined by photoemission and density functional theory but is entirely consistent, as is compensation, with LiPB's giant Nernst coefficient over

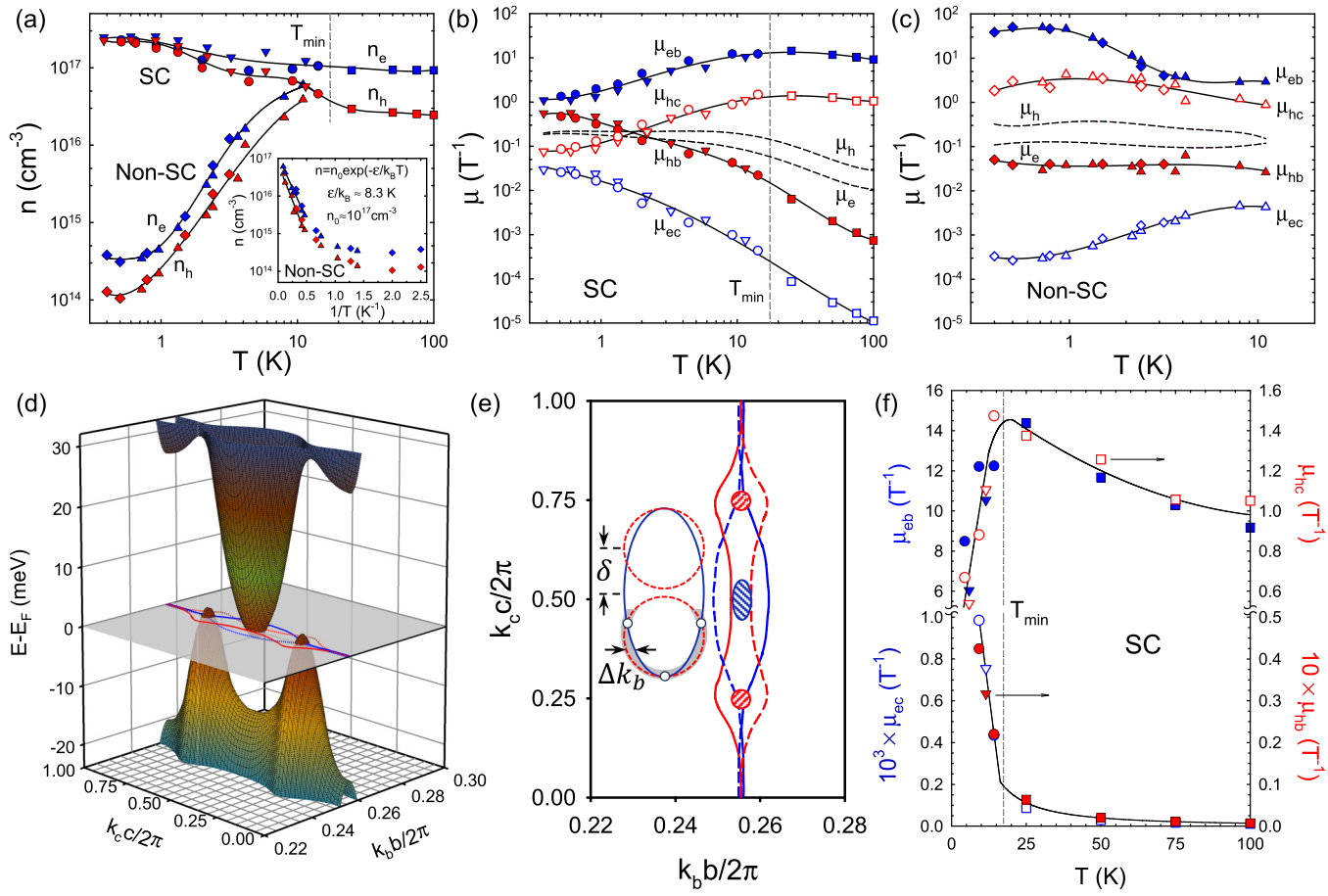

FIG. 3. Carrier densities (a) and mobilities for SC (b) and non-SC specimens (c) determined by simultaneous fitting to the anisotropic two-band model (see text and Supplemental Material). Different symbols represent the two crystals for which $\mathbf{J}\|b$ and $\mathbf{J}\|c$. Solid and dashed curves are guides for the eye. (d) Energy band scheme and Fermi plane (adapted from Ref. [19]) assuming a SDW gap-induced reconstruction to a semimetal with $E_F = 1.5$ meV for both hole and electron bands (see text). Shown in the $E = E_F$ plane of (d) and in (e) is the incomplete nesting of the unreconstructed FS (solid curves: upper sheet, red; lower sheet, blue) and their translations by the nesting vector $q_{\rm SDW} = 2k_F \simeq \pi/b$ along k_b (dashed curves), defining hole (red) and electron (blue) pockets between their respective boundaries. Note the greatly expanded scale for the k_b axis in both (d) and (e). The inset in (e) shows a magnified view of potential nesting for the electron and hole pockets (hatched regions in main panel): The best nesting is shown by the dashed hole pockets translated along k_c by $q = \pm(\pi/2c \pm \delta)$, with $\delta \sim 0.1(\pi/2c)$. The shaded region for the lower translation represents the approximate phase space at $T \approx T_{\rm min}$ for its nesting instability, the width of which normal to the FS is $\sim k_B T$ and at $T = 0$ is confined to the hot spots (small open circles). (f) Mobilities for SC samples with linear scaling (curves are guides for the eye).

