



**Superconductivity from orbital-selective electron-phonon coupling in  $AV_3Sb_5$** Ethan T. Ritz,<sup>1</sup> Henrik S. Røising ,<sup>2</sup> Morten H. Christensen,<sup>2</sup> Turan Birol,<sup>1</sup> Brian M. Andersen ,<sup>2</sup> and Rafael M. Fernandes<sup>3</sup><sup>1</sup>*Department of Chemical Engineering and Materials Science, University of Minnesota, Minnesota 55455, USA*<sup>2</sup>*Niels Bohr Institute, University of Copenhagen, DK-2200 Copenhagen, Denmark*<sup>3</sup>*School of Physics and Astronomy, University of Minnesota, Minneapolis, Minnesota 55455, USA*

(Received 8 May 2023; revised 10 August 2023; accepted 15 September 2023; published 27 September 2023)

Recent experiments have shown that the phase diagrams of the kagome superconductors  $AV_3Sb_5$  are strongly impacted by changes in the  $c$ -axis lattice parameter. Here, we show that  $c$ -axis deformations impact primarily the Sb apical bonds and thus the overlap between their  $p_z$  orbitals. Changes in the latter, in turn, substantially affect low-energy electronic states with significant Sb character, most notably the central electron pocket and the van Hove singularities located above the Fermi level. Based on the orbital-selective character of  $c$ -axis strain, we argue that these electronic states experience a non-negligible attractive electron-phonon pairing interaction mediated by fluctuations in the apical Sb bonds. We thus propose a multiband model for superconductivity in  $AV_3Sb_5$  that includes both the Sb pocket and the V-derived van Hove singularities. Upon comparing the theoretical phase diagram with the experimentally observed vanishing of the  $T_c$  dome across a Lifshitz transition of the Sb pocket, we propose that either an  $s^{+-}$  or an  $s^{++}$  state is realized in  $AV_3Sb_5$ .

DOI: [10.1103/PhysRevB.108.L100510](https://doi.org/10.1103/PhysRevB.108.L100510)

The discovery of superconductivity (SC) in the family of kagome metals  $AV_3Sb_5$  ( $A$ : K, Rb, Cs) has sparked significant interest since the interference between different electronic hopping paths in the kagome lattice endows the electronic structure with flat bands, van Hove singularities (vHs), and Dirac points. These features have the potential to promote collective electronic behavior characteristic of materials with strong electronic correlations or nontrivial band topology [1–4]. Indeed, upon a cursory examination, the phase diagrams of  $AV_3Sb_5$  resemble those of Cu- and Fe-based superconductors, in that SC appears in close proximity to another electronic order, in this case a charge-density wave (CDW) phase, which has been intensely scrutinized both theoretically [5–11] and experimentally [12–16]. While the three-dimensional nature of the CDW wave-vector is well established [17–20], there remains considerable debate whether it also breaks time-reversal and rotational symmetries [21–28].

Studies of the SC properties of  $AV_3Sb_5$  have lagged the investigations of the CDW phase, partly because the latter onsets at much higher temperatures ( $T_{CDW} \approx 100$  K) than the former ( $T_c \approx 1$  K). There have been reports of both nodeless [29–35] and nodal [15,36,37] gap structures, as well as conflicting accounts of whether the electron-phonon coupling can explain the SC instability [38–41]. Proposals have been put forward in favor of both conventional and unconventional pairing, most of which focus on the electronic states derived from the V  $d$  orbitals [5,6,8,42–46], which give rise to saddle points in the band structure near the M point. However, recent experimental studies of the doping-temperature and pressure-temperature phase diagrams of  $CsV_3Sb_5$  have shown that the end of the SC dome in either case coincides with the disappearance of an electron pocket at the  $\Gamma$  point derived from the Sb  $p$  orbitals, highlighting their relevance for the onset of pairing [47,48].