a broad range of T [$\sim$45 μV/(K^2 T) at 100 K] [36]. A reconstruction of the FS (at $T > 100$ K) into small electron and hole pockets with highly anisotropic q1D character is implied. The prospect of spin-density-wave gapping of the FS for commensurate nesting vector $q_{\rm SDW} = 2k_F$ along k_b was considered in Ref. [19]. The nesting is imperfect due to small warping of the two d_{xy} FS sheets, associated with interchain (k_c) dispersions, and caused by hybridization with the gapped xz and yz valence and conduction bands via long-range indirect hopping. Gapping throughout the Brillouin zone occurs for $\Delta_{\rm SDW} \approx 65$ meV, though the interaction strength was estimated to be two to three times too small for such an instability [19]. Assuming a slightly smaller value for $\Delta_{\rm SDW}$, Fig. 3(d) depicts a semimetallic reconstruction of the bands [45] and FS using the gapped (unreconstructed) k_b (k_c) dispersions from Ref. [19] (Fig. S10 [33]). Consistent with estimates above from the thermoelectric coefficients, a small overlap was assumed with electron and hole Fermi energies being the same, $E_{F,e} = E_{F,h} = 1.5$ meV. The occupied FS areas for electrons and holes within this picture are each $\sim 3 \times 10^{-4} A_{\rm BZ}$ [$A_{\rm BZ} = (2\pi)^2/bc$ is the unreconstructed Brillouin zone area], consistent with the observed carrier densities [Fig. 3(e)]. Note the greatly expanded scale for the k_b axes in Figs. 3(d) and 3(e): The reconstructed pockets are highly anisotropic with a width along k_b of only $\sim 0.01(\pi/b)$. Within mean-field theory, the SDW transition temperature would be estimated as $T_{\rm SDW} \simeq 2\Delta_{\rm SDW}/(3.5k_B) \approx 420$ K, though incomplete nesting [46] can suppress $T_{\rm SDW}$. Alternatively, it is possible that rather than gapping large portions of the FS, strong scattering associated with density-wave fluctuations localizes states in extended, nearly nested regions of the FS sheets so that the photoemission and transport observations could be reconciled.

The overlapping electron and hole bands of the semimetallic FS reconstruction have very similar parabolic b-axis

dispersions (Fig. S10 [33]), and thus comparable values for μ_{eb} and μ_{hb} are anticipated. Indeed, for SC crystals at the lowest T ($\sim$0.4 K) this condition holds true [Fig. 3(b)]. Given that the unreconstructed band structure does not provide for in-chain hole conduction, this observation, along with the low density, provides compelling support for a semimetallic reconstruction such as that depicted in Figs. 3(d) and 3(e). However, this low-T electronic structure evolves gradually with the turning on of strong T-dependent mobilities at $T \lesssim T_{\min}$, as more clearly seen on the linear scaling of Fig. 3(f): μ_{hb} and μ_{ec} (in-chain holes and interchain electrons, lower panel) *increase* sharply below $T_{\min}$, while μ_{eb} and μ_{hc} (in-chain electrons and interchain holes, upper panel) *decrease* sharply. This opposing scattering behavior for the two groups of carriers is also reflected in opposing signs for their partial Seebeck coefficients (Fig. S8 [33]), as dictated by the scattering term in the Mott expression for diffusion thermopower, $S \sim d \ln \sigma(E)/dE|_{E_F} \sim d \ln \mu(E)/dE|_{E_F}$.

The values for μ_{hb} and μ_{ec} at $T \gtrsim 10$–20 K imply incoherence, with mean free paths that are comparable to or smaller than the interatomic spacing (Fig. S11 [33]) and three or more orders of magnitude smaller than those for in-chain electrons and interchain holes. Such highly anisotropic scattering on the FS pockets is likely associated with density-wave fluctuations and interpocket nesting for wave vectors along k_c [inset of Fig. 3(e)]. The substantial increase in the SC mobile carrier densities from $T_{\min}$ to $T \lesssim 1$ K (where they become constant), suggests that portions of the FS harbor large densities of localized states for in-chain holes and interchain electrons, the delocalization of which occurs gradually with decreasing T. This behavior may arise because the phase space for nesting [shaded region for the dashed hole FS; inset of Fig. 3(e)] declines with the thermal energy and at $T = 0$ is confined to hot spots at the intersections of the pockets (small open circles).