In this paper, we combine density-functional theory (DFT) calculations and low-energy modeling to show that the Sb degrees of freedom play an essential role for the superconductivity of  $AV_3Sb_5$ . Our starting point is the empirical observation made in Ref. [49] that the phase diagrams of  $CsV_3Sb_5$  under pressure and under uniaxial in-plane stress fall essentially on top of each other when  $T_{CDW}$  and  $T_c$  are expressed as a function of the  $c$ -axis expansion or contraction. Moreover, thermal expansion measurements report a  $c$ -axis response much more pronounced than the  $a$ -axis response at both  $T_c$  and  $T_{CDW}$  [50]. These results are strong indication that the  $c$ -axis lattice parameter is a key control parameter for both types of electronic order. From DFT, we find that the states primarily affected by changes in the  $c$  axis are those that have a significant contribution from the apical Sb orbitals: the vHs above the Fermi level at the M point and the electron band centered at the  $\Gamma$  point, whose bottom shifts by hundreds of meV for strain values of a few percent. In contrast, the energies of the vHs below the Fermi level remain nearly unchanged. Such an “orbital-selective” modification of the electronic spectrum provides a mechanism by which the  $c$ -axis lattice parameter can impact the CDW and SC transitions, as empirically seen in Ref. [49]. Based on these results, we construct a low-energy model for the SC state of  $AV_3Sb_5$  consisting of a central Sb-dominated electron pocket and a large V-dominated Fermi surface associated with the vHs. By studying the evolution of  $T_c$  as the Sb band raises above the Fermi level, we find that only  $s^{++}$  and  $s^{+-}$  states are compatible with the observation of a vanishing  $T_c$  as the Sb pocket undergoes a Lifshitz transition, in agreement with experiments [47,48].

We start by employing DFT to elucidate the impact of  $c$ -axis distortions on the band structure of  $AV_3Sb_5$ , focusing on  $A = Cs$  for concreteness. For details, see the Supplemental Material (SM) [51]. Above  $T_{CDW}$  and at ambient pressure,  $CsV_3Sb_5$  adopts the  $P6/mmm$  (#191) space group, with Cs

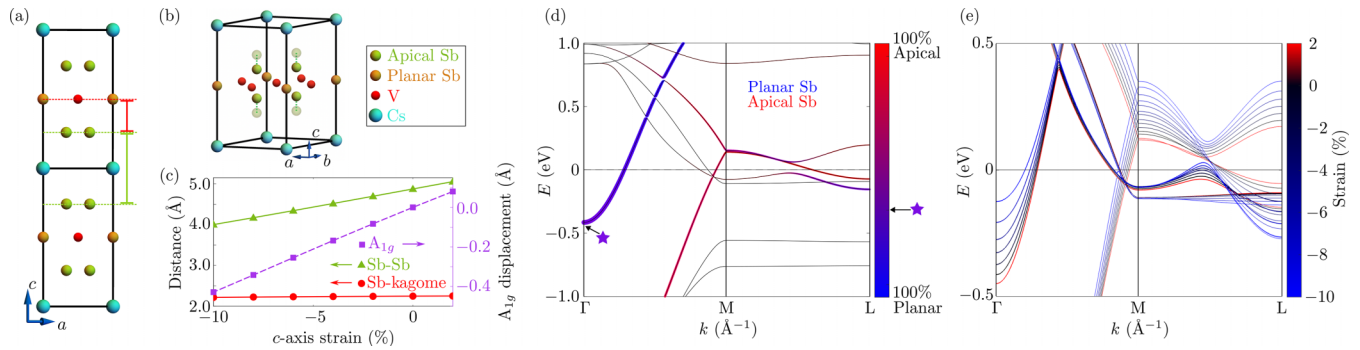


FIG. 1. [(a), (b)] Schematic illustrations of two neighboring  $AV_3Sb_5$  unit cells and of the displacement pattern of the apical Sb promoted by the  $A_{1g}$  phonon mode, respectively. We choose a sign convention such that the displacement of apical Sb towards the kagome plane corresponds to positive  $A_{1g}$ . (c) Changes in the distances between the Sb apical atom and its nearest-neighbor (green triangles) and the V atoms (red circles) as a function of  $c$ -axis strain for  $CsV_3Sb_5$ . The purple squares give the atomic displacements from the equilibrium structure corresponding to a frozen excitation of the optical  $A_{1g}$  phonon mode. (d) Low-energy band structure of  $CsV_3Sb_5$ . The thickness of the bands is proportional to the total projection onto the  $p_z$  orbitals of the Sb atoms, whereas their color is proportional to the projection onto the planar Sb (blue) and apical Sb (red). The  $\Gamma$  band has contributions from both Sb sites. (e) Modifications in the low-energy band structure as a function of  $c$ -axis strain. The momentum L is located above M in the hexagonal Brillouin zone; the other momenta are defined in Fig. 2(a).

occupying the  $1a$  Wyckoff site, V the  $3g$  site, and Sb the  $4h$  (apical) and  $1b$  (planar) sites, as illustrated in Figs. 1(a) and 1(b). The V atoms form a kagome sublattice, whereas the planar (apical) Sb atoms, a hexagonal (honeycomb) sublattice. Besides the lattice parameters, the reduced  $z$  coordinate of the apical Sb atoms is the only free structural parameter. Interestingly,  $z$  increases significantly upon compression of the  $c$  axis in a way that approximately preserves the Sb–V bond distances between the apical Sb and the kagome layer, while shortening the Sb–Sb bond distances between apical Sb in adjacent unit cells, as shown Fig. 1(c).

To address whether this displacement pattern is capable of affecting the low-energy electronic states, we first calculate via DFT the atomically resolved band structure near the Fermi energy in the undistorted phase [Fig. 1(d)]. In agreement with previous works [47,48,59], we find dominant spectral-weight contributions from both types of Sb atoms (planar and apical) to the  $\Gamma$ -point electron band, as well as a significant contribution from the apical Sb to the V-dominated saddle points located above the Fermi level at the M point. It is this hybridization between apical Sb orbitals and V orbitals that endow the corresponding vHs with a significant  $k_z$  dispersion, to the point that they even cross the Fermi level along the M-L line.

In Fig. 1(e), we show how the low-energy band structure is modified by both compressive (negative) and tensile (positive)  $c$ -axis strain (see also Ref. [60]). We include large absolute values of strain to highlight the effect. Note that all internal lattice parameters are relaxed for a given  $c$ -axis distortion, while keeping the in-plane lattice parameter fixed. The bands that are most affected are those exhibiting a sizable contribution from the apical Sb atoms, such as the vHs located above the Fermi level. Since the CDW is associated with the condensation of phonon modes at the M and L points [9,17], this provides a possible mechanism by which  $c$ -axis strain can impact the CDW phase. Besides these saddle points, the bottom of the electron pocket at the  $\Gamma$  point moves substantially with  $c$ -axis changes, with shifts of 100 meV for strains of about 1% (see also Fig. S1 in the SM [51]). In contrast, the

energies of the M-point vHs located below the Fermi level barely change, reflecting their dominant V character. The large shifts of the bottom of the  $\Gamma$ -point electron band can be attributed to the out-of-phase overlap between the  $p_z$  orbitals of apical Sb atoms of neighboring unit cells. This overlap generates a bonding and an antibonding state, the latter of which gives rise to the  $\Gamma$ -point electron band. Upon compression of the  $c$  axis, the orbital overlap increases and, consequently, the energy of the antibonding state increases, leading to the observed shift in the bottom of the electron band.

The electronic properties of  $AV_3Sb_5$  should be impacted not only by static strain, but also by thermal fluctuations associated with the atomic displacement pattern promoted by the  $c$ -axis strain. These fluctuations are expected to be strongly coupled to the electronic states with significant Sb character. Because the displacement pattern associated with the Sb–Sb bonds does not break crystal symmetries, it cannot be decomposed in terms of a single phonon mode. Instead, there are two different phonon modes that modify the bond lengths along the  $c$  axis without modifying other features in the crystal structure: a longitudinal acoustic-phonon mode with out-of-plane dispersion and a  $\Gamma$ -point optical phonon mode that transforms as the  $A_{1g}$  irreducible representation of the point group. Note that the  $A_{1g}$  displacements, represented in Fig. 1(b), also involve changes in the Sb–V bond distances. As shown in Fig. 1(c), the strong  $c$ -axis strain dependence of the displacement associated with this  $A_{1g}$  mode resembles that displayed by the Sb–Sb bond distance. This result confirms that the  $A_{1g}$  phonon mode leads to Sb–Sb bond fluctuations.