Supporting this picture, the in-chain hole and interchain electron states with greatest velocities lie within the shaded (nested) portions of their FSs [inset of Fig. 3(e)], while the most dispersive in-chain electron and interchain hole states remain unaffected or only partially so. Thus the decrease of the latter mobilities at $T < T_{\min}$ is a consequence of FS averaging and an increased weighting, with decreasing T, of delocalized portions of the FS having lower mobilities. Then $k_B T_{\min}$ should correspond to the maximum energy mismatch of pseudonesting, expressed approximately as $(\partial E/\partial k_b)\Delta k_b = \hbar v_{F,b} \Delta k_b$, where $v_{F,b}$ is the in-chain Fermi velocity and Δk_b is depicted in the inset of Fig. 3(e). We find $\hbar v_{F,b} \Delta k_b \simeq 0.9$ meV ($v_{F,b} = 1.8 \times 10^5$ m/s (Table S1 [33]), $E_{F,e} = E_{F,h} = 1.5$ meV as in Fig. 3(e)) and $\hbar v_{F,b} \Delta k_b \simeq 1.8$ meV ($v_{F,b} = 2.3 \times 10^5$ m/s, $E_{F,e} = 2.0$ meV, $E_{F,h} = 2.5$ meV), in reasonable accord with $k_B T_{\min}$ (1.5 meV).

A competition between further density-wave gapping of the FS and the occurrence of superconductivity will undoubtedly be sensitive to the Fermi energies of the electron and hole pockets, which presumably differ in SC and non-SC crystals. Indeed, further density-wave gapping for most of the FS is implicated in non-SC specimens by the exponential decline in carrier densities at $T \lesssim 10$ K [Fig. 3(a) and inset therein], with $n = n_0 \exp(-\varepsilon/k_B T)$ at $T \gtrsim 2$ K and averaged values $\varepsilon/k_B \simeq 8.3$ K (0.7 meV), $n_0 \simeq 10^{17}$ cm^{-3}. In spite of this carrier freeze-out, a residual density of carriers survives [$\simeq (1$–$3) \times 10^{14}$ cm^{-3}], and the in-chain conductivity extrapolates to a finite value as $T \to 0$ (Fig. S12 [33]): Metallicity is maintained by a concomitant increase in the electron mobility μ_{eb} [Fig. 3(c)]. The high values for μ_{eb} are a consequence of a small band effective mass for the reconstructed k_b dispersions ($\sim 0.016 m_e$, Table S1 [33]) and the fact that defects in LiPB (e.g., Li vacancies or O interstitials [35]) are far from the q1D chains confining electrons and expected to interact with weak Coulomb character [22]. Further confirming this extreme low-density metallic state is the thermopower, with $\lim_{T\to 0} S_b/T \simeq 150$ μV/K [top dashed line, Fig. 2(f)]. This value is among the largest reported for any metal [47], exceeding those for strongly correlated compounds known to have substantial fractions of their FSs gapped by novel ordering [48,49]. The non-SC interchain conductivity extrapolates to zero at finite T (Supplemental Material, Fig. S12): This absence of metallicity is consistent with expectations that superconductivity is not possible in lower than two dimensions.

Comparing the non-SC mobilities with those of SC samples at the lowest T, it is notable that the values of both μ_{eb} and μ_{hc} for the former exceed those of the latter by more than an order of magnitude while the opposite is true for μ_{hb} and μ_{ec}. This is consistent with better interpocket nesting for the non-SC samples and a full gapping of these portions of the FS. The absence of this gapping in SC specimens evidently sets the stage for superconductive pairing. $T_{\min}$ effectively behaves as a dimensional crossover scale, below which the q1D electron and hole transport along mutually perpendicular directions gradually evolves to the quasi-two-dimensional character of the low-T semimetal characterized by mobile states extending in both crystallographic directions on each FS pocket.

LiPB's low carrier density is comparable to those of $SrTiO_3$ ($T_c \simeq 0.86$ K at $n = 5.5 \times 10^{17}$ cm^{-3}) [31] and pure Bi ($T_c = 0.53$ mK at $n = 3 \times 10^{17}$ cm^{-3}) [32], and thus its much higher T_c is remarkable. The interelectron distance at T_c, $d_{ee} \simeq 1/n^{1/3} \approx 22$ nm, is comparable to the relevant superconducting coherence lengths [7], $\xi_b = 30$ nm and $\xi_c = 10$ nm, i.e., Cooper pairs do not substantially overlap. This and the ratio of critical temperature to effective Fermi temperature, $T_c/T_F \gtrsim 0.1$, place LiPB's parameters near the border between BCS superconductivity and BEC [50,51]. The characteristics of LiPB revealed in this Research Letter have similarities to those of Fe-based superconductors [4] and elevate the prospect that unconventional physics is at play, e.g., spin-fluctuation-induced interpocket pairing or pairing without phase coherence at $T > T_c$ [52]. Regarding the latter, the coexistence of pairs with single-particle excitations is evidenced in LiPB [53] for specimens with partial superconducting transitions intermediate between the SC and non-SC crystals reported here.

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