The coupling between the electronic states with significant Sb spectral weight and these phonon modes should lead to a non-negligible attractive pairing interaction. To assess its impact, we construct a low-energy model for the SC phase considering a simplified Fermi surface that consists of a small Sb electron-pocket at the  $\Gamma$  point and a large hexagonal-like Fermi surface originating from one of the V vHs [42,46,47,59]. The V band is modeled in terms of a single orbital on the sites of the kagome lattice whereas the Sb band is parametrized as a nearly isotropic dispersion,

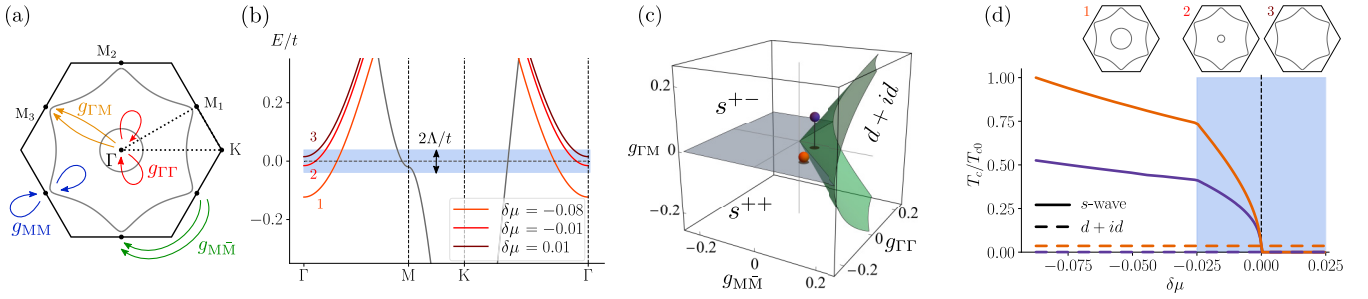


FIG. 2. (a) Pairing interactions of the four-patch model involving fermions at the  $M_i$  and  $\Gamma$  points. The Fermi surface is shown in gray. (b) Tight-binding dispersions, highlighting the Lifshitz transition of the  $\Gamma$ -point electron pocket as a function of the parameter  $\delta\mu \equiv (\mu_\Gamma - \mu_c)/\mu_c$ ;  $\Lambda$  is the pairing interaction cutoff. (c) SC phase diagram of the four-patch model (away from the Lifshitz transition) as a function of the interactions shown in panel (a);  $s$ -wave corresponds to either  $s^{++}$  or  $s^{+-}$  states depending on the sign of  $g_{\Gamma M}$ . (d)  $T_c$  as a function of the parameter  $\delta\mu$  that tunes the  $\Gamma$  pocket across the Lifshitz transition at  $\delta\mu = 0$ , as shown in the insets. The interaction parameters, marked by the orange and purple symbols shown in panel (c), are  $(g_{M\bar{M}}, g_{\Gamma M}, g_{\Gamma\Gamma}, g_{MM}) = (0.1, 0.015, -0.15, 0)$  for the orange lines and  $(0.07, 0.1, -0.03, 0)$  for the purple lines.  $T_{c0}$  is the SC transition temperature for the first set of parameters (orange) at  $\mu_{\Gamma 0} = -3.65\tilde{t}$ .

$\xi_\Gamma(\mathbf{k}) = \tilde{t}f_\Gamma(\mathbf{k}) - \mu_\Gamma$ ; details are given in the SM [51]. The parameter  $\mu_\Gamma$  defines the energy of the bottom of the electron band and is set to  $\mu_{\Gamma 0} = -3.65\tilde{t}$  for the undistorted compound based on comparison with angle-resolved photoemission spectroscopy (ARPES) measurements [61]. Upon decreasing  $\mu_\Gamma$ , which mimics the effect of hole doping, a Lifshitz transition occurs at  $\mu_c \equiv -4\tilde{t}$ , where the  $\Gamma$ -point Fermi pocket disappears. For simplicity, we thus define  $\delta\mu \equiv (\mu_\Gamma - \mu_c)/\mu_c$ .

To derive the SC gap equations, we generalize a patch approach commonly employed to describe systems with vHs near the Fermi level [62–67]. Because of the logarithmic enhancement of the density of states (DOS) at the M-point vHs, it is sufficient to consider only the pairing interactions involving states on the three Fermi-surface patches centered at each of the three M points. Symmetry restricts these interactions to two different types: intrapatch  $g_{MM}/N_M$  and interpatch  $g_{M\bar{M}}/N_M$ , where  $N_M$  is the DOS of the M-point patches. We approximate the small  $\Gamma$  pocket by a fourth patch subjected to an intrapatch pairing interaction  $g_{\Gamma\Gamma}/N_\Gamma$  and an interpatch interaction  $g_{\Gamma M}/\sqrt{N_M N_\Gamma}$  with the M-point patches. Based on our results above, we assume an attractive interaction  $g_{\Gamma\Gamma} < 0$  arising from the electron-phonon coupling involving the apical Sb degrees of freedom. Note that this parametrization of the pairing interaction in terms of the DOS of each patch is not valid close to the Lifshitz transition; we will return to this point later.

The resulting four-patch model is schematically shown in Fig. 2(a). Denoting  $\vec{\Delta} \equiv (\Delta_{M_1}, \Delta_{M_2}, \Delta_{M_3}, \Delta_\Gamma)^T$  for the gap functions on the four patches, the corresponding linearized gap equations can be written in matrix form as  $\chi_{pp}\vec{\Delta} = \vec{\Delta}$ , with

$$\chi_{pp} = -V_\Lambda \begin{bmatrix} g_{MM} & g_{M\bar{M}} & g_{M\bar{M}} & \eta g_{\Gamma M} \\ g_{M\bar{M}} & g_{MM} & g_{M\bar{M}} & \eta g_{\Gamma M} \\ g_{M\bar{M}} & g_{M\bar{M}} & g_{MM} & \eta g_{\Gamma M} \\ \eta^{-1} g_{\Gamma M} & \eta^{-1} g_{\Gamma M} & \eta^{-1} g_{\Gamma M} & g_{\Gamma\Gamma} \end{bmatrix}, \quad (1)$$

where  $V_\Lambda \equiv \int_{-\Lambda}^{\Lambda} d\varepsilon \tanh(\beta\varepsilon/2)/(2\varepsilon) \approx \ln(2e^\gamma \beta \Lambda/\pi)$  is the particle-particle bubble with  $\beta = 1/(k_B T)$  and  $\eta \equiv \sqrt{N_\Gamma/N_M}$  is the ratio between the DOS. Here,  $\Lambda$  is the cutoff for the pairing interaction, as shown in Fig. 2(b), and  $\gamma \approx 0.577$  is

Euler's constant.  $T_c$  is found by imposing that the largest eigenvalue of  $\chi_{pp}$  is 1. The two leading eigenvalues are

$$\lambda_{E_{2g}} = (g_{M\bar{M}} - g_{MM}) \ln(2e^\gamma \beta \Lambda/\pi), \quad (2)$$

$$\lambda_{A_{1g}} = \frac{1}{2}(\tilde{g} - 2g_{M\bar{M}} - g_{MM} - g_{\Gamma\Gamma}) \ln(2e^\gamma \beta \Lambda/\pi), \quad (3)$$

where  $\tilde{g} \equiv \sqrt{12g_{\Gamma M}^2 + (g_{\Gamma\Gamma} - 2g_{M\bar{M}} - g_{MM})^2}$ . Analysis of the eigenvectors of  $\lambda_{E_{2g}}$ , which is doubly degenerate, shows that they describe  $d_{x^2-y^2}$ -wave and  $d_{xy}$ -wave SC states, which transform as the two-dimensional (2D) irreducible representation  $E_{2g}$  of the point group  $D_{6h}$  (see SM [51]). As discussed elsewhere [62], going beyond the linearized gap equation reveals that the linear combination  $d_{x^2-y^2} \pm id_{xy}$  minimizes the free energy, leading to a time-reversal symmetry-breaking SC phase. The second eigenvalue  $\lambda_{A_{1g}}$  corresponds to a pairing state that transforms as the trivial representation  $A_{1g}$ , corresponding to two isotropic gaps  $\Delta_\Gamma$  and  $\Delta_M$ . While the symmetry of this state is  $s$  wave, there are two qualitatively different possible gap configurations depending on the signs of  $\Delta_\Gamma$  and  $\Delta_M$ : an  $s^{++}$  state, in the case of equal signs, or an  $s^{+-}$  state, in the case of opposite signs—similar to that realized in the Fe-based superconductors [68].

Only positive eigenvalues correspond to attractive pairing channels. For the  $E_{2g}$  channel ( $d + id$ ),  $\lambda_{E_{2g}} > 0$  requires a strong enough inter-M-patch repulsion to overcome the intra-M-patch repulsion,  $g_{M\bar{M}} > g_{MM} > 0$ , as found in renormalization-group studies of the three-patch model [62]. As for the  $A_{1g}$  channel ( $s^{++}$  or  $s^{+-}$ ),  $\lambda_{A_{1g}} > 0$  requires either a strong interpatch interaction  $g_{\Gamma M}$ , which can be repulsive or attractive, or a strong intra- $\Gamma$ -patch attraction  $g_{\Gamma\Gamma} < 0$ . Note that the sign of  $g_{\Gamma M}$  does not impact the eigenvalue  $\lambda_{A_{1g}}$ , but only whether the eigenvector corresponds to the  $s^{++}$  ( $g_{\Gamma M} < 0$ ) or the  $s^{+-}$  ( $g_{\Gamma M} > 0$ ) state (see SM [51]).

Figure 2(c) shows the SC phase diagram in the  $\{g_{MM}, g_{\Gamma\Gamma}, g_{\Gamma M}\}$  parameter space. As anticipated, the  $d + id$  state is only stabilized by a dominant repulsive interaction  $g_{M\bar{M}} > 0$ , whereas attractive interactions of any kind favor an  $s$ -wave state. An increase in the magnitude of the interpatch interaction  $g_{\Gamma M}$ , be it attractive or repulsive, further expands the regime where the  $s$ -wave state is realized. While this plot is obtained for  $g_{MM} = 0$ , the main effect of a nonzero  $g_{MM}$  is

in the case where it is repulsive, as it suppresses the regime in which SC is stabilized (see SM [51]).

To elucidate which of these SC regimes are consistent with the experimental observation of a suppression of  $T_c$  across the Lifshitz transition [47,48], we compute the evolution of  $T_c$  as  $\mu_\Gamma$  approaches the critical value  $\mu_c$  for which the electron-band bottom crosses the Fermi level (see inset of Fig. 2(d)). Near the Lifshitz transition, where  $|\mu_\Gamma - \mu_c| \ll \Lambda$ , the gap equations (1) have to be modified, as it is not justified to remove the DOS from the integrand of the particle-particle bubble [69,70]. The modified  $\chi_{pp}$  is shown in the SM [51]. By numerically computing its eigenvalues, we obtain  $T_c(\mu_\Gamma)$  for the various regimes in Fig. 2(c). Because the  $d + id$  state is insensitive to the  $\Gamma$  pocket, its  $T_c$  does not change across the Lifshitz transition. Meanwhile, the behavior of  $T_c$  of the  $s$ -wave state depends on the nature of the dominant pairing interaction. If the  $s$ -wave state is driven by large attractive interactions involving the M patches only,  $g_{MM}$ ,  $g_{MM} < 0$ ,  $T_c$  is not significantly changed at  $\mu_c$ . On the other hand, for dominant intra- $\Gamma$ -patch attraction  $g_{\Gamma\Gamma} < 0$  or dominant interpatch  $g_{\Gamma M}$  of either sign,  $T_c$  is strongly suppressed across the Lifshitz transition. This is shown in Fig. 2(d) for the parameter values corresponding to the orange symbol (dominant  $g_{\Gamma\Gamma}$ ) and the purple symbol (dominant  $g_{\Gamma M}$ ) in Fig. 2(c). Additional  $T_c(\mu_\Gamma)$  plots for other parameter values are shown in the SM [51].

A large attractive intrapocket pairing interaction  $g_{\Gamma\Gamma}$  could be mediated by the Sb–Sb bond fluctuations discussed above. On the other hand, CDW fluctuations with wave vector M could boost  $g_{\Gamma M}$ , rendering it repulsive (attractive) if the CDW breaks (preserves) time-reversal symmetry. However, these CDW fluctuations should also enhance  $g_{MM}$ , since the M patches are connected by the same wave vector. Because the latter couples states with similar orbital compositions (V-V orbitals), whereas  $g_{\Gamma M}$  couples states with different orbital compositions (Sb-V orbitals), the CDW boost of  $g_{MM}$  is expected to be larger, particularly if the CDW is enhanced by the vHs. Interestingly, the Sb–Sb bond fluctuations could switch this hierarchy if the relevant vHs is one of those located above the Fermi level. Indeed, as shown in Figs. 1(d) and 1(e), those vHs have a sizable Sb orbital weight and as such should be impacted by the phonon modes associated with Sb–Sb bond displacements.

We now discuss the experimental implications of our results. All three states obtained in our model,  $d + id$ ,  $s^{+-}$ , and  $s^{++}$ , are fully gapped, which makes it challenging to distinguish between them solely via spectroscopy. Directly probing time-reversal symmetry breaking, for instance via

Kerr rotation, would help exclude or confirm  $d + id$ . The suppression of  $T_c$  across the Sb electron-pocket Lifshitz transition shown in Fig. 2(d) is qualitatively consistent with the experimental results of Refs. [47,48], suggesting that either an  $s^{+-}$  or an  $s^{++}$  state is realized, at least in the region of the phase diagram where the CDW is absent. These  $s$ -wave states are also compatible with the robustness of  $T_c$  against impurities reported in Ref. [32] for CsV<sub>3</sub>Sb<sub>5</sub> and with the observed multigap structure of the SC state seen in the parent compounds, where SC coexists with CDW. If one of these gaps is small, it may reconcile reports favoring both a nodeless and a nodal pairing state [29–34,37]. Alternatively, coexistence of an  $A_{1g}$  SC state with CDW may lead to nodes in the reconstructed Fermi surface [71]. As for unconventional SC, even if the  $d + id$  state is subleading with respect to the  $s^{+-}$  or  $s^{++}$  channels, interesting mixed states can emerge when the ground states are close in energy. These include not only an  $s + d + d$  state that has twofold anisotropy, but also an  $s + e^{i\theta}(d + id)$  state that breaks time-reversal symmetry, as discussed in Refs. [65,72]. Due to the presence of inversion symmetry, mixed singlet-triplet states are not expected.

In summary, we showed that changes in the  $c$ -axis lattice parameter of AV<sub>3</sub>Sb<sub>5</sub> lead to significant changes in the electronic dispersion promoted by the apical Sb  $p_z$  orbitals. Not only the energies and the  $k_z$  dispersion of the vHs located above the Fermi energy are modified, but also the bottom of the  $\Gamma$ -point electron band shifts strongly with  $c$ -axis strain. We proposed that fluctuations of the Sb–Sb bonds promote a non-negligible electron-phonon pairing interaction for states with sizable Sb orbital character, which includes both the central electron pocket as well as the saddle points located above the Fermi level. The resulting  $s^{+-}$  and  $s^{++}$  states are consistent with several experimental observations, including the full suppression of  $T_c$  across the Lifshitz transition involving the Sb pocket [47,48], the nodeless gaps recently observed in ARPES [73], as well as the robustness of  $T_c$  against disorder [32,35].

We thank N. Ni, Z. Wang, and S. Wilson for fruitful discussions. E.R. and T.B. were supported by the NSF CAREER Grant No. DMR-2046020. H.S.R. was supported by research Grant No. 40509 from VILLUM FONDEN. M.H.C. has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie Grant Agreement No. 101024210. R.M.F. was supported by the Air Force Office of Scientific Research under Award No. FA9550-21-1-0423.

E.R. and H.S.R. contributed equally to this work.

